

PS (Sunday's Session)

↳ fill cf (incl. cf)

Today: [Arrays: Subarrays → Interview Probs - 2]

Q1: Arrays - Interviews - 1 (HW Q2)

Max positivity

Given an  $a[]$ . Return max size subarr of  $a[]$  having non negative elements only.  $\geq 0$  If same 2 subarr have same len, return the one which occurs first

Eg:  $A = [5, 6, -1, 7, 8]$   
↓  
 $ans = \{5, 6\}$

$A = [1, 2, 3, 4, 5, 6]$   
↳  $ans = \{1, 2, 3, 4, 5, 6\}$

# Brute force:

↳ use 2 loops to generate subarrays

↳ 3rd loop to check if subarr contains non-negative elements

for ( $i=0; i < n; i++$ ) {

for ( $j=i; j < n; j++$ ) {

// subarr  $[i, j]$

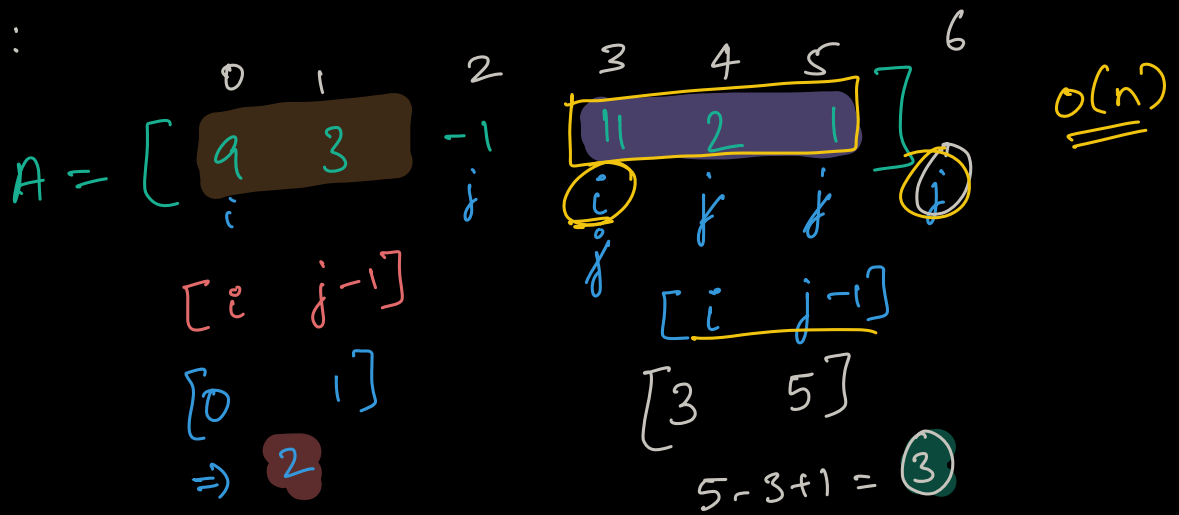
for ( $k=i; k \leq j; k++$ ) {

↳ Compare & update ans.

→ Tc:  $O(N^3)$

Sc:  $O(N)$

#idea 2 :



int[] solve(int a[], int N) {

    i = 0

    max-len = 0

    start-idx = 0, end-idx = 0

    while (i < n) {

        if (A[i] >= 0) {

            int len = 0

            int start = i

            while (start < n & A[start] >= 0) {

                len++

                start++

            }

            if (len > max-len) {

                max-len = len

                start-idx = i

                end-idx = start - 1

            }

            i = start + 1

        }

    else {

        i++

    }

}

```

for (j = start - idx; j <= end - idx; j++) {
    ans.add(A[j])
}
return ans

```

TC:  $O(N)$   
SC:  $O(1)$

Q2: Subarrays, HW Q2

Alternating Sub-arrays Easy

Given a binary  $a[]$  & int  $B$ . Find <sup>all</sup> the idx of  $a[]$  that can act as centre of  $2B+1$  alternating subarr.

