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# Triangulation of Solid Models having Flat Shapes

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## Problem Definition

To Triangulate a flat shaped solid model of SOLIDWORKS® using Delaunay Triangulation and then generate a .STL file.

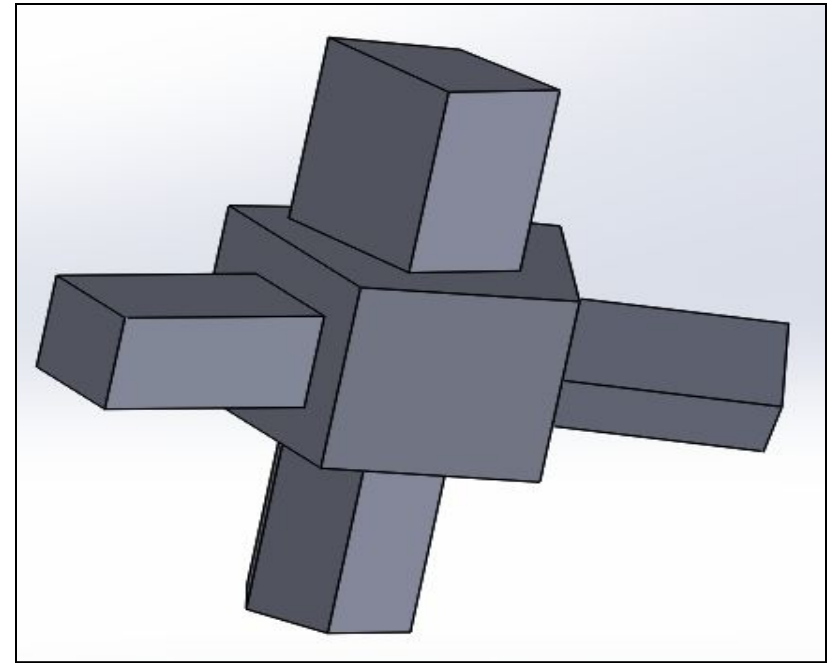
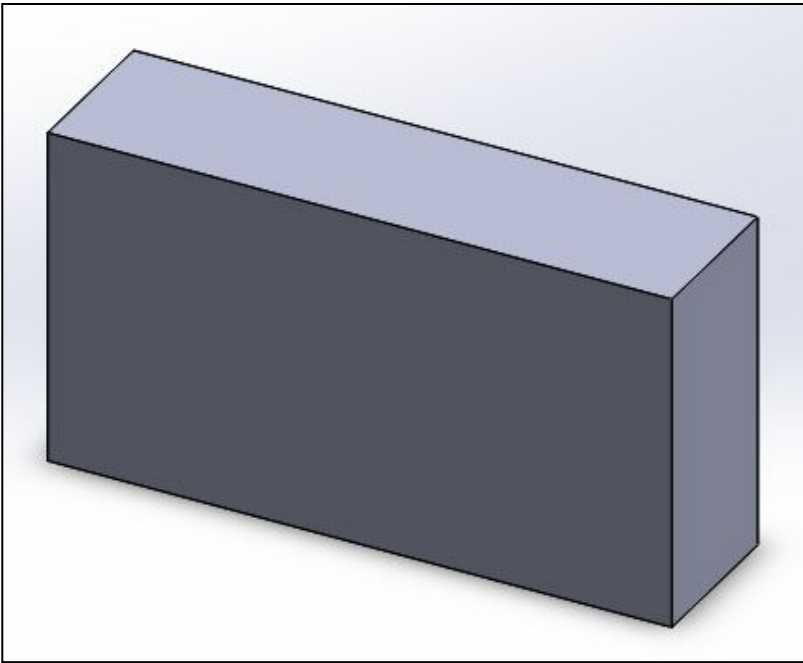


Fig : Solid Model

## Problem Definition

To Triangulate a flat shaped solid model of SOLIDWORKS® using Delaunay Triangulation and then generate a .STL file.

