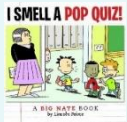


# ECE 20010 Data Structures

## Chapter 4

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- *singly linked list*
- *linked stacks and queues*
- *polynomials (and sparse matrices)*
- *doubly linked list*





## Chapter 4 – Linked lists

---

### 4.1 Singly linked lists and chains

Let's suppose that we have a list of words to store in an array in alphabetical order. The available storage is an array of strings and an array of integers only. The words are given in a random order.


**Example. HAT, CAT, EAT, WAT, BAT, FAT, VAT**

## Chapter 4 – Linked lists

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<b>Data:</b>	hat	cat	eat	wat	bat	fat	vat
<b>Link:</b> first = 0	-1						

## Chapter 4 – Linked lists

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## Chapter 4 – Linked lists

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## Chapter 4 – Linked lists

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## Chapter 4 – Linked lists

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<b>Link:</b> first = 4	3	2	5	-1	1	0	?	



## Chapter 4 – Linked lists

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Let's suppose that we have a list of words to store in an array in alphabetical order. The available storage is an array of strings and an array of integers only. The words are given in a random order.

**Example. HAT, CAT, EAT, WAT, BAT, FAT, VAT**

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<b>Data:</b>	hat	cat	eat	wat	bat	fat	vat	
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<b>Link:</b> first = 1	-1	0						
<b>Link:</b> first = 1	-1	2	0					
<b>Link:</b> first = 1	3	2	0	-1				
<b>Link:</b> first = 4	6	2	5	-1	1	0	3	

How about adding **act** ?

## Chapter 4 – Linked lists

### 4.1 Singly linked lists and chains

## Two types of data representations: sequential vs linked

**Example.**

	<i>data</i>	<i>link</i>
1	HAT	7
2		
3	CAT	4
4	EAT	9
5		
6		
7	WAT	0
8	BAT	3
9	FAT	1
10		
11	VAT	7
	.	.
	.	.
	.	.

**first = 8** →

→ **link 0 is end of list**

**Q:** How are the words listed above? (BAT, CAT, ...)

**BAT, CAT, EAT, FAT, HAT, WAT**

## Chapter 4 – Linked lists

### 4.1 Singly linked lists and chains

## Two types of data representations: sequential vs linked

**Example.**

	<i>data</i>	<i>link</i>
1	HAT	7
2		
3	CAT	4
4	EAT	9
5		
6		
7	WAT	0
8	BAT	3
9	FAT	1
10		
11	VAT	7
	.	.
	.	.
	.	.

**first = 8**

**data[8] = BAT**  
**link[8] = 3**

**data[3] = CAT**  
**link[3] = 4**

**data[link[3]]**

**link 0 is end of list**

**Q:** How is the words listed above? (BAT, CAT, ....

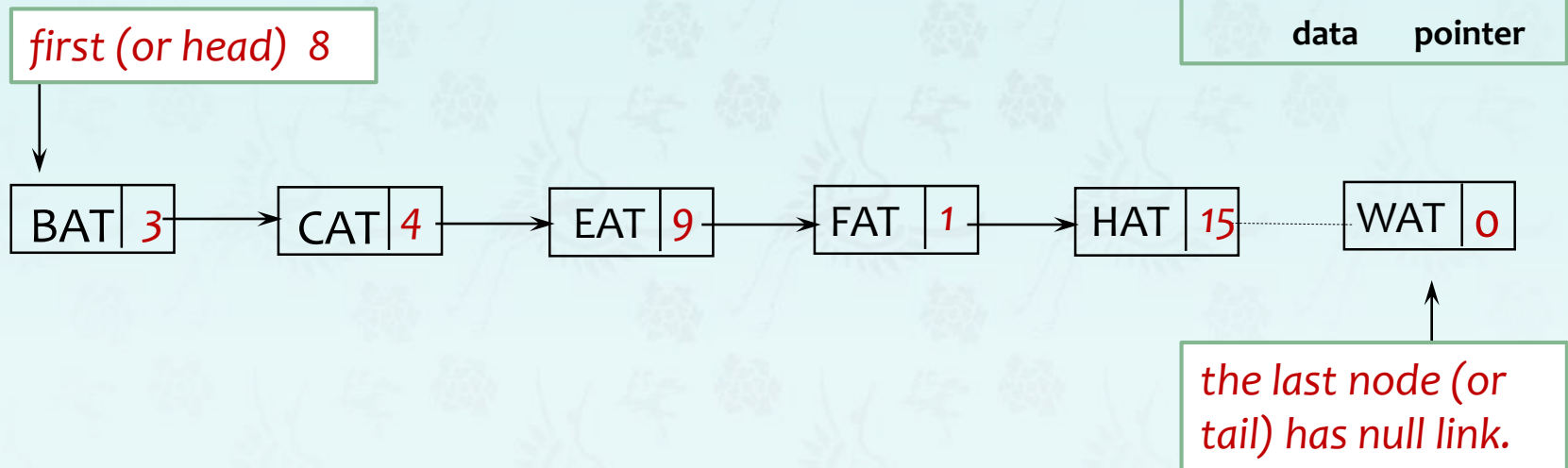
**BAT, CAT, EAT, FAT, HAT, WAT**

## Chapter 4 – Linked lists

### 4.1 Singly linked lists and chains

Two types of data representations: sequential vs linked

**Example.** a common way to draw a linked list



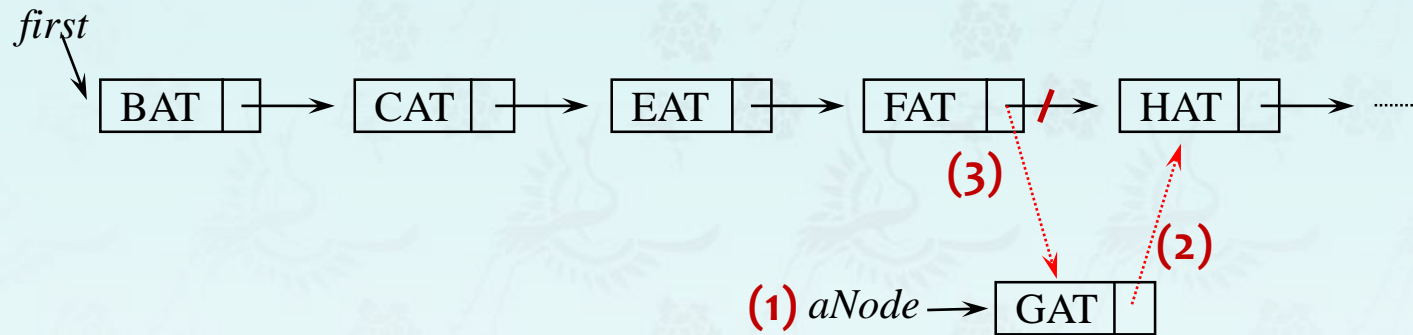
**Q:** How do you **insert** or **delete** a node in a middle of the ordered list above?

