# Programming 2 - Assignment 5

Felix Dreßler (k12105003) email FelixDressler<br/>01@gmail.com

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## 1 Testing the Program

### 1.1 Main.cpp

For testing the *Main.cpp* was adapted to work with the new templates.

```
1
   // "Main.cpp"
 2
 3
 4
   // is used to test the functions of Ring and its subclasses.
 5
    // created by: Felix Dressler - 24.05.2022
 6
 7
 8
   #include "Integer.h"
9
   #include "RecPoly.h"
10
11
   #include <iostream>
12
13
   using namespace std;
14
15
   int main() {
16
       //tests from the assignment
        Integer* c[] = { new Integer(-5), new Integer(2), new Integer(0), new Integer(-3) };
17
18
19
       UniPoly* p = new UniPoly("x", 4, c); // p = -3x^3 + 2x - 5
20
        cout << p->str() << endl;
21
22
       UniPoly* q = // q = p+p = -6x^3 + 4x - 10
          p->operator+(p);
23
24
        cout << q->str() << endl;
25
26
        UniPoly* r = // r = p*q = 50 - 40 x + 8 x^2 + 60 x^3 - 24 x^4 + 18 x^6
27
           p->operator*(q);
28
        cout << r->str() << endl;
29
30
       //additional tests
31
32
33
34
        UniPoly* z = //zero polynomial
35
           p->zero();
36
        cout << z->str() << endl;
37
38
        UniPoly* z2 = // = p + 0
39
           p->operator+(z);
40
        cout << z2->str() << endl;
41
42
        UniPoly* z3 = // = p * 0
43
           p->operator*(z);
44
        cout << z3->str() << endl;
45
46
        //negation
47
48
        UniPoly* g = //= -p
           p->operator-();
49
50
        cout << g->str() << endl;
51
        UniPoly* g2 = // = -p + p = 0
52
53
           g->operator+(p);
```

```
54
        cout << g2->str() << endl;
55
56
        //multivariate polynomials
57
        UniPoly* k[] = { p,q };
58
        UniPoly* 1[] = { p };
59
60
61
        BiPoly* s = new BiPoly("y", 2, k);
62
        cout << s->str() << endl;
63
        BiPoly* s2 = new BiPoly("y", 1, 1);
64
        cout << s2->str() << endl;</pre>
65
66
67
        BiPoly* s3 = // s2 + s
68
            s2->operator+(s);
69
        cout << s3->str() << endl;
70
71
        BiPoly* s4 = //s2*s
72
           s2->operator*(s);
73
        cout << s4->str() << endl;
74
75
        return 0;
76
```

#### 1.2 output

## 2 RecPoly.h

```
1
    #pragma once
 2
 3
    #include<string>
 4
    #include<iostream>
 5
    #include"Integer.h"
 6
 7
 8
 9
    using namespace std;
10
11
    template < class Ring > class RecPoly
12
13
   private:
14
        Ring** coeff;
15
        int n;
16
        string var;
17
    public:
18
19
20
        // polynomial with n>=0 coefficients and given variable name
21
        RecPoly(string var, int n, Ring** coeffs) {
            this->var = var;
22
23
24
            int zeros = 0;
25
26
            //cuts of all 0s at the end of the coeffs array
27
            if (n != 0) {
28
                 Ring* z = coeffs[0] \rightarrow zero();
29
```

```
30
                 for (int i = n - 1; i >= 0; i--) {
31
                     if (!(coeffs[i]->operator==(z))) {
32
                         break:
33
34
                     zeros++;
35
36
                 delete z;
37
            }
38
39
            this->n = n - zeros;
40
            this->coeff = new Ring * [n];
41
            for (int i = 0; i < n; i++) {</pre>
                 coeff[i] = coeffs[i] - > clone(); // clone to make sure only we have control over
42
                     the array
43
44
        }
45
46
        // copy constructor, copy assignment operator
47
        RecPoly(RecPoly& p) {
48
            this->var = p.var;
49
            this->n = p.n;
50
            this->coeff = new Ring * [n];
51
52
            for (int i = 0; i < n; i++) {</pre>
53
                coeff[i] = p.coeff[i]->clone();
54
            }
55
        }
56
        RecPoly& operator=(RecPoly& p) {
57
58
            this->var = p.var;
59
            this->n = p.n;
60
            delete[] this->coeff;
61
            this->coeff = new Ring * [n];
62
63
64
            for (int i = 0; i < n; i++) {</pre>
                 coeff[i] = p.coeff[i]->clone();
65
66
67
68
            return *this;
69
        }
70
71
        //destructor for RecPoly
72
        ~RecPoly() {
73
            for (int i = 0; i < this->n; i++) {
74
                 delete coeff[i];
75
76
            delete[] coeff;
77
        }
78
79
        // a heap-allocated duplicate of this element
80
        RecPoly* clone() {
81
82
            return new RecPoly(*this);
83
        }
84
85
        // the string representation of this element
86
        string str() {
87
            string str = "";
88
            if (n == 0) {
```

```
str = "0";
 89
90
             }
91
             else {
92
                 str += "(";
93
                 for (int i = 0; i < n; i++) {</pre>
94
                      if (!(coeff[i]->operator==(coeff[i]->zero()))) {
95
                          str += coeff[i]->str();
96
                          if (i != 0) {
                              str += "*" + var + "^" + to_string(i);
97
98
99
                          if (i < n - 1) {
                              str += "+";
100
101
102
                      }
103
                 }
                 str += ")";
104
105
106
107
             return str;
108
         }
109
110
         // the constant of the type of this element and the inverse of this element
         RecPoly* zero() {
111
112
             return new RecPoly(this->var, 0, {});
113
114
115
         RecPoly* operator-() {
116
117
             Ring** temp = new Ring * [this->n];
118
             for (int i = 0; i < this->n; i++) {
119
120
                 temp[i] = this->coeff[i]->operator-();
121
122
123
             RecPoly* ret = new RecPoly(this->var, this->n, temp);
124
125
             for (int i = 0; i < this->n; i++) {
126
                 delete temp[i];
127
128
             delete[] temp;
129
130
             return ret;
131
         }
132
133
         // sum operator for polynomials
134
         RecPoly* operator+(RecPoly* x) {
135
             if (this->var != x->var) {
136
                 cout << "Error: Addition with incompatible Polynomials performed (wrong
                     variables) " << endl;</pre>
137
                 exit(4);
138
             }
139
140
             else {
141
                 int n_{temp} = max(this->n, x->n);
142
143
                 Ring** temp = new Ring * [n_temp];
144
                 if (this->n == 0) {
145
                      for (int i = 0; i < x->n; i++) {
146
147
                          temp[i] = x->coeff[i]->clone();
```

```
148
149
150
                     RecPoly* add = new RecPoly(this->var, x->n, temp);
151
152
                      for (int i = 0; i < n_temp; i++) {</pre>
153
                          delete temp[i];
154
155
                      delete[] temp;
156
157
                      return add;
158
159
                 else {
160
161
                      for (int i = 0; i < this->n && i < x->n; i++) {
162
                          temp[i] = this->coeff[i]->operator+(x->coeff[i]);
163
164
165
                      if (this->n > x->n) {
166
                          for (int i = x->n; i < this->n; i++) {
167
                              temp[i] = this->coeff[i];
168
169
170
                      else if (this->n < x->n) {
171
                          for (int i = this->n; i < x->n; i++) {
172
                              temp[i] = x->coeff[i];
173
174
                      }
175
176
                     RecPoly* add = new RecPoly(this->var, n_temp, temp);
177
                      //for (int i = 0; i < n_temp; i++) {
178
179
                      // delete temp[i];
180
181
                      //delete[] temp;
182
183
                     return add;
184
                 }
185
             }
186
187
188
189
         // multiplication operator for polynomials
190
         RecPoly* operator*(RecPoly* x) {
191
             if (this->var != x->var) {
192
                 cout << "Error: Multiplication with incompatible Polynomials performed (wrong
                      variables) " << endl;</pre>
193
                 exit(6);
194
             }
195
196
             else {
197
                 if (this->n == 0 || x->n == 0) {
198
                      return this->zero(); // new RecPoly(this->var, 0, {});
199
200
                 else {
201
202
                      int length = this->n + x->n - 1;
203
                     Ring** temp = new Ring * [length];
204
205
206
                      for (int i = 0; i < length; i++) {</pre>
```