$A = [1, 0, 1, 0, 1]$   
 $\hookrightarrow \text{ans} = \{1, 2, 3\}$

$[1, 0, 1, 0, 1] \checkmark$

$[0, 1, 0, 1, 0] \checkmark$

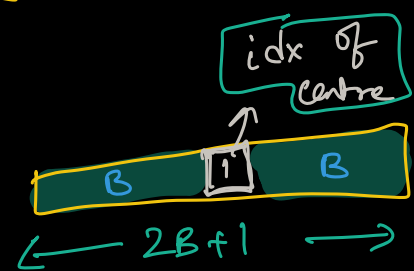
$[0, 1, 1, 0] \hookrightarrow \times$

$[0, 0, 1, 0, 1, 0] \hookrightarrow \times$

$B = 1$   
 $\hookrightarrow 2B+1 = 3$

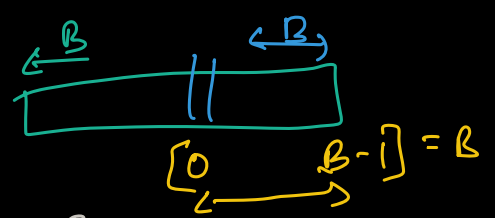
$[0, 2] = \{1, 0, 1\} \checkmark$   
 $[1, 3] = \{0, 1, 0\} \checkmark$   
 $[2, 4] = \{1, 0, 1\} \checkmark$   
 $\text{ans} = \{1, 2, 3\}$

$2B+1$   $\hookrightarrow$  odd  $\hookrightarrow B+1+B$



# Brute force: Consider every idx  $i$  as middle idx / centre  
 $\hookrightarrow$  check  $B$  elements on left  $\rightarrow$  left  
 $\hookrightarrow$  check  $B$  elements on right  $\rightarrow$  right  
 $\hookrightarrow$  if both left & right,  $\hookrightarrow$  add  $i$  to ans

int[] solve (int a[], int N, int B) {



int ans[]

for (i = B ; i < N-B ; i++) {

// i is middle element

// Check left of i

bool left = true

for (j = i-1 ; j >= i-B ; j--) {

if (A[j+1] == A[j]) {

left = false

break

}

}

// Check right of i

bool right = true

for (j = i+1 ; j <= i+B ; j++) {

if (A[j] == A[j-1]) {

right = false

break

}

}

if (left == true && right == true) {

ans.add(i)

}

}

return ans

TC:  $(N-2B) * (B+B+1)$

=  $O(N^2)$

SC:  $O(1)$

$\{B \quad N-B-1\}$

$\Rightarrow N-B-1-B+1$

=  $N-2B$



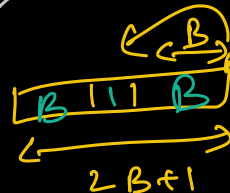
$A = \begin{bmatrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \\ 1 & 0 & 1 & 0 & 1 & 1 & 0 & 1 & 0 \end{bmatrix}$   
 (Underline from index 0 to 4 with '5' below it, and from index 5 to 8 with 'x' below it)

$B = 1$

$2B+1 = 3$

Code: int[] solve(int a[], int n, int B) {  
     len = 2B+1  
     curr\_window\_len = 1  
     if(B==0) { ans.add(0) }  
     for(i=1; i<n; i++) {  
         if(A[i-1] == A[i]) {  
             curr\_window\_len = 1  
         }  
         else {  
             curr\_window\_len++  
         }  
         if(curr\_window\_len >= len) {  
             ans.add(i-B)  
         }  
     }  
     return ans  
 }

TC:  $O(n)$   
 SC:  $O(1)$



$B=1 \Rightarrow 2$   
 $len=3$

$A = \begin{bmatrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \\ 1 & 0 & 1 & 0 & 1 & 1 & 0 & 1 & 0 \end{bmatrix}$   
 (Underline from index 5 to 7)

cwl: 4

ans: (1, 2, 3, 6, 7)

$$\underline{B=0} \Rightarrow 2B+1 = \underline{1}$$

Break: 10 mins

8:45 am

Magic No.  
 $\hookrightarrow 5, 25, 30, 125, 130, 150, \underline{155}$   
 $\downarrow$   
 $625, 630, 650, 655$   
 $\downarrow \quad \downarrow \quad \downarrow$   
 $625+5 \quad 625+25 \quad 625+25+5$   
 $5^1 \quad 5^2 \quad 5^3$   
 $5+25+125$

Q3: Interview Prob -1, HW Q1

Christmas Trees

Given an  $A[]$ , having height of trees &  $B[]$  having cost of each tree.

