

# Likelihood Ratios for Out-of-Distribution Detection

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**ADOPT** | Advanced Design, Optimization and  
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- Introduction
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# Problem Statement 1/2

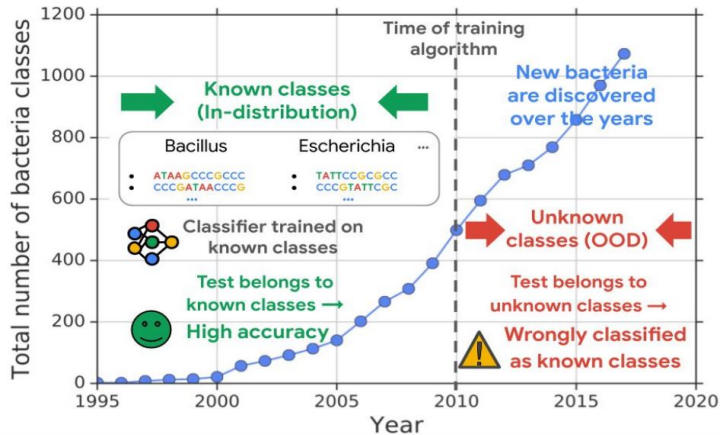


Figure 1: Bacteria identification based on genomic sequences

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**”Need accurate OOD detection to ensure safe deployment of classifier”**

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In-distribution dataset  $\mathbf{D}$  of  $(\mathbf{x}, \mathbf{y})$  pairs sampled from the distribution  $\mathbf{p}^*(\mathbf{x}, \mathbf{y})$ :

- $x_d \in [A, C, G, T]$  for genomic sequences and  $x_d \in [0, \dots, 255]$  for images
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Existing methods:

- **Classifier-based:** taking the confidence or entropy of the predictive distribution  $p(y|x)$
- **Density-based:** fit a generative model  $p(x)$  to the input data, and then evaluate the likelihood of new inputs under that model

# Background

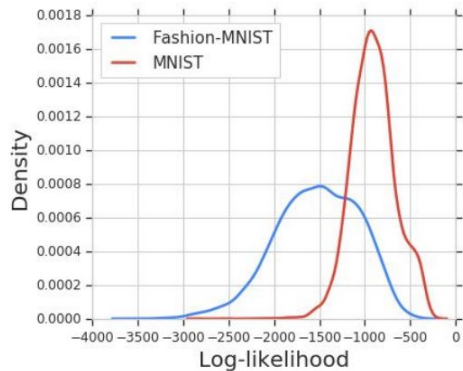


Figure 2: MNIST (OOD) vs Fashion-MNIST (in-dist.)  
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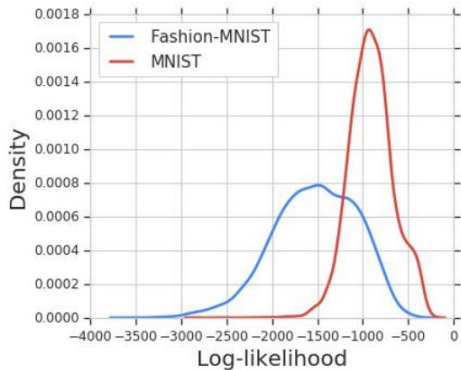


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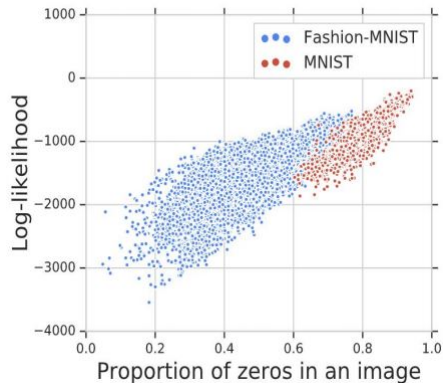


Figure 3: Likelihood is highly correlated with the background

# High level idea 1/2

## Background vs Semantic Component:

Assume that an input  $\mathbf{x}$  is composed of two components:

$$\mathbf{x} = \mathbf{x}_B + \mathbf{x}_S$$

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## Background vs. Semantics Examples:

- Images: **background** + **object**
- Text: **stop words** + **key words**
- Genomics: **GC content** + **motifs**
- Speech: **background noise** + **speaker**

## High level idea 2/2

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$$LLR(x) = \log \frac{p_\theta(x)}{p_{\theta_0}(x)} = \log \frac{p_\theta(x_B)p_\theta(x_S)}{p_{\theta_0}(x_B)p_{\theta_0}(x_S)} \quad (2)$$



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Assume that both models capture the background information equally well:

$$LLR(x) = \log(p_\theta(x_S)) - \log(p_{\theta_0}(x_S)) \quad (3)$$

# Likelihood Ratio for OOD detection 1/2

## Algorithm 1: Training the Background Model

- **Inputs:** D-dimensional input  $\mathbf{x} = x_1 \dots x_D$ ,  $x_d \in F$ , where  $F = [A, C, G, T]$  or  $[0, \dots, 255]$
- **Output:** perturbed input  $\bar{\mathbf{x}}$

