



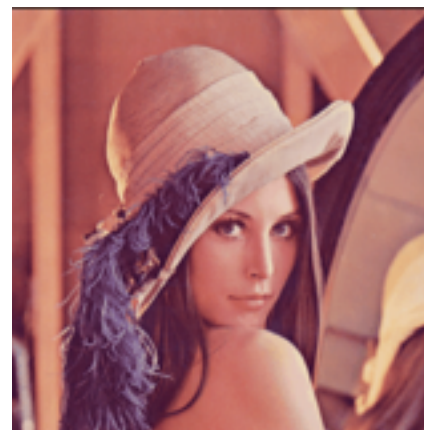
# EE 604

# Digital Image Processing

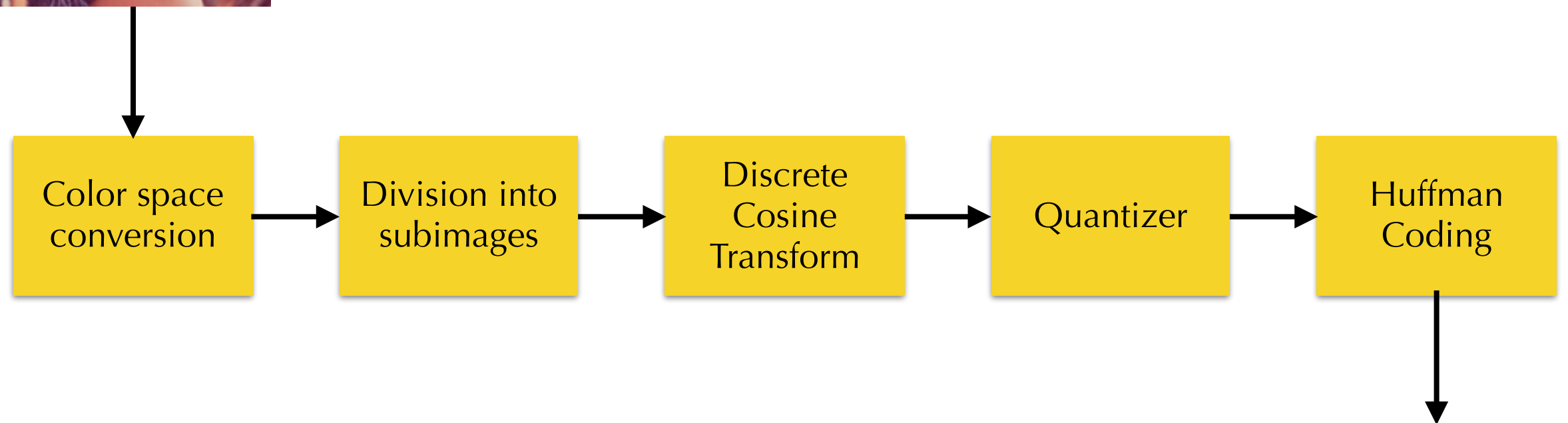
# JPEG Compression

- JPEG stands for **Joint Photographic Experts Group**
- JPEG is a compression algorithm, NOT a file format.
- JPEG is standardized, first issued in 1992.
- JPEG is a lossy compression.

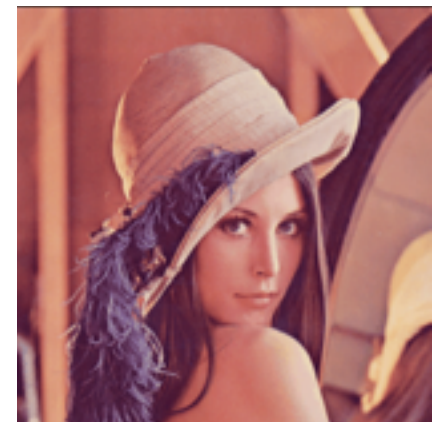
# JPEG Compression



Original



Compressed



# Huffman Coding

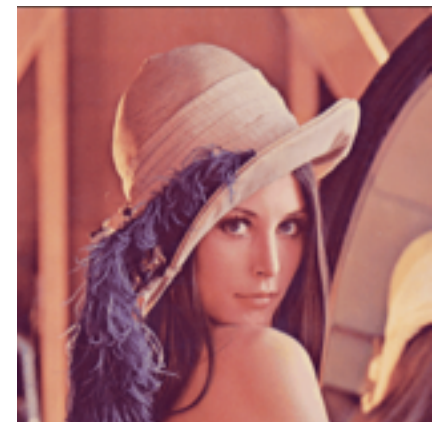


Original

Huffman  
Coding



Compressed



# Huffman Coding

- Introduced by Huffman in 1952
- Produces **variable-length** code to achieve compression
- **Optimal** for single symbol coding
- Uniquely decodable
- Prefix (free) code

# Huffman Coding

Symbol	Probability
$a_4$	0.6
$a_1$	0.2
$a_2$	0.1
$a_3$	0.05
$a_5$	0.05

Symbol	Probability	Assigned Code
$a_4$	0.6	0
$a_1$	0.2	10
$a_2$	0.1	110
$a_3$	0.05	1110
$a_5$	0.05	1111

see class notes for details

# Color space conversion



Original

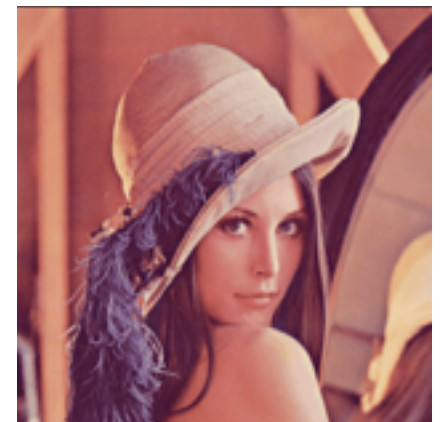


Color space  
conversion

Huffman  
Coding



Compressed

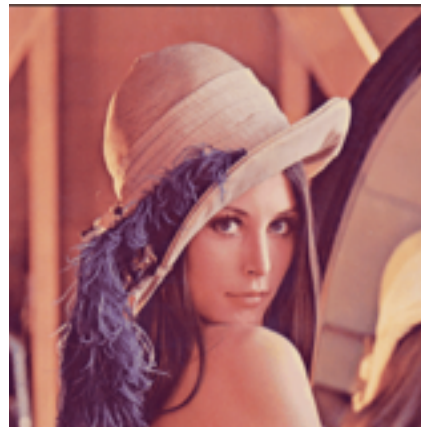


# Color space conversion

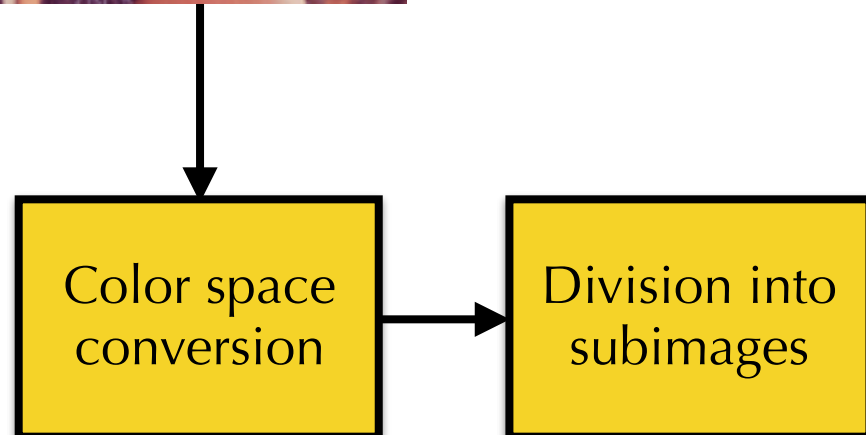
- Convert **RGB** to **YCbCr**
  - Y : luminance channel  $C_B$ ,  $C_R$  : color channels
  - Separate brightness and color components
- Resolution of  $C_B$  and  $C_R$  are then reduced by a factor of 2 or more (downsampling). So, greater compression can be achieved.
- This takes advantage of the fact that humans are less sensitive to color details than intensity details.
- This step is skipped when highest quality is required.



