



Quantifying The Dimensionality Of Image Manifold For Classification

DEEPALI BIDWAI, HOMERO ESMERALDO, MENNAT ALLAH KHALIFA, MOHAMED GAMAL, PAWAN THAPALIYA, TULIKA KHARGONKAR

AWESOME MENTORS: MOBIN NESARI, REZA RAJABLI

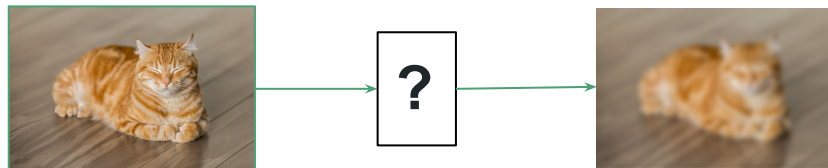
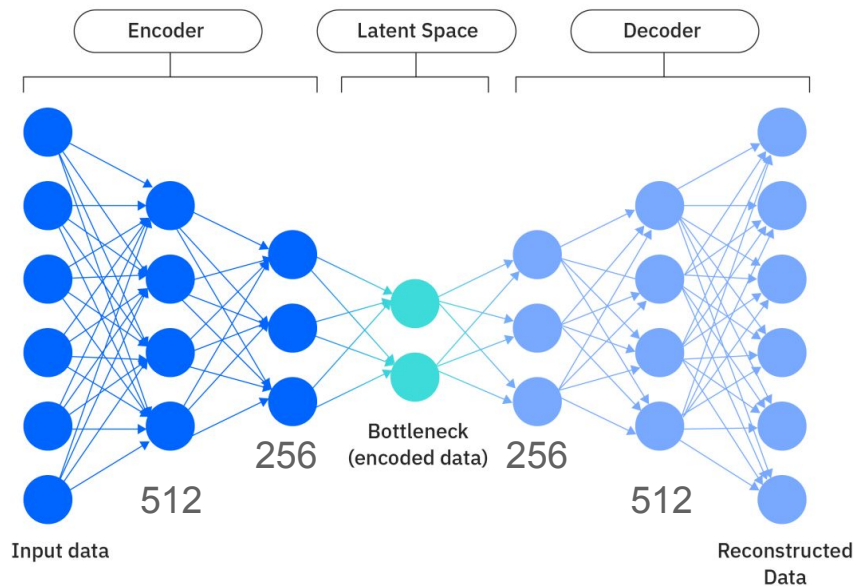


