

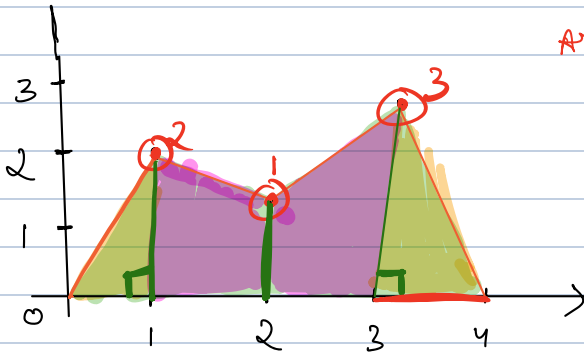
# Contest discussion

class starts at 9:05

Q

2	1	3
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$$\text{Area } \Delta 1 = \frac{1 \times 1 \times 2}{2} = \textcircled{1}$$



$$\text{Area } \Delta 2 = \frac{1 \times 1 \times 3}{2} = \textcircled{\frac{3}{2}}$$

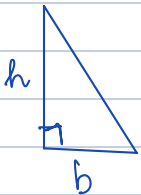
for (1  $\rightarrow$  n-2.)  
 trapezium 1 =  $\frac{1}{2} (2+1) \times 1 = \textcircled{\frac{3}{2}}$

$$\text{trapezium 2} = \frac{1}{2} (1+3) \times 1 = \textcircled{2}$$

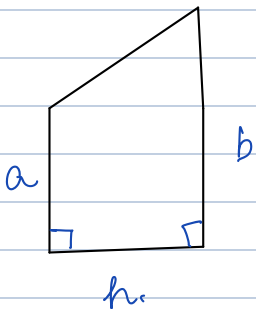
$$1 + \frac{3}{2} + \frac{3}{2} + 2 = \textcircled{6}$$

1) Area of right  $\triangle$  =  $\frac{1}{2} \times b \times h$ .

2) Area of a trapezium =  $\frac{1}{2} \times (a+b) \times h$ .



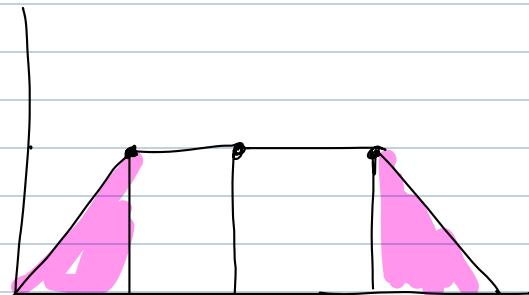
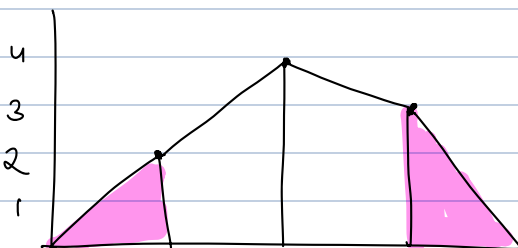
$$= \frac{1}{2} \times b \times h$$



$$\frac{1}{2} \times (a+b) \times h$$

$$TC \rightarrow O(N)$$

2 4 3



Q. Candies

$$A = \begin{array}{|c|c|c|c|} \hline 0 & 0 & 0 & 0 \\ \hline \end{array}$$

1    2   3   4

$$B = \begin{bmatrix} [1, 2] \\ [4, 4] \\ [1, 3] \end{bmatrix}$$

$$\Rightarrow \begin{array}{cccc} 1 & 1 & 0 & 0 \\ 1 & 1 & 0 & 1 \\ 2 & 2 & 1 & 1 \end{array}$$

$$C = [1, 2, 3]$$

$$\begin{array}{ccc} \downarrow & \downarrow & \downarrow \\ 4 & 2 & 0 \end{array}$$

O/P

Brute force  $\rightarrow$  Distributing  $|M| \times |A|$

$$m \times n.$$

$\rightarrow$  queries  $|C| \times |A|$

$$c \times n.$$

$$T.C \rightarrow (m \times n) + (c \times n)$$

Optimisation  $\rightarrow$  Prefix Sum

$$A = \begin{array}{|c|c|c|c|} \hline 0 & 0 & 0 & 0 \\ \hline \end{array}$$

1    2   3   4

$$B = \begin{bmatrix} [1, 2] \\ [4, 4] \\ [1, 3] \end{bmatrix}$$

$$\begin{array}{cccc} & & \text{+1} & & \\ & 1 & 0 & -1 & 0 \rightarrow \\ \text{prefix} & 1 & 0 & -1 & 1 \\ & 2 & 0 & -1 & 0 \\ & 2 & 2 & 1 & 1 \end{array}$$

$$\begin{array}{cccc} 1 & 2 & 3 & 4 \\ \downarrow & \downarrow & \downarrow & \downarrow \\ \text{prefix} & 2 & 2 & 1 & 1 \end{array}$$

put +1 at l and put -1 at (r+1) if exists

$$C = [1, 2, 3]$$

$$1 \quad 1 \quad 2 \quad 2$$

either exactly equal to 1 or just greater than 1.