**Exercise:** How about deleting CAT?

## Chapter 4 – Linked lists

### 4.1 Singly linked lists and chains

**Q:** How do you **insert** a node **GAT** after **FAT** and before **HAT** in the list?

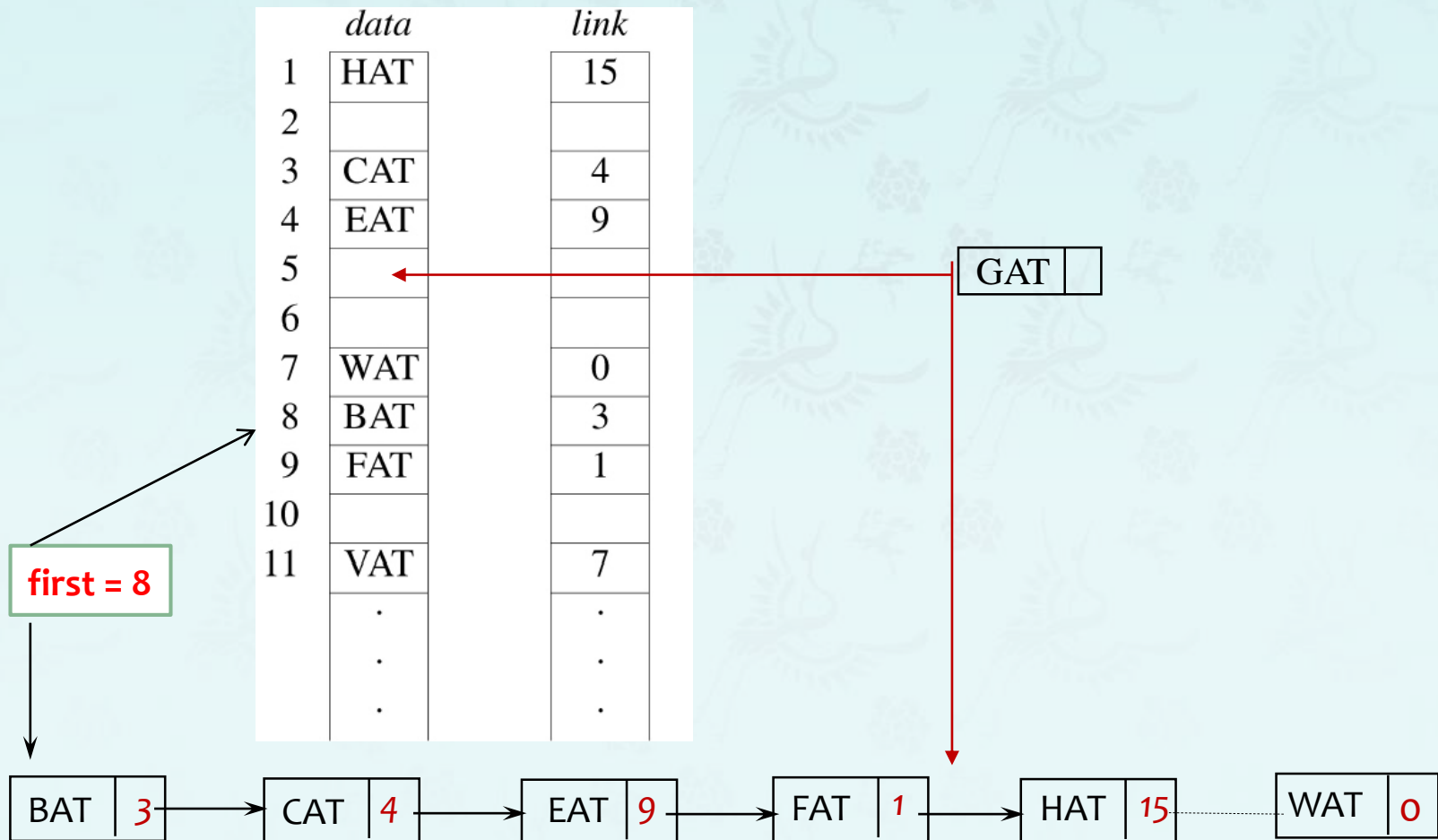


- (1) **Create** a node *aNode* and set its data field to **GAT**
- (2) Set the node **GAT**'s link field to point the node **HAT**.
- (3) Set the node **FAT**'s link field to point the node **GAT**.

## Chapter 4 – Linked lists

### 4.1 Singly linked lists and chains

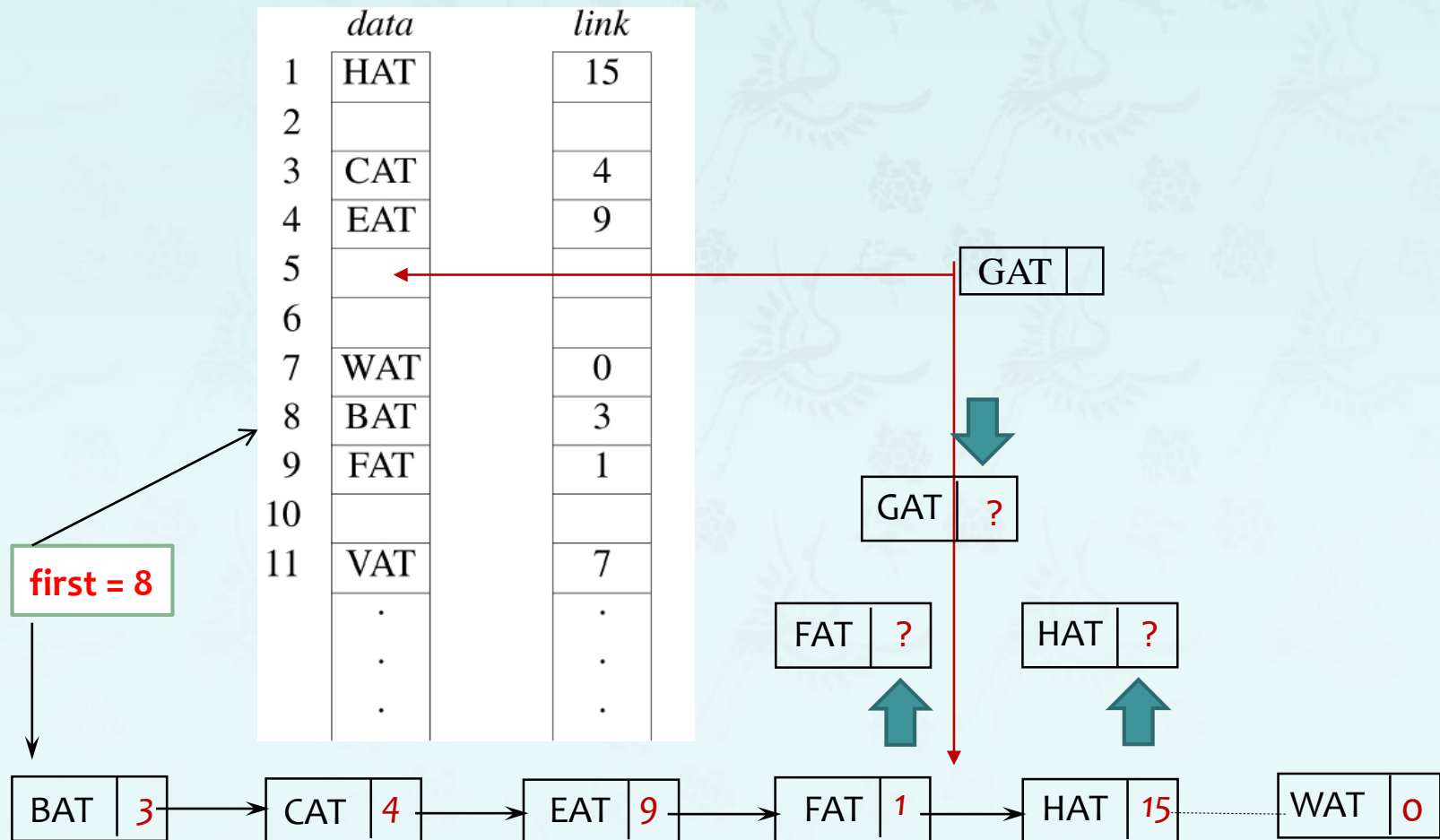
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## Chapter 4 – Linked lists