3 INTEGER Page 6

```
207
                          temp[i] = x->coeff[0]->zero();
208
                      }
209
                      for (int i = 0; i < this->n; i++) {
210
                          for (int j = 0; j < x->n; j++) {
211
                              Ring* del = temp[i + j];
212
213
                              temp[i + j] = temp[i + j]->operator+(this->coeff[i]->operator*(x)
                                  ->coeff[j]));
214
                              delete del;
215
216
217
218
219
                     RecPoly* mult = new RecPoly(this->var, length, temp);
220
                      for (int i = 0; i < length; i++) {</pre>
221
222
                          delete temp[i];
223
224
                      delete[] temp;
225
226
                      return mult;
227
228
             }
229
230
231
232
         // comparison function for Plynomials
233
        bool operator==(RecPoly* x) {
234
             bool same = true;
235
236
             for (int i = 0; i < this->n; i++) {
                 if (this->coeff[i] != x->coeff[i]) {
237
238
                      same = false;
239
240
241
             return same;
242
243
     };
244
245
    typedef RecPoly<Integer> UniPoly;
246
247
    typedef RecPoly<UniPoly> BiPoly;
```

## 3 Integer

#### 3.1 Integer.h

```
#pragma once

#include<string>
#include<iostream>

using namespace std;

class Integer {
private:
```

3 INTEGER Page 7

```
10
      int n;
   public:
11
12
      // integer with value n (default 0)
13
      Integer(int n = 0);
14
15
      // destructor - empty because in Integer no new arrays/pointers are created
16
      ~Integer() {
17
18
19
      // a heap-allocated duplicate of this element
20
21
      Integer* clone();
22
23
      // the string representation of this element
24
      string str();
25
26
      // the constant of the type of this element and the inverse of this element
27
      Integer* zero();
28
      Integer* operator-();
29
      // sum and product of this element and c
30
31
      Integer* operator+(Integer* c);
32
      Integer* operator*(Integer* c);
33
34
      // comparison function
35
     bool operator==(Integer* c);
36
    };
```

#### 3.2 Integer.cpp

```
1
   #include"Integer.h"
2
    // integer with value n (default 0)
3
4
   Integer::Integer(int n) {
5
       this->n = n;
6
7
8
   // a heap-allocated duplicate of this element
9
   Integer* Integer::clone() {
10
       Integer* c = new Integer(this->n);
11
12
       return c;
13
14
15
   // the string representation of this element
16
   string Integer::str() {
17
18
       return to_string(this->n);;
19
20
21
   // the constant of the type of this element and the inverse of this element
22
   Integer* Integer::zero() {
23
24
       return new Integer(0);
25
26
27
   Integer* Integer::operator-() {
28
```

3 INTEGER Page 8

```
29
        return new Integer(-(this->n));
30
   }
31
32
   // sum and product of this element and c
33
   Integer* Integer::operator+(Integer* x) {
34
35
        int t = this->n + x->n;
36
37
        return new Integer(t);
38
39
40
   Integer* Integer::operator*(Integer* x) {
41
42
        return new Integer(this->n * x->n);
43
44
45
    // comparison function
46
   bool Integer::operator==(Integer* x) {
47
48
        if (this->n == x->n) {
49
            return true;
50
51
        else {
52
            return false;
53
54
55
```