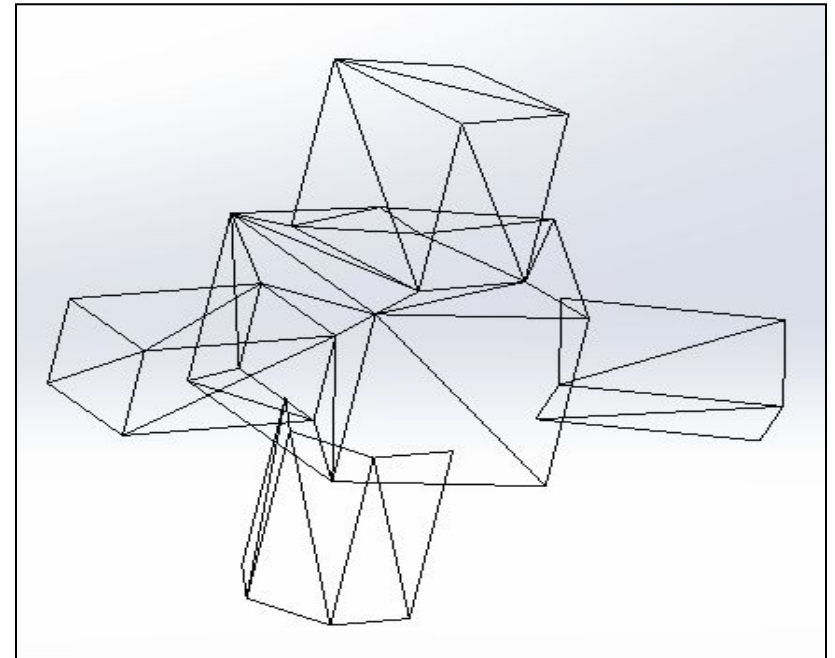
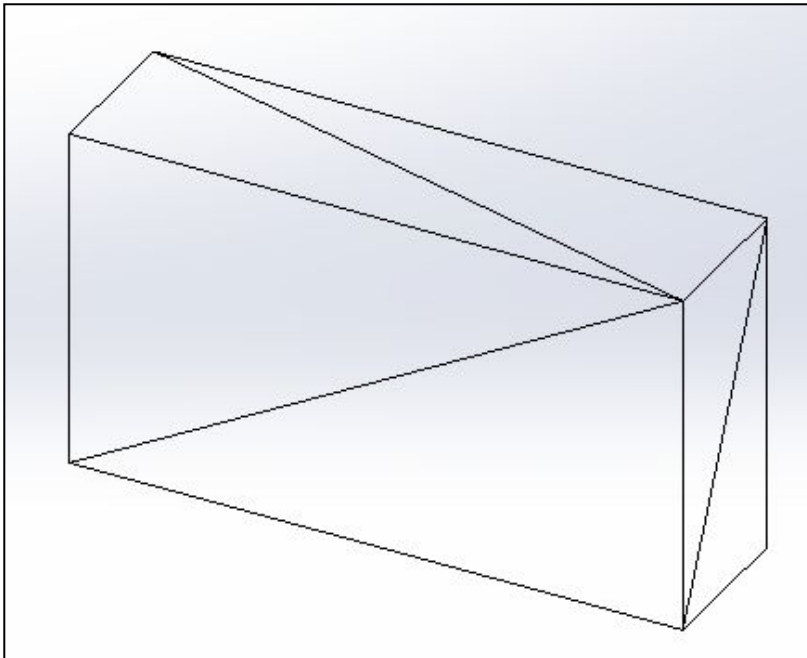


Fig : Triangulated Model

## Rapid Prototyping Industry:

- In all RP processes, the solid model of a component to be produced is created in CAD environment. A tessellated (.STL) version of the CAD model can then be exported and is sliced before transferring the data to the RP machine.
- Tessellated CAD model has become a standard of RP technology

