

Digital Signal Processing Lab

Name: Deep C. Patel

Roll No: 1401010

Lab Report

Lab Work:-

Lab – 6

1).

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% Use MATLAB to obtain Symbolic Z-Transform of some basic signals.
% a.  $X(n) = u(n)$ 
% b.  $X(n) = nu(n)$ 
% c.  $X(n) = (1+n) u(n)$ 
% d.  $X(n) = \cos(w_0n)u(n)$ 
% e.  $X(n) = \sin(w_0n)u(n)$ 
% f.  $X(n) = (a^n)\cos(w_0n)u(n)$ 
% g.  $X(n) = (a^n)\sin(w_0n)u(n)$ 
% h.  $X(n) = n(a^n)u(n)$ 
% i.  $X(n) = -n(a^n)u(-n-1)$ 
% j.  $X(n) = n((-1)^n)u(n)$ 
% k.  $X(n) = (n^2)u(n)$ 

clc;
clear;

syms z n a w;
sympref('HeavisideAtOrigin','default');

% (a)
disp('A:');
out = ztrans(1,n,z);
disp(out);

% (b)
disp('B:');
f(n) = n;
out = ztrans(f(n),n,z);
disp(out);
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% (c)
disp('C:');
f(n) = (1+n);
out = ztrans(f(n),n,z);
disp(out);

% (d)
disp('D:');
f(n) = cos(w*n);
out = ztrans(f(n),n,z);
disp(out);

% (e)
disp('E:');
f(n) = sin(w*n);
out = ztrans(f(n),n,z);
disp(out);

% (f)
disp('F:');
f(n) = (a^n)*cos(w*n);
out = ztrans(f(n),n,z);
disp(out);

% (g)
disp('G:');
f(n) = (a^n)*sin(w*n);
out = ztrans(f(n),n,z);
disp(out);

% (h)
disp('H:');
f(n) = n*(a^n);
out = ztrans(f(n),n,z);
disp(out);

% (i)
disp('I:');
f(n) = n*(a^-n);
out = ztrans(f(n),n,1/z);
disp(out);

% (j)
disp('J:');
f(n) = n*(-1^n);
out = ztrans(f(n),n,z);
disp(out);

% (k)

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disp('K:');
f(n) = n^2;
out = ztrans(f(n),n,z);
disp(out);

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A:

$$z/(z - 1)$$

B:

$$z/(z - 1)^2$$

C:

$$z/(z - 1) + z/(z - 1)^2$$

D:

$$(z*(z - \cos(w)))/(z^2 - 2*\cos(w)*z + 1)$$

E:

$$(z*\sin(w))/(z^2 - 2*\cos(w)*z + 1)$$

F:

$$-(z*(\cos(w) - z/a))/(a*(z^2/a^2 - (2*z*\cos(w))/a + 1))$$

G:

$$(z*\sin(w))/(a*(z^2/a^2 - (2*z*\cos(w))/a + 1))$$

H:

$$(a*z)/(a - z)^2$$

I:

$$a/(z*(a/z - 1)^2)$$

J:

