

## Today's Content

→ Pair Sum = K

→ Pair Difference = K

→ Distinct elements in every window of size = K

→ Subarray with sum = K

Q1: Given  $A[N]$ , check if there exists a pair  $(i, j)$   
s.t.  $A[i] + A[j] = K$ ,  $i \neq j$

arr[] = 

0	1	2	3	4	5	6	7	8	9
8	9	1	-2	4	5	11	-6	7	5

K = 11 : arr[4] + arr[8]  $\Rightarrow 4 + 7 = 11 \Rightarrow \text{YES}$

K = 6 :  $\left. \begin{array}{l} \text{arr}[2] + \text{arr}[5] \Rightarrow 1 + 5 \\ \text{arr}[0] + \text{arr}[3] \Rightarrow 8 - 2 \end{array} \right\} = 6 \Rightarrow \text{YES}$

K = 22 : arr[6] + arr[6] = 11 + 11 = ~~YES~~ <sup>x</sup> NO!  $i \neq j$

idea: check all pair sum = K, TC:  $O(N^2)$ , SC:  $O(1)$

```
for(i=0; i<n; i++) {  
    int a = A[i], b = K - A[i]  
    for(j=i+1; j<n; j++) {  
        if(A[j] == b) {  
            return true  
        }  
    }  
}
```

## idea2: Optimise using Hashset

\* insert all elements into hashset

0 1 2 3 4 5 6 7 8 9  
arr[] = 8 9 1 -2 4 5 11 -6 7 5

HS = { 8, 9, 1, -2, 4, 5, 11, -6, 7 }

a + b = 11 (k=11)

<u>a</u>	<u>b(k-a)</u>
8	3
9	2
1	10
-2	13
4	7

b is present in HS

No X

No X

No X

No X

Yes

{ return true }

a + b = 5 (k=5)

<u>a</u>	<u>b(k-a)</u>
8	-3
9	-4
1	4

b is present in HS

No

No

Yes

a + b = -4 (k=-4)

<u>a</u>	<u>b(k-a)</u>
8	-12
9	-13
1	-5
-2	-2

is b present in HS

No

No

No

YES

↳ Error!

### idea 3: Use hashmap

\* insert all elements into hashmap & store their frequency.

arr = 

0	1	2	3	4	5	6	7	8	9
8	9	1	-2	4	5	11	-6	7	5

HM = 

$\langle 8, 1 \rangle$	$\langle 1, 1 \rangle$	$\langle 4, 1 \rangle$	$\langle 11, 1 \rangle$	$\langle 7, 1 \rangle$
$\langle 9, 1 \rangle$	$\langle -2, 1 \rangle$	$\langle 5, 2 \rangle$	$\langle -6, 1 \rangle$	

$$a + b = 5$$

<u>a</u>	<u>b (k-a)</u>
8	-3
9	-4
1	4

is b present in map

No

No

4 is present,  $\Rightarrow$  return true.  
 $\hookrightarrow (a \neq b \ \&\& \ b \text{ is present in map})$

$$a + b = 10$$

<u>a</u>	<u>b (k-a)</u>
8	2
9	1

is b present in map

x

Yes  $\rightarrow$  true.

arr = { 8 9 4 5 11 -6 7 5 -2 4 }

HM = 

$\langle 8, 1 \rangle$	$\langle 5, 2 \rangle$	$\langle 7, 1 \rangle$
$\langle 9, 1 \rangle$	$\langle 11, 1 \rangle$	$\langle -2, 1 \rangle$
$\langle 4, 2 \rangle$	$\langle -6, 1 \rangle$	

$$a + b = 10$$

<u>a</u>	<u>b(k-a)</u>
8	2
9	1
4	6
5	5

is b present in map

NO

NO

NO

YES

$a == b \ \&\& \ \text{freq}(a) > 1$

Pseudocode:

TC:  $O(N)$   
SC:  $O(N)$

```

bool pairSum (int a[], int k) {
    HashMap <int, int> hm
    Insert a[] into hm // Todo

    for (i=0; i < n; i++) {
        a = a[i], b = k - a
        if (a != b && hm.search(b) == true) {
            return true
        }
        if (a == b && hm[a] > 1) {
            return true
        }
    }
    return false
}
    
```

idea 4: Why does HS not work?  $\Rightarrow$  can contain duplicates.

ar[] = 8 9 5 -2 11 5 7 -6 4 1

K=10

<u>a</u>	<u>b (k-a)</u>	<u>HS</u>	<u>b is present in HS</u>
8	2	{ }	No
9	1	{ 8 }	No
5	5	{ 8, 9 }	No
-2	12	{ 8, 9, 5 }	No
11	-1	{ 8, 9, 5, -2 }	No
5	5	{ 8, 9, 5, -2, 11 }	<u>YES</u> return true.