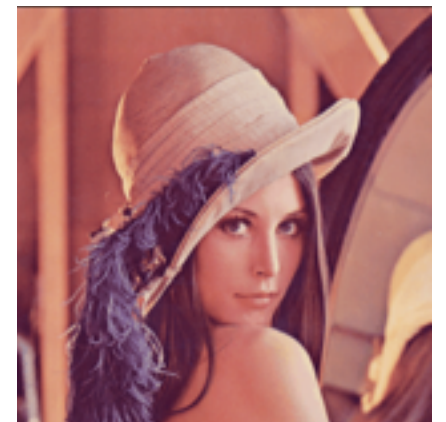
# JPEG Compression



Original

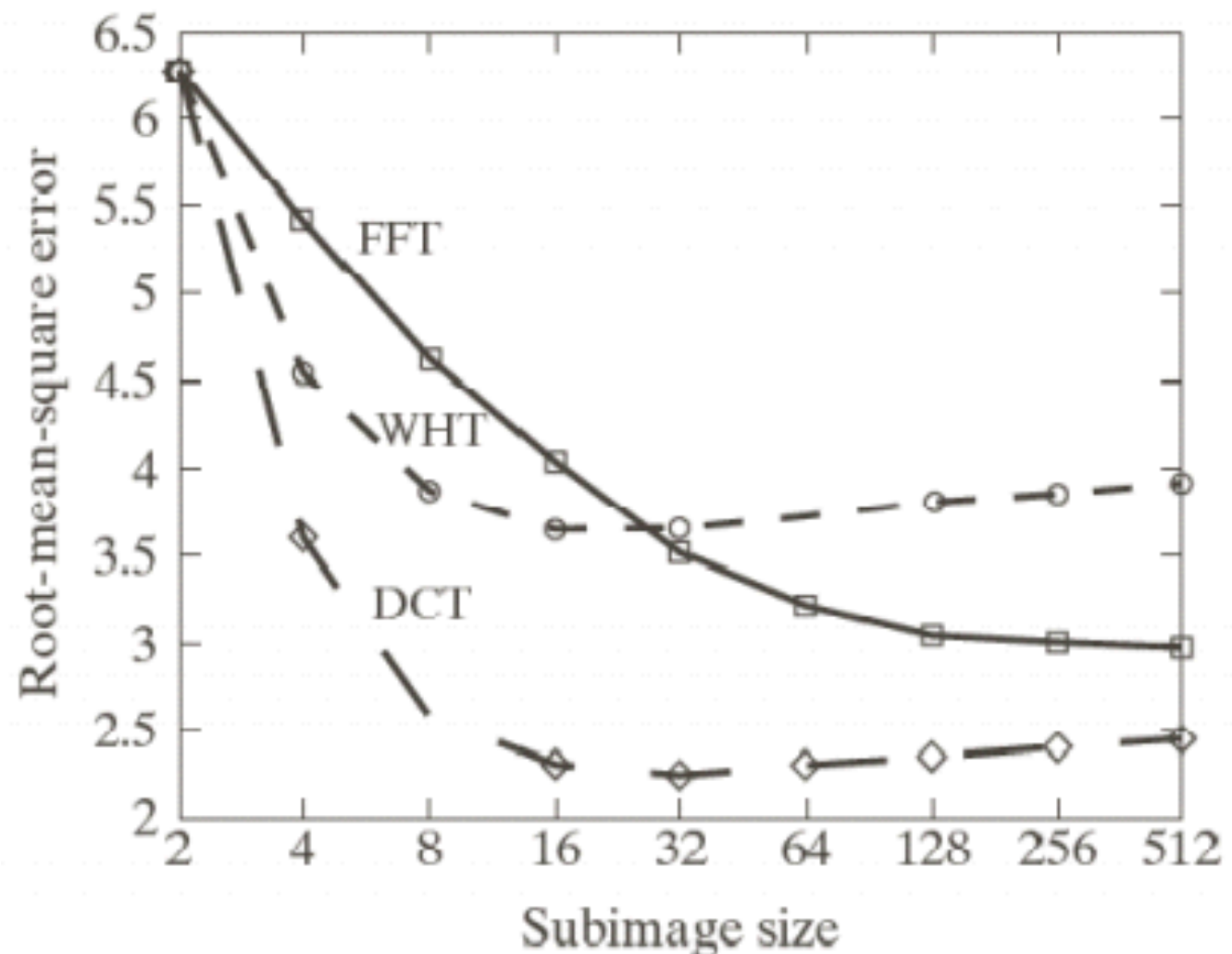


Compressed

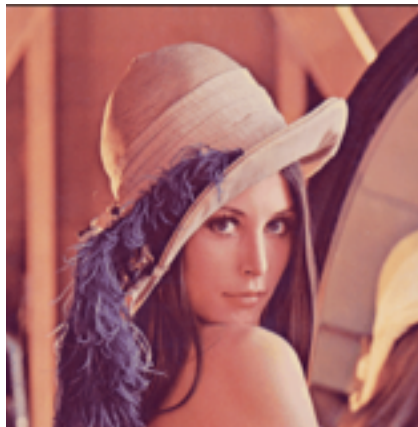


# Subimage size selection

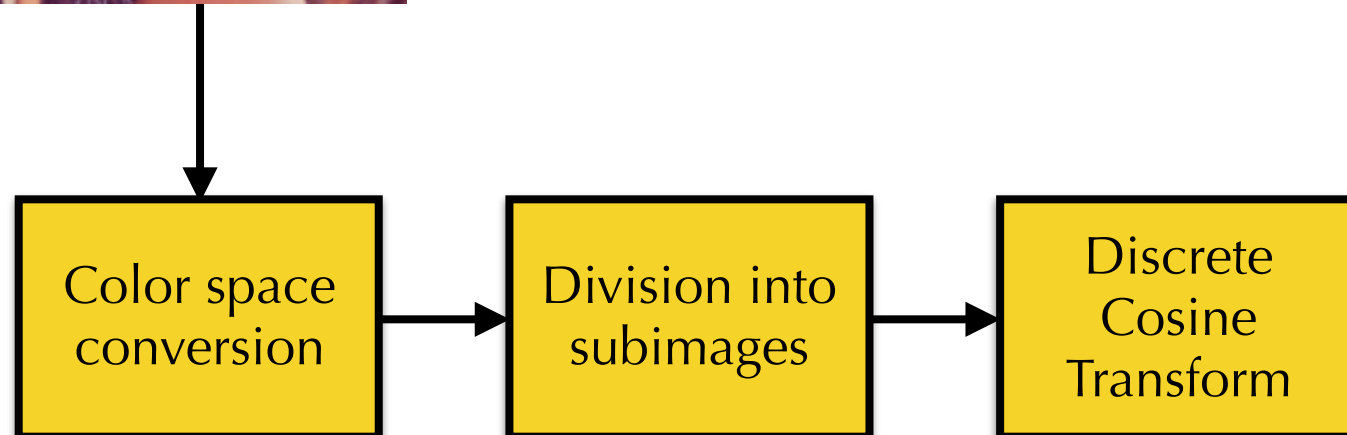
- Image is split into 8x8 or 16x16 blocks or subimages
- Each subimage is called minimum coded unit or macroblock.



