

**JALPAIGURI GOVERNMENT ENGINEERING COLLEGE**  
**[A GOVERNMENT AUTONOMOUS COLLEGE]**  
**COE/B.TECH.(ME/CE/EE/ECE)/ BS-M201B/2022-23**  
**2023**  
**MATHEMATICS-IIB**

Full Marks: 70

Time: 3 Hours

*The figures in the margin indicate full marks.*  
*Candidates are requested to write their answers in their own words as far as practicable.*

**GROUP-A**  
**[OBJECTIVE TYPE QUESTIONS]**

Answer **all** questions

- |   |             |
|---|-------------|
| 1. Transform the differential equation $xy \cos x^2 dx + 2 \sin x^2 dy = 0$ into an exact differential equation.                            | 5x2=10<br>2 |
| 2. Show that $J_{\frac{1}{2}}(x) = \sqrt{\frac{2}{\pi x}} \sin x$ .   | 2           |
| 3. Using Green's theorem, show that $\frac{1}{2} \oint_C (x dy - y dx) = \text{area of the region enclosed by the closed curve } C$ .       | 2           |
| 4. Locate and classify (with reason) the singular points of the equation<br>$x(x-1)^3 \frac{d^2 y}{dx^2} + 2(x-1)^3 \frac{dy}{dx} + 3y = 0$ | 2           |
| 5. Show that the function $f(z) = \bar{z}$ is continuous at $z = 0$ but not differentiable there.   | 2           |

**GROUP-B**  
**[LONG ANSWER TYPE QUESTIONS]**

Answer any **five** questions

- |  |          |
|--|----------|
| 6. i) Solve : $xy dx + (2x^2 + 3y^2 - 12) dy = 0$  | 4        |
| ii) Solve: $\frac{dy}{dx} + y = y^3(\cos x - \sin x)$  | 4        |
| iii) Find the general solution and the singular solution of the differential equation<br>$y = x \frac{dy}{dx} + \sqrt{49 \left( \frac{dy}{dx} \right)^2 + 25}$ | 2+2<br>4 |
| 7. i) Solve: $\frac{d^2 y}{dx^2} - 5 \frac{dy}{dx} + 6y = (xe^x)^3$ .  | 4        |
| ii) Solve by the method of variations of parameters : $\frac{d^2 y}{dx^2} + a^2 y = x \cos ax, a \neq 0$ .   | 4        |
| iii) Solve: $x^2 \frac{d^2 y}{dx^2} - x \frac{dy}{dx} + 4y = x \sin(\log x)$ .   | 6        |
| 8. i) Find the power series solution of the equation $(1+x^2) \frac{d^2 y}{dx^2} + x \frac{dy}{dx} - xy = 0$ in powers of $x$ .                                | 2+2      |
| ii) Use Rodrigue's formula to evaluate $P_0(x), P_1(x), P_2(x), P_3(x)$ . Hence express $f(x) = 4x^3 + 6x^2 + 7x + 2$ in terms of Legendre's polynomials.      | 2        |
| iii) Write the solution of the equation $x^2 \frac{d^2 y}{dx^2} + x \frac{dy}{dx} + (k^2 x^2 - n^2)y = 0$ by reducing it to Bessel's equation.                 | 2        |

i) Evaluate  $\iint_R \frac{\sqrt{a^2b^2 - b^2x^2 - a^2y^2}}{\sqrt{a^2b^2 + b^2x^2 + a^2y^2}} dx dy$  where  $R$  is the positive quadrant of the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ .

6

ii) Evaluate  $\iint_R xy(x+y) dx dy$  where  $R$  is the region enclosed by the curves  $y = x, y = x^2$ .

6

10. i) State Green's theorem. Use Green's theorem to evaluate

1+5

$\int_C [(3x - 8x^2)dx + (4y - 6xy)dy]$  where  $C$  is the boundary of the region bounded by  $x = 0, y = 0$  &  $x + y = 1$ .

ii) State Stoke's theorem. Evaluate  $\int_C \vec{F} \cdot d\vec{r}$  by Stoke's theorem, where

1+5

$\vec{F} = y^2\hat{i} + x^2\hat{j} - (x+z)\hat{k}$  and  $C$  is the boundary of the triangle with vertices at  $(0,0,0), (1,0,0), (1,1,1)$ .