THE MORRIGAN | 7-LAYER PERCEPTRON

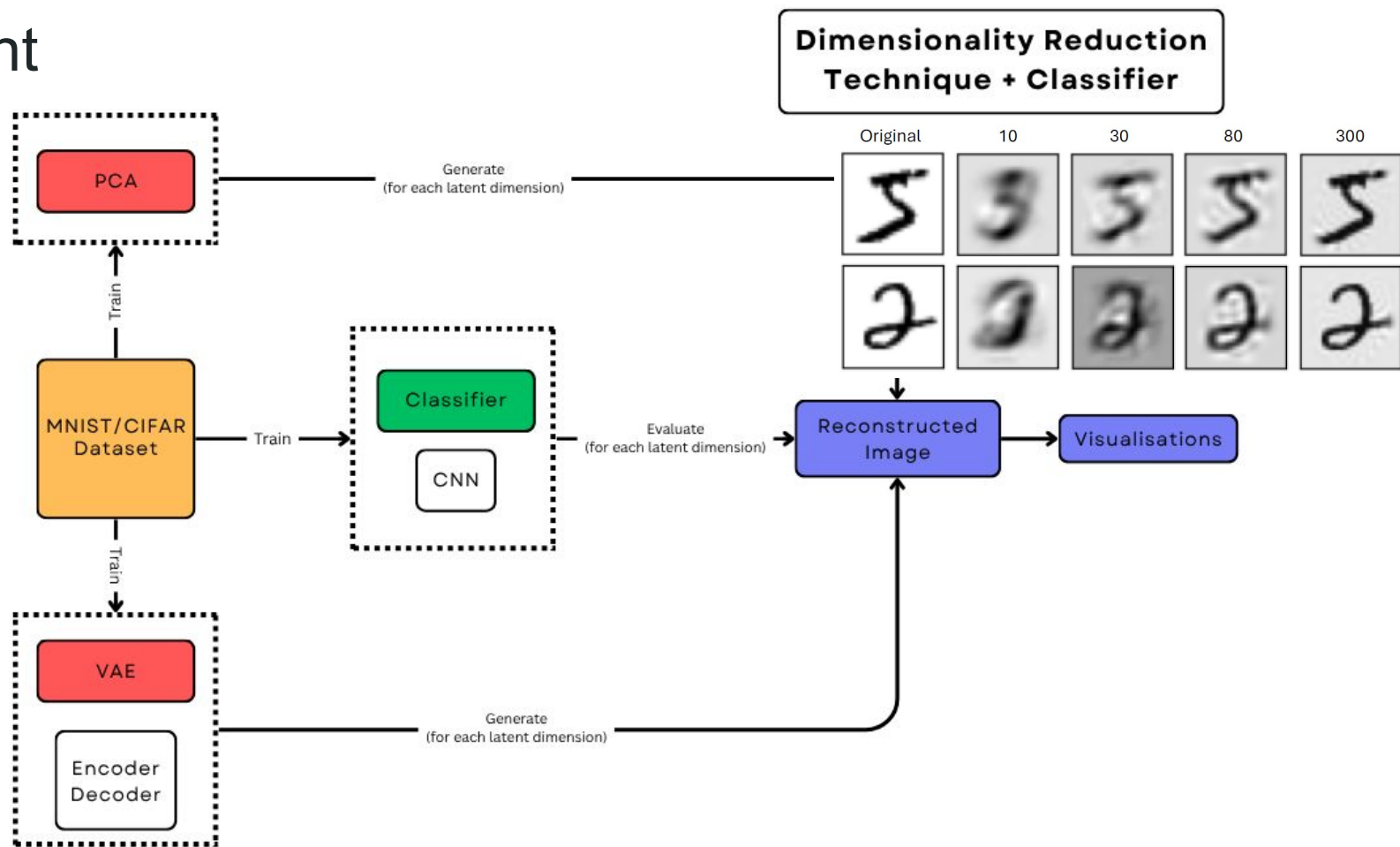
Introduction

Why quantify dimensionality of a dataset?

- Manifold Hypothesis: A low dimensional manifold can approximate the dataset embedded in a high dimensional space (Causin & Marta, 2025).
- Dimensionality of input affects representations of networks trained on it (Huh et al, 2024).



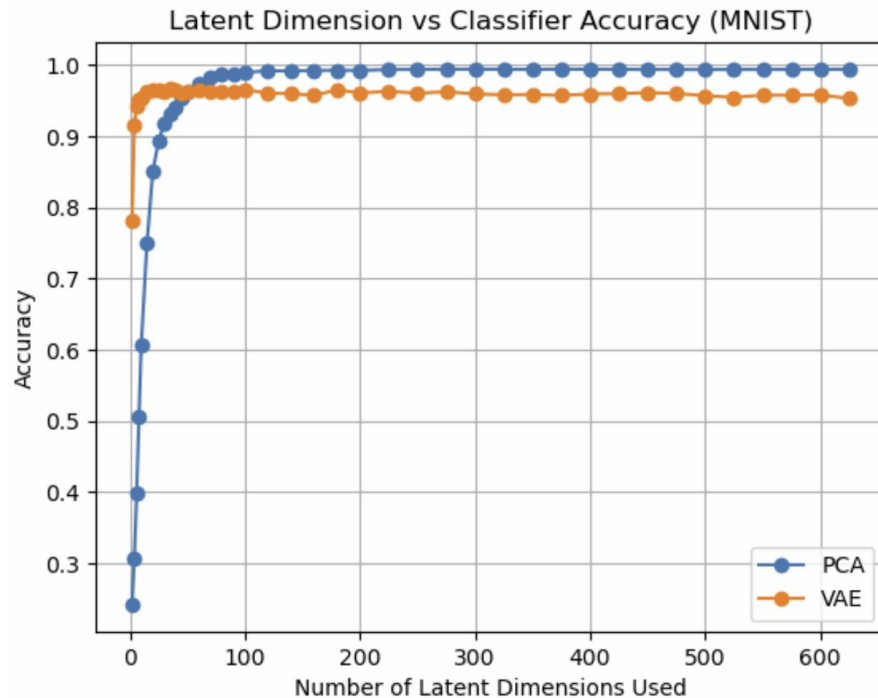
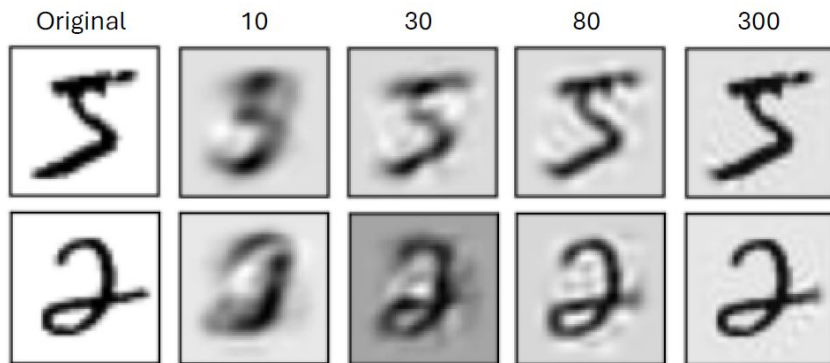
Experiment Pipeline