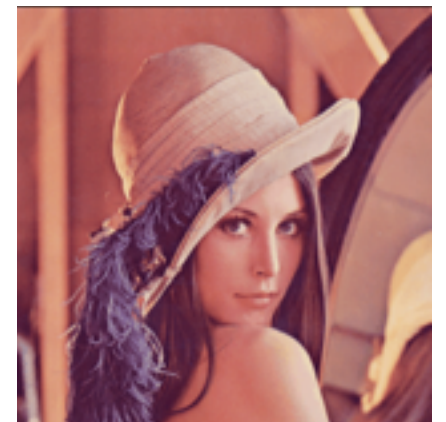
# DCT Transform



Original



Compressed



# Discrete Cosine Transform

## Discrete Cosine Transform

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Published in:

- Journal  
IEEE Transactions on Computers [archive](#)  
Volume 23 Issue 1, January 1974  
Pages 90-93  
IEEE Computer Society Washington, DC, USA  
[table of contents](#) doi> [10.1109/T-C.1974.223784](#)



1974 Article

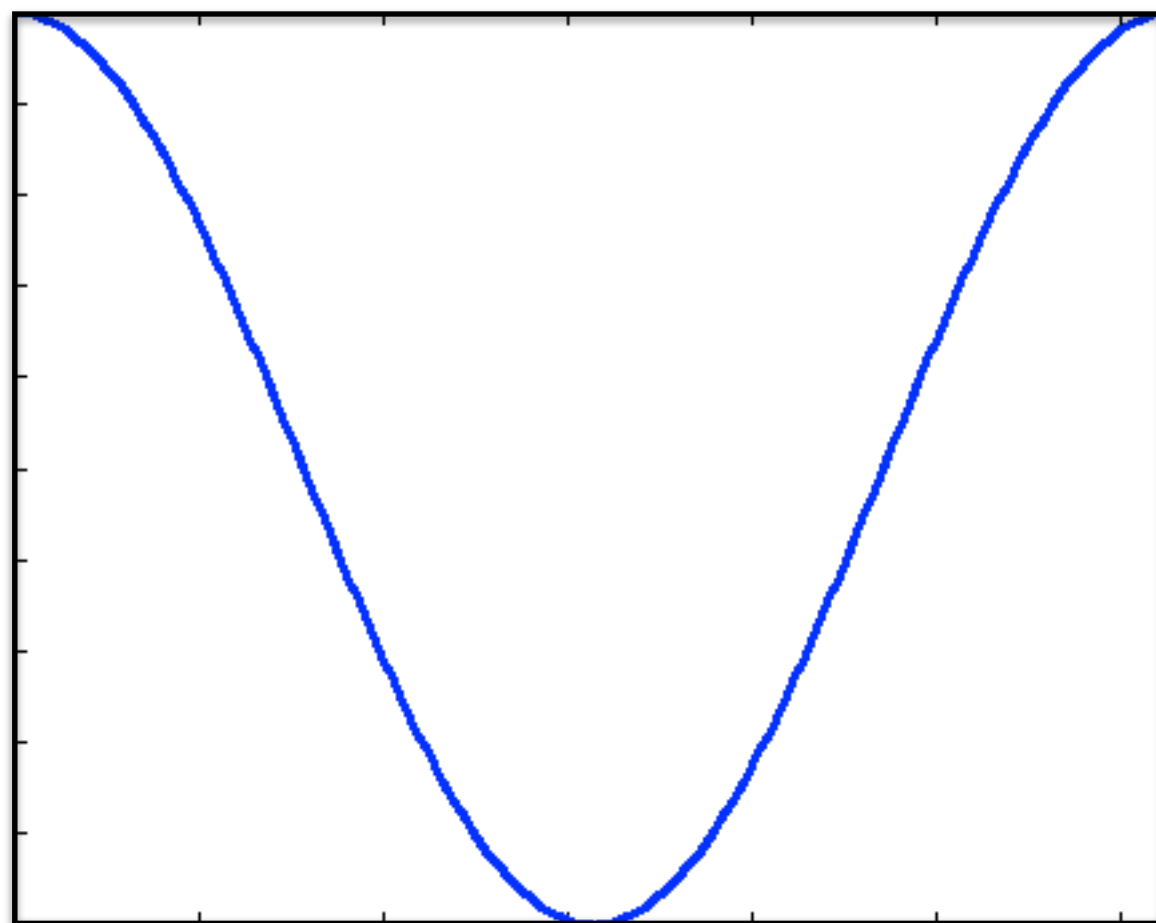
- orig-research



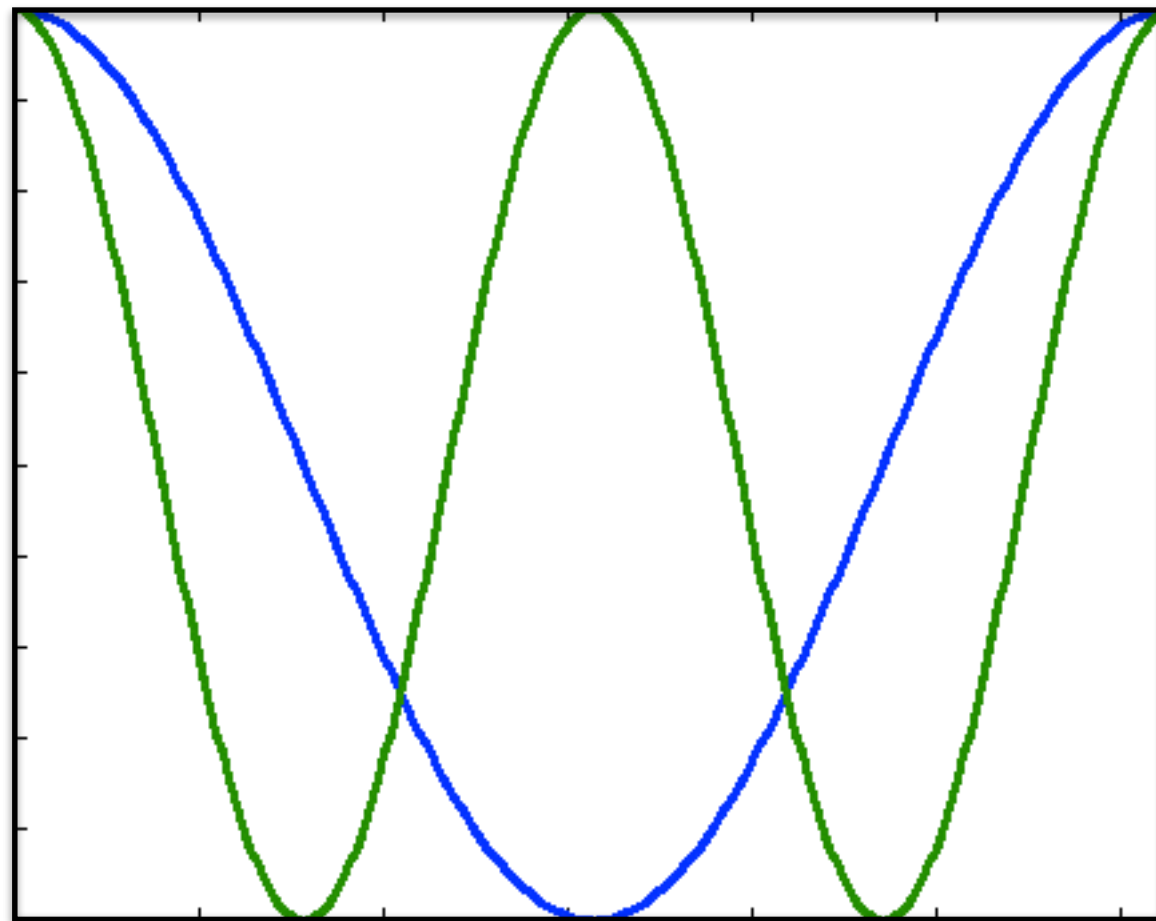
### [Bibliometrics](#)