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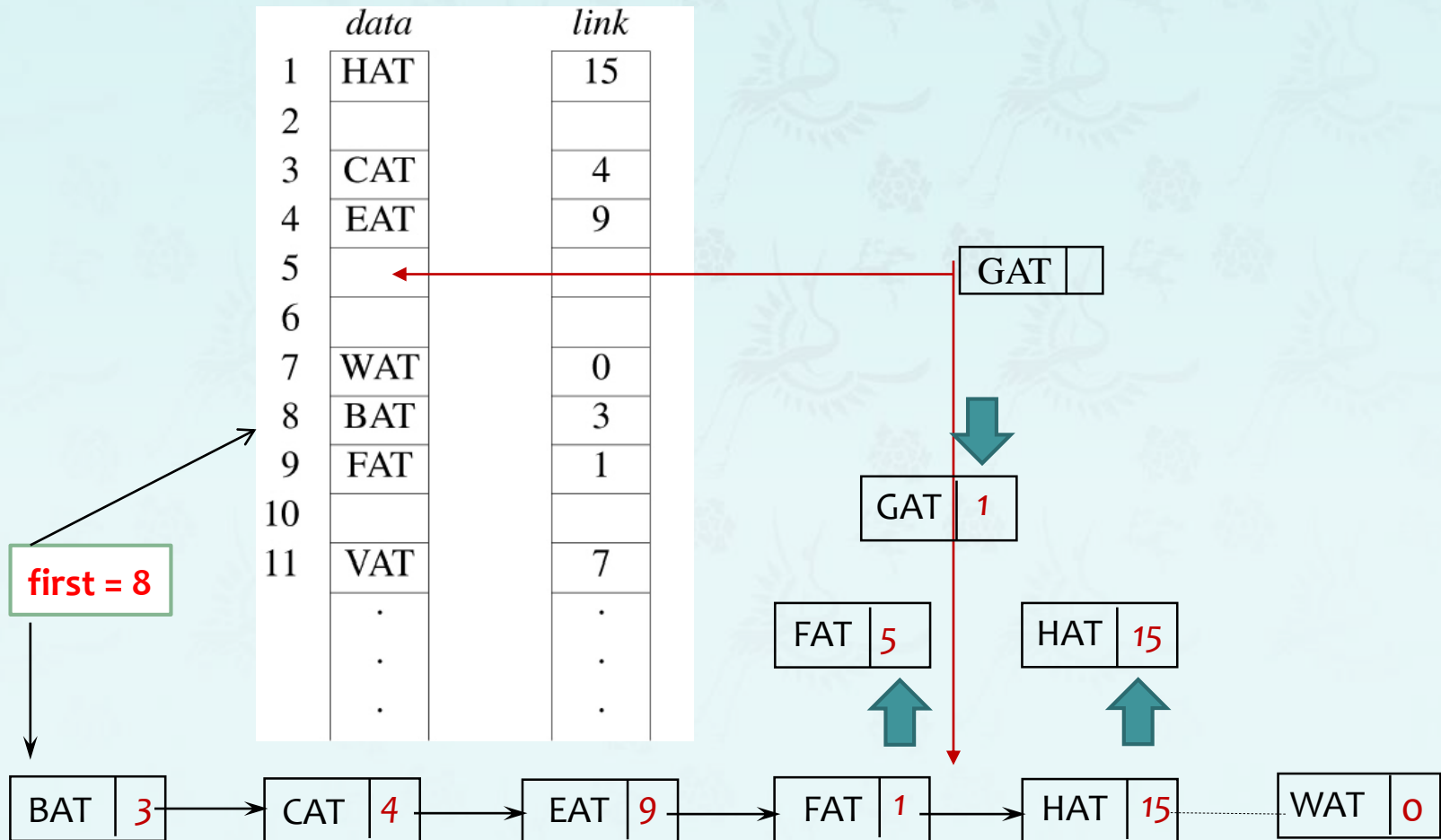
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## Chapter 4 – Linked lists

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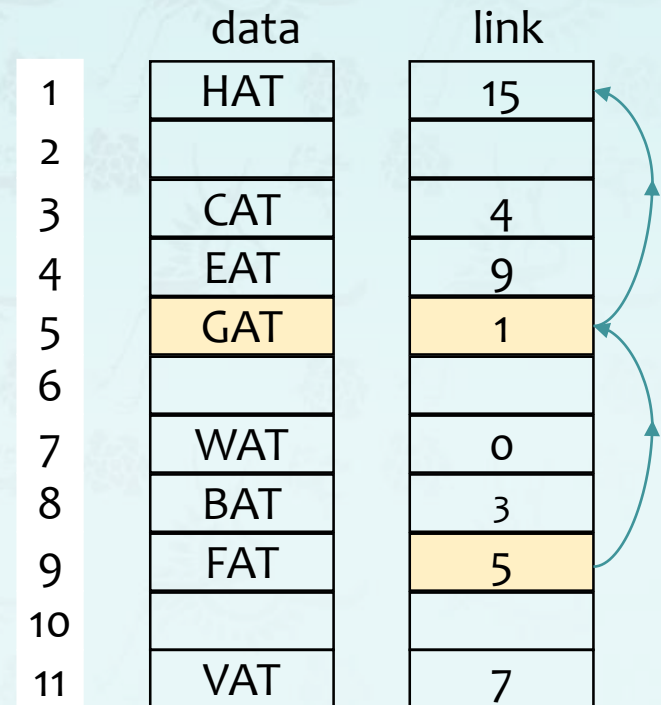
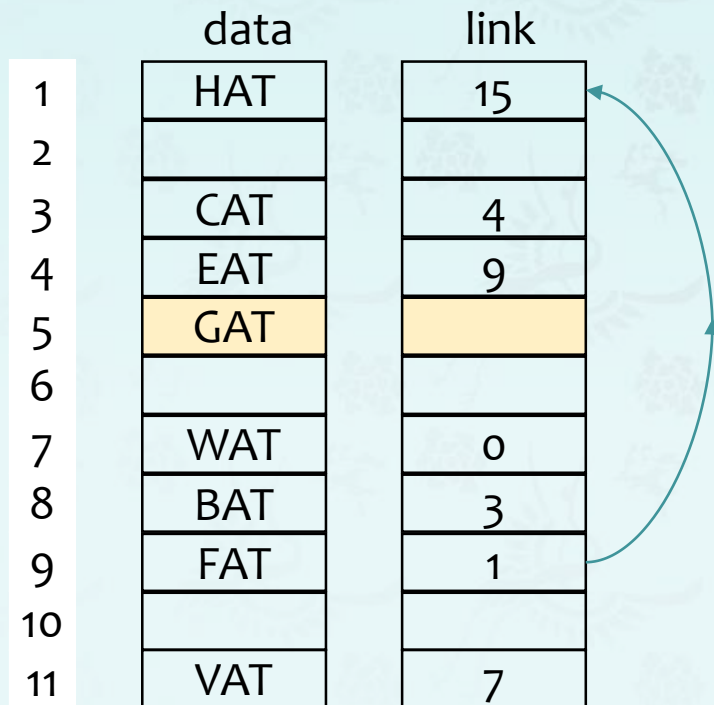




## Chapter 4 – Linked lists

### 4.1 Singly linked lists and chains

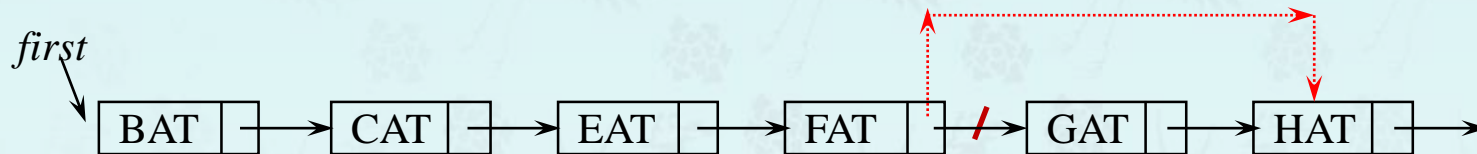
**Q:** How do you **insert** a node **GAT** after **FAT** or before **HAT** in the ordered list?



## Chapter 4 – Linked lists

### 4.1 Singly linked lists and chains

**Q:** How do you **delete** a node **GAT** in the linked list below?



- (1) Find the node **FAT** that is in front of **GAT**.
- (2) Set the node **FAT** link field to point the node **HAT**.
- (3) Free the node **GAT**.

# Chapter 2 – Arrays and structures

## 2.3 Self-referenced structures

**Exercise:** Link a, b and c nodes;

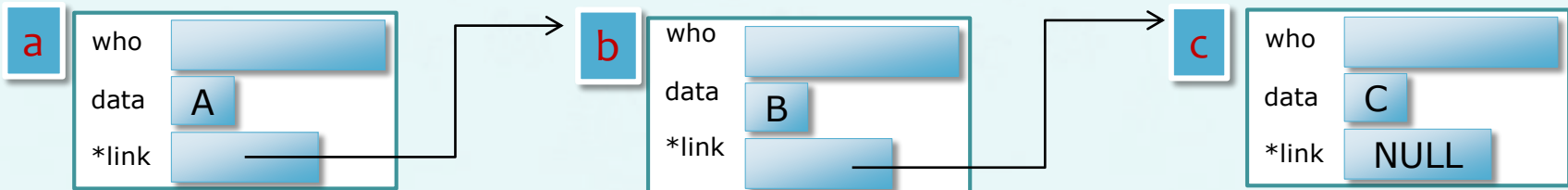
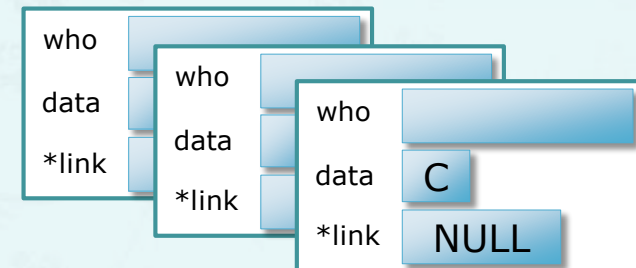
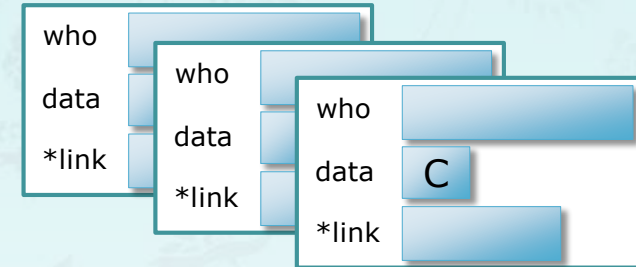
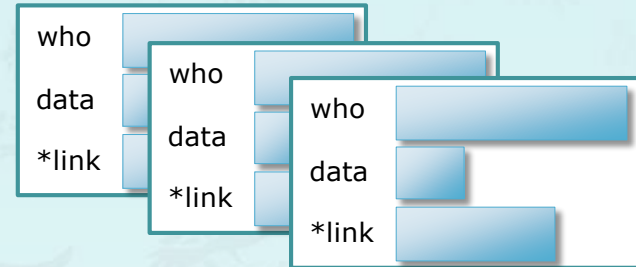
```
typedef struct list {
    student who;
    char data;
    list *link; // pointer to list type
}list;
```

```
list a, b, c;
a.data = 'A';
b.data = 'B';
c.data = 'C';
a.link = b.link = c.link = NULL;
```

list a, b, c;

a.data = 'A';  
b.data = 'B';  
c.data = 'C';

a.link = b.link = c.link = NULL;