11. i) Prove that the function  $f(z)$  defined by  $f(z) = \begin{cases} \frac{(z)^2}{z}, & z \neq 0 \\ 0, & z = 0 \end{cases}$

3+3

is not differentiable at the origin though Cauchy-Riemann equations are satisfied at that point.

ii) Show that the function  $u(x, y) = e^x(x \cos y - y \sin y)$  is harmonic and find a function  $v(x, y)$  such that  $f(z) = u + iv$  is analytic. Then express  $f(z) = u + iv$  as a function of  $z$ .

2+2+2

12. i) State Laurent's theorem. Expand the function  $f(z) = \frac{z^2-1}{z^2+5z+6}$  as a Laurent's series in the region  $2 < |z| < 3$ .

2+4

ii) Evaluate  $\int_{\Gamma} z^2 dz$  where  $\Gamma$  is the boundary of the triangle with vertices  $0, 1+i, -1+i$  and traversed in the clockwise sense.

6

13. Find the bilinear transformation which maps the points  $z = 1, i, -1$  into the points  $w = i, 0, -1$  respectively.

3

ii) Use Cauchy's integral formula to evaluate  $\iint_C \frac{e^z}{z^2+4} dz$  where  $C$  is the positively oriented circle  $|z-i| = 2$ .

3

iii) Evaluate  $\int_0^{2\pi} \frac{\cos 2\theta}{5+4 \cos \theta} d\theta$ , using Cauchy's residue theorem.

6

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**JGEC/B.TECH/ CE/EE/ME/ ES- EE 201/ 2022-23**  
**2023**  
**BASIC ELECTRICAL ENGINEERING**

Full Marks: 70

Times: 3 Hours

*The figures in the margin indicate full marks.*  
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**GROUP-A**  
**[OBJECTIVE TYPE QUESTIONS]**

5x2=10

Answer **all** questions

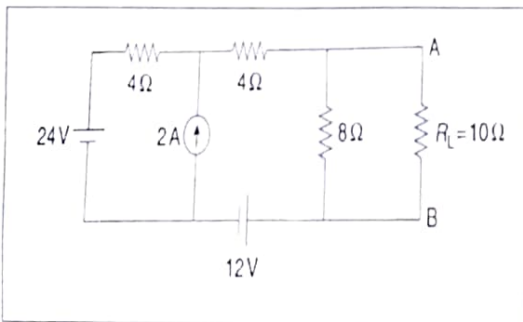
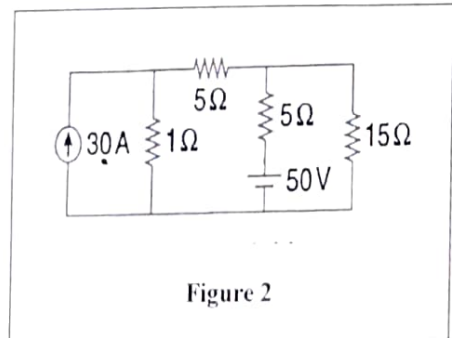
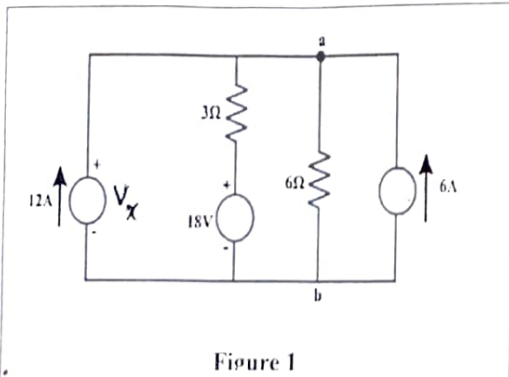
1. Differentiate between active and passive circuit element.
2. How much power is represented by a circuit in which the equations of voltage across and current through the circuit are given by  $e(t) = 160 \sin 314t$  and  $i(t) = 42.5 \sin 314t$ ? Find both the instantaneous power and average power.
3. What is 'exciting current' of a transformer and what is the function of it?
4. What for brushes are employed in dc machines? Why the armature core of a dc machine is laminated?
5. How is the capacity of a storage battery determined- explain.