Pseudo code

```

bool pairSet (int a[], int k) {
    HashSet<int> hs
    n = a.length
    for (i=0; i<n; i++) {
        a = A[i], b = k-a
        if (hs.search(b) == true) { return true }
        hs.insert(a)
    }
    return false
}
    
```

TC: O(N)  
SC: O(N)

Q2: Given  $A[N]$ , check if there exists a pair  $(i, j)$  st.  $A[i] - A[j] = K$ ,  $i \neq j$

$a[] = \{ \overset{0}{1} \overset{1}{3} \overset{2}{7} \overset{3}{9} \overset{4}{2} \overset{5}{5} \overset{6}{6} \}$

$K = 2$

$$\left. \begin{array}{l} a[1] - a[0] \\ a[3] - a[2] \end{array} \right\} 2$$

Prev Qn:  $A[i] + A[j] = K$  ( $i \neq j$ )

or  $A[j] + A[i] = K$

fix  $A[i]$  :  $a = \underline{A[i]}$  :  $b = K - A[i]$

fix  $A[j]$  :  $a = A[j]$  :  $b = K - A[j]$

In this Qn:

$$A[i] - A[j] = K$$

fix  $A[i]$

$$a = A[i], \Rightarrow b = A[j] + K$$

$$A[j] - A[i] = K$$

fix  $A[i]$

$$a = A[i]$$

$$c = A[j] - K$$

idea: Search for both  $b$  &  $c$  in idea 4 above  
 $\hookrightarrow$  if any is present  
 $\hookrightarrow$  return true.

(Todo)



# idea 3: Use hashmap

arr [10] = 2 4 3 8 3 9 4 9 4 10

H.M. Size

K=4.

[0 3]

Hashmap

{ <2,1> <3,1> }  
{ <4,1> <8,1> }

4

[1 4]

remove  
s-1

a[0]

add  
e  
a[4]

{ ~~<2,1>~~ <3,2> }  
{ <4,1> <8,1> }

3

[2 5]

a[1]

a[5]

{ <9,1> <3,2> }  
{ ~~<4,1>~~ <8,1> }

3

[3 6]

a[2]

a[6]

{ <9,1> <3,2> }  
{ <8,1> <4,1> }

4

[4 7]

a[3]

a[7]

{ <9,2> <3,1> }  
{ ~~<8,1>~~ <4,1> }

3

[5 8]

a[4]

a[8]

{ <9,2> <3,1> }  
{ <4,2> }

2

[6 9]

a[5]

a[9]

{ <9,2> <4,2> }  
{ <10,1> }

3



void printDistinctMap (int a[], int k) {

n = a.length

HashMap <int, int> hm

for (i = 0; i < k; i++) {

if (hm.search(a[i]) == true) {

hm[a[i]]++

}

else {

hm.insert(a[i], 1)

}

print(hm.size)

s = 1, e = k

while (e < n) {

// Get subarray [s, e], remove a[s-1], add a[e]

hm[a[s-1]]--

if (hm[a[s-1]] == 0) {

hm.remove(a[s-1])

if (hm.search(a[e]) == true) {

hm[a[e]]++

else {

hm.insert(a[e], 1)

print(hm.size)

s++, e++

TC: O(N)

SC: O(K)

}

Qu: Check if there exists a subarray with sum = K

$a[] =$ 

	0	1	2	3	4	5	6	7	8	9
	2	2	1	-3	4	3	1	-2	-3	2

$pf[] =$ 

	2	4	5	2	6	9	10	8	5	7
--	---	---	---	---	---	---	----	---	---	---

$$\text{sum}([i \dots j]) = K$$

$$\downarrow$$

$$pf[j] - pf[i-1] = K$$

fix this

$$a = pf[i-1], \quad b = pf[j] - K$$

sum=0  
K=0

$pf[i-1] = pf[j]$  or search for duplicates.

