

PROBLEM - SOLVING - SESSION

PRE
QUES

$$\begin{array}{r}
 a = 101101 \\
 b = 100001 \\
 \hline
 \text{BITWISE OR} \quad 101101
 \end{array}$$

$$\begin{array}{r}
 a = 101 \\
 b = 100 \\
 c = 101 \\
 \hline
 \begin{array}{ccc}
 \uparrow & \uparrow & \uparrow \\
 1 & 0 & 1
 \end{array}
 \end{array}$$

BITWISE OR

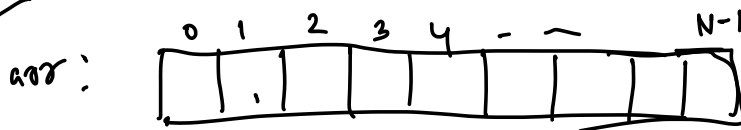
1	1	1
0	1	1
1	0	1
0	0	0

BITWISE OR \Rightarrow If any of the bit is 1

CONCLUSION

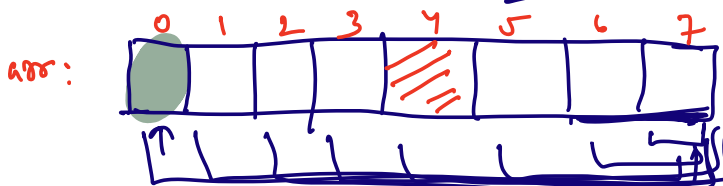
the the BITWISE OR is 1

PRE-2



N integers array

- 1) what do you mean by subarray?
- 2) How many total subarray are possible from array of N integers? $\frac{N \times (N+1)}{2}$



array size = 8

$$= 1 + 2 + 3 + \dots + 8$$

$$= 8(8+1)$$

N terms

$$\frac{2}{2}$$

$$\frac{N * (N+1)}{2}$$

QUES

Given an array A of N integers

with elements 1 & 0.

Number of subarrays with BITWISE OR as 1.

arr: [1, 0, 1]

$$[1] = 1 \checkmark$$

$$[1, 0] = 1 \checkmark$$

Ans = 5

$$[0] = 0$$

$$[0, 1] = 1 \checkmark$$

$$[1] = 1 \checkmark$$

$$[1, 0, 1] = 1 \checkmark$$

Solution

arr:

0	1	2
1	0	1

ending with 0th index: 1

ending with 1st index: 1

$$[0] = 0$$

$$[1, 0] = 1$$

ending with 2nd index = 3

$$[1] = 1$$

$$[0, 1] = 1$$

$$[1, 0, 1] = 1$$

take care about last one.

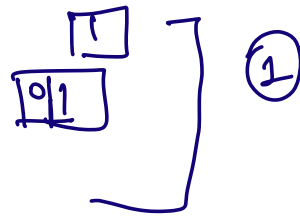
arr:

0	1	2	3	4	5	6	7	8
0	0	0	0	1	0	0	1	0

ending 0th index = [0]

ending with 3rd index = there is no 1's before this
index
= 0

ending with 4th index = 5



CODE:

```
long solve (vector<int> A)
{
```

```
    int last_one = 0; // position of
    long ans = 0;      last_one
                       present.
```

```
    for (int i=0; i<n; i++)
```

```
    { if (A[i] == 1) last_one = i+1; }
```

```
    ans += last; }
```

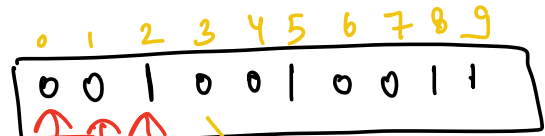
Time-complexity
= O(N)

3

space
= $O(1)$ 3

return ans;

ans:



ans += 0

ans += 0

1

last-one = 3

0 1

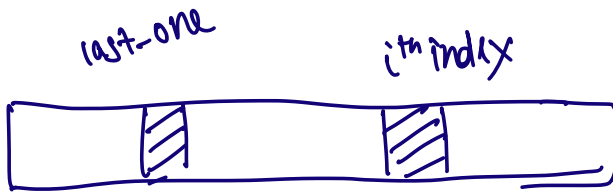
ans += last-one.

0 0 1

ans += 3

last-one = 3

ans = 3



1

[] = 1

[] = 1

[] = 1

QUES-2

PRE-REQ-1

{1, 2, 3} = ^{subsets} { } {1} {2} {3}

{1, 2} {2, 3} {1, 3}

3 size

{1, 2, 3} = 8

{1, 2} = { }

2 size

{1} {2}

{1, 2} = 4



$$\{1, 2, 3, 4\} =$$

$$\{1\} = 2^1$$

$$\{1, 2\} = 2^2$$

$$\{1, 2, 3\} = 2^3$$

$$\{1, 2, 3, 4\} = 2^4$$

$$\{1\} = 2^1$$

$$\{1, 2\} = 4 = 2^2$$

$$\{1, 2, 3\} = 8 = 2^3$$

$$\{1, 2, 3, 4\} = 16 = 2^4$$

$$\{1, 2, \dots, N\} = 2^N$$

$$\{1, 2, 3, \dots, 13\} = 2^{13} = 8192$$

Total no. of subsets.