**GROUP-B**  
**[LONG ANSWER TYPE QUESTIONS]**

4x15 = 60

Answer any **four** questions

- i) For the circuit shown in Figure-1, find  $V_X$ .
- ii) For the circuit of figure-2 calculate the value of current through  $15 \Omega$  resistor.



- iii) Apply Thevenin's theorem to the circuit of figure-3, to obtain current through the load resistance  $R_L = 10\Omega$

7. i) What is the relationship between apparent power, true power, and reactive power of an ac circuit? Draw the power triangle. 2
- ii) A 50 Hz voltage of 230 volts (rms) is impressed on an inductance of 0.2 H. Write down the time domain (instantaneous) equations for the voltage across and current through the inductance at steady state. Let the zero point of the voltage wave be at  $t=0$ . 2
- iii) A voltage  $v(t) = 100 \sin 314t$  is applied to a circuit consisting of  $25 \Omega$  resistance and an  $80 \mu\text{F}$  capacitance in series. Determine a) instantaneous current b) power factor c) Draw the phasor diagram. 6
- iv) Prove that for star connected three phase circuit, the line voltage is equal to  $1.732$  times the phase voltage, whereas line current is equal to phase current. Also draw phasor diagram in support of your answer. 5
8. i) What is Maximum power transfer theorem? Prove the theorem. 1+4
- ii) Calculate the value of  $R_L$  for which maximum power will be transferred from the source to the load in the network shown in the Figure-4. Hence calculate the value of maximum power transferred also. 3+1
- iii) A circuit consists of the following in parallel:  
a) A resistance of  $500 \Omega$   
b) An inductance of  $2 \text{ H}$   
c) A capacitance of  $10 \mu\text{F}$ .  
A source voltage of 200 volts 50 Hz is applied. Determine the total current drawn from the supply and active power. Draw the phasor diagram. 6
9. i) In what way a practical transformer differs from an ideal transformer? Develop an equivalent circuit for the practical transformer in support of your answer and explain the working of it on load. 5+3
- ii) Draw the phasor diagram of it. 2
- iii) A 200 kVA, 6600/400 V, 50 Hz single phase transformer has 80 turns on the secondary. Calculate 3
- a) the approximate values of the primary and secondary currents.  
b) the approximate number of primary turns and  
c) the maximum value of core flux. 2
- iv) Define voltage regulation of a transformer. 6
10. i) Derive the torque equation of dc motor. 4
- ii) A 4-pole, 220 V dc shunt motor has armature and shunt field resistances of  $0.2 \Omega$  and  $220 \Omega$  respectively. It takes 20 A at 220 V from the source while running at a speed of 1000 rpm. Find  
a. field current  
b. armature current  
c. back emf  
d. torque developed. 5
- iii) Explain why 3- $\Phi$  induction motor cannot run at synchronous speed
11. Write short notes on any three: 3x5
- i) Superposition theorem  
ii) Transformer losses and efficiency.  
iii) Speed control of DC motors  
iv) UPS (Battery backup device)  
v) Single phase auto transformer

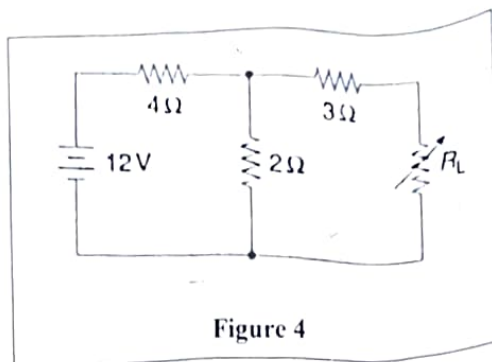


Figure 4



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**JGEC/B.TECH/CE/EE/ME/BS-CH201/2022-23**  
**2023**  
**CHEMISTRY**

Full Marks: 70

Times: 3 Hours

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**GROUP-A**  
**[OBJECTIVE TYPE QUESTIONS]**

Answer **all** questions

5x2=10

1. Define the term electron affinity.
2. Comment on the behavior of urea in liquid ammonia.
3. State the second law of thermodynamics.
4. How many stereoisomers are possible for the compound  $\text{CH}_3\text{CH}(\text{Br})\text{CH}=\text{CHBr}$ ?
5. Explain the term meso form with a suitable example.

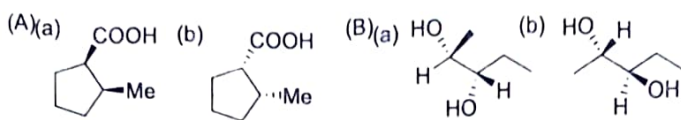
**GROUP-B**  
**[LONG ANSWER TYPE QUESTIONS]**

Answer any **four** questions

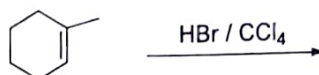
4x15=60

6. i) What is the physical significance of  $\Psi$ . Derive the energy expression for a particle in one dimensional box. 2+3  
 ii) Evaluate the value of normalization constant for a general wave function describing a particle confined in 1- dimensional box. Explain Heisenberg uncertainty principle considering a particle in 1-dimensional box. 3+2  
 iii) For the free particle, the energies vary almost continuously – justify the statement. 2  
 iv) Calculate the wave number associated with the first transition of butadiene molecule. Given that the length of the molecule is  $5.78 \times 10^{-8}$  cm. 3
7. i) What is electronegativity? Electron affinity of chlorine is greater than fluorine atom. Explain with proper reasons. Calculate the electronegativity of Pb (82) in Allred-Rochow's scale of electronegativity. Given  $r_{\text{cov}} = 120$  pm. 1+2+3  
 ii) Determine the first ionization energy for Lithium using the Slater's rule. 3  
 iii) Write down the basic postulates of crystal field theory. What are the coordination number and spin-only ( $\mu_{\text{spin-only}}$ ) magnetic moment value of the central metal ion of complex  $[\text{Mn}(\text{H}_2\text{O})_6]^{2+}$ . 2+2  
 iv) LiCl is soluble in pyridine but not in water -why? 2
8. i) 'AgCl' is more covalent than NaCl'-explain with proper reasons. 3  
 ii) First electron gain enthalpy of oxygen is an exothermic process where as second electron gain enthalpy is an endothermic- explain. 2  
 iii) Calculate the effective nuclear charge ( $Z_{\text{eff}}$ ) for 4s and 3d electron in Cu ( $Z=29$ ). 3  
 iv) Draw the molecular orbital diagram for  $\text{N}_2$  and  $\text{O}_2$  molecules. From this diagram state the magnetic character of  $\text{N}_2$  and  $\text{O}_2$  molecules. Calculate the bond order of each molecule. 3+2+2
9. i) If  $TdS = dE + P dV$ , prove that  $(dS/dV)_T = (dP/dT)_V$ . Symbols have usual significances. 3  
 ii) Using Carnot cycle prove that the efficiency of a cyclic heat engine is always less than one. 4  
 iii) Discuss the term Gibb's free energy. What is its physical significance? 2+2  
 iv) Explain the physical significance of entropy. Calculate the entropy change involved in the isothermal reversible expansion of 5 moles of an ideal gas from a volume 10 litres to a volume of 100 litres at 300 K. 2+2
10. i) A sample of pure 2-butanol has specific rotation of  $+129^\circ$ . A solution of 2-butanol placed in 5cm polarimeter tube shows a rotation of  $+85^\circ$ . Calculate the concentration of 2-butanol in the solution. 3  
 ii) Define the term enantiomer. An enantiomeric mixture shows an optical purity 50% with respect to (+)-enantiomer. What is the composition of enantiomers in mixture? 1-3

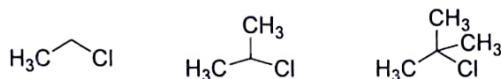
iii) What are the stereochemical relations (identical, enantiomer, diastereomer) of the following pairs? 2+6  
Assign absolute configuration at each stereogenic center.