Results

PCA vs VAE

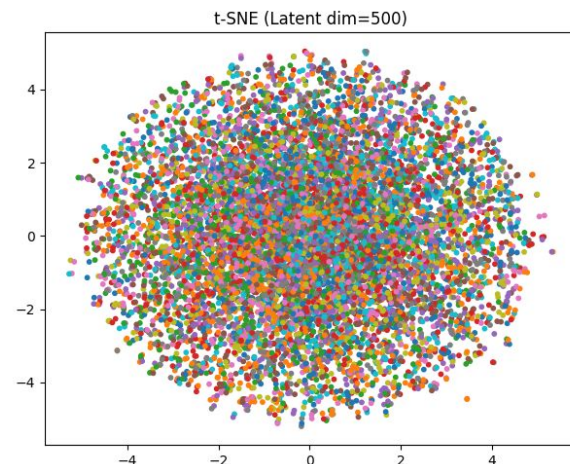
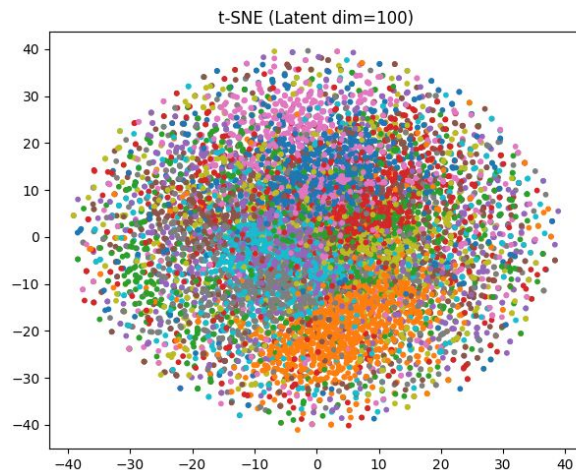
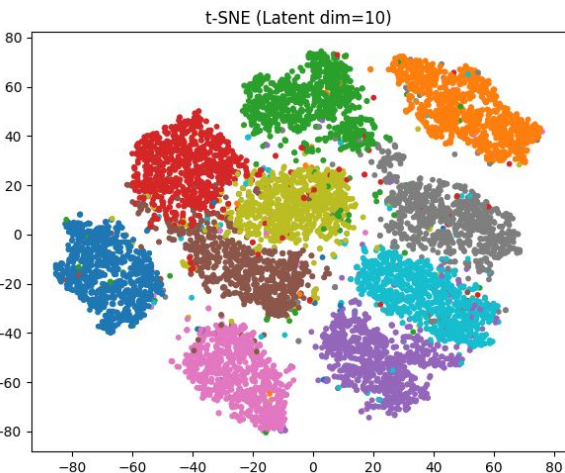
Example reconstructed images



- Test accuracy rises with latent size, then plateaus.
- VAE rises much earlier than PCA (nonlinear technique is more powerful)
- PCA has higher accuracy at the plateau

Effect of Latent Dimension on Latent Space Structure (MNIST)

t-SNE



- t-SNE shows clear clusters at low latent dims.
- Clusters blur at high dims, showing less structure.
- Tradeoff: small latent spaces compress well; large ones better reconstruct but low dimensionality visualization shows less clusters

