```
In [260]:
          from numpy import *
          #data = genfromtxt('airfoil self noise.dat')
In [261]:
          data = genfromtxt('yacht_hydrodynamics.data')
          #data = genfromtxt('slump_test.data', delimiter=",", skip_header=1)
          #shape(data)
          Z- score normalization
In [262]:
          data_s = zeros(shape(data))
          for i in range(shape(data)[1]):
              data_s[:,i] = (data[:,i] - data[:,i].mean())/(data[:,i].std())
In [263]:
          def my_regression(trainX,testX,noutput):
              x = [0, 0.01, 0.1, 1, 10, 100, 1000]
              test_pred =[]
              for lamda in x:
                  \# Lamda = 0.1
                  train mat= trainX[:,0:shape(trainX)[1]-noutput]
                  trainT_mul = lamda*eye(shape(trainX)[1]-noutput)+ matmul(train_mat.transp
                   trainT inv = linalg.pinv(trainT mul)
                   final train = matmul(trainT inv, train mat.transpose())
                   n columns = shape(trainX)[1]
                  W = matmul(final train, trainX[:,(n columns-noutput): ])
                  test pred.append(matmul(testX,W))
              return test pred
```

Dividing the data in to train and test using k-fold division and as per requirements for "my_regression" function

```
In [264]:
          k = 5
                        \#K \ fold = 5 \ fold
          noutput = 1 #number of output in data
          data lst = [] #Adding seperate data set of each fold in to list
          for i in range(k):
              if i != (k-1):
                  data_lst.append(data_s[i*(len(data_s)/k):(i+1)*(len(data_s)/k),:])
              else:
                  data_lst.append(data_s[i*(len(data_s)/k):,:])
          trainX_lst = [] #Forming the 5 train datasets in to list
          testX_lst =[] #Forming the 5 test datasets in to list
          for i in range(k):
              data = data lst[i]
              for j in range(i+1,i+k-1):
                  data = concatenate((data, data_lst[j%k]),axis =0)
              trainX lst.append(data)
              testX_lst.append(data_lst[(i+k-1)%k])
```

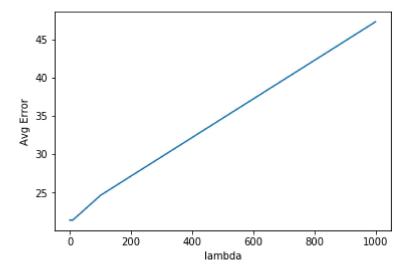
Performing my_regression for linear basis fuction on each of the K-fold data sets and outputting the average square error over k-fold cross validation

```
In [265]: Err = zeros(7)
          for i in range(k):
              trainX_data = trainX_lst[i] #selecting the train dataset from the already sto
              [row,col] = shape(trainX data)
              trainX = ones((row,col+1))
              #Adding bias to data
              trainX[:,1:] = trainX_data
              testX data = testX lst[i] #selecting the test dataset from the already stored
              [row,col] = shape(testX data)
              testX = ones((row,col+1-noutput))
              testX[:,1:] = testX data[:,0:shape(testX data)[1]-noutput]
              testX_output = testX_data[:,shape(testX_data)[1]-noutput:]
              testX_pred = my_regression(trainX,testX,noutput)
              for m in range(7):
                  diff = testX pred[m] - testX output
                  Err[m] = Err[m]+ sum(diff**2)
          print(Err/k)
```

[21.37839087 21.37800249 21.37531095 21.36817659 21.3976475

24.61271058 47.27798177

```
In [266]: import matplotlib.pyplot as plt
lamda = [0, 0.01, 0.1, 1, 10, 100, 1000]
plt.plot(lamda, Err/k)
plt.ylabel('Avg Error')
plt.xlabel('lambda')
plt.show()
```



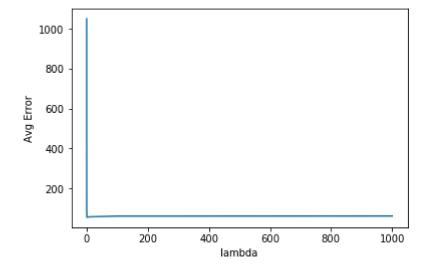
Using Gaussian radial basis function

```
In [267]: #defining Radial basis function with input vector and mean as inputs
    def RBF(x,u):
        sqdist = sum((x-u)**2)
        return exp(-0.5*sqdist)
```

Performing my_regression for Gaussian basis fuction on each of the K-fold data sets and outputting the average square error over k-fold cross validation

```
In [268]:
          Err = zeros(7)
          k = 5
          noutput = 1
          for i in range(k):
              trainX_data = trainX_lst[i]
              trainG_data = trainX_data[:,:-noutput]
              train_data = zeros((shape(trainX_data)[0], 10))
              trainX_output = trainX_data[:,shape(trainX_data)[1]-noutput:]
              testX_data = testX_lst[i]
              testG_data = testX_data[:,:-noutput]
              test_data = zeros((shape(testX_data)[0], 10))
              testX_output = testX_data[:,shape(testX_data)[1]-noutput:]
              data = concatenate((trainG_data, testG_data),axis =0)
              #Getting the mean from the data set
              mean = random.randint(0, shape(data)[0], size=10)
              mean_data = data[mean]
            #Forming new feature matrix using Gaussian RBF function
              for j in range(10):
                  for 1 in range(shape(trainX_data)[0]):
                      train data[1][j] = RBF(trainG data[1,:], mean data[j])
                  for 1 in range(shape(testX_data)[0]):
                      test data[1][j] = RBF(testG data[1,:], mean data[j])
              train data = hstack((train data, trainX output))
              testX pred = my regression(train data,test data,noutput)
              for m in range(7):
                  diff = testX pred[m] = testX output
                  Err[m] = Err[m] + sum(diff**2)
          print(Err/k)
```

```
In [269]: lamda = [0, 0.01, 0.1, 1, 10, 100, 1000]
    plt.plot(lamda, Err/k)
    plt.ylabel('Avg Error')
    plt.xlabel('lambda')
    plt.show()
```



In []:

In []: