

Problem 1. Rewriting the problem in standard form:

$$\begin{array}{ll} \min & -e^{-w^T x} \\ \text{s.t} & w^T A w - w^T A y - w^T x \leq -a \\ & y^T w - w^T x = b \end{array}$$

Problem 5. Let m be the number of milk bottles and k be the number of knobs. Then

$$\begin{array}{ll} \min & -(0.07m + 0.05k) \\ \text{s.t} & 4m + 3k \leq 240,000 \\ & 2m + 1k \leq 6000 \end{array}$$

Problem 6. Solving for the critical points:

$$\begin{aligned} f(x, y) &= 2x^2y + 4xy^2 + xy \\ f_x &= 4xy + 4y^2 + y \\ f_y &= 2x^2 + 8xy + x \\ f_{xx} &= 4y \\ f_{yy} &= 8x \\ f_{xy} &= f_{yx} = 4x + 8y + 1 \end{aligned}$$

Set $f_y = 0$, then

$$2x^2 + 8xy + x = 0 \Rightarrow x(2x^2 + 8y + 1) = 0 \Rightarrow x = 0, y = \frac{-2x^2 - 1}{8}$$

Set $f_x = 0$, then

$$\begin{aligned} 4xy + 4y^2 + y &= 0 \\ x = 0 \Rightarrow y(4y + 1) &= 0 \Rightarrow y = 0, -\frac{1}{4} \end{aligned}$$

Problem 11. Let $f(x) = ax^2 + bx + c$ where $a > 0$ and $b, c \in \mathbb{R}$.

Problem 14.