β -VAE

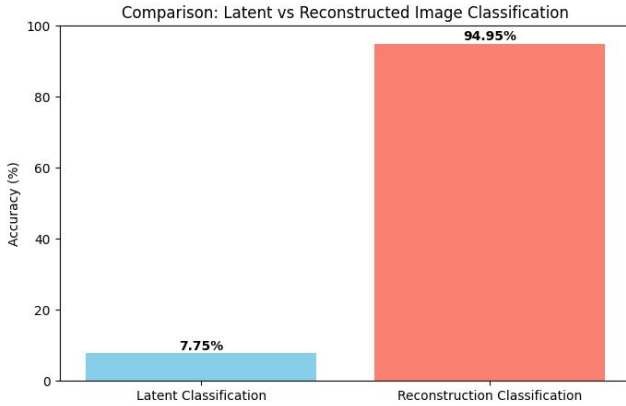
We manipulated Loss function parameters to understand how it affects classification of the reconstructed images and of the bottleneck features

$$\text{Loss Function} = \text{BCE} + \textit{beta} * \text{KLD} + \textit{alpha} * \text{CE}$$

Reconstruction

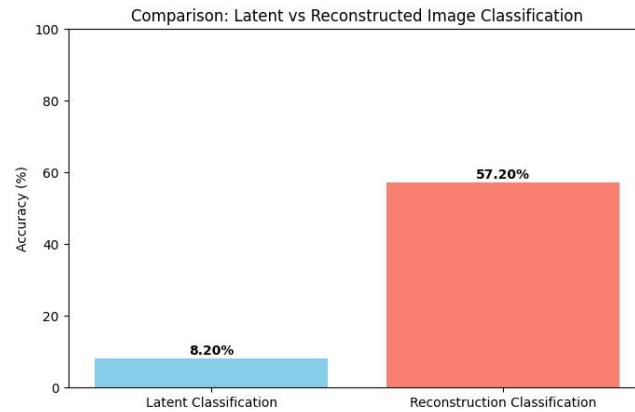
Bottleneck distribution regularization (Gaussian)

Classifiability of the bottleneck



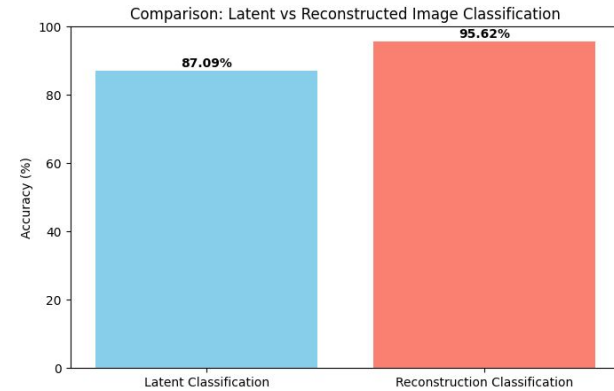
$\alpha=0$, $\beta=1$

Bottleneck features are not linearly classifiable



$\alpha=0$, $\beta=10.0$

Increasing beta collapses representations in the bottleneck and harms classification accuracy

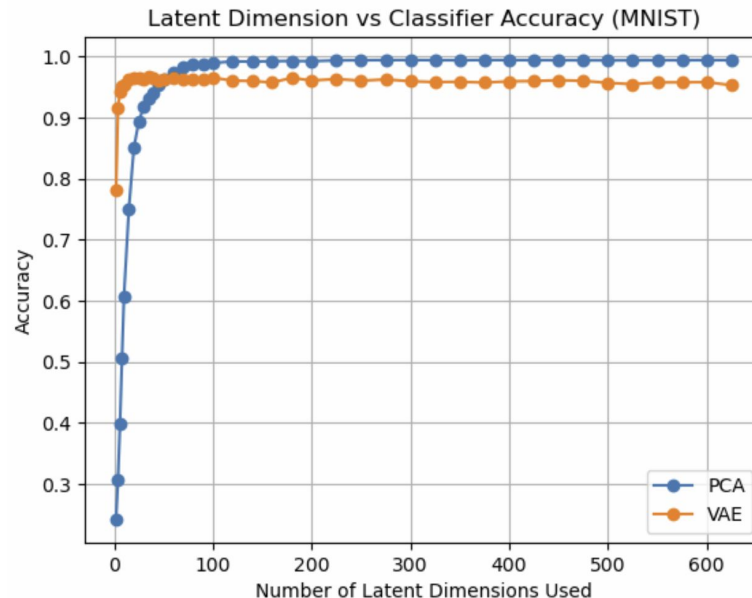


$\alpha=1$, $\beta=1$

Including bottleneck classification in the loss increases its classifiability

Conclusion

- VAE can represent images with fewer latent dimensions than PCA, preserving classification accuracy for low dimensional latent space
- PCA does better than VAE at higher dimensions
- Better understanding of manifold dimensionality by comparing VAE and PCA



In the next episode...

