



J. de Curtò y DíAz.

I. de Zarzà y Cubero.

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c@decurto.be z@dezarza.be





De Curtò y DíAz. De Zarzà y Cubero.

J. de Curtò, I. de Zarzà, Hong Yan, Carlos T. Calafate (2022). Signature and Log-signature for the Study of Empirical Distributions Generated with GANs. <a href="https://doi.org/10.36227/techrxiv.19930712">https://doi.org/10.36227/techrxiv.19930712</a>

https://github.com/decurtoydiaz/signatures

J. de Curtò, I. de Zarzà, Hong Yan, Carlos T. Calafate (2022). Learning with Signatures. On this manuscript we extend the metrics to be used for classification tasks. <a href="https://arxiv.org/abs/2204.07953">https://arxiv.org/abs/2204.07953</a>

https://github.com/decurtoydiaz/learning\_with\_signatures/



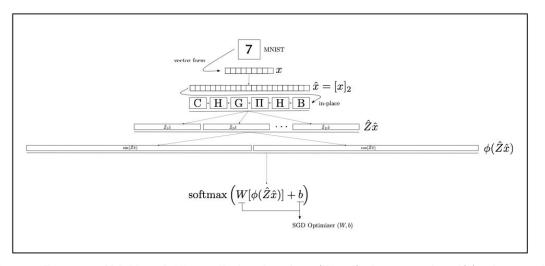
## On the Applicability of the Hadamard as an Input Modulator for Problems of Classification.

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C++ library that includes a complete learning framework.

https://doi.org/10.2 4433/CO.3851581. v1

https://github.com/ curto2/mckernel



c@decurto.be z@dezarza.be

Figure 1: **Diagram of McKernel**. We visually describe softmax  $(W\tilde{x}+b)$  where  $\tilde{x}=\operatorname{mckernel}(x)$ . The original image is padded in form of long vector to the nearest power of 2, mapping  $\hat{Z}$  is applied in-place. Calibration C defines the choice of Kernel. The tensor is expanded by the number of Kernel Expansions E building a network with high compositionality. Finally, use real feature map  $\phi$ , Equation 2. SGD Optimizer finds appropriate weights W and bias b. Compute  $\hat{Z}$  on-the-fly keeping same seed both for training and testing.



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#### **Highlights**

- C++ fast open-source Hadamard that works for any input size. Widely deployed in Signal Processing, Communications and Compressed Sensing.
- Approximate kernel expansions in log-linear time.
- Useful to foster new DL architectures with better human-induced/mathematical priors.
- DL research framework that offers multiple open questions. Domains that could be further explored are: end-to-end training, self-supervised learning, meta-learning, integration with evolution strategies, NAS reducing substantially the search space and many others.

<u>c@decurto.be</u> <u>z@dezarza.be</u> J. de Curtò, I. de Zarzà, Hong Yan, Carlos T. Calafate.
On the applicability of the Hadamard as an input modulator for problems of classification. Software Impacts. 2022. <a href="https://doi.org/10.24433/CO.3851581.v1">https://doi.org/10.24433/CO.3851581.v1</a>





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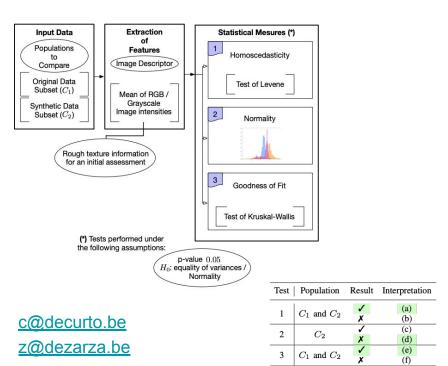
#### **Key contributions:**

- We propose two frameworks to assess GAN convergence based on analytical measures, one based on statistical tests and the other leveraging tools from harmonic analysis (a recently proposed generalization of Fourier).
- The metrics are efficient and effective and can be computed in seconds.

Since its first appearance in 2014, measures to assess GAN convergence have been mainly based on empirical evaluations (MS-SSIM and FID).

Goodfellow, I., Pouget-Abadie, J., Mirza, M., Xu, B., Warde-Farley, D., Ozair, S., Courville, A., Bengio, Y.: Generative adversarial networks. NIPS 27 (2014)





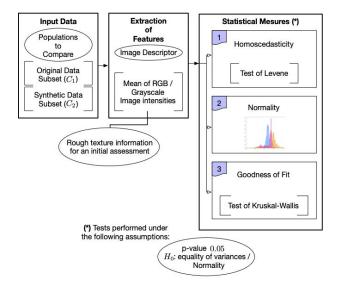


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Description and interpretation of statistical measures are provided in Table I:

- (a) Necessary condition but not sufficient to assert that both populations originate from the same distribution.
- (b) There is not enough statistical evidence to attest both populations samples originate from the same distribution.
- (c) With high probability the synthetic distribution generated is still close enough to the initial distribution of noise from the GAN architecture. The samples may not show enough fidelity, and there is probably bad generalization behavior.
- (d) The synthetic distribution is far from the initial distribution of noise and has deviated from the original Normal, and may be close to the target distribution.
- (e) If (a) then there is enough statistical evidence to confirm that both populations originate from the same distribution given this image descriptor. If (a) is not fulfilled, then we can only ascertain that the synthetic population is a good approximation.
- (f) There is not enough statistical evidence to attest both populations are from the same distribution.