Choose 3 trees  $p, q, r$  st.

$$A_p < A_q < A_r$$

where  $p < q < r$

Minimise the cost  $B_p + B_q + B_r$

$$A = [\underline{1}, 6, 4, \underline{2}, \underline{6}, 9]$$

$$B = [\underline{2}, 5, 7, 3, \underline{2}, \underline{7}]$$

$$\underline{p < q < r}$$

$$0 \quad 3 \quad 4$$

$$0 \quad 3 \quad 5$$

$$0 \quad 1 \quad 5$$

$$2 \quad 4 \quad 5$$

$$3 \quad 4 \quad 5$$

$$\underline{A_p < A_q < A_r}$$

$$1 \quad 2 \quad 6$$

$$1 \quad 2 \quad 9$$

$$1 \quad 6 \quad 9$$

$$4 \quad 6 \quad 9$$

$$2 \quad 6 \quad 9$$

$$\underline{B_p + B_q + B_r} \downarrow$$

$$2 + 3 + 2 = \underline{7}$$

$$2 + 3 + 7 = 12$$

$$2 + 5 + 7 = 14$$

$$7 + 2 + 7 = 16$$

$$3 + 2 + 7 = 12$$

0 2 4  
0 2 5  
0 4 5

1 4 6  
1 4 9  
1 6 9

$2 + 7 + 2 = 11$   
 $2 + 7 + 7 = 16$   
 $2 + 2 + 7 = 11$

# Brute force:

↳ 3 nested loops

→ check for  $A_p < A_q < A_r$

↳ minimise  $(B_p + B_q + B_r)$

# Keep in middle

$p < q < r$   
 $= i$

→ For every element  $i$ , keep  $i$  in middle

check left

find elements  
lesser than  
 $A[i]$

??  
 $\min(B_p)$

check right

find elements  
greater than  
 $A[i]$

??  
 $\min(B_r)$

if found  $B_p$  &  $B_r$

$ans = \min(ans, B_p + B_r + B_i)$

Code's To-do

↳ ask TA

↳ ask Batchmates

↳ ask me

Q:4 N/3 majority element  
Interview Prob-2, HW Q1

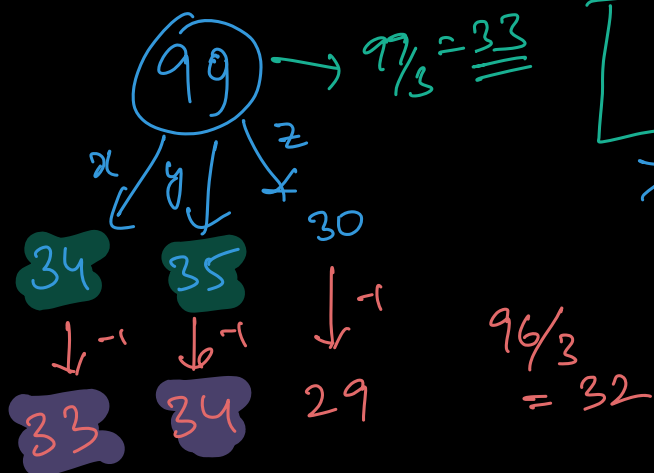
Given an array, find if any element occurs more than  $N/3$  times.