$$-z/(z - 1)^2$$

$$K: (z*(z + 1))/(z - 1)^3$$

2).

```
% Use MATLAB to Plot pole and zeros of the Z-transform obtained for following signals.
% a.  $X(n) = ((1/2)^n) u(n) + ((-1/3)^n) u(n)$ 
% b.  $X(n) = ((-1/3)^n) u(n) - ((1/2)^n) u(-n-1)$ 
% c.  $X(n) = ((1/2)^n) u(-n)$ 
% d.  $X(n) = \{-1, 0, -1, 0, -1, 0, -1, 0, -1, \dots\}$ 

clc;
clear;

% (a)
syms z n a;

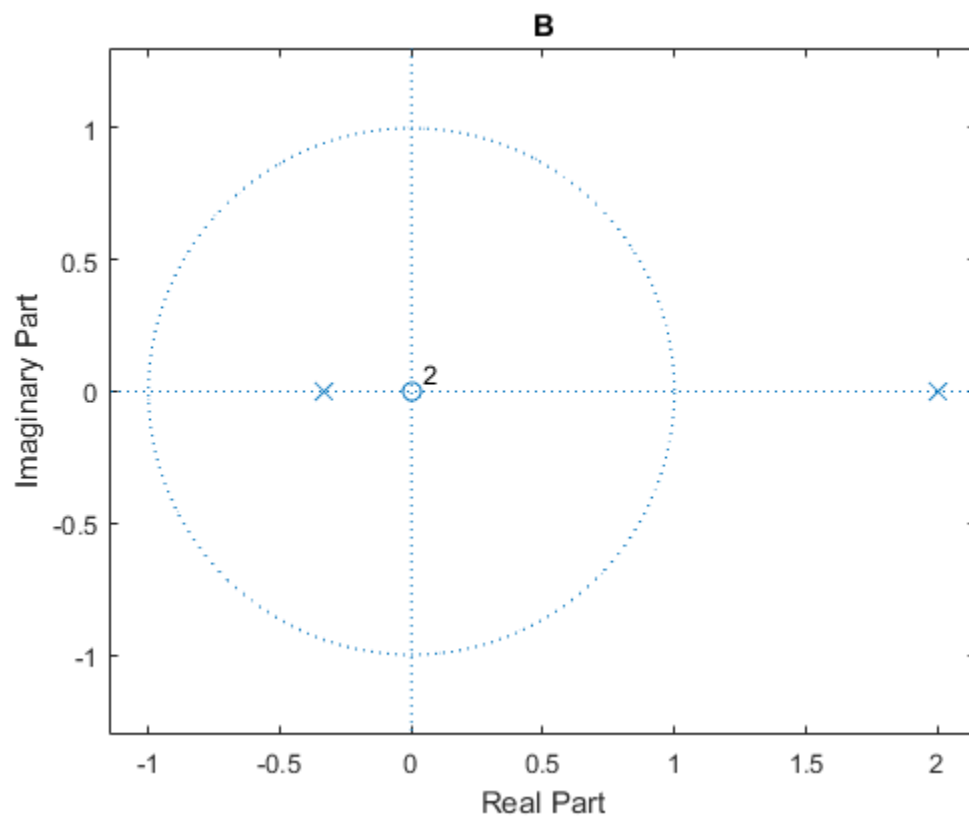
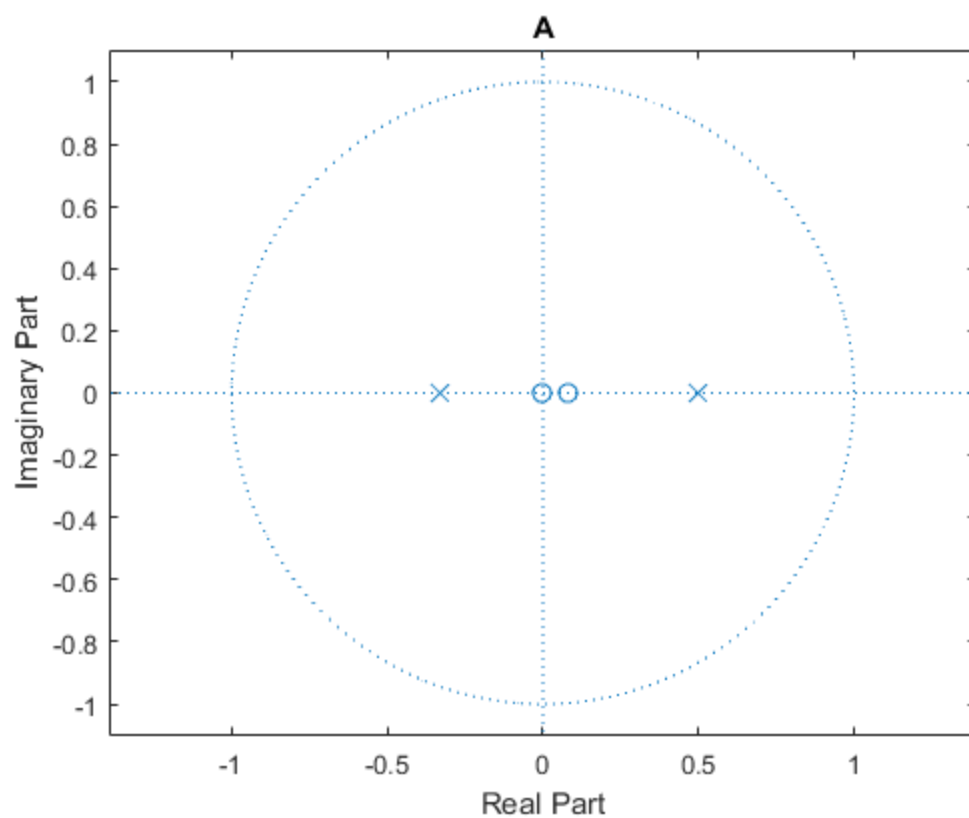
f(n) = ((1/2)^n) + ((-1/3)^n);
X = collect(ztrans(f(n),n,z));
[n, d] = numden(X);
figure;
zplane(sym2poly(n),sym2poly(d));
title('A');

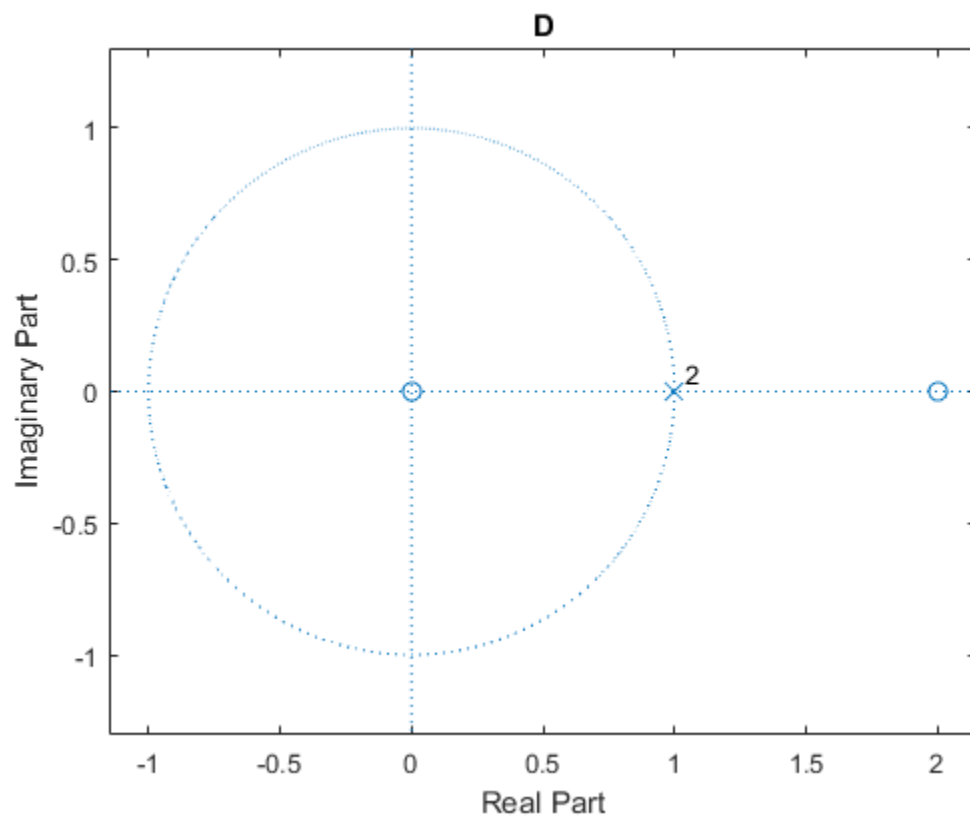