0, 4

$$0 \quad 0 \quad 0 \quad 0$$



```

lowerbound (int arr[], int low, high, element) {
    while (low < high) {
        mid = low + (high - low) / 2;
        if (arr[mid] < element) {
            low = mid + 1;
        }
        else {
            high = mid;
        }
    }
    return low;
}

```

$$TC = O(N) + (N \log N)$$

$$q * \log N$$

$$1 \quad 1 \quad 4 \quad 6 \quad 8$$

$$q = 2$$

Q.  $A \rightarrow 1 \quad 3 \quad 4 \quad 4 \quad 2 \quad 2$

make all elements of the array or a multiple of 4.

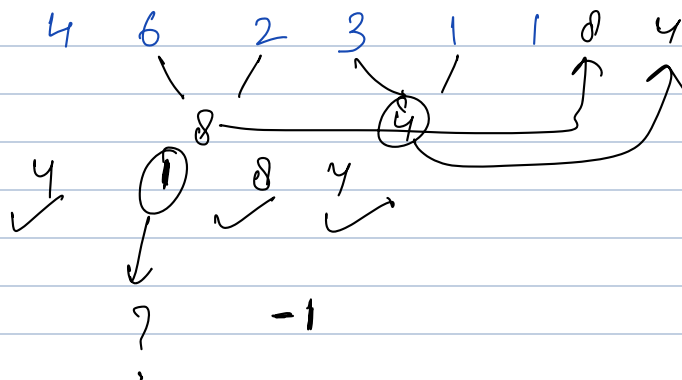
of  $A = 1 \quad 3 \quad 4 \quad 4 \quad 2 \quad 2$

$$\Rightarrow 4 \quad 4 \quad 2 \quad 2 \quad 4$$

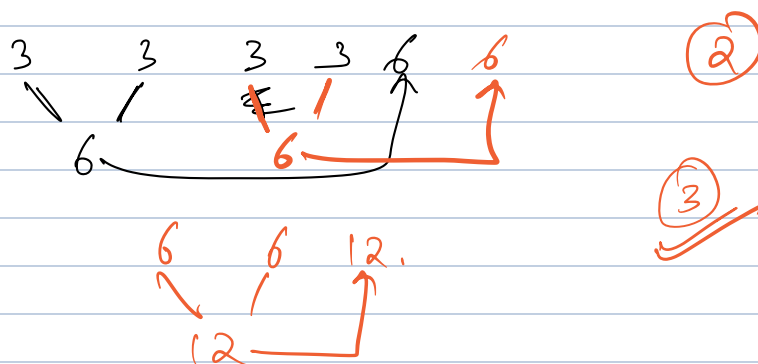
$$4 \quad 4 \quad 4 \quad 4$$

Return total no of steps req to do this  
if impossible then return -1; only +ve nos.

ex.



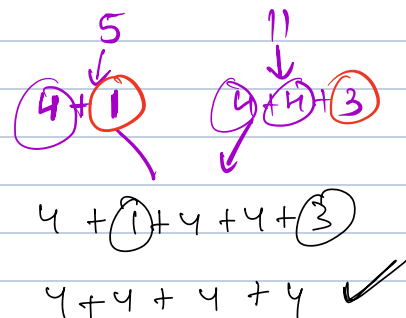
⇒ ex



1.) Calc mod 4 for each element.

$$\text{arr}[i] = \text{arr}[i] \% 4;$$

0  
1  
2  
3



2.) Sum the element [mod 1 & mod 3]  
3 2

$$\text{count} = \text{count} + 2.$$

a mod 2 ✓

3.) Sum element [mod 3 & mod 3] and  
[mod 1 & mod 1]

$$\text{count} = \text{count} + \text{pair}.$$

b mod 2 ✓

$$\text{count} \% 2 = a + b.$$

$$\begin{array}{c}
 4+4+3 \quad \quad 4+4+3 \\
 \searrow \quad \quad \swarrow \\
 4+4+4+4+6 \\
 \quad \quad \quad \swarrow \searrow \\
 \quad \quad \quad 4+2
 \end{array}$$

	4	5	11	2	3
	↓	↓	↓	↓	↓
mod	[0]	1	3	2	3]
	0		2	3	4
		↓		↓	
Count 1 =	2		(1, 3)	(1, 3)	
Count 3 =	0		1		

②

$$1 + 1 \rightarrow \text{not } \%4 = 2$$

Count 2 ++;

$$\left[ \begin{array}{l} \text{count 1} \rightarrow 1/0 \\ \text{count 3} \rightarrow 2/0 \end{array} \right]$$