QUES

Find the N^{th} Magic Number

Magic Number :

A number that can be expressed as a power of 5 or sum of unique powers of 5

Few Magic Numbers \Rightarrow 5, 25, 30, 125, 130, ...

3rd magic number = 30

$$\begin{array}{ccccccc} & & & & & & 7 \\ & & & & & & \downarrow \\ & & & & & & (5^3 + 5^1) \\ & & & & & & \downarrow \\ & & & & & & (5^3) \\ & & & & & & \downarrow \\ & & & & & & (5^3) \end{array}$$

$$\Rightarrow (5^1, 5^2, 5^3)$$

$$\Rightarrow \{5\} = 5$$

$$= \{5^2\} = 25$$

$$= \{5^3\} = 125$$

Ath Magic Number
(1 ≤ A ≤ 5000)

$$(5^1, 5^2) = \{5^1 + 5^2\} = 30$$

$$(5^2, 5^3) = 25 + 125 = 150$$

$$(5^1, 5^3) = 130$$

$$(5^1, 5^2, 5^3) = 5 + 25 + 125 = 155$$

$$\{5^1, 5^2, 5^3, 5^4\} \Rightarrow 15 \text{ Magic number.}$$

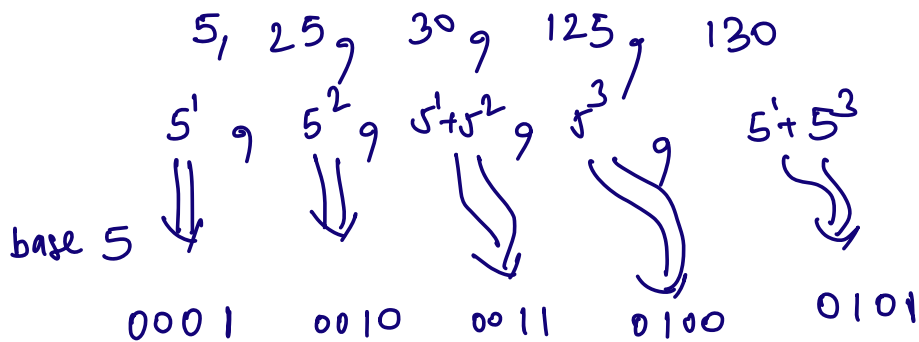
$$\{5^1, 5^2, 5^3, \dots, 5^{13}\} \Rightarrow 5000^{\text{th}} \text{ Magic number}$$

$$\underline{\underline{\{5^1, 5^2, 5^3, \dots, 5^{13}\}}} \rightarrow 8192 \text{ numbers (subsets)}$$

all the subsets.

$$\{5^1, 5^2, 5^3, \dots, 5^{13}\} \Leftarrow$$

all the subsets. sort them
 and ans = Arr[5000]



0001 = 5	1 st Magic = 0001	
0010 = 25	2 nd = 0010	
0011 = 30	3 rd = 0011	
0100 = 125	4 th = 0100	
0101 = 130	5 th = 0101	← (130)
0110 = 150	6 th = 0110	
0111 = 155	7 th = 0111	

value of Ath magic number = ?
 assuming
 Ath Magic = 10010011

convert this into base 5
then Ath Magic number
value.

Code: int Ath Magic number (int A)

int ans = 0 ; int pow-5 = 5 ;

for (int i=0 ; i<32 ; i++)

{

if (A & (1<<i) == 1)

whether its bit
is set
or not

ans += pow-5 ;

ans += pow (5, i)

pow-5 = pow 5 * 5 ;

pow (5, i+1)

T.C → O(32)

S.C → O(1)

}

return ans ;

0th bit

1 0 0 1 0 1 1

↑ ith

4th Magic = 0 0 0 1 0 1 = 5

5⁰
5¹

7

5⁺
x
~~5~~

5⁺

$$\Rightarrow 125 + 5 = 130$$

ROW TO COL ZERO

2-D integer matrix A.
positive

Make all the element in the
row or col. zero (0)

$$\text{if } A[i][j] == 0$$

Mat: $\begin{bmatrix} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 0 \\ 9 & 2 & 0 & 4 \end{bmatrix}$

Make the entire row & col. to zero

Output Matrix $\begin{bmatrix} 1 & 2 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$

row $\Rightarrow \begin{bmatrix} 1 & 2 & 3 & 4 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$

col $\Rightarrow \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$

$\begin{bmatrix} 1 & 2 & 3 & 4 \\ 9 & 6 & 7 & 0 \\ 9 & 2 & 0 & 4 \end{bmatrix} \Rightarrow \begin{bmatrix} 1 & 2 & 3 & 4 \\ x & x & x & 0 \\ x & x & 0 & x \end{bmatrix}$

\Downarrow

$n = -1$

$$\begin{bmatrix} 1 & 2 & 2 & 2 \\ 2 & 2 & 2 & 0 \\ 2 & 2 & 0 & 2 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

code:

$N = \text{no. of rows}$ $M = \text{columns}$

for (int i=0 ; i<n ; i++)

 int flag = 0

 for (int j=0 ; j<m ; j++)

 0 is present

 if (A[i][j] == 0) flag = 1

 }

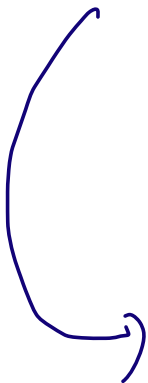
 if (flag == 1)

 for (int j=0 → m)

 if (A[i][j] != 0)

 A[i][j] = -1;

 }



columns

```

for (int i → n)
    for (j → (0, m)) {
        if (A[i][j] == -1)
            A[i][j] = 0;
    }
return A;

```

T.C = $O(N \times M)$
 S.C = $O(1)$

QUES

PRE-REQ

Array of N integers.

(*) answer always exists.

majority element
more than $\lfloor N/2 \rfloor$
times.

arr: $\begin{bmatrix} 6 & 6 & 5 & 3 & 6 \end{bmatrix}$

ans = 6

$N = 5$

$N/2 = 2$

element

arr: $\begin{bmatrix} 3, 2, 5, 3, 3 \end{bmatrix}$ ans = 3

arr: $\begin{bmatrix} 2, 2, 2, 2, 1, 1, 1 \end{bmatrix}$ ans = 2

is there possibility to have
2 majority elements?
if yes array = ?

ⓧ always 1 majority
element

arr : $\left[\begin{array}{ccccccc} 2 & 2 & 2 & 2 & 1 & 1 & 1 \end{array} \right]$
 $\begin{array}{ccccccc} & & & & -1 & -1 & -1 \end{array}$
 $\begin{array}{ccccccc} +1 & +1 & +1 & +1 & & & \end{array}$

arr : $\left[\begin{array}{cccc} 6 & 6 & 3 & 6 \end{array} \right]$
 Maj 6 req = 1 Maj 6 req = 2 Maj 6 req = 1 Maj 6 req = 0 Maj = 6

TC $O(N)$
SC $O(1)$

Ques $N/3$ repeat number
array of N integers.

value which occurs
more than $N/3$

arr: $\boxed{3 \ 2 \ 3}$ $n=3$
 $\frac{3}{3} = 1$
 Ans = 3

Time.

arr: $\boxed{4 \ 4 \ 2 \ 1 \ 4}$ = 4

arr: $\boxed{2 \ 3 \ 2 \ 3 \ 5 \ 6}$ = ? = no majority
 $\frac{6}{3} = 2$ times.
 maj1
 maj2

⊛ at most 2 majority elements are possible

$n/2$ repeat number

```
int maj (vector<int> nums)
{
  int maj = 0;
  int freq = 0;

  for (int i=0; i<n; i++)
  {
    if (nums[i] == maj)
      freq++;
    else if (freq == 0)
  }
```

$n/3$ repeat nums.

```
int maj (vector<int> nums)
{
  int maj1 = 0; int freq1 = 0;
  int maj2 = 0; int freq2 = 0;

  for (int i=0; i<n; i++)
  {
    if (nums[i] == maj1)
      freq1++;
    else if (nums[i] == maj2)
      freq2++;
  }
```

req 2 = 0

Σ maj = nums[i]
req = 1

use if (req1 == 0)
{
maj1 = nums[i]
req1 = 1
}

}
else req--;

int count = 0;
for (int i = 0; i < n; i++)
if (nums[i] == maj)
count++;

if (count > n/2 + 1)
return maj;

use if (req2 == 0)
{
maj2 = nums[i]
req2 = 1
}

else {
req1--; req2--;
}

whether maj1 & maj2
has n/3 more than

arr: [2 3 2 3 5 6]

maj1 = 2 req1 = 1

maj2 = 3 req2 = 1

maj1 = 2 req1 = 2
maj = 3 req2 = 2

Maj1 = 2 req1 = 2

$$\text{maj}_2 = 3 \quad \text{freq}_2 = 1$$

decrease the frequency.

$$\text{maj}_1 = 2 \quad \text{freq}_1 = 1$$

$$\text{maj}_2 = 3 \quad \text{freq}_2 = 1$$

$$\begin{aligned} \text{maj}_1 &= 2 & \text{freq}_1 &= 0 \\ \text{maj}_2 &= 3 & \text{freq}_2 &= 0 \end{aligned}$$

$$\begin{aligned} N/2 \text{ repeat} &= O(N) \text{ Time complexity} \\ &= O(1) \text{ s.c.} \end{aligned}$$

ans: $[1, 1, 1, 2, 2, 2]$

$$N/2 = 2$$

$$\begin{aligned} \text{maj}_1 &= 1 \\ \text{maj}_2 &= 2 \end{aligned}$$

ans: $[1, 2] \quad N/2 = 0$

$$\begin{aligned} \text{maj}_1 &= 1 \\ \text{maj}_2 &= 2 \end{aligned}$$