

Simple Epidemic

Consider a closed population of N individuals.

There are two states:

- Susceptible
- Infected

Initially I_0 are infected, $N - I_0$ are therefore susceptible. We assume the population is well mixed. The probability that a susceptible and infectious individual meet is proportional to their abundances, with effective transmission rate β . In simple model, we consider the population (N) is closed and mixed.

We introduce, $s = \frac{S}{N}$ and $i = \frac{I}{N}$

$$\frac{di}{dt} = \beta i(1 - i)$$

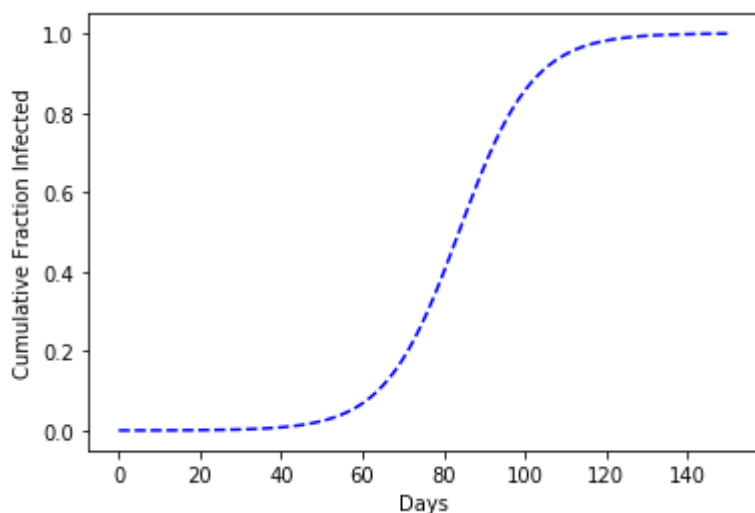
To calculate the number infected at time t , $i(t)$, integrate this equation from time zero to time t , yielding:

$$i(t) = \frac{1}{1 + \frac{1-i_0}{i_0} e^{-\beta t}}$$

This equation yields what is known as the epidemic curve.

In [6]:

```
import numpy as np
i_0=0.0001# initial fraction of infected
beta=0.11# effective transmission rate
def i(t,a0,b):
    return 1/(1+ (np.exp(-b*t)*(1-a0)/a0))
import matplotlib.pyplot as plt
t=np.linspace(0,150,100)
plt.plot(t,i(t,i_0,beta),"b--")
plt.xlabel("Days")
plt.ylabel("Cumulative Fraction Infected")
plt.show()
```

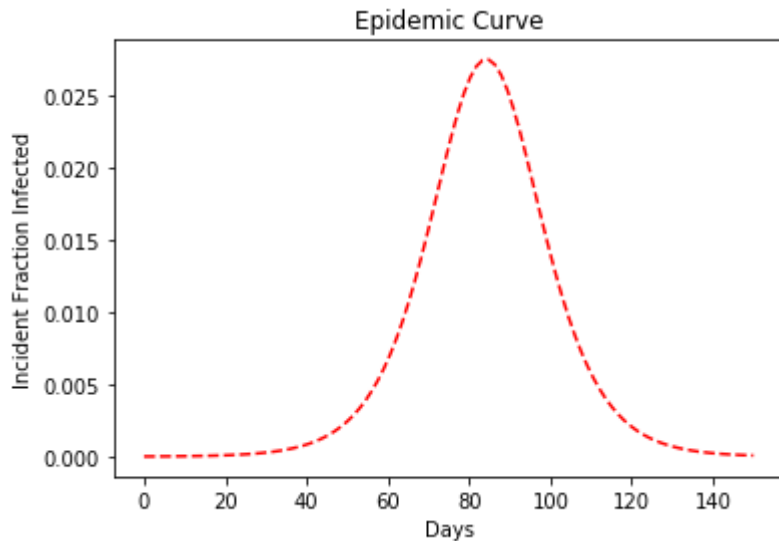


Interpreting the Epidemic Curve

The above figure plots the cumulative prevalence of the infection. We might also want to know about the shape of the incidence of infection, that is, the number of new cases per unit time.

In [7]:

```
plt.plot(t,i(t,i_0,beta)-i(t-1,i_0,beta),"r--")
plt.xlabel("Days")
plt.ylabel("Incident Fraction Infected")
plt.title("Epidemic Curve")
plt.show()
```



More Interpretations of the Epidemic Curve

This is the classic epidemic curve. The epidemic curve is “bell-shaped”, but not completely symmetric. There is a greater force of infection early on. Note that in the limit $t \rightarrow \infty$, everyone in the population becomes infected.