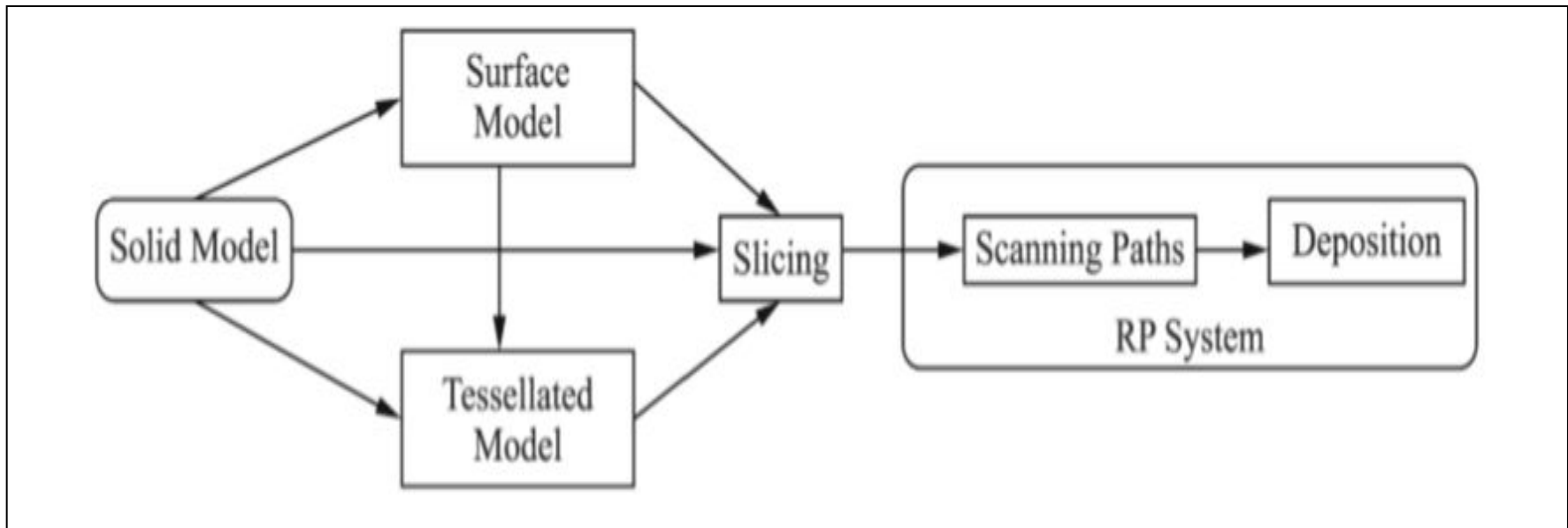