# Chapter 2 – Arrays and structures

## 2.3 Self-referenced structures

**Exercise:** Link a, b and c nodes;

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    student who;
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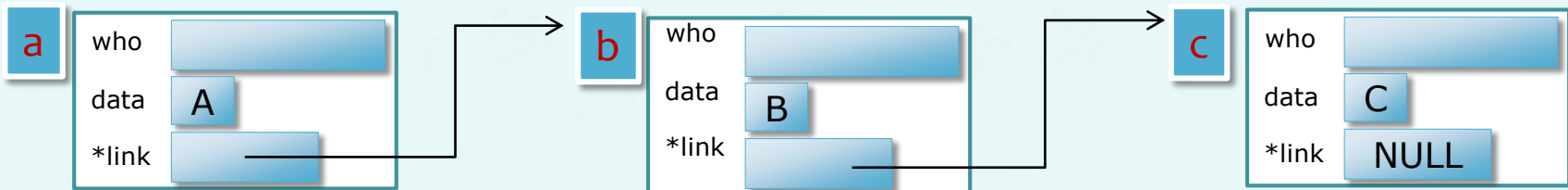
list **a, b, c**;  
list \*p, \*q, \*r;

list a, b, c;

a.data = 'A';  
b.data = 'B';  
c.data = 'C';

a.link = b.link = c.link = NULL;

- (1) Let each p, q, and r points to a, b, and c;
- (2) Store each 'a', 'b', and 'c' in data, and NULL in link, respectively.
- (3) Connect them using p, q and r as shown below:

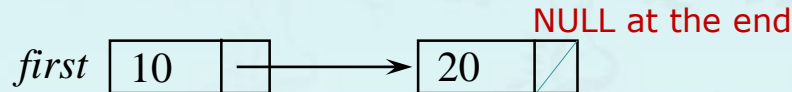


# Chapter 4 – Linked lists



## 4.2 Representing chains in C

**Q:** Write a function that **creates** linked list with two nodes & **returns** the first node:




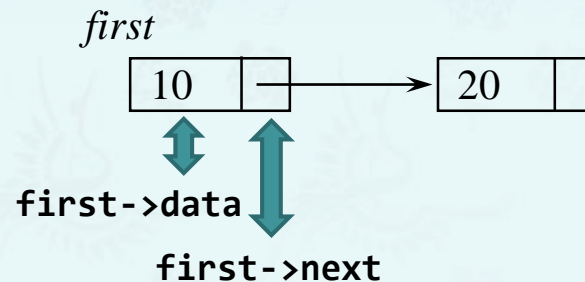
```
typedef struct node *pNode
typedef struct node {
    int    data;    // data
    pNode next;    // link
}node;
```

```
pNode newNode(int item) {
    pNode node = (pNode)malloc(sizeof(node));
    node->data = item;
    node->next = NULL;
}
```

**A:** `pNode newList2(int a, int b)`

```
    first = newNode(a);
    second = newNode(b);
```

```
    
}
```

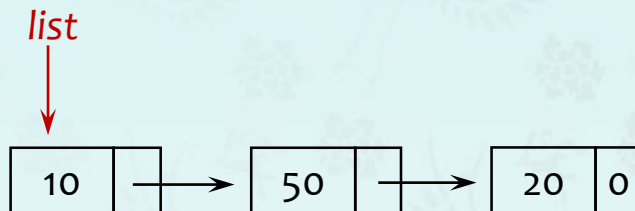


# Chapter 4 – Linked lists

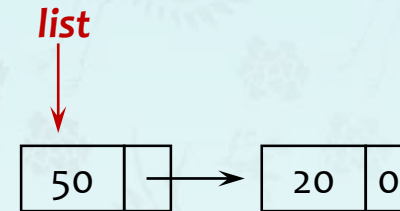
## 4.2 Representing chains in C

```
typedef struct node *pNode  
  
typedef struct node {  
    int    data;    // data  
    pNode next;    // link  
}node;
```

**deleteFirst():** Deleting the first node in the **list**. The second node becomes "first".



(a) before deletion



(b) after deletion

```
void deleteFirst(pList list)
```

```
list = list->next;
```

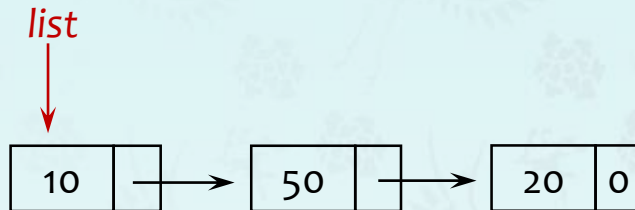
What's wrong? Then how do we deallocate the first node(10)?

# Chapter 4 – Linked lists

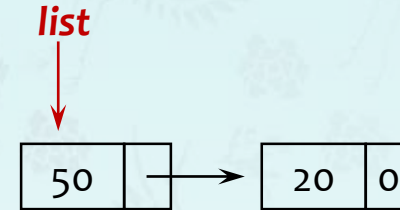
## 4.2 Representing chains in C

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```
pNode deleteFirst(pList list)
```

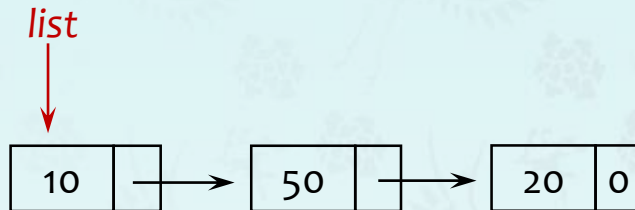
```
pNode x = list;  
list = list->next;  
free(x);
```

# Chapter 4 – Linked lists

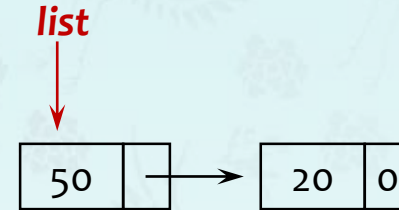
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(a) before deletion



(b) after deletion

```
pNode deleteFirst(pList list)
```

```
pNode x = list;  
list = list->next;  
free(x);  
return list
```



# Chapter 4 – Linked lists

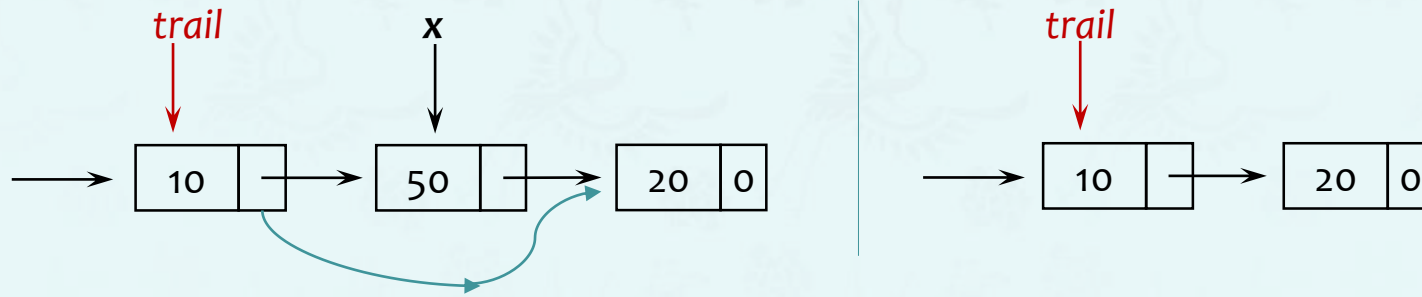
## 4.2 Representing chains in C

