

2.5 mamy $S(x_k) = ax_k + b$

x_k	0	10	20	30	40	80	90	95
$S(x_k)$	68.0	67.1	66.4	65.6	64.6	61.8	61.0	62.0

rozwiązujemy metody 2 iloczynami skalarnymi

$$f_1 = 1 \quad f_2 = x$$

$$\begin{bmatrix} \langle 1, 1 \rangle & \langle 1, x \rangle \\ \langle x, 1 \rangle & \langle x, x \rangle \end{bmatrix} \begin{bmatrix} b \\ a \end{bmatrix} = \begin{bmatrix} \langle 1, S \rangle \\ \langle x, S \rangle \end{bmatrix}$$

$$\langle 1, 1 \rangle = \sum_{i=0}^7 1(x_i) \cdot 1(x_i) = 8$$

$$\langle 1, x \rangle = \langle x, 1 \rangle = \sum_{i=0}^7 x_i \cdot 1 = ~~365~~ 365$$

$$\langle x, x \rangle = \sum_{i=0}^7 x_i \cdot x_i = ~~26525~~ 26525$$

$$\langle 1, S \rangle = \sum_{i=0}^7 S(x_i) = 514,5$$

$$\langle x, S \rangle = \sum_{i=0}^7 x_i \cdot S(x_i) = 22685$$

$$86 + 365a = 514,5$$

$$365b + 22685a = 22685$$

$$b = \frac{514,5 - 365a}{8}$$

$$23474,0625 - 16653,125a + 22685a = 22685 \quad a = 22685$$

$$b = 67,96$$

$$9871,875a = -789,0625$$

$$a = -0,08$$

$$b = 65,25$$