- Downloads (6 Weeks): 0
- Downloads (12 Months): 0
- Downloads (cumulative): 0
- Citation Count: 189

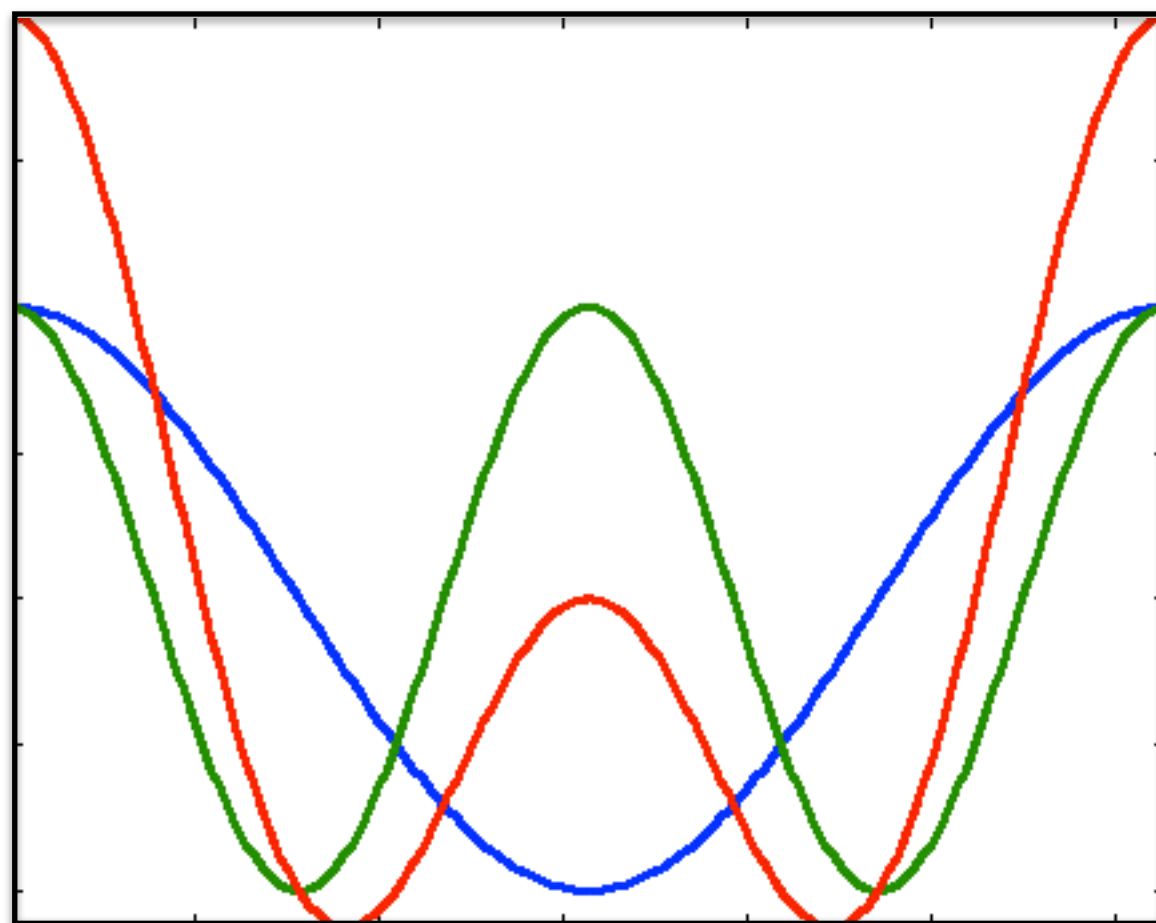
# 1D DCT Basis



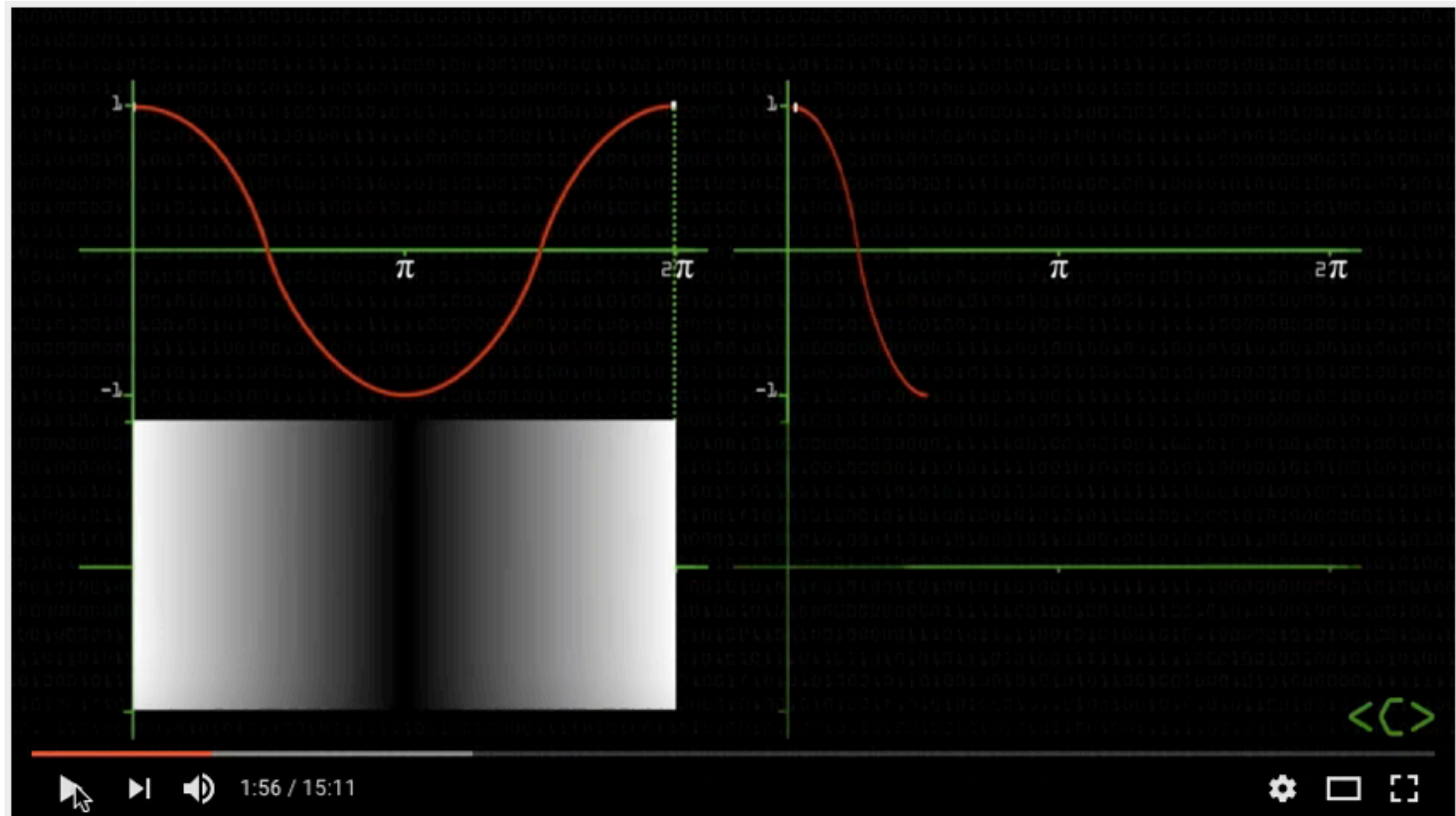