```
typedef struct node *pNode  
  
typedef struct node {  
    int    data;    // data  
    pNode next;    // link  
}node;
```

**Deletion:** Deleting a node x which is located in the middle of the list.

Given: **trail**, **x**

```
trail->next = x->next;  
free(x);
```



# Chapter 4 – Linked lists

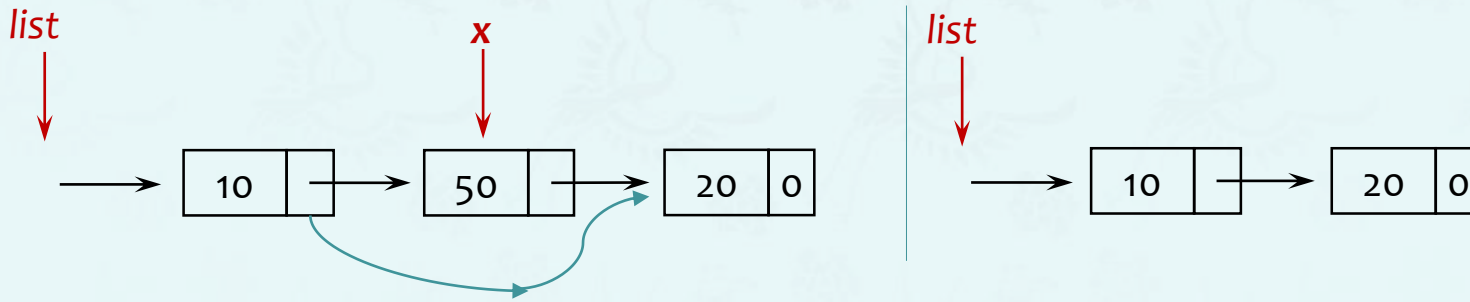
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Given: list, x

**Q:** How about deleting x without trail node given?



# Chapter 4 – Linked lists

## 4.2 Representing chains in C

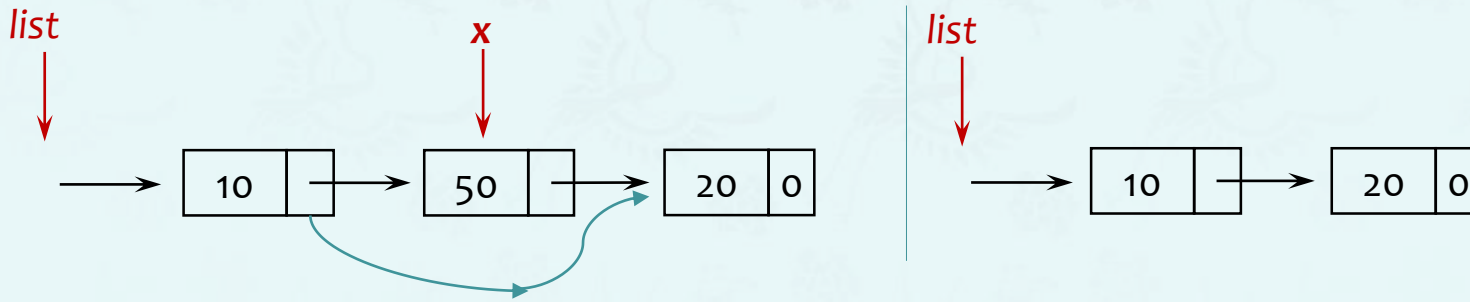
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typedef struct node {  
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    pNode next;    // link  
}node;
```

**Deletion:** Deleting a node x which is located in the middle of the list.

Given: **list**, **x**

**Q:** How about deleting **x** without trail node given?

**A:** While searching for **x**, get the trail node as well.



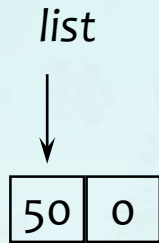
# Chapter 4 – Linked lists

## 4.2 Representing chains in C

**Q:** Make a node **item** = 50, Add it **at last of the list** .

If given **list** is null (or empty list), the node becomes **list**. (program4.2)

```
typedef struct node *pNode  
  
typedef struct node {  
    int    data;    // data  
    pNode next;    // link  
}node;
```



```
pNode newNode(int data) {  
    pNode node = (pNode)malloc(sizeof(node));  
    node->data = data;  
    return node;  
}node;
```

```
pNode addNodeLast(pNode list, int item)  
  
if (list == NULL) {  
    list = newNode(item);  
}
```

(a)

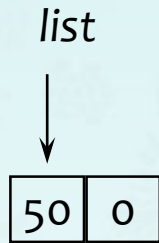
# Chapter 4 – Linked lists

## 4.2 Representing chains in C

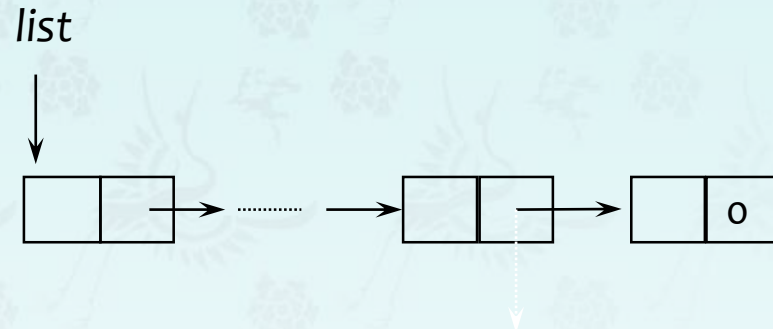
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(a)



(b)

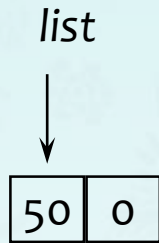
# Chapter 4 – Linked lists

## 4.2 Representing chains in C

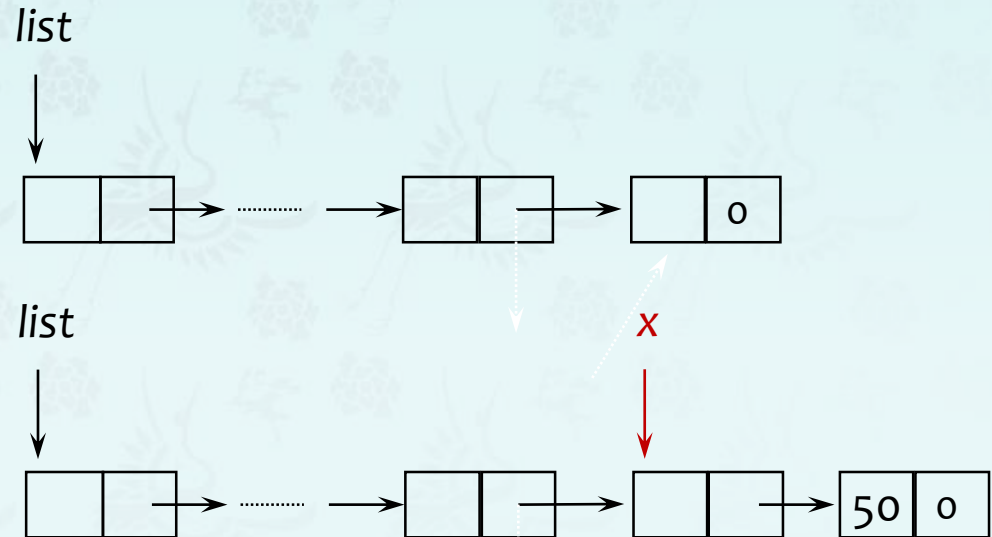
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(a)



(b)

