NumPy

Solve the following exercises and upload your solutions to Moodle until the specified due date. Make sure to use the *exact filenames* that are specified for each individual exercise. Unless explicitly stated otherwise, you can assume correct user input and correct arguments.

Exercise 1 - Submission: ex1.py

30 Points

Write a function extend(arr: np.ndarray, size: int, fill=None) -> np.ndarray that extends a 1D array arr to a given size size using the fill value determined by fill and returns this new array. The original arr must not be changed. The function works as follows:

- If arr is not 1D, a ValueError must be raised.
- If size is smaller than the 1D array, a ValueError must be raised.
- size determines the size of the new, extended array, where all elements from arr are copied and the new elements at the end are filled according to fill (see below). More specifically, the new array content is [a1, a2, ..., an, f, f, ..., f], where ai are the elements of arr and f is the fill value. Note that size can be equal to the size of arr, in which case a new array is still created and arr is copied, but there are no new elements f that need to be filled.
- fill determines which value is used to fill up the extended array. An arbitrary value can be chosen (you can assume the user chooses a value compatible with the array data type). However, there are two special cases:
 - fill=None: In this case, no fill value should be used, i.e., the new, extended array elements might have arbitrary/uninitialized data.
 - fill="mean": If the array has a numeric data type, the mean value of arr should be used as fill value. Otherwise (array is not numeric), it is just a regular string fill value.
- The new, extended array must be returned. It must have the same data type as arr.

Example program execution:

```
print(extend(np.arange(4), 7))
print(extend(np.arange(4), 7, fill=0))
print(extend(np.arange(4), 7, fill="mean"))
print(extend(np.arange(4, dtype=float), 7, fill="mean"))
print(extend(np.array([/hello", "world"]), 5, "mean"))
Example output (first output might vary):
                                        3 125632899 41684340 42140028]
[0 1 2 3 0 0 0]
Γ0 1 2 3
         1 1 1]
     1.
             3.
                     1.5 1.5]
['hello'
         'world'
                  'mean' 'mean'
```

Hints:

- The functions np.empty_like and np.full_like might be helpful.
- To determine whether an array arr has a numeric data type, you can use the function np.issubdtype(arr.dtype, np.number), according to the NumPy type hierarchy.

Exercise 2 – Submission: ex2.py

20 Points

Write a function matrix_stats(matrix: np.ndarray) -> dict that computes summary statistics for a 2D array/matrix. The function works as follows:

- If matrix is not 2D, a ValueError must be raised.
- The function returns a dictionary with the following entries:
 - "total_sum: The sum of all elements of matrix.
 - "row_sums: A NumPy array containing the sums of each row in matrix.
 - "column_sums: A/NumPy array containing the sums of each column in matrix.

Example program execution:

```
print(matrix_stats(np.arange(3 * 4).reshape(3, 4)))
Example output:
{'total_sum': 66, 'row_sums': array([ 6, 22, 38]),
   'column_sums': array([12, 15, 18, 21])}
```

Exercise 3 – Submission: ex3.py

20 Points

Write a function create_data(setups: list[dict], seed=None) -> dict that creates random-ized data arrays in the following way:

- setups specifies a list of dictionaries, where each such dictionary has the following entries:
 - "id": The ID of the randomized data array to create.
 - "n": The shape of the randomized data array to create. Can be an integer or a tuple of the form (d1, d2, ..., dn), where di is a dimension entry.
 - "a": Specifies the lower (inclusive) bound of the range [a, b), from which random elements are sampled.
 - "b": Specifies the upper (exclusive) bound of the range [a, b), from which random elements are sampled.
- For each dictionary in setup, a new randomized NumPy array must be created. The array has the shape n, and its elements must be drawn from a uniform distribution specified by [a,b). The data type must be some floating point data type (which one does not matter, e.g., both np.float32 and np.float64 are fine).
- seed is used to initialize the seed of the random number generator.
- The function must return a dictionary where the keys are the respective IDs (id) and the values the created arrays (according to n, a and b).

```
Example program execution:
```

```
for id_, arr in create_data([
    {"id" "classA", "n": 10, "a": 0, "b": 1.5}, {"id" "classB", "n": 20, "a": 3, "b": 4},
    {"id": "classC", "n": (5, 10), "a": 0, "b": 10}
], 0).items():
   print(id_, arr.shape)
   print(arr)
Example output (randomization might vary depending on the version of NumPy):
classA (10.)
[0.95544253 0.40468007 0.06146029 0.02479145 1.21990536 1.36913337
0.90995366 1.09424484 0.81543749 1.40260864]
classB (20,)
[3.81585355 3.0027385 3.85740428 3.03358558 3.72965545 3.17565562
 3.86317892 3.54146122 3.29971189 3.42268722 3.02831967 3.12428328
3.67062441 3.64718951 3.61638511 3.38367755 3.99720994 3.98083534
3.68554198 3.65045928]
classC (5, 10)
[[6.88446731 3.88921424 1/.35096505 7.2148834 5.25354322 3.10241876
  4.85835359 8.89487834 9.34043516 3.57795197]
 [5.71529831 3.21869391 5.9430003 3.37911226 3.91619001 8.90274352
 2.27157594 6.23187145 0.84015344 8.32644148]
 [7.87098307 2.39369443 8.76484231 0.58568035 3.36117061 1.50279467
  4.50339367 7.3632427 2.30642209 0.52021301]
```