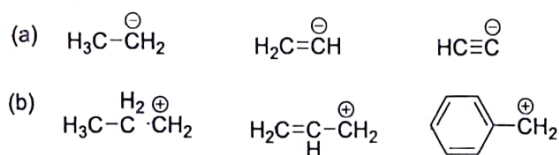
11. i)  $S_N1$  reaction give rise to racemate product but  $S_N2$  reaction result inverted product. explain 3  
ii) Write stereochemical formula for all the products that you would expect from each of the following 4  
reactions.



iii) Compare the rate of nucleophilic substitution reaction of the following compounds through  $S_N1$  and  $S_N2$  4  
path and explain.



iv) Compare the stability



12. Write short notes on **any three** of the following: 3x5  
(i) London dispersion forces, (ii) Nernst equation, (iii) Fajan's rule, (iv) resonance and hyperconjugation, (v) Carnot cycle (vi) carbocation and carbanion

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**JGEC/B.TECH/CE/EE/ME/CSE/ECE/IT/HM-HU201/2022-23**  
**2023**  
**ENGLISH**

Times: 3 Hours

Full Marks: 70

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**GROUP-A**  
**[OBJECTIVE TYPE QUESTIONS]**

5x2=10

Answer **all** questions

Point out and correct the errors in the following sentences.

1. One of the most widely spread bad habit is the use of tobacco. 2
2. He was not blind from birth. 2
3. Krishna is the taller boy in the class. 2
4. The man is a social animal           . 2
5. The principal threatened to inform to his father about his misdeeds. 2

**GROUP-B**  
**[LONG ANSWER TYPE QUESTIONS]**

4x15=60

Answer any **four** questions

6. a) Write an essay in 250 words arguing 'Is Engineering hard?' 10  
 b) Fill in the blanks with appropriate prepositions: 5
  - i) The truth of the matter finally dawned            Tina.
  - ii) The employees called            the strike.
  - iii) The flight will take            any minute now.
  - iv) The neighbour asked us to turn            the music.
  - v) Call            the surgeon immediately; the patient needs her.
7. a) You are the Sales representative of your company. Write a letter to the business manager of ABC ENTERPRISES introducing one of your new products/services. Be sure to give the important details about the product. 10  
 b) Form meaningful sentences with each word in the pair of homophones given below: 5
  - i) coral/choral ii) brake/break iii) bury/berry iv) cache/cash v) coughers/coffers
8. a) You have completed your post-graduation recently and wish to start applying for various Ph.D. programmes. In about 250 words, draft your statement of purpose. 10  
 b) Put the right alternative in the right place: 5
  - i) He has the            of keeping regular hour. (custom, habit)
  - ii) The building was            to the ground. (raised, razed)
  - iii) The Irish            settled in Canada. (immigrants, emigrants)
  - iv) The Third World War is           . (eminent, imminent)
  - v) Guru Nanak Dev led a            life. (godly, godlike)
9. a) You have completed your graduation recently. Apply for the post of Junior Engineer in an institution of your choice. Invent necessary details. 10  
 b) Rewrite the following sentences according to the instructions given: 5
  - i) They haven't stamped the letter. (End:.... Stamped)
  - ii) Don't walk on the grass. (use: keep off)
  - iii) You have nothing to complain of. (End with: ... complain)
  - iv) He has refused to help me. (Rewrite using said)
  - v) This apple is bigger than any other that I have ever seen. (Begin: I have never...)
10. a) You have been given the responsibility of writing a product launch email on behalf of your institution to promote a new product for a targeted set of customers. Mention the details about the new product. Invent necessary details. 10  
 b) Fill in the blanks with the appropriate form of the verb: 5

My guide told me if I wanted to meet these people I would have to walk two miles. We finally \_\_\_\_\_ (reach) a village where I \_\_\_\_\_ (meet) a lady whose age I \_\_\_\_\_ (can) not immediately ~~make out~~ make out. My translator \_\_\_\_\_ (find) it difficult to interpret the lady's words because her dialect \_\_\_\_\_ (be) quite different.

11 a) Write an essay in 250 words on the Importance of perfecting Communication Skills.

10

b) Insert articles where necessary:

5

i) Tiger is native of Asia.

ii) Moon shone through night.

iii) Priest was old Brahmin.

iv) Man cannot survive without water.

v) Sun rises in east.

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