# Chapter 4 – Linked lists

## 4.2 Representing chains in C

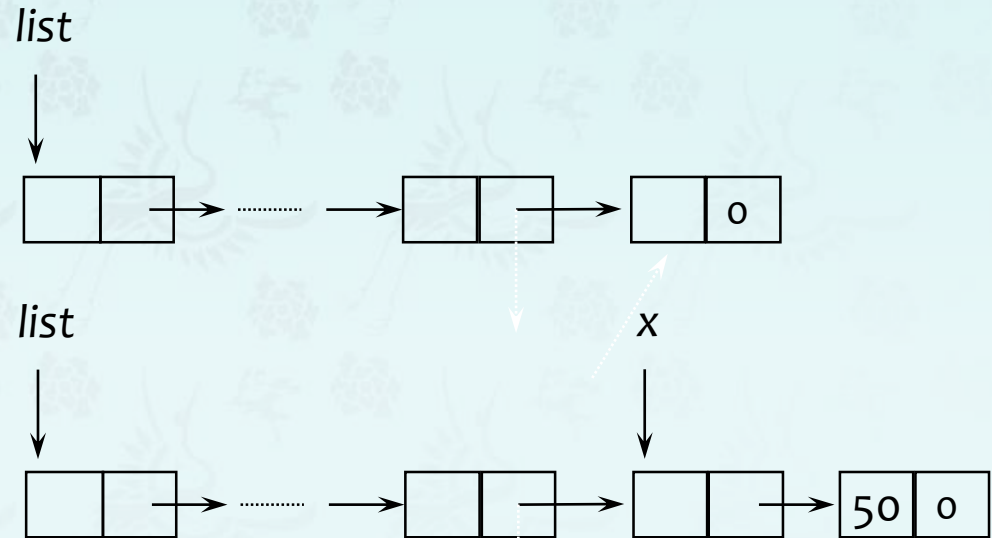
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```
typedef struct node *pNode  
  
typedef struct node {  
    int    data;    // data  
    pNode next;    // link  
}node;
```

Given: **list**, **item** = 50

```
// find the last node x  
pNode x = list  
While (x != NULL) {  
  
}
```



(b)

# Chapter 4 – Linked lists

## 4.2 Representing chains in C

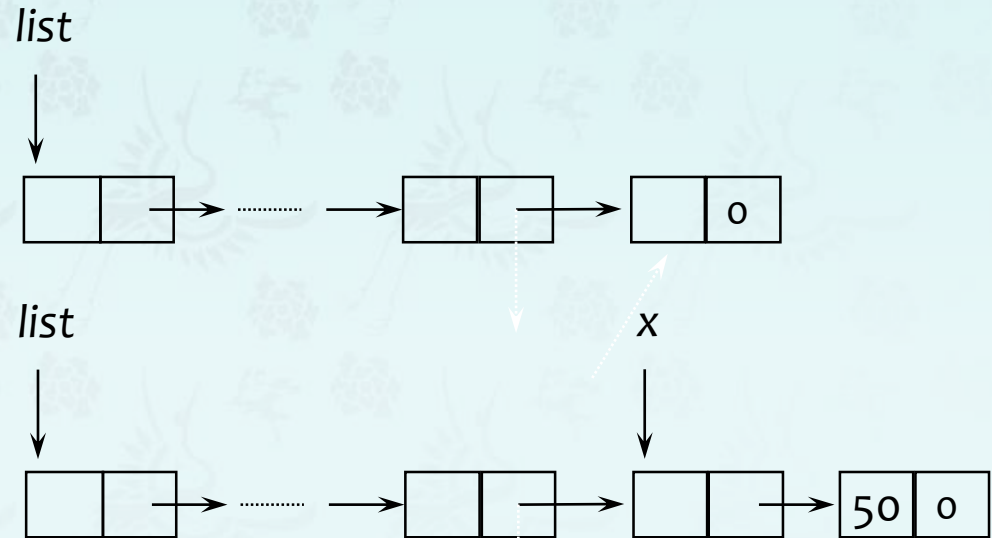
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}node;
```

Given: **list**, **item** = 50

```
// find the last node x  
pNode x = list  
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    x = x->next;  
}
```



(b)



# Chapter 4 – Linked lists

## 4.2 Representing chains in C

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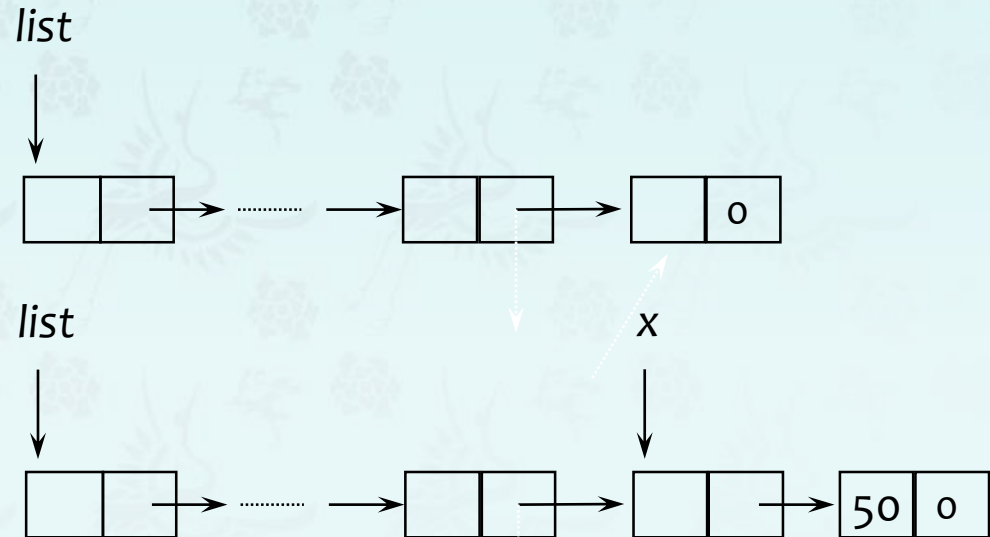
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typedef struct node *pNode
```

```
typedef struct node {  
    int    data;    // data  
    pNode next;    // link  
}node;
```

Given: **list**, **item** = 50

```
// find the last node x  
pNode x = list  
While (x != NULL) {  
    if (x->next == NULL) {  
          
    }  
    x = x->next;  
}
```



(b)

# Chapter 4 – Linked lists

## 4.2 Representing chains in C

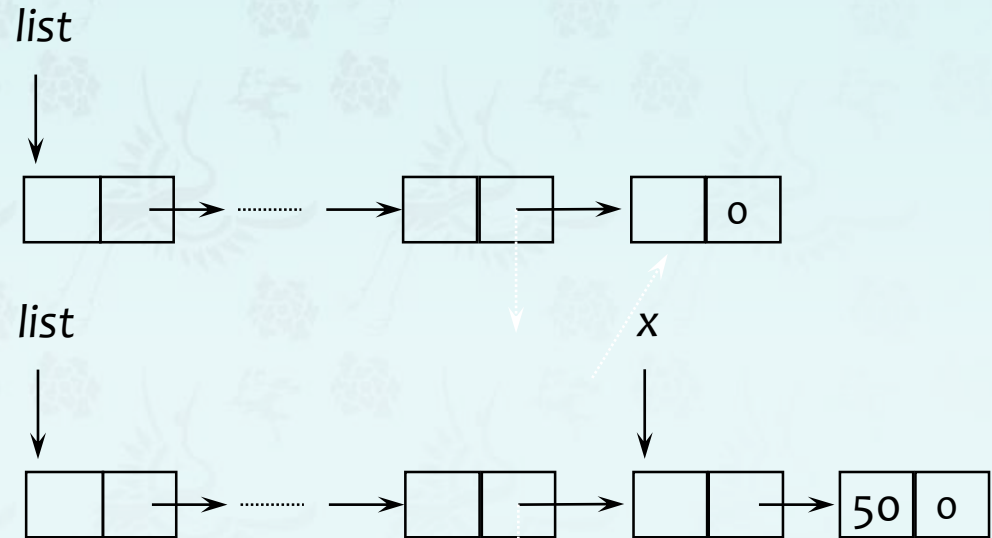
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If given **list** is null (or empty list), the node becomes **list**. (program4.2)

Given: **list**, **item** = 50

```
// find the last node x  
pNode x = list  
While (x != NULL) {  
    if (x->next == NULL) {  
        x->next = newNode(item);  
        break;  
    }  
    x = x->next;  
}
```



(b)

# Chapter 4 – Linked lists

## 4.2 Representing chains in C

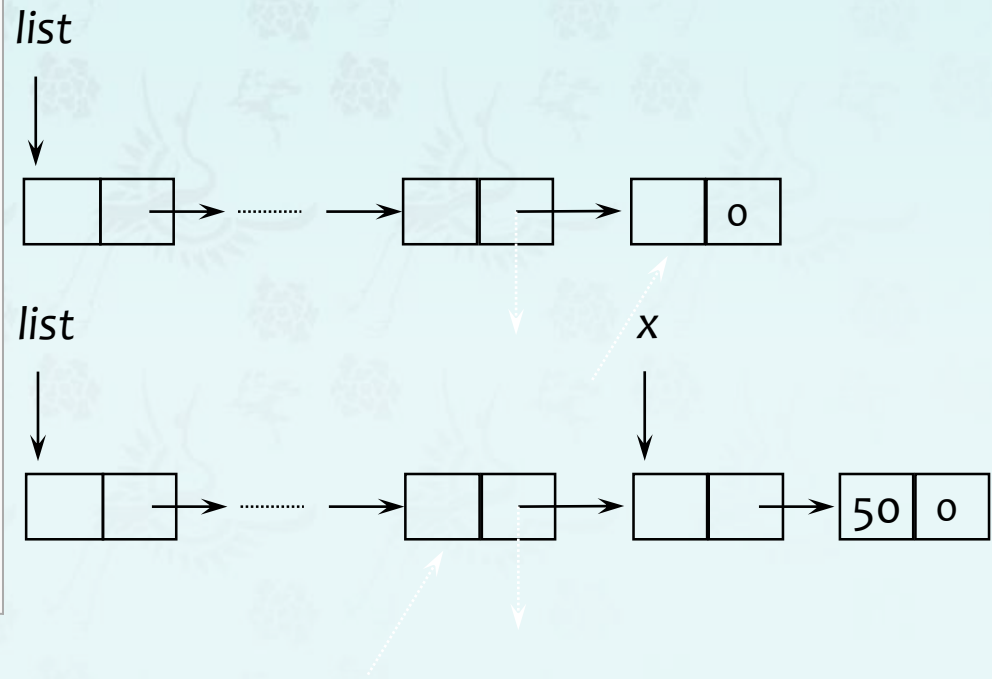
**Q:** Make a node **item** = 50, Add it **at last of the list** .

If given **list** is null (or empty list), the node becomes **list**. (program4.2)

```
typedef struct node *pNode  
  
typedef struct node {  
    int    data;    // data  
    pNode next;    // link  
}node;
```

```
pNode addNodeLast(pList list, int item)
```

```
{  
    if (list == NULL) {  
        list = newNode(item);  
    }  
    else // find the last node x  
        pNode x = list  
        while (x != NULL) {  
            if (x->next == NULL) {  
                x->next = newNode(item);  
                break;  
            }  
            x = x->next;  
        }  
    return list;  
}
```



(b)

# Chapter 4 – Linked lists

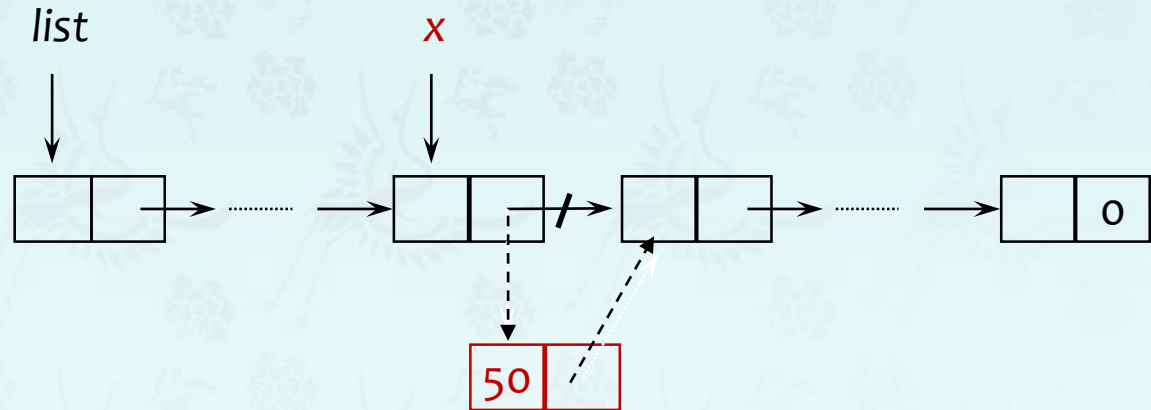
## 4.2 Representing chains in C

```
typedef struct node *pNode  
  
typedef struct node {  
    int    data;    // data  
    pNode next;    // link  
}node;
```

**Q:** Make a node **item** = 50, Add it **after** some arbitrary node **x**.  
If given **list** is null (or empty list), the node becomes **list**. (program4.2)



(a)



(b)

# Chapter 4 – Linked lists

## 4.2 Representing chains in C

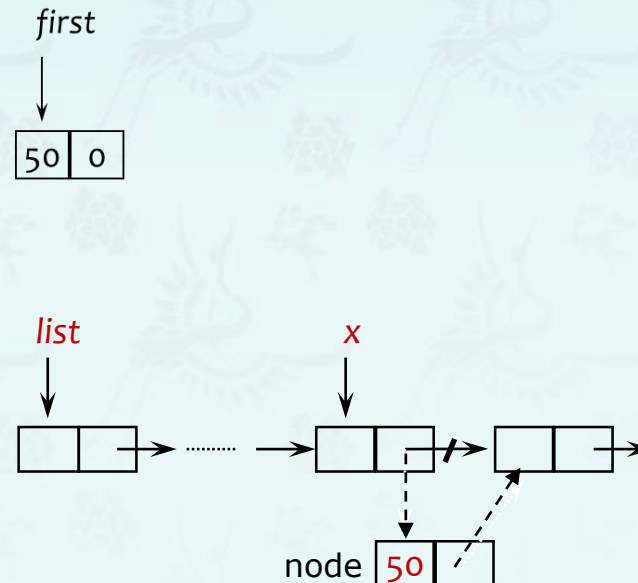
**Q:** Make a node **item** = 50, Add it **after** some arbitrary node **x**.  
If given **list** is null (or empty list), the node becomes **list**. (program4.2)

```
pNode newNode(int data) {  
    pNode node = (pNode)malloc(sizeof(node));  
    node->data = data;  
    return node;  
}node;
```

Given: **list**, **x**, **item** = 50

```
if (list == NULL) {  
    list = newNode(item);  
}  
else {  
    pNode node = newNode(item);  
  
}  
return list;
```

```
typedef struct node *pNode  
  
typedef struct node {  
    int    data;    // data  
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}node;
```



# Chapter 4 – Linked lists

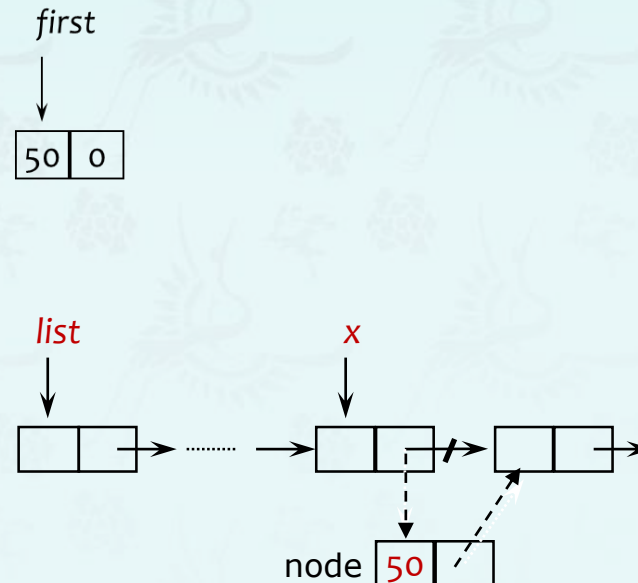
## 4.2 Representing chains in C

**Q:** Make a node **item** = 50, Add it **after** some arbitrary node **x**.  
If given **list** is null (or empty list), the node becomes **list**. (program4.2)

```
pNode newNode(int data) {  
    pNode node = (pNode)malloc(sizeof(node));  
    node->data = data;  
    return node;  
}node;
```

Given: **list**, **x**, **item** = 50

```
if (list == NULL) {  
    list = newNode(item);  
}  
else {  
    pNode node = newNode(item);  
    node->next = x->next;  
    x->next = node;  
}  
return list;
```

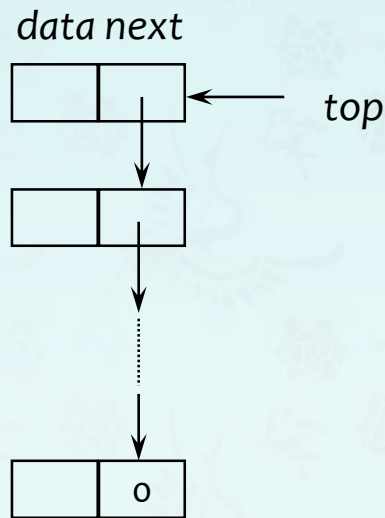


