

6)

### Calculating work done in strassens' multiplication

#### Multiplication

level	Instance	Size of instance	workdone
0	1	N	0
1	7	n/2	0
K=log n	$7^k$	$n/2^k=1$	$7^k$

Total work done in multiplication =  $7^k = n^{\log_2 7}$

#### Addition

Level	Instances	Size of instance	workdone
0	1	n	$(10/4)n^2$
1	7	n/2	$7(10/4)(n/2)^2$
i	$7^i$	$n/2^i$	$7^i(10/4)(n/2)^{2i}$
K	$7^k$	1	0

$$\begin{aligned}
 \text{Total work done in addition} &= \sum_{i=0}^{k-1} \left(\frac{10}{4}\right)(n^2)7^i/4^i \\
 &= \sum_{i=0}^{k-1} \left(\frac{10}{4}\right)n^2 (7/4)^i \\
 &= (10/4)n^2 ([7/4]^k - 1)/((7/4)-1) \\
 &= (10/3)n^2 (7^{\log_2 n} - n^2)/n^2 \\
 &= (10/3)(n^{\log_2 7} - n^2)
 \end{aligned}$$

$$\text{Total work done} = 2n^{\log_2 7} + (10/3)(n^{\log_2 7} - n^2) \quad \text{----> Equation 1}$$

Considering multiplication takes twice as long as addition.

$$\text{Work done in iterative matrix multiplication} = 2n^3 + n^3 = 3n^3 \quad \text{-----> Equation 2}$$

Again considering multiplication takes twice as long as addition.

For all values of n lesser than the point where Equation 1 = Equation 2 meet, iterative performs better.

For values of n greater than the point of intersection, strassens' multiplication takes lesser time.

$$2n^{\log_2 7} + (10/3)(n^{\log_2 7} - n^2) - 3n^3 = 0$$

Solving for n, we get n=12.9118

Rounding upto the next power of n, we get n = 16