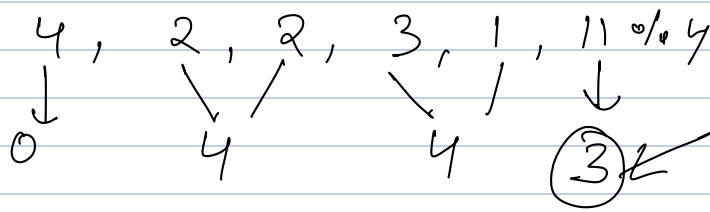


count 2. <

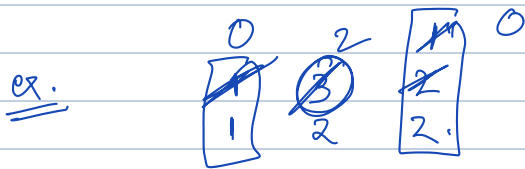
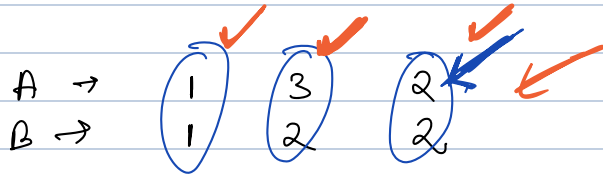
$$\begin{array}{cc}
 (2+2) & (2+2) \\
 \downarrow & \downarrow \\
 4 & 4
 \end{array}$$

4. Calc the count 2 is even, array will be div by 4  
 " " odd, return -1;

count 1 or count 3 or count 2 1 = 0  
 return -1;



Q. Little Penny & Tax Saving.

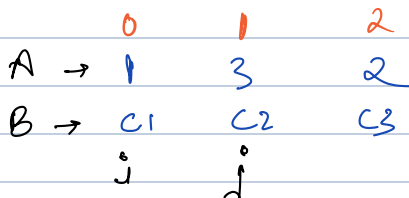


$$\begin{aligned}
 d1 \text{ Tax} &= 1 + 2 + 2 = 5 \\
 d2 \text{ Tax} &= 1 + 2 + 2 = 5 \\
 d3 &= 1 + 2 + 2 = 5 \\
 d4 &= 2 + 2 = 4 \\
 d5 &= 2 \\
 d6 &= 2
 \end{aligned}$$

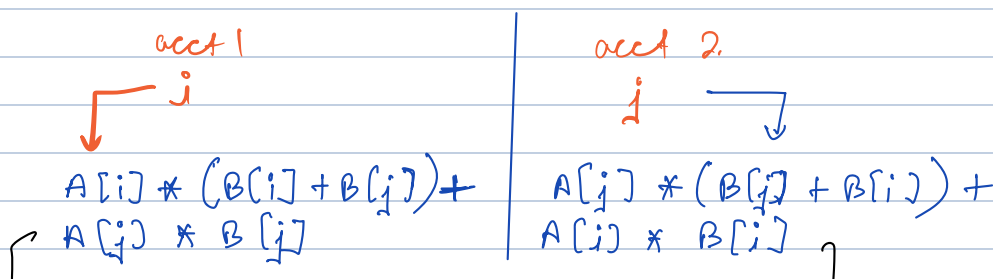
$$= 23.$$

①

Observation  $\rightarrow$  select 1 acct & empty it completely first.



lets have 2 acct, see which one to choose.



$$\begin{array}{l}
 \rightarrow A[i] * B[i] + \\
 A[i] * B[j] + \\
 A[j] * B[j]
 \end{array}
 \quad
 \begin{array}{l}
 A[j] * B[j] + \\
 A[j] * B[i] + \\
 A[i] * B[i]
 \end{array}$$

$$A[i] * B[j] \quad \leftarrow \quad A[j] * B[i]$$



Sorted.

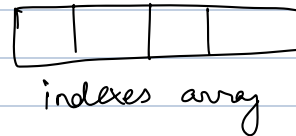
A	2	1	3
B	2	1	2

$2 + 1 + 2$

$$2 \times 2 + 1 \times (2+1) + (2+1+3) \times 2.$$

$$= 19.$$

$$\begin{array}{l}
 \text{for } (i=0; i < n; i++) \{ \\
 \quad \text{sum} += A[i] \\
 \quad \text{tax} = \text{tax} + (B[i] \times \text{sum}). \\
 \}
 \end{array}
 \quad \left. \vphantom{\begin{array}{l} \text{for } (i=0; i < n; i++) \{ \\ \text{sum} += A[i] \\ \text{tax} = \text{tax} + (B[i] \times \text{sum}). \\ \} } \right\} O(N)$$



$$TC \rightarrow O(N \log N) + O(N)$$

$$= O(N \log N).$$

$$SC \rightarrow \underline{\underline{O(N)}}.$$

Q5. Array A. Find  $B^{\text{th}}$  smallest element from the sum of all the triplets in A.