```
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typedef struct node {  
    int data; // data  
    pNode next; // link  
}node;
```

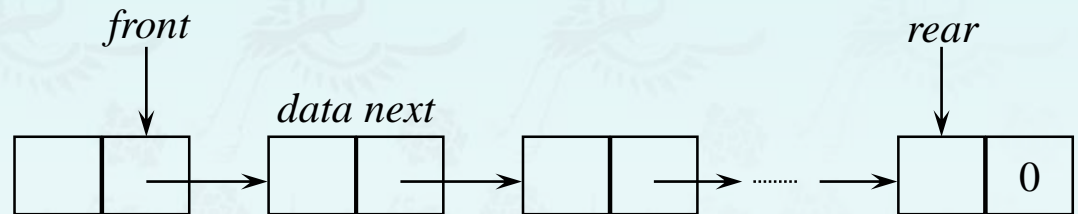
## Chapter 4 – Linked lists

### 4.3 Linked list stacks and queues

Using linked lists, stacks and queues facilitate easy insertion and deletion of nodes.



(a) linked stack



(b) linked queue



## Chapter 4 – Linked lists

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### 4.3 Linked list stacks and queues

#### ❖ resizing array vs. linked list

**Tradeoffs.** Can implement a stack with either resizing array or linked list; client can use interchangeably. Which one is better?

#### Linked-list implementation

- Every operation takes constant time in the worst case.
- Uses extra time and space to deal with the links.

#### Resizing-array implementation

- Every operation takes constant amortized time.
- Less waste space



## Chapter 4 – Linked lists

### 4.4 Polynomials (다항식)

#### ❖ Polynomials representation

$$A(x) = a_{m-1}x^{e_{m-1}} + \dots + a_0x^{e_0}$$

$a_i$  = nonzero coefficients

$e_i$  = nonnegative integer exponents such as

$$e_{m-1} > e_{m-2} > \dots > e_0 \geq 0$$

#### ❖ We may draw a **poly node** as

coef	expo	next
------	------	------

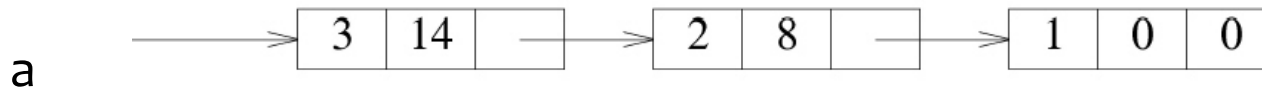
#### ❖ Type definition

```
typedef struct node *pPoly;  
typedef struct poly {  
    double      coef;  
    double      expo;  
    pPoly      next;  
}poly;
```

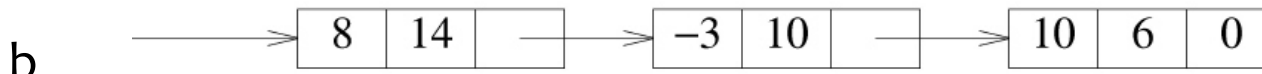
## Chapter 4 – Linked lists

### 4.4 Polynomials (다항식)

❖ Example:



$$(a) 3x^{14} + 2x^8 + 1$$



$$(b) 8x^{14} + 3x^{10} + 10x^6$$

**Q:** How to add two polynomials?  $c = a + b$

# Chapter 4 – Linked lists

## 4.4 Polynomials (다항식)

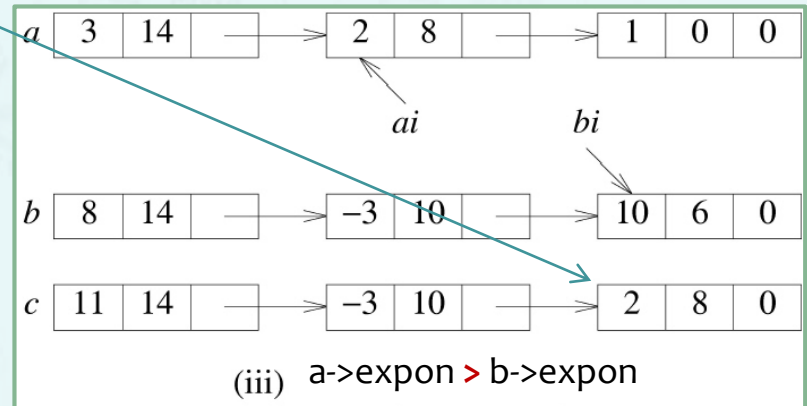
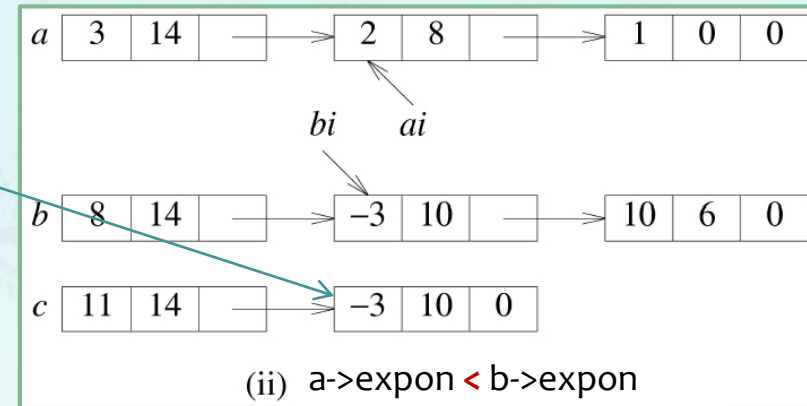
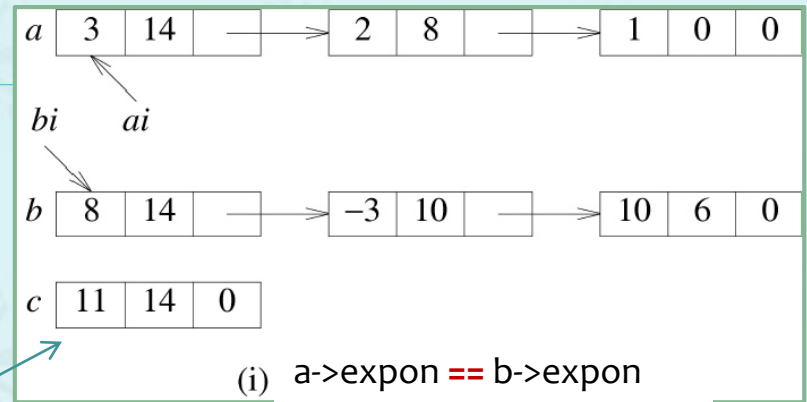
**Q:** How to add two polynomials?

$$a = 3x^{14} + 2x^8 + 1$$

$$b = 8x^{14} - 3x^{10} + 10x^6$$

$$c = a + b$$

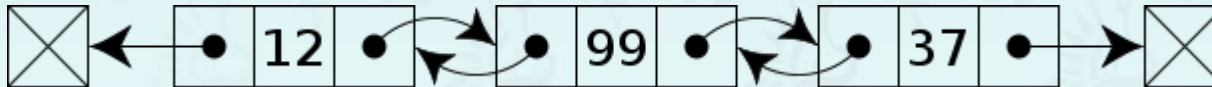
$$= 11x^{14} - 3x^{10} + 2x^8 + 10x^6 + 1$$



## Chapter 4 – Linked lists

### 4.8 Doubly linked list

- ❖ **Doubly linked list:** each node contains, besides the **next**-node link, a second link field pointing to the **previous** node in the sequence. The two links may be called **forward** and **backward**, or **next** and **prev(ious)**.



- ❖ **Type definition**

```
typedef struct node *pDNode
typedef struct node {
    int      item;
    pDNode  prev;
    pDNode  next;
} node;
```

Q. Array vs. Singly linked list vs. Doubly linked list, **Why?**

## Chapter 4 – Linked lists

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### 4.8 Doubly linked list

Q. Array vs. Singly linked list vs. Doubly linked list, **Why?**

#### Advantages of linked list:

- Dynamic structure (Memory Allocated at run-time)
- Have more than one data type.
- Re-arrange of linked list is easy (Insertion-Deletion).
- It doesn't waste memory.

#### Disadvantages of linked list:

- In linked list, if we want to access any node it is difficult.
- It is occupying more memory.

#### Advantages of doubly linked list:

- A doubly linked list can be **traversed in both directions** (forward and backward). A singly linked list can only be traversed in one direction.



# ITP20001/ECE 20010 Data Structures

## Data Structures

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### Chapter 4

- *singly linked list*
- *linked list stacks and queues*
- *polynomials (and sparse matrices)*
- *doubly linked list*