# 1D DCT Basis



# 1D DCT Basis



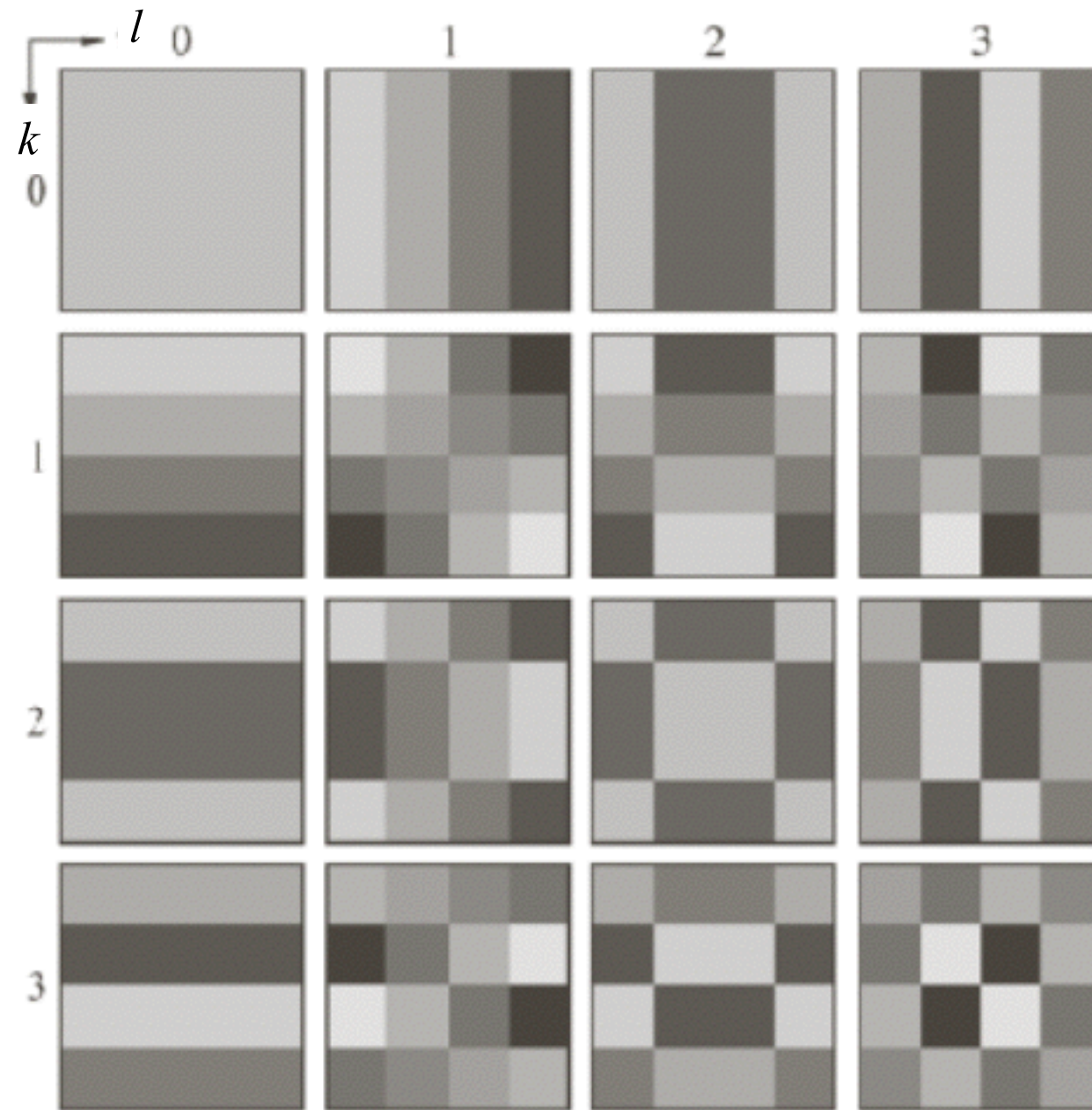
# DCT Basis



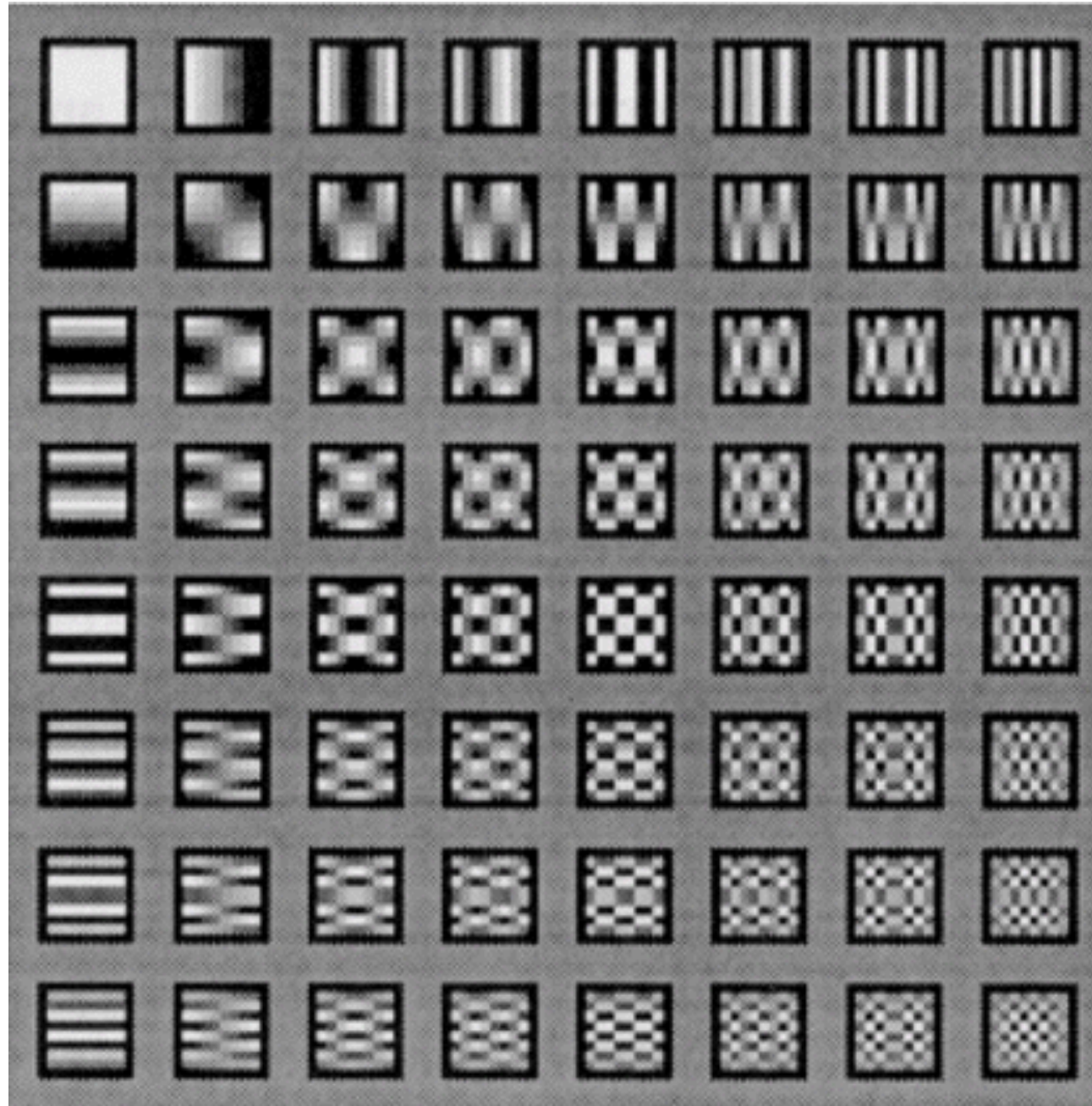
see class notes for the mathematical details