K=3

$a[] =$ 

	0	1	2	3	4	5	6	7	8	9
	2	2	1	-3	4	3	1	-2	-3	2

$pf[] =$ 

	2	4	5	2	6	9	10	8	5	7
--	---	---	---	---	---	---	----	---	---	---

a

2

4

5

2

6

9

b (a-K)

-1

1

2

-1

3

6

HS

{ } → No

↓

{ 2 } → No

↓

{ 2, 4 } → YES!  $pf[2] - pf[0]$   
 $5 - 2$   
[1 2]

↓

{ 2, 4, 5 } → No

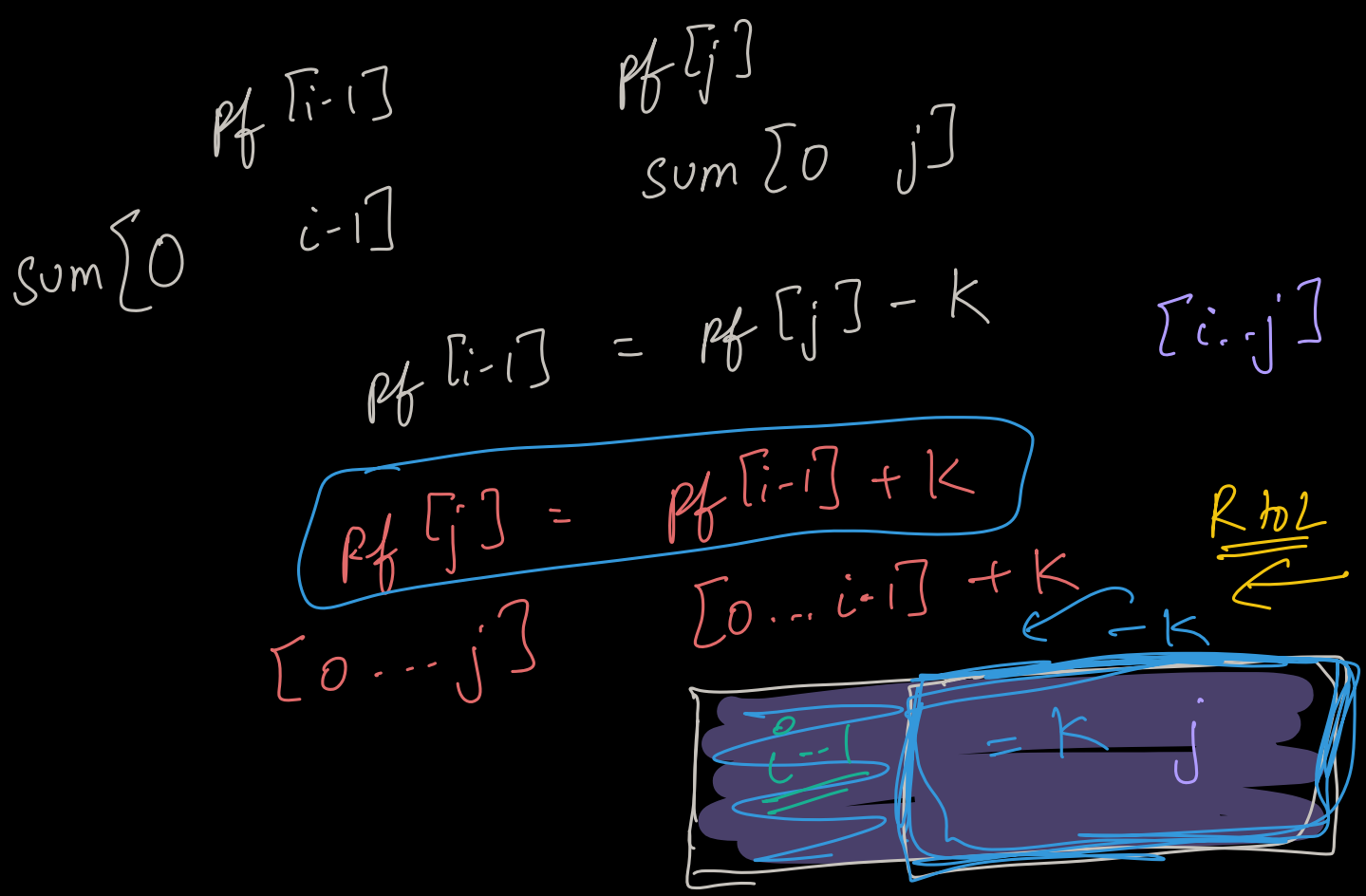
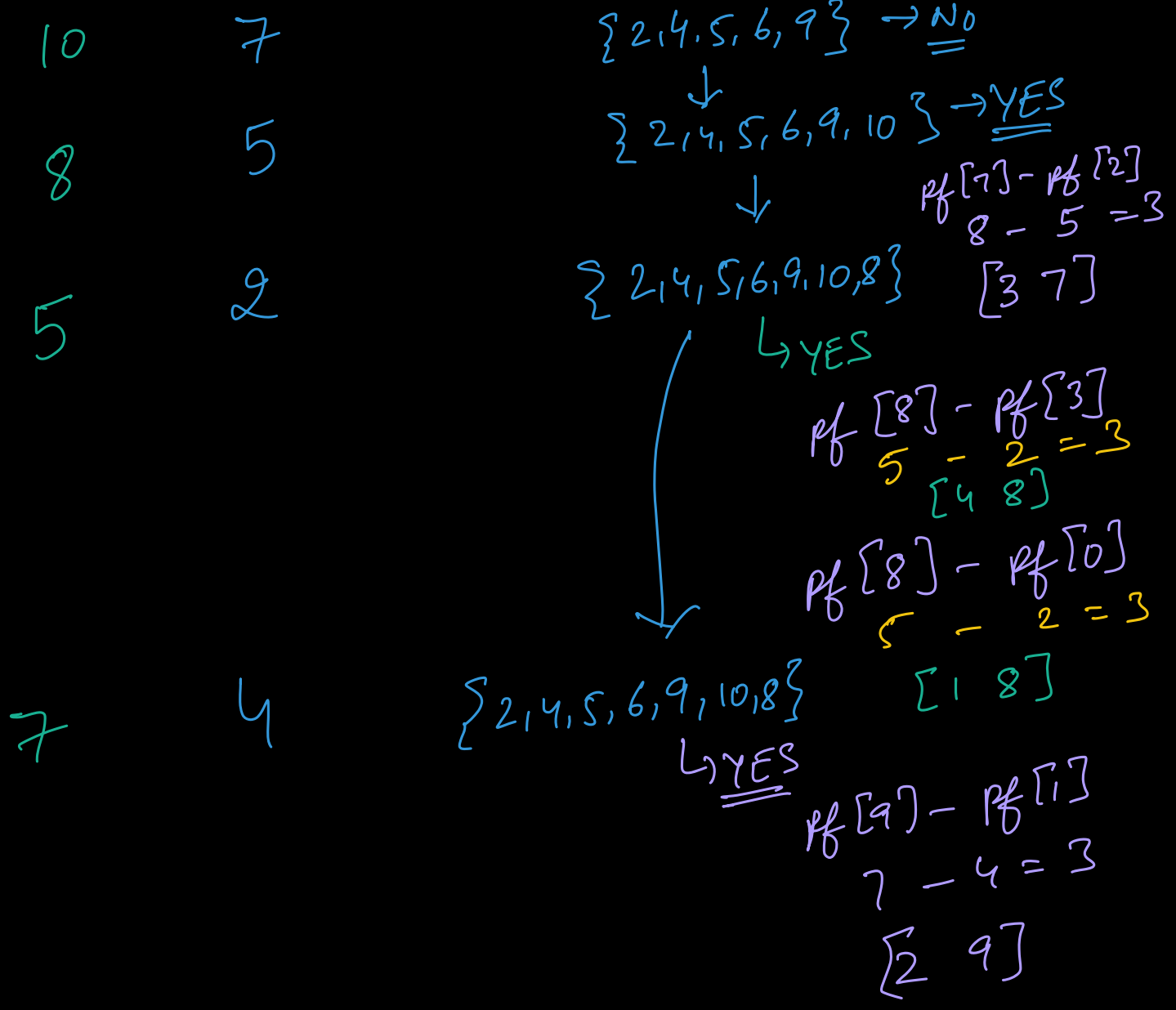
↓

{ 2, 4, 5 } → No

↓

{ 2, 4, 5, 6 } → YES

$pf[5] - pf[4]$   
 $9 - 6 = 3$   
[5 5]



```

bool subarrWithSumK (int a[], int k) {
    Hashset <int> hs;
    int pf[n]
    // Create pf array → Todo
    sum = 0
    for (i = 0; i < n; i++) {
        int a = pf[i] // sum = sum + a[i]
        int b = a - k // b = sum - k
        // Edge case
        if (pf[i] == k) { // (sum == k)
            return true
        }
        if (hs.search(b) == true) {
            return true
        }
        hs.insert(a) // hs.insert(sum)
    }
}

```

TC:  $O(N)$   
 SC:  $O(N)$

Note: →  $pf[i] == k$  handles the  
 $sum([0 \dots i]) = k$  case  
 $hs.search(b) == true$  handles  
 the  $sum([i \dots j])$  case