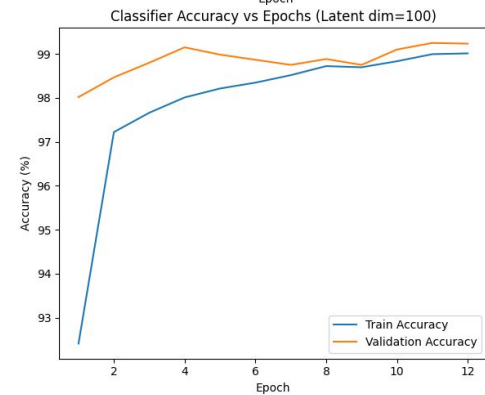
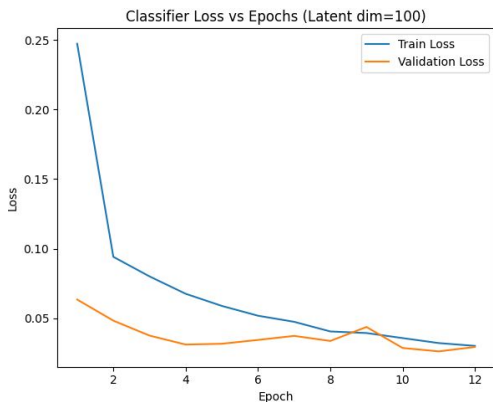
- We're closer to quantifying latent dimensionality but not entirely
- Why is VAE's accuracy lower than PCA at higher dimensions? Can it potentially change with different VAE modifications?
- How do these results change with more complex datasets?

Thank you to our colleagues, TAs and
NMA!

Appendix

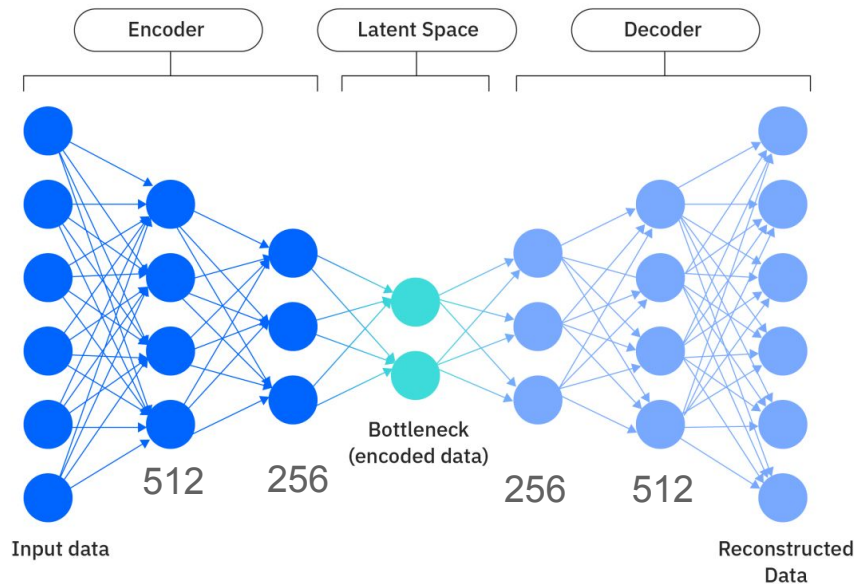
Training

No overfitting:



VAE architecture

BatchNorm1d, ReLU



Classifier

```
nn.Conv2d(1, 32, kernel_size=3, padding=1),  
nn.BatchNorm2d(32),.ReLU(), nn.MaxPool2d(2, 2),
```

```
nn.Conv2d(32, 64, kernel_size=3, padding=1),  
nn.BatchNorm2d(64), .ReLU(), .MaxPool2d(2, 2),
```

```
nn.Flatten(),  
nn.Linear(64 * 7 * 7, 128),  
nn.ReLU(),  
nn.Dropout(0.25),  
nn.Linear(128, 10)
```

t-SNE | PCA

