

```

(struct state (point  $\sigma$   $\kappa$ ) #:transparent)
(struct ar (e p) #:transparent)
(struct fn (v) #:transparent)
(struct mt () #:transparent)
(struct rt (ctx) #:transparent)
(struct ref (x) #:transparent)
(struct app (e0 e1) #:transparent)
(struct lam (x e) #:transparent)
(define-values (F R Seen M  $\Xi$ )
  (values (mutable-set) (mutable-set) (mutable-set)
    (make-hash) (make-hash)))
(define (hash-add h k v)
  (hash-set h k (set-add (hash-ref h k (set)) v)))
(define (hash-add! h k v)
  (hash-set! h k (set-add (hash-ref h k (set)) v)))
(define (add-state! s)
  (unless (set-member? Seen s)
    (set-add! F s)
    (set-add! Seen s)))
(define (add-reduction! s0 s1)
  (set-add! R (cons s0 s1))
  (add-state! s1))
(define (step s)
  (match s
    [(state (cons (ref x) p)  $\sigma$   $\kappa$ )
     (for ([v (in-set (hash-ref  $\sigma$  (hash-ref p x)))]
       (add-reduction! s (state v  $\sigma$   $\kappa$ )))]
    [(state (cons (app e0 e1) p)  $\sigma$   $\kappa$ )
     (add-reduction! s
       (state (cons e0 p)  $\sigma$  (cons (ar e1 p)  $\kappa$ )))]
    [(state v  $\sigma$  (cons (ar e p)  $\kappa$ ))
     (add-reduction! s
       (state (cons e p)  $\sigma$  (cons (fn v)  $\kappa$ )))]
    [(state v  $\sigma$  (cons (fn (cons (lam x e) p))  $\kappa$ ))
     (define a (alloc s))
     (define  $\rho^*$  (hash-set p x a))
     (define  $\sigma^*$  (hash-add  $\sigma$  a v))
     (define ctx (list e  $\rho^*$   $\sigma^*$ ))
     (hash-add!  $\Xi$  ctx  $\kappa$ )
     (match (hash-ref M ctx #f)
       [#f
        (add-reduction! s
          (state (cons e  $\rho^*$ )  $\sigma^*$  (rt ctx)))]
       [results
        (for ([r (in-set results)])
          (match-define (cons v*  $\sigma^{**}$ ) r)
          (add-state! (state v*  $\sigma^{**}$   $\kappa$ )))]
       [(state v  $\sigma$  (rt ctx))
        (hash-add! M ctx (cons v  $\sigma$ ))
        (for ([ $\kappa$  (in-set (hash-ref  $\Xi$  ctx))])
          (add-reduction! s (state v  $\sigma$   $\kappa$ )))]))]
    [(state v  $\sigma$  (rt ctx))
     (hash-add! M ctx (cons v  $\sigma$ ))
     (for ([ $\kappa$  (in-set (hash-ref  $\Xi$  ctx))])
       (add-reduction! s (state v  $\sigma$   $\kappa$ )))]))]
(define (analyze e)
  (set-clear! F) (set-clear! R) (set-clear! Seen)
  (hash-clear!  $\Xi$ ) (hash-clear! M)
  (set-add! F (state (cons e (hash)) (hash) (mt)))
  (let loop ()
    (unless (set-empty? F)
      (define  $\varsigma$  (set-first F))
      (set-remove! F  $\varsigma$ )
      (step  $\varsigma$ )
      (loop)))
  'the final system
  (list R M  $\Xi$ ))

```