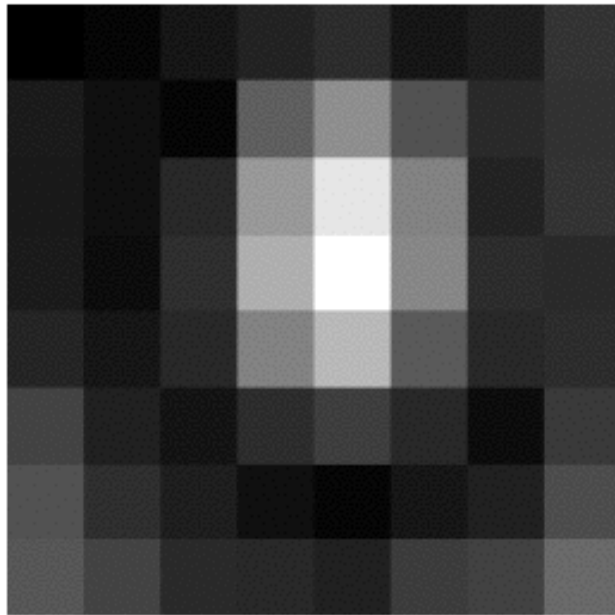
# DCT Basis ( $N = 4$ )

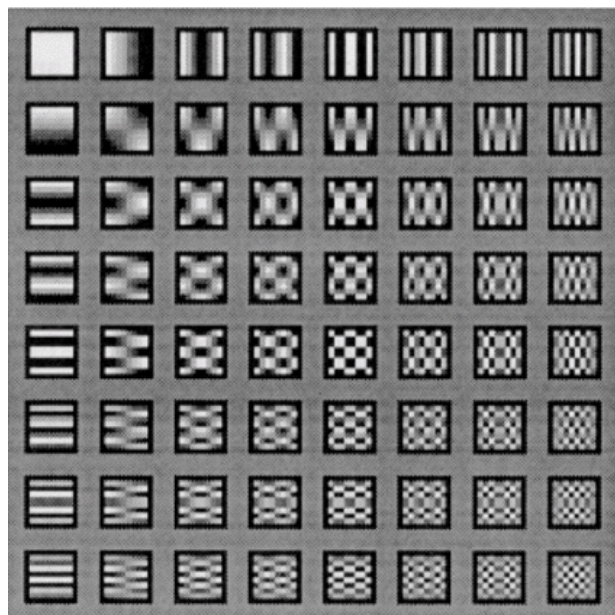


# DCT Basis ( $N = 8$ )



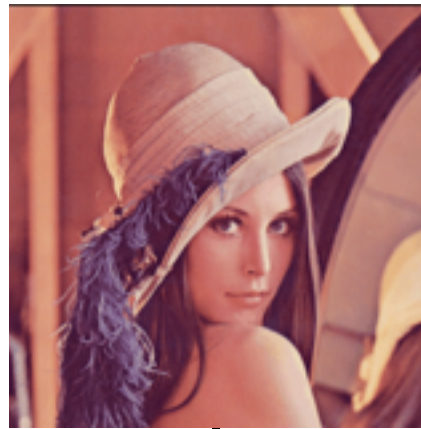
# DCT Transform



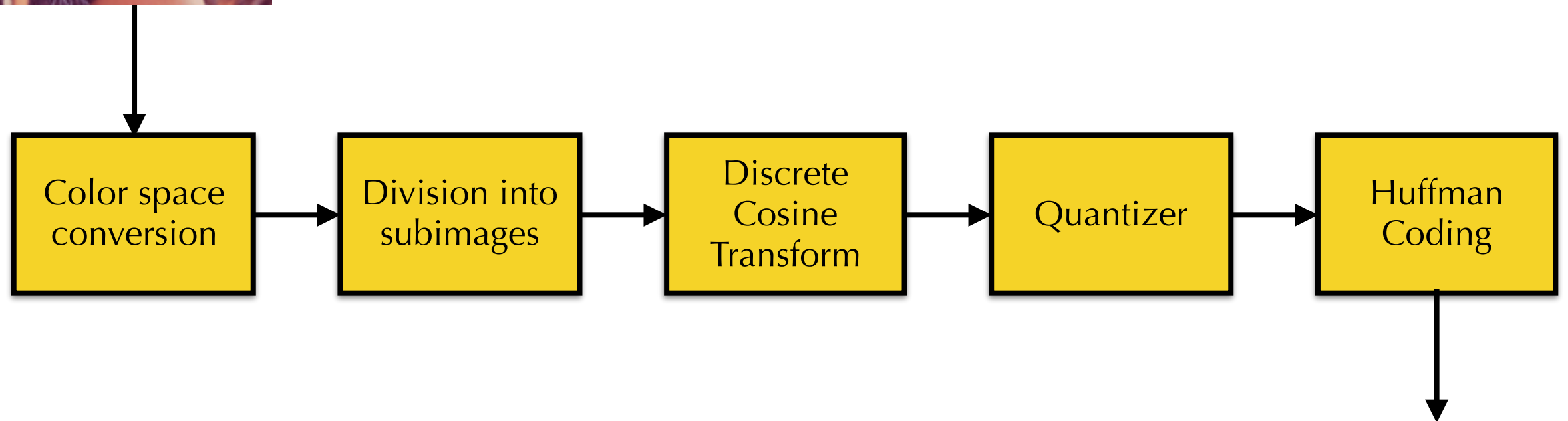
$$\begin{bmatrix} 52 & 55 & 61 & 66 & 70 & 61 & 64 & 73 \\ 63 & 59 & 55 & 90 & 109 & 85 & 69 & 72 \\ 62 & 59 & 68 & 113 & 144 & 104 & 66 & 73 \\ 63 & 58 & 71 & 122 & 154 & 106 & 70 & 69 \\ 67 & 61 & 68 & 104 & 126 & 88 & 68 & 70 \\ 79 & 65 & 60 & 70 & 77 & 68 & 58 & 75 \\ 85 & 71 & 64 & 59 & 55 & 61 & 65 & 83 \\ 87 & 79 & 69 & 68 & 65 & 76 & 78 & 94 \end{bmatrix}$$


$$\begin{bmatrix} -415 & -30 & -61 & 27 & 56 & -20 & -2 & 0 \\ 4 & -22 & -61 & 10 & 13 & -7 & -9 & 5 \\ -47 & 7 & 77 & -25 & -29 & 10 & 5 & -6 \\ -49 & 12 & 34 & -15 & -10 & 6 & 2 & 2 \\ 12 & -7 & -13 & -4 & -2 & 2 & -3 & 3 \\ -8 & 3 & 2 & -6 & -2 & 1 & 4 & 2 \\ -1 & 0 & 0 & -2 & -1 & -3 & 4 & -1 \\ 0 & 0 & -1 & -4 & -1 & 0 & 1 & 2 \end{bmatrix}$$

