

d. Buktikan  $3^{2n} + 2^{2n+2}$  habis dibagi 5.

1)  $n = 1$   
 $3^{2n} + 2^{2n+2}$

$$3^{2 \cdot 1} + 2^{2 \cdot 1 + 2}$$

$$3^2 + 2^4$$

$$9 + 16 = 25 \rightarrow \text{habis dibagi 5.}$$

benar.

2)  $n = k$   
 $3^{2 \cdot n} + 2^{2 \cdot n + 2}$

$$3^{2 \cdot k} + 2^{2 \cdot k + 2}$$

$$3^{2k} + 2^{2k} \cdot 2^2$$

$$3^{2k} + 4 \cdot 2^{2k} \rightarrow \text{Asumsikan habis dibagi 5.}$$

sehingga

$$3^{2k} + (4 \cdot 2^{2k}) = 5p$$

$$3^{2k} = 5p - (4 \cdot 2^{2k})$$

$$3 \gg n = k+1$$

$$3^{2 \cdot n} + 2^{2 \cdot n + 2}$$

$$3^{2 \cdot (k+1)} + 2^{2 \cdot (k+1) + 2}$$

$$3 + 2$$

$$3^{2k+2} + 2^{2k+2+2}$$

$$3 + 2$$

$$3^{2k+2} + 2^{2k+4}$$

$$3 + 2$$

$$3^{2k} \cdot 3^2 + 2^{2k} \cdot 2^4$$

→ nilai dari pers. 2

$$5p - (4 \cdot 2^{2k}) \cdot 9 + 2^{2k} \cdot 16$$

(anggap  $2^{2k} = a$ ) sehingga

$$5p - (4 \cdot a) \cdot 9 + a \cdot 16$$

$$5p - 4a \cdot 9 + 16a$$

$$5p - 36a + 16a$$

$$5p - 20a$$



habis dibagi 5. → terbukti.