$A = [1 \ 2 \ 3 \ 1 \ 1]$   
 $\text{freq}(1) = 3$   
 $\boxed{\text{ans} = 1}$

$N = 5$

$$5/3 = 2$$

# maj elements = 2



x	y	z
---	---	---

$> N/3 \quad > N/3$

Eg:  $A[] = [2, 2, 2, 1, 4, 2, 3, 2, 1, 4, 4, 4, 3, 4]$

$\text{Me1} = 2$   
 $\text{freq1} = \underline{\hspace{2cm}}$

$\text{Me2} = 4$   
 $\text{freq2} = \underline{\hspace{2cm}}$

// Cross-check

$\text{freq}(2) = 5$   
 $\text{freq}(4) = 5$

$N = 14$

$$14/3 = 4$$





Q5: 2D-Matrix, HW Q5  
Row to Col to Zero

Given 2D matrix, make row & col as 0  
 if  $A[i][j] = 0$

Constraint:-

$$1 \leq A_{ij} \leq 10^3$$

Eg:  $A = \begin{bmatrix} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 8 \\ 9 & 10 & 11 & 0 \\ 13 & 14 & 0 & 16 \end{bmatrix}_{N \times M} = \begin{bmatrix} 1 & 2 & 0 & 0 \\ 5 & 6 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$

# ideal (with extra space)

Row  $[N] = \{ \}$   
 Col  $[M] = \{ \}$   
 (1)  $\rightarrow$  Traverse the matrix, if

TC:  $O(N \times M)$   
SC:  $O(N+M)$

if  $A[i][j] = 0$  {  
 $\hookrightarrow \text{row}[i] = 1$   
 $\hookrightarrow \text{col}[j] = 1$

(2) Traverse the matrix:  $i, j$   
 if  $(\text{row}[i] == 1 \parallel \text{col}[j] == 1)$   
 $A[i][j] = 0$

# idea 2 (w/o extra space)

$\hookrightarrow$  Traverse the matrix, row-wise

if  $A[i][j] = 0$   
 change all non-zero elements  
 in row  $[i]$  to  $-1$

→ Traverse the matrix, col-wise  
 if  $(A[i][j] == 0)$   
 make all non zero col elements  $-1$   
 $\boxed{j}$

→ Traverse the matrix  
 change  $-1$  to  $0$ .

$$A = \begin{bmatrix} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 8 \\ 9 & 10 & 11 & 0 \\ 13 & 14 & 0 & 16 \end{bmatrix} \Rightarrow \begin{bmatrix} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 8 \\ -1 & -1 & -1 & 0 \\ -1 & -1 & 0 & -1 \end{bmatrix} \quad \begin{array}{l} \text{Row} \\ \text{wise} \\ \text{traversal} \end{array}$$

$$\begin{bmatrix} 1 & 2 & 0 & 0 \\ 5 & 6 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} \quad \begin{array}{l} \text{Col wise} \\ \text{traversal} \end{array} \quad \begin{bmatrix} 1 & 2 & -1 & -1 \\ 5 & 6 & -1 & -1 \\ -1 & -1 & -1 & 0 \\ -1 & -1 & 0 & -1 \end{bmatrix}$$

update  $-1$  to  $0$

TC:  $O(N \times M)$   
SC:  $O(1)$

$$\rightarrow A = \begin{bmatrix} 1 & 2 & 3 & 4 \\ 5 & 0 & 6 & 7 \\ 8 & 9 & 0 & 10 \\ 11 & 12 & 13 & 14 \end{bmatrix} \Rightarrow \begin{bmatrix} 1 & 0 & 3 & 4 \\ 0 & 0 & 0 & 0 \\ 8 & 0 & 0 & 10 \\ 11 & 0 & 13 & 14 \end{bmatrix}$$

DocuBot :

A      B  
Set A<sup>th</sup> bit in 0  
B<sup>th</sup> bit in 0

A = 3, B = 5

5	4	3	2	1	0
0	0	0	0	0	0
1	0	1	0	0	0

⇒  
2<sup>5</sup>  
32 + 8 = 40

Set ⇒ 1  
Unset ⇒ 0

A = 4

B = 4

4	3	2	1	0
0	0	0	0	0

1	0	0	0	0
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2<sup>4</sup> = 16

BIT manip 1

Hw Q3

Sub arr with OR = 1