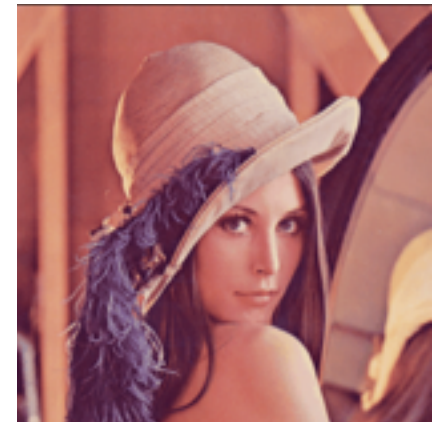
# Qunatization



Original

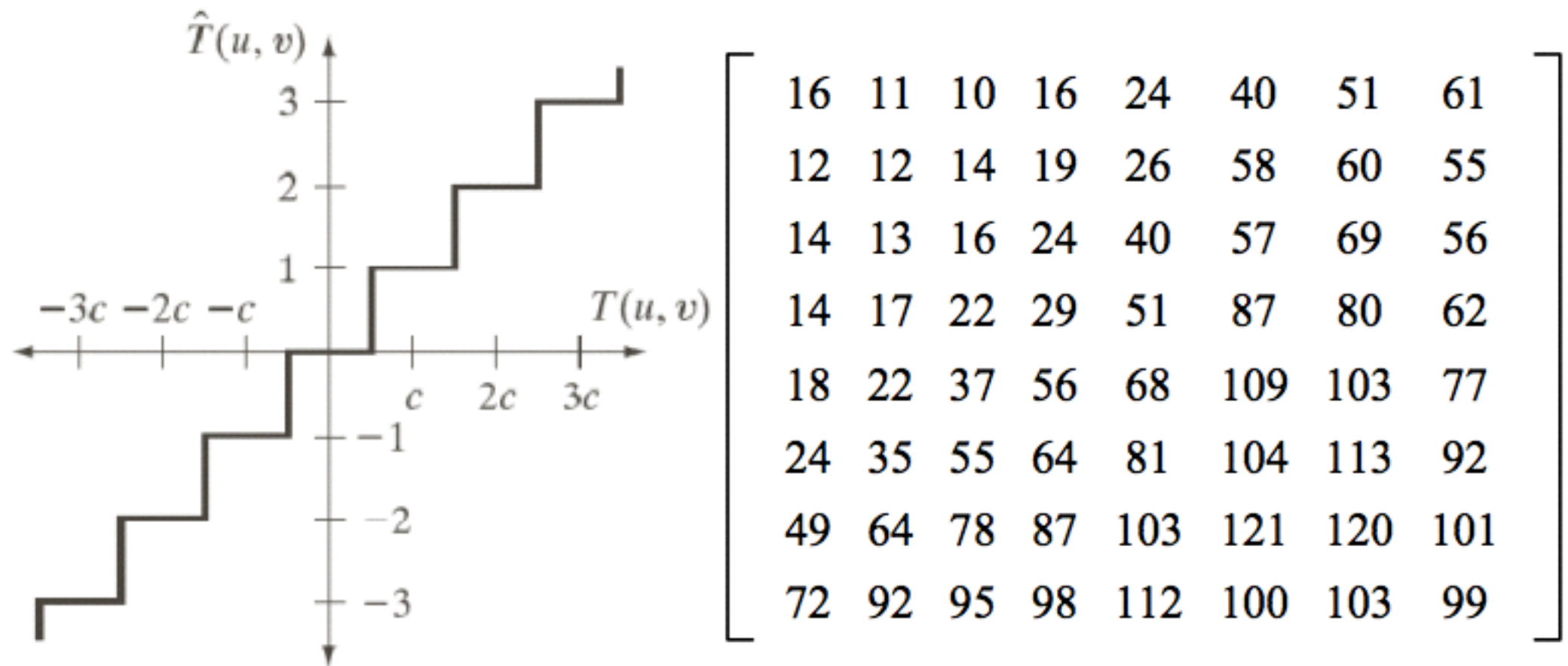


Compressed





# Quantizer



# Quantizer

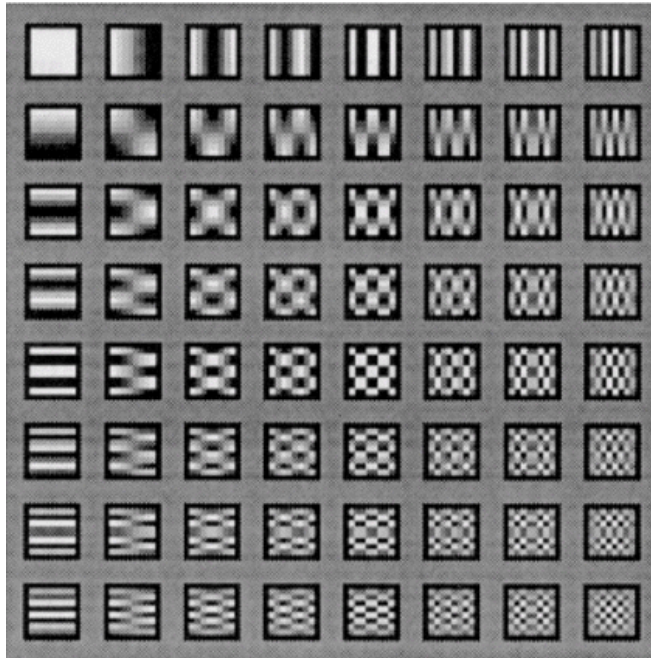
$$Q_{50} = \begin{bmatrix} 16 & 11 & 10 & 16 & 24 & 40 & 51 & 61 \\ 12 & 12 & 14 & 19 & 26 & 58 & 60 & 55 \\ 14 & 13 & 16 & 24 & 40 & 57 & 69 & 56 \\ 14 & 17 & 22 & 29 & 51 & 87 & 80 & 62 \\ 18 & 22 & 37 & 56 & 68 & 109 & 103 & 77 \\ 24 & 35 & 55 & 64 & 81 & 104 & 113 & 92 \\ 49 & 64 & 78 & 87 & 103 & 121 & 120 & 101 \\ 72 & 92 & 95 & 98 & 112 & 100 & 103 & 99 \end{bmatrix}$$

# Quantizer

$$Q_{90} = \begin{bmatrix} 3 & 2 & 2 & 3 & 5 & 8 & 10 & 12 \\ 2 & 2 & 3 & 4 & 5 & 12 & 12 & 11 \\ 3 & 3 & 3 & 5 & 8 & 11 & 14 & 11 \\ 3 & 3 & 4 & 6 & 10 & 17 & 16 & 12 \\ 4 & 4 & 7 & 11 & 14 & 22 & 21 & 15 \\ 5 & 7 & 11 & 13 & 16 & 12 & 23 & 18 \\ 10 & 13 & 16 & 17 & 21 & 24 & 24 & 21 \\ 14 & 18 & 19 & 20 & 22 & 20 & 20 & 20 \end{bmatrix}$$

$$Q_{10} = \begin{bmatrix} 80 & 60 & 50 & 80 & 120 & 200 & 255 & 255 \\ 55 & 60 & 70 & 95 & 130 & 255 & 255 & 255 \\ 70 & 65 & 80 & 120 & 200 & 255 & 255 & 255 \\ 70 & 85 & 110 & 145 & 255 & 255 & 255 & 255 \\ 90 & 110 & 185 & 255 & 255 & 255 & 255 & 255 \\ 120 & 175 & 255 & 255 & 255 & 255 & 255 & 255 \\ 245 & 255 & 255 & 255 & 255 & 255 & 255 & 255 \\ 255 & 255 & 255 & 255 & 255 & 255 & 255 & 255 \end{bmatrix}$$

# Quantizer



$$\begin{bmatrix} -415 & -30 & -61 & 27 & 56 & -20 & -2 & 0 \\ 4 & -22 & -61 & 10 & 13 & -7 & -9 & 5 \\ -47 & 7 & 77 & -25 & -29 & 10 & 5 & -6 \\ -49 & 12 & 34 & -15 & -10 & 6 & 2 & 2 \\ 12 & -7 & -13 & -4 & -2 & 2 & -3 & 3 \\ -8 & 3 & 2 & -6 & -2 & 1 & 4 & 2 \\ -1 & 0 & 0 & -2 & -1 & -3 & 4 & -1 \\ 0 & 0 & -1 & -4 & -1 & 0 & 1 & 2 \end{bmatrix}$$

DCT coefficients

JPEG quantization matrix

16	11	10	16	24	40	51	61
12	12	14	19	26	58	60	55
14	13	16	24	40	57	69	56
14	17	22	29	51	87	80	62
18	22	37	56	68	109	103	77
24	35	55	64	81	104	113	92
49	64	78	87	103	121	120	101
72	92	95	98	112	100	103	99



# Quantizer

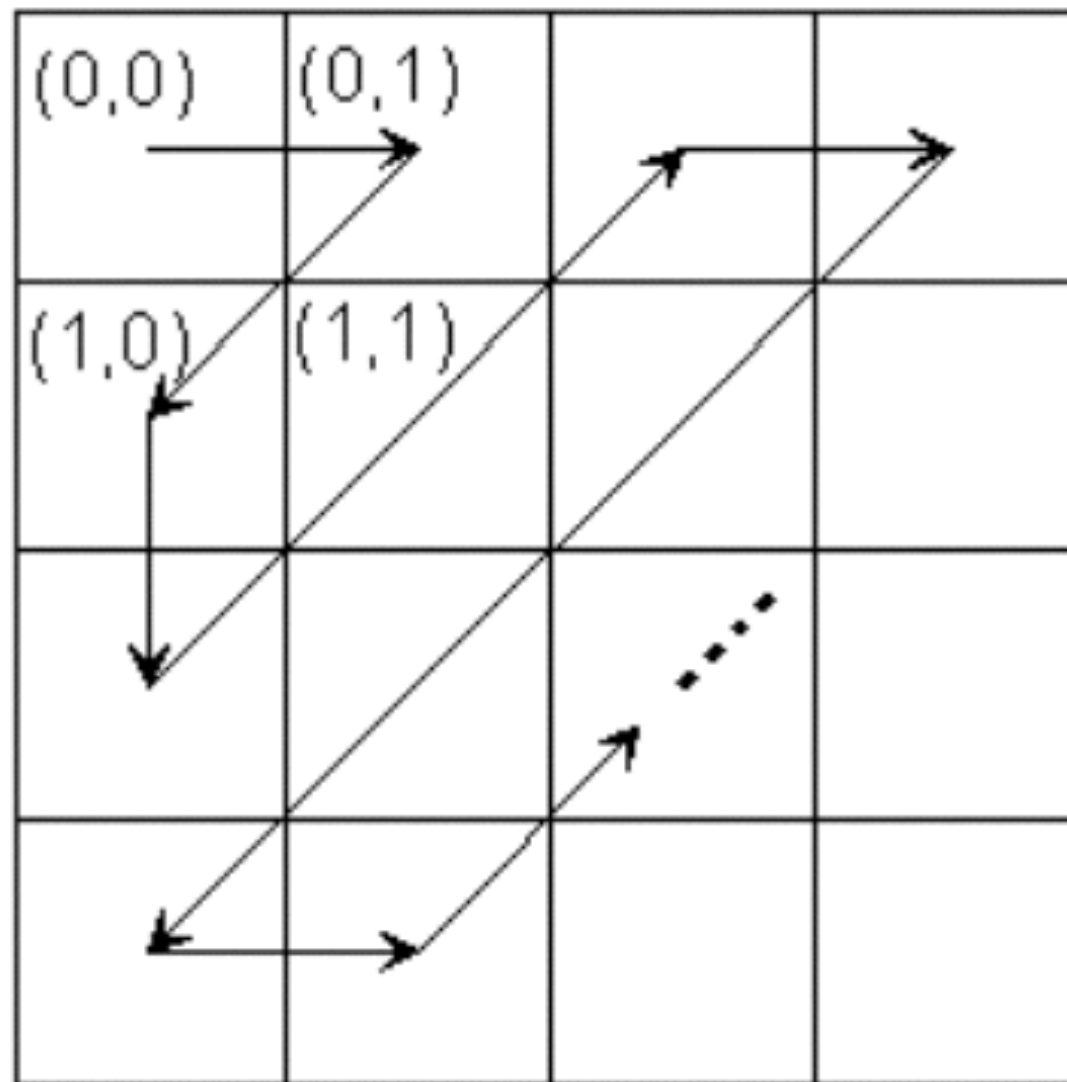
$$\begin{bmatrix} -415 & -30 & -61 & 27 & 56 & -20 & -2 & 0 \\ 4 & -22 & -61 & 10 & 13 & -7 & -9 & 5 \\ -47 & 7 & 77 & -25 & -29 & 10 & 5 & -6 \\ -49 & 12 & 34 & -15 & -10 & 6 & 2 & 2 \\ 12 & -7 & -13 & -4 & -2 & 2 & -3 & 3 \\ -8 & 3 & 2 & -6 & -2 & 1 & 4 & 2 \\ -1 & 0 & 0 & -2 & -1 & -3 & 4 & -1 \\ 0 & 0 & -1 & -4 & -1 & 0 & 1 & 2 \end{bmatrix}$$

DCT coefficients

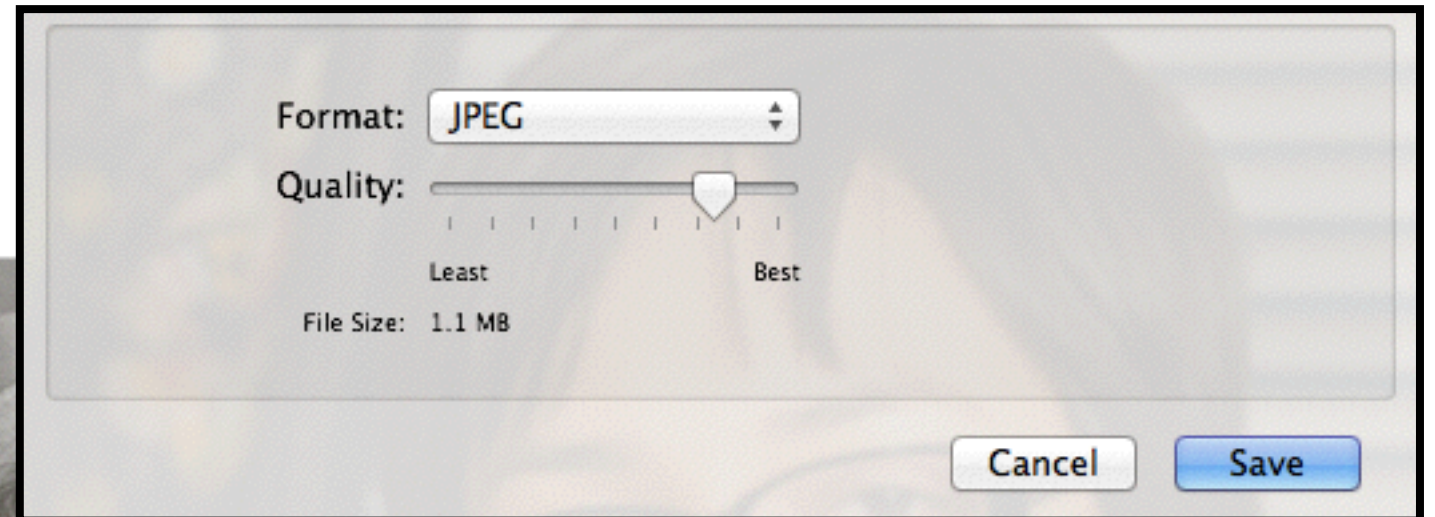
$$\begin{bmatrix} -26 & -3 & -6 & 2 & 2 & -1 & 0 & 0 \\ 0 & -2 & -4 & 1 & 1 & 0 & 0 & 0 \\ -3 & 1 & 5 & -1 & -1 & 0 & 0 & 0 \\ -4 & 1 & 2 & -1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

Quantized DCT  
matrix

# Coding



# Quantizer



# De-Compression