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- Generate a D-dimensional vector  $\mathbf{v} = v_1 \dots, v_D$ , where  $v_d \in [0, 1]$  are independent and identically distributed according to a Bernoulli distribution with rate  $\mu$
- **for** index  $d \in [1, \dots, D]$ 
  - if**  $v_d = 1$ 
    - Sample  $\bar{x}_d$  from the set  $F$  with equal probability
  - else**
    - $\bar{x}_d = x_d$
  - end**
- end**

## Likelihood Ratio for OOD detection 2/2

### Algorithm 2: OOD detection using Likelihood Ratio

- **Inputs:** D-dimensional test input  $x = x_1 \dots x_D$
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- Fit a background model  $p_{\theta_0}(x)$  using perturbed input data  $\bar{D}_{in}$  (generated using Algorithm 1) and (optionally) model regularization techniques
- Compute the likelihood ratio statistic:

$$LLR(x) = \log(p_\theta(x_S)) - \log(p_{\theta_0}(x_S)) \quad (4)$$

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### Algorithm 2: OOD detection using Likelihood Ratio

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- **Predict OOD if  $LLR(x)$  is small**

# OOD detection for Images 1/2

- **Fashion-MNIST (in-dist.) vs. MNIST (OOD):** PixelCNN++ model is trained on Fashion-MNIST
- **Likelihood** is dominated by the **background pixels**  $\implies p(\text{Fashion-MNIST}) < p(\text{MNIST})$
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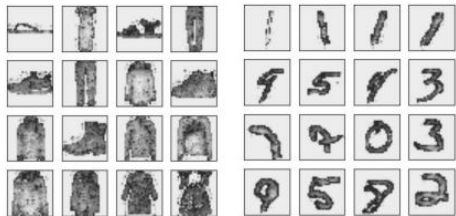


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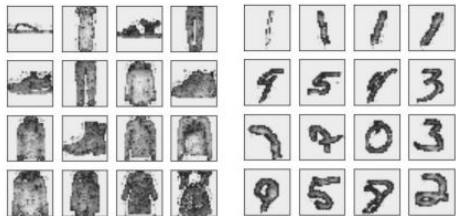


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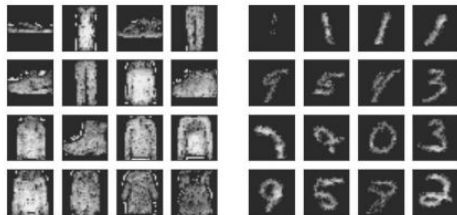


Figure 5: Likelihood ratio of pixels

# OOD detection for Images 2/2

## Error Metric

- **AUROC**↑: Area under the ROC curve
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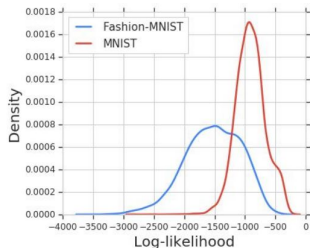


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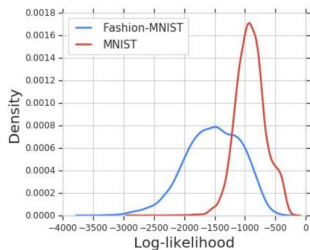


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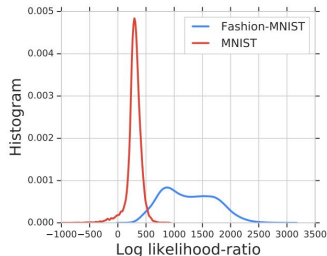


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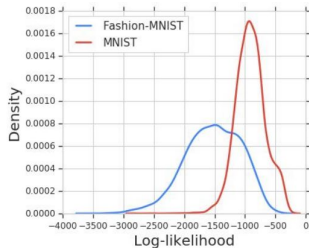


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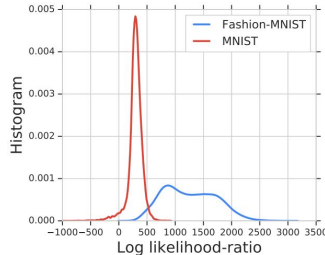


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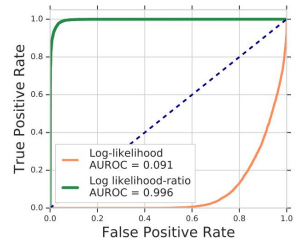


Figure 8: Likelihood ratio significantly improves the AUROC of OOD detection from 0.091 to 0.996

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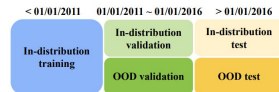


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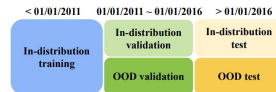