[6.29108152 9.27154553 4.40377155 9.54590494 4.99895814 4.25228625

Exercise 4 – Submission: ex4.py

1.99515444 9.42113111 3.65110168 1.0549528]

6.20213452 9.95096505 9.48943675 4.60045139]]

30 Points

Write a function

```
create_minefield(
    rows: int,
    cols: int,
    n_mines: int,
    seed=None
) -> np.ndarray
```

that creates an array which could be used to implement the game Minesweeper. In Minesweeper, the goal is to uncover all cells of a 2D grid (=the minefield) that are not mines. Such a minefield can, for instance, be represented as a 2D integer array, where a value of -1 represents a mine cell and a value ≥ 0 a non-mine cell. The value x of a non-mine cell indicates how many mines there are in its neighboring cells, where "neighboring" is defined as the 8 surrounding cells (visualized with -):

```
- x -
```

We can also define the minefield via the mine cells: A mine cell increments the values of all neighboring cells by 1 (except if a neighboring cell is a mine cell itself). Out-of-grid cells are simply ignored.

Either definition is fine, they result in the same minefield output array. Here is an example of a 7×7 minefield with 3 mines (character m; left) and the resulting 2D integer array (right):

```
0 ]]
       0
          0
              0
                  0
                     0
                         0]
 Γ0
                  0
                         01
       0
              0
 Γ0
              1
 [ 0
       1
              2 - 1
                         01
 [ 0
       1 -1
              3
                  2
                         01
 [ 0
       1
              2 - 1
                         0]
          1
                         0]]
 [ 0
       0
          0
              1
                     1
                  1
```

Your task is to implement the above function so that it returns such 2D integer minefield arrays. The function works as follows:

- rows specifies the number of rows of the minefield. If rows is smaller than 2, a ValueError must be raised.
- cols specifies the number of columns of the minefield. If cols is smaller than 2, a ValueError must be raised.
- n_mines specifies the number of mines that should be randomly placed on the minefield (=number of mine cells). If n_mines is smaller than 1 or ≥ rows·cols, a ValueError must be raised. Mines must be placed on different cells, i.e., a single cell can only contain a single mine.
- seed is used to initialize the seed of the random number generator.
- The function must return a 2D array of data type int.

Example function calls and results (randomization might vary depending on the version of NumPy):

```
create_minefield(7, 7, 3, 0) =
                                                create_minefield(7, 7, 1, 0) =
0 0]]
          0
             0
                 0
                    0
                        07
                                                0 ]]
                                                       0
                                                          0
                                                              0
                                                                 0
                                                                     0
                                                                        07
 0 ]
      0
                                                   0
          0
             0
                 0
                        0]
                                                  0
                                                          0
                                                                 0
                                                                        0]
                    0
                                                              0
                                                                     0
   0
                                                    0
      0
          0
             1
                 1
                    1
                        0]
                                                       0
                                                           0
                                                              0
                                                                 0
                                                                     0
                                                                         0]
             2
 0
      1
          1
               -1
                    1
                        07
                                                    0
                                                       0
                                                          0
                                                              0
                                                                 0
                                                                     0
                                                                         07
  0
                 2
                    2
      1 -1
             3
                        0]
                                                   0
                                                       0
                                                          0
                                                              0
                                                                 0
                                                                     1
                                                                         17
      1
          1
             2
               -1
                    1
                        0]
                                                       0
                                                           0
      0
          0
             1
                 1
                    1
                        011
                                                  ΓΟ
                                                       0
                                                                 0
                                                                         177
create_minefield(7, 7, 20, 0) =
                                                create_minefield(7,
                                                                       7, 5, 2) =
[[-1 -1 -1 2
                                                0 ]]
                                                       0
                                                          0
                 1
                    1 -1]
                                                              0
                                                                 2 -1
                                                                        2]
 [ 3 -1 5 -1
                 2
                                                  [ 1
                                                                  2 -1
                                                                        3]
                    2
                                                       1
                                                           0
 [ 2
     3 -1
             3
                 4 -1
                        2]
                                                  [-1
                                                       1
                                                           0
                                                              0
                                                                  1
                                                                       -1]
 [-1 3
          3
             4 - 1 - 1
                        2]
                                                  [ 1
                                                       1
                                                          0
                                                              0
                                                                 0
                                                                         1]
 [ 2 -1
          3 - 1 - 1
                    4
                        1]
                                                    0
                                                       1
                                                           1
                                                              1
                                                                        0]
      3 -1
             6
               -1
                    4
                        1]
                                                  [ 0
                                                       1
                                                          -1
                                                              1
                                                                 0
                                                                     0
                                                                        07
     2 2 -1 -1 -1
                        1]]
                                                  ΓΟ
                                                       1
                                                              1
                                                                        011
```

Hints:

- Take a look at the random number generator NumPy documentation for useful methods.
- The implementation is up to you, but try to utilize NumPy's functionality such as broadcasting.