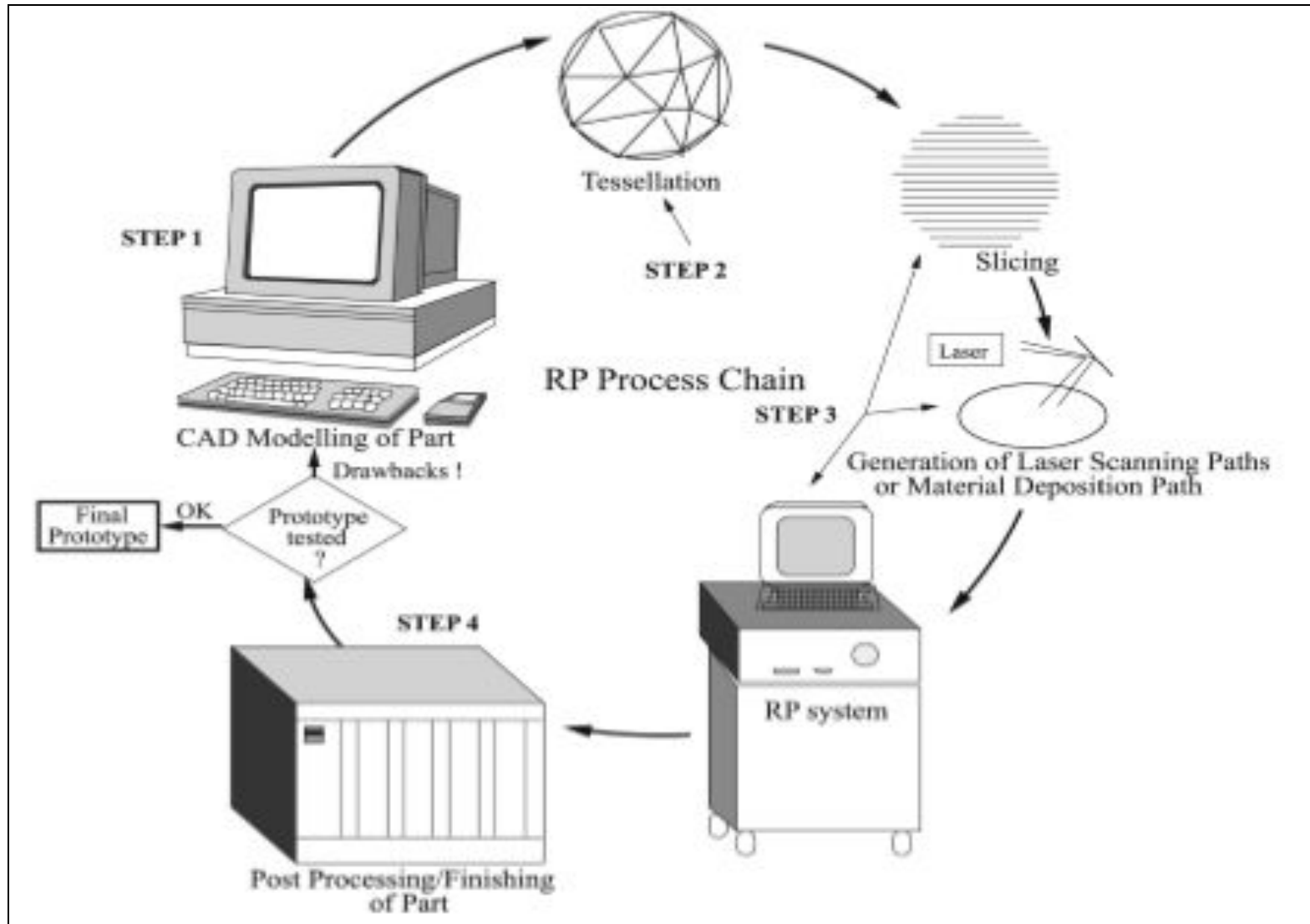


Fig: Rapid Prototyping Process

# Application

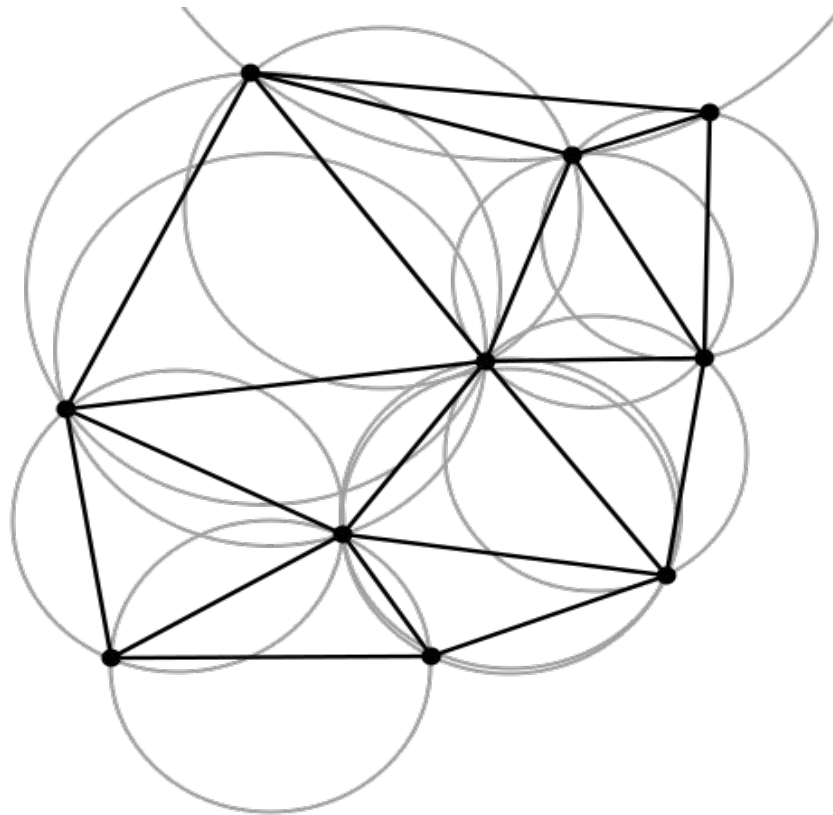
## Rapid Prototyping Process



## Background Research

**Keywords: Delaunay Triangulation, .STL File**

**1. Delaunay Triangulation:** A Delaunay triangulation for a set  $P$  of points in a plane is a triangulation  $DT(P)$  such that no point in  $P$  is inside the circumcircle of any triangle in  $DT(P)$ .



### 2. STL File:

- STL is a file format native to the stereo lithography CAD software created by 3D Systems.
- STL stands for "Standard Triangle Language" and "Standard Tessellation Language."
- An STL file describes a raw unstructured triangulated surface by the unit normal and vertices (ordered by the right-hand rule) of the triangles using a three-dimensional Cartesian coordinate system
- Syntax:

```
facet normal ni nj nk
  outer loop
    vertex v1x v1y v1z
    vertex v2x v2y v2z
    vertex v3x v3y v3z
  endloop
endfacet
```

## Solution Algorithm

Import the Given part file  
(.sldprt) in SOLIDWORKS



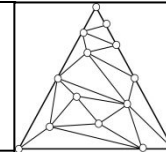
Obtain the vertices of all  
faces as .txt file



Read the Text file  
using MATLAB.



Apply Delaunay  
Triangulation on each face



Obtain the Output as  
.STL file.





## Solution Approach

**1. Obtain the vertices of all faces as .txt file:**

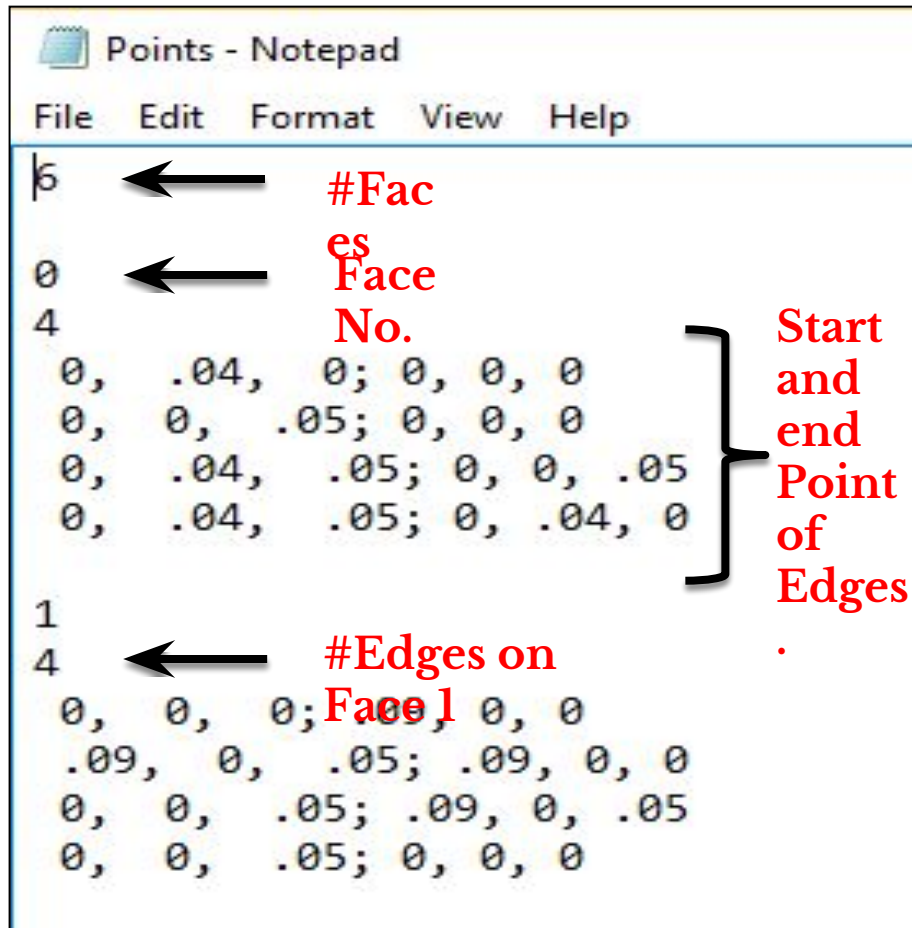
The Following Syntax of SW API Programming are used for generating the .txt file:

