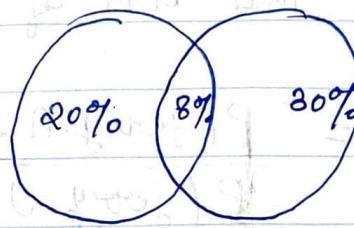


DEEPALI NAGWADE

Assignment - 1

①



Susan at Bank

Susan not at Bank

Jerry at Bank

8%

12%

Jerry not at Bank

22%

58%

- (a) Susan was there last monday, what is the probability that Jerry was there too.

Solⁿ

$$P(\text{Jerry} | \text{Susan}) = \frac{P(\text{Jerry} \cap \text{Susan})}{P(\text{Susan})}$$

$$= 8/30 = \boxed{26.66\%}$$

- (b) Last friday, Susan wasn't at the bank. What's the probability that Jerry was there

Solⁿ

$$P_{\text{sol}}(\text{Jerry} | \text{Susan}') = \frac{P(\text{Jerry} \cap \text{Susan}')}{P(\text{Susan}')} = \frac{12}{70} = \boxed{17.14\%}$$

- c) last wednesday, at least one of them was at the bank
 what is the probability that both of them were there?

$$P(\text{Jerry} | \text{Susan}) = \frac{P(\text{Jerry} \cap \text{Susan})}{P(\text{Jerry} \cup \text{Susan})}$$

$$= \frac{18}{42} = 19.04\%$$

Homework 1.2

Given

Harold's chances of getting B = 80%

Sharon's chances of getting B = 90%

Both atleast 1 = 91%

- a) Probability of only Harold getting B

$$\Rightarrow P(\text{only Harold}) = P(\text{Harold}) - P(\text{Harold} \cap \text{Sharon})$$

$$= 80 - 79$$

$$= \boxed{1\%}$$

- b) Probability of ^{only} Sharon get a B

$$\Rightarrow P(\text{only Sharon}) = P(\text{Sharon}) - P(\text{Harold} \cap \text{Sharon})$$

$$= 90 - 79$$

$$= \boxed{11\%}$$

- c) Probability that both ^{would} _{won't} get a "B"

$$\begin{aligned}
 P(\text{Harold n Sharon}) &= 100 - P(\text{Harold or Sharon}) \\
 &= 100 - 91 \\
 &= \boxed{9\%}
 \end{aligned}$$

Homework 1.3

Are the events "Jerry at the bank" and "Susan is at the bank" independent?

Ans if the events were independent, then their visit to the bank have no effect on each other and Probability of both being there would be product of their individual probabilities $(20\% * 30\%) = 6\%$

\therefore Both events are not independent

Homework 1.4

(a) Events "the sum is 6" and "second die shows 5" independent

Ans $P(\text{second die} = 5 \text{ and sum} = 6) = P(\text{sum} = 6) * P(\text{Second die} = 5)$

$$\frac{5}{36} * \frac{6}{36} = \frac{1}{36} \quad (\text{which is not equal})$$

\therefore Both events are not independent

b) Are events "the sum is 7" and "first die shows 5" independent?

Ans

$$P(\text{first die} = 5 \text{ & sum} = 7) = P(\text{sum} = 7) * P(\text{first} = 5)$$

$$\frac{1}{36} = \frac{6}{36} * \frac{6}{36}$$

∴ As both events are equal, events are independent.

Homeworks 1.5

(a) Given $\cdot TX = 60\% \quad NJ = 10\%$

$$P(\text{finding oil}) = TX = 30\% \quad | \quad AK = 20\% \quad | \quad NJ = 10\%$$

(a) Probability of finding oil = ?

Solⁿ Prob. of finding oil in a state & Prob. of choosing that state.

$$\text{for } TX : P(\text{oil} | TX) * P(TX) = 30\% * 60\% = 18\%$$

$$\text{for } AK : P(\text{oil} | AK) * P(AK) = 20\% * 30\% = 6\%$$

$$\text{for } NJ : P(\text{oil} | NJ) * P(NJ) = 10\% * 10\% = 1\%$$

Aus Probability of finding oil = $18\% + 6\% + 1\% = \underline{25\%}$

(b) Probability that they drill in TX

Aus $P(TX|oil) = \frac{P(TX * oil)}{P(oil)} = \frac{18}{25} = 72\%$

TW 1.6 Titanic survivor data

a) Prob that passenger didn't survive

Sol $P(\text{Not S}) = \frac{1490}{2201} = \underline{0.6769}$

b) Prob that passenger was staying in first class.

Sol $P(F) = \frac{203+122}{2201} = \frac{325}{2201} = \underline{0.1476}$

c) Prob that pass survived who are first class.

Sol $P(S) = P(S \& FC) = \frac{203}{711} = \underline{0.2855}$

d) Are survival & staying in FC independent?

Sol

PTD

"if prob of staying in FC and survival are equal then they are independent as mutually exclusive to each other."

$$\begin{aligned} P(\text{surviving}) &= 100 - P(\text{not surviving}) \\ &= 100 - 67.69 \end{aligned}$$

$$P(\text{surviving}) = 32.31\% \rightarrow 0.3231$$

$$\begin{aligned} P(\text{staying in FC}) * \text{Prob of survival} \\ 0.1476 * 0.3231 = 0.4768 \end{aligned}$$

\therefore Events are not independent

(e) Prob of surviving passenger (Fc & child)

Ans

$$P(S, Fc, \text{child}) = \frac{6}{711} = 0.0084$$

(f) Prob of surviving pass & adult

Ans

$$P(S, P, \text{Adult}) = 597/711 = 0.8396$$

(g) are age & FC independent?

Ans

$$P(\text{age of P sur}) = 654/711 + 57/711 = 711/711 = 1$$

$$P(C) = 203/711 = 0.2855$$

$$P(\text{age} \& \text{FC}) \rightarrow 1 * 0.2855 = 0.2855$$

equal \therefore independent