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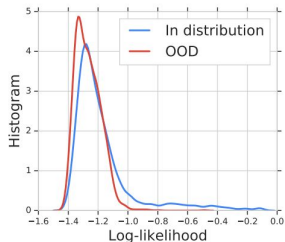


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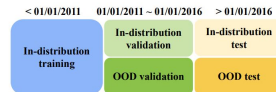


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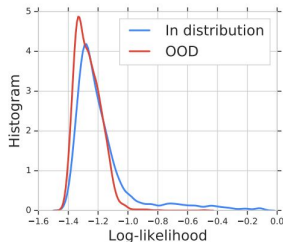


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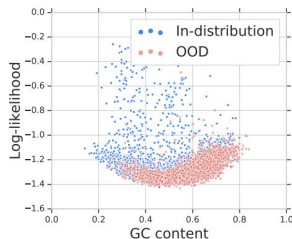


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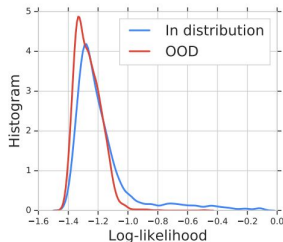


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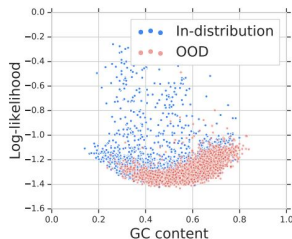


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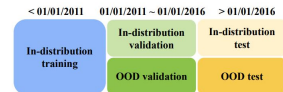


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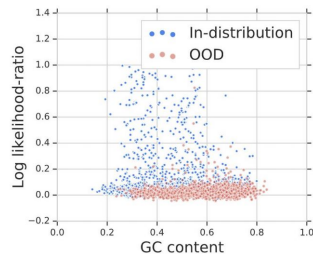


Figure 12: Corrected GC-content of a sequence

# OOD detection for Genomic Sequences 2/2

- LSTM model is trained using sequences from in-distribution classes
- Likelihood Ratio significantly improves OOD Detection
- Effect of background GC-content is corrected
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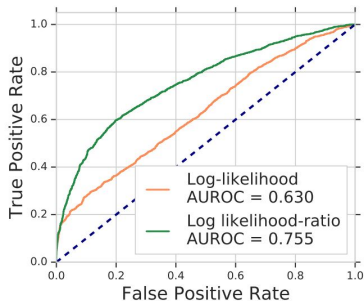


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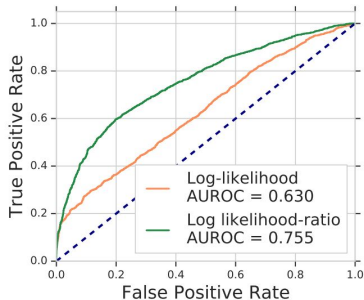


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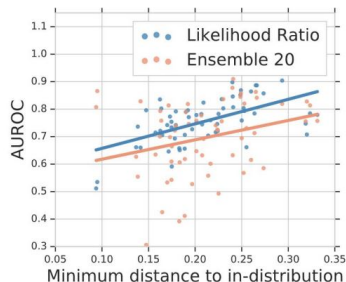


Figure 14: Correlation between the AUROC of OOD detection and distance to in-distribution classes



# Summary

- Create a **realistic benchmark dataset** for OOD detection (and open-set classification) in genomics
- Show that the likelihood from deep generative models can be **confounded by background statistics**
- Propose a **likelihood ratio method** for unsupervised OOD detection, outperforming the raw likelihood
- Proposed method performs well on **images and achieves state of the art (SOTA) performance on genomic dataset**



- Author assumes that background and semantic component of input are independent, which may not be true in many practical application
- GC content of a sequence is similarly a function of the semantic component when classifying bacterial sequences
- The AUROC being significantly worse than random on the Fashion MNIST dataset isn't explained
- Given the experimental evidence and the novelty of the method, it is important contribution for OOD detection
- **Given the genomics sequence, this method can be used for finding out new strain of COVID'19**
- **Proposed method can be used for early detection of disease, which is significant contribution in respective area**

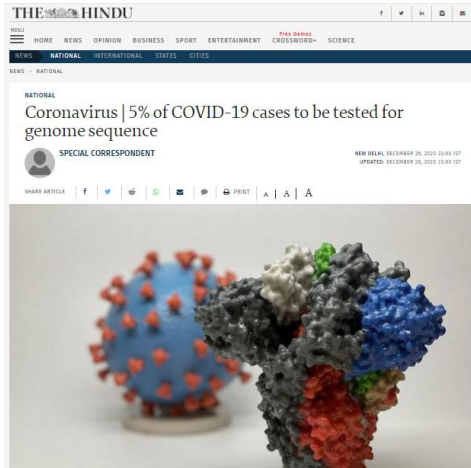


Figure 16: New variant of COVID'19 identification based on genomic sequencing

# References

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# Thank You