Operation	Syntax
Number of Faces:	swBody.GetFaceCount
Select a Face	swBody.GetFaces
Number of Edges	swFace.GetEdgeCount
Select a Edge	swFace.GetEdges
Get Start Point	startVertexObj.GetPoint
Get End Point	endVertexObj.GetPoint
Create Text file	file.CreateTextFile("Points.txt")
Write Text File	filecreate.WriteLine
Execute MATLAB	Interaction.Shell ("matlab.exe")

## Solution Approach

### 2. Read the Text file using MATLAB:

The Code has been written for reading the following text file.



Points - Notepad

File Edit Format View Help

```
6 ← #Faces
0 ← Face No.
4
0, .04, 0; 0, 0, 0
0, 0, .05; 0, 0, 0
0, .04, .05; 0, 0, .05
0, .04, .05; 0, .04, 0
1
4 ← #Edges on Face 1
0, 0, 0; .09, 0, 0
.09, 0, .05; .09, 0, 0
0, 0, .05; .09, 0, .05
0, 0, .05; 0, 0, 0
```

Start and end Point of Edges

### *MATLAB code:*

```
%% Input Points
Data = fileread('Points.txt');
Data = strrep(Data, ',', '');
Data = strrep(Data, ';', ' ');
FID = fopen('Points1.txt', 'w');
fwrite(FID, Data, 'char');
fclose(FID);
N = textread('points1.txt');
```

## Solution Approach

### 2. Apply Delaunay Triangulation on each face.

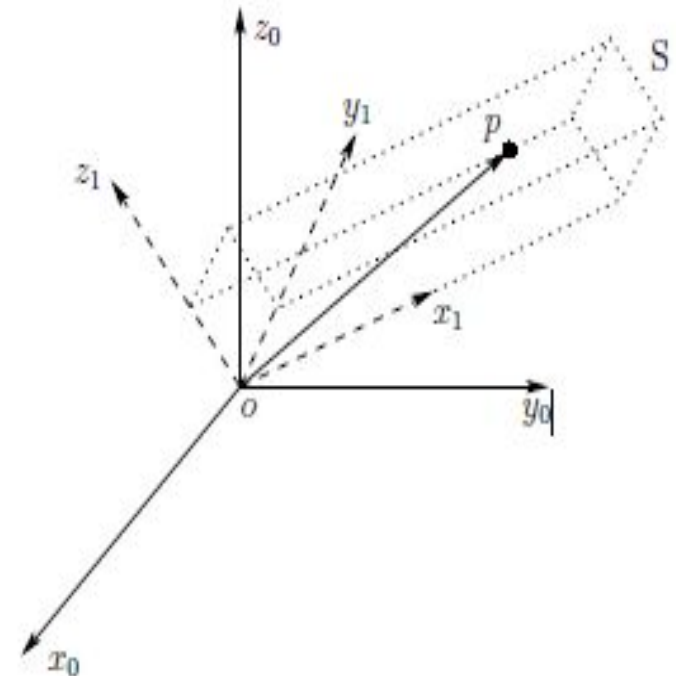
The Delaunay Triangulation is done with following steps:

#### Step 1: Rotation of any Arbitrary Plane :

- An arbitrary plane is rotated such that it is parallel to x-y plane
- $x_o, y_o, z_o$  are the original coordinates (i,j,k).
- $w$  is the unit normal vector to the plane.
- $u, v$  are the orthonormal vectors with respect to  $w$ .
- $(P^1)^T = (P^o)^T * R$

$$R = \begin{bmatrix} u_1 & v_1 & w_1 \\ u_2 & v_2 & w_2 \\ u_3 & v_3 & w_3 \end{bmatrix}$$

- **Syntax:**  $R = [\text{null}(w), \text{transpose}(w)]$ ;



**Source:** Mark W. Spong , “Robot Modeling and Control”, First Edition, John Wiley & Sons, Inc., New York.

## Solution Approach

**STEP 2:** Make a super Triangle

**STEP 3:** Insert points of plane one by one .

**STEP 4:** Check whether the point violates the Delaunay Triangulation Principle. If yes, Collect all the edges of violated triangles.

**STEP 5:** Join those edges with a added point to form new triangles.

**STEP 6:** Delete the super Triangle

**STEP 7:** Get the number of faces (triangle) and vertices of all triangles.

**STEP 8:** Retransform the Triangle back to its plane and obtain new triangle vertices. Calculate its normal.

## 3. Obtain the Output as .STL file format:

File Edit Format View Help

```
solid Part1
  facet normal -1.000000e+00 0.000000e+00 0.000000e+00
    outer loop
      vertex 0.000000e+00 0.000000e+00 0.000000e+00
      vertex 0.000000e+00 0.000000e+00 3.000000e-02
      vertex 0.000000e+00 6.352088e-02 3.000000e-02
    endloop
  endfacet
  facet normal -1.000000e+00 0.000000e+00 0.000000e+00
    outer loop
      vertex 0.000000e+00 0.000000e+00 0.000000e+00
      vertex 0.000000e+00 6.352088e-02 3.000000e-02
      vertex 0.000000e+00 6.352088e-02 0.000000e+00
    endloop
  endfacet
  facet normal 0.000000e+00 1.000000e+00 0.000000e+00
    outer loop
      vertex 0.000000e+00 0.000000e+00 0.000000e+00
      vertex 0.000000e+00 0.000000e+00 3.000000e-02
      vertex 1.150124e-01 0.000000e+00 3.000000e-02
    endloop
  endfacet
```

*MATLAB code:*

```
%% STL File
fid = fopen('stl.txt','at');
for st=1:NF
    for v=1:3
        xv(v)=X(T_out(st,v));
        yv(v)=Y(T_out(st,v));
        zv(v)=Z(T_out(st,v));
    end
    TM=[xv',yv',zv'];
    Tnew=TM*(inv(RM));
    Tnew=round(Tnew,5);
    v1=Tnew(2,:)-Tnew(1,:);
    v2=Tnew(3,:)-Tnew(1,:);
    ntc=cross(v1,v2);
    nt(st,:)=ntc/norm(ntc);
```

## References

**1. SOLIDWORKS API HELP:**

<http://help.solidworks.com/2012/English/api/sldworksapiproguid e/Welcome.htm>

**2. Create .txt file using SW Macro:**

[https://msdn.microsoft.com/en-us/library/aa265018\(v=vs.60\).aspx](https://msdn.microsoft.com/en-us/library/aa265018(v=vs.60).aspx)

**3. Rotate 3D object to align with x-y plane.**

Book: Mark W. Spong , “Robot Modeling and Control”, First Edition, John Wiley & Sons, Inc., New York.

[http://in.mathworks.com/matlabcentral/newsreader/view\\_thread/306882](http://in.mathworks.com/matlabcentral/newsreader/view_thread/306882)

**4. Free online STL viewer.**

<http://www.viewstl.com/>