$$A \rightarrow \boxed{2} \boxed{4} \boxed{3} \boxed{2}$$

$$B = 3$$

All triplets -

$$2 \ 4 \ 3 \rightarrow 9$$

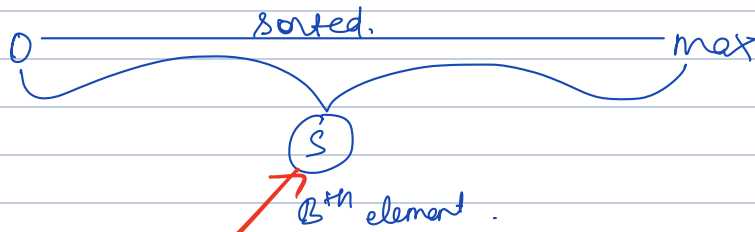
$$2 \ 4 \ 2 \rightarrow 8$$

$$2 \ 3 \ 2 \rightarrow 7$$

$$4 \ 3 \ 2 \rightarrow 9$$

$$\begin{array}{c}
 7 \ 8 \ 9 \\
 \downarrow \downarrow \downarrow \\
 1^{\text{st}} \ 2^{\text{nd}} \ 3^{\text{rd}}
 \end{array}$$

$$O(n^3) + n \log.$$



mid element

if it has exact  $(B-1)$  elements less than itself

$$\text{count} > B.$$

$$B+S < \text{mid}$$

$< B-1$  element.

1.) Sort the array

2.) Use 2 pointer approach to find no of triplet sum less than value mid,

A  $\rightarrow$ 

2	4	3	2
---	---	---	---

$$B = 3$$

All triplets -

$$2 \ 4 \ 3 \rightarrow 9$$

$$2 \ 4 \ 2 \rightarrow 8$$

$$2 \ 3 \ 2 \rightarrow 7$$

$$4 \ 3 \ 2 \rightarrow 9$$

$$- \begin{matrix} 7 & 8 & 9 & 9 \\ 1^{\text{st}} & 2^{\text{nd}} & 3^{\text{rd}} & \end{matrix}$$

sorted. 

2	2	3	4
---	---	---	---

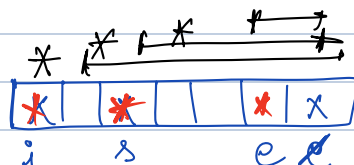
$s$   $e$

$$\text{mid} = 7$$

$$\text{sum} = \text{arr}[i] + \text{arr}[s] + \text{arr}[e]$$

if (sum > mid.) {  
     $e--$ ;  
}

else {



sum < ~~to~~ mid.

$$\text{count} = \text{count} + e - s.$$

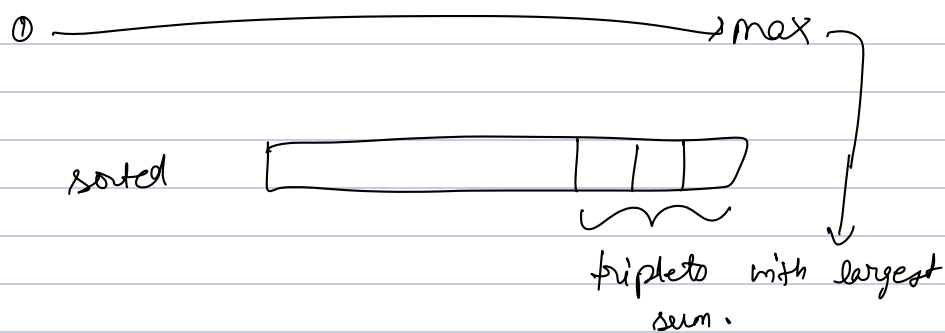


$O(N^2)$

```

func (
    for (int i = 0; i < n; i++) {
        int s = i + 1, e = n;
        while (s < e) {
            if (A[i] + A[s] + A[e] < mid) {
                count += e - s;
            }
            else
                e--;
        }
    }
    return count;
}

```



low = 0, high =  $A[n-1] + A[n-2] + A[n-3]$

```

while (low <= high) {
    int mid = low + (high - low) / 2;
    // count no of triplets sum less than mid.
    int count = func(mid, A);

```

```

    if (count == B - 1)
        return mid;

```

```

    else if (count >= B)
        high = mid - 1;

```

```

    else {
        ans = mid;
        low = mid + 1;
    }

```

```

return ans;

```

2	1	3	8	4	6
---	---	---	---	---	---

$i$                    $j$                    $k$

$i$                    $j$                    $k$   
 $i$                    $k$   
 $j$                    $k$