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Table 4: Evaluation of the statistical test measures of homoscedasticity (T1), normality (T2) and goodness of fit (T3) on AFHQ and MetFaces using state-of-the-art pretrained models of Stylegan2-ada [21] and Stylegan3-ada [22] and NASA Perseverance.

Model	Dataset		T1   T2   T3		
Stylegan2-ada	NASA Perseverance		Х	1	X
	AFHQ	Cat	Х	X	1
		Dog	Х	1	X
		Wild	Х	X	1
			Х	X	X
r-Stylegan3-ada	MetFaces		X	X	X
t-Stylegan3-ada			X	X	X

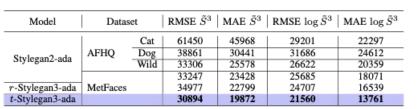


Following [2], the truncated signature of order N of the path  $\mathbf{x}$  is defined as a collection of coordinate iterated integrals

$$S^{N}(\mathbf{x}) = \left( \left( \int \cdots \int_{0 < t_{1} < \cdots < t_{a} < 1} \prod_{c=1}^{a} \frac{\mathrm{d}f_{z_{c}}}{\mathrm{d}t}(t_{c}) \mathrm{d}t_{1} \cdots \mathrm{d}t_{a} \right)_{1 \leq z_{1}, \dots, z_{a} \leq d} \right)_{1 \leq a \leq N}.$$
(1)

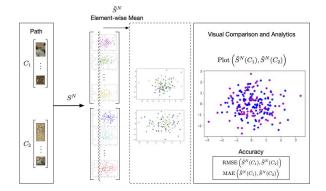
Bonnier, P., Kidger, P., Arribas, I.P., Salvi, C., Lyons, T.: Deep signature transforms. NIPS (2019)

Lyons, T.: Rough paths, signatures and the modelling of functions on streams. Proceedings of the International Congress of Mathematicians (2014)



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**Definition 4.** Given n components of the element-wise mean of the signatures  $\{y^{(c)}\}_{c=1}^n \subseteq T(\mathbb{R}^d)$  from the model chosen as a source of synthetic samples and the same number of components of the element-wise mean of the signatures  $\{x^{(c)}\}_{c=1}^n \subseteq T(\mathbb{R}^d)$  from the original distribution, then we define the Root Mean Squared Error (RMSE) and Mean Absolute Error (MAE) by

$$\text{RMSE}\left(\left\{x^{(c)}\right\}_{c=1}^{n}, \left\{y^{(c)}\right\}_{c=1}^{n}\right) = \sqrt{\frac{1}{n}\sum_{c=1}^{n}\left(y^{(c)} - x^{(c)}\right)^{2}},$$

and

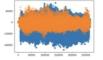
$$\text{MAE}\left(\left\{x^{(c)}\right\}_{c=1}^{n}, \left\{y^{(c)}\right\}_{c=1}^{n}\right) = \frac{1}{n} \sum_{c=1}^{n} |y^{(c)} - x^{(c)}|.$$

The case for log-signature is analogous.

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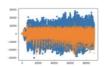


Fig. 8: Spectrum of the element-wise mean of the signatures (left) and log-signatures (right) of order 3 and size  $64 \times 64$  of original ('o') against synthetic ('x') samples.

Model	FID	RMSE $ ilde{S}^3$
Stylegan2-ada	15.22	33247
r-Stylegan3-ada	15.33	34977
t-Stylegan3-ada	15.11	30894



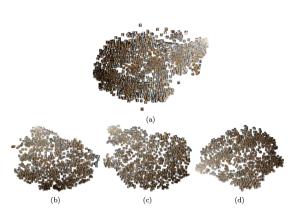


Fig. 14: Visualization of PCA Adaptive t-SNE on original (top) versus synthetic (bottom) samples of MetFaces using Stylegan2-ada (b), r-Stylegan3-ada (c) and t-Stylegan3-ada (d).

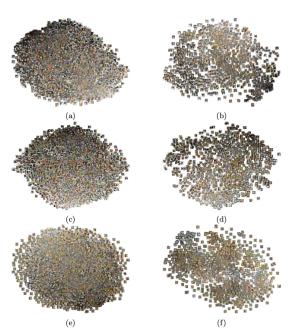


Fig. 13: Visualization of PCA Adaptive t-SNE on original (left) versus synthetic (right) samples of AFHQ Cat (a,b), Dog (c,d) and Wild (e,f) using Stylegan2-ada



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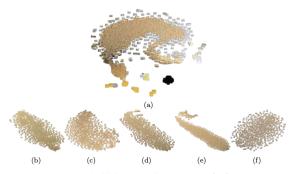


Fig. 15: Visualization of PCA Adaptive t-SNE on original (top) versus synthetic (bottom) samples of NASA Perseverance using Stylegan2-ada across several epoch iterations: 193 (b), 371 (c), 596 (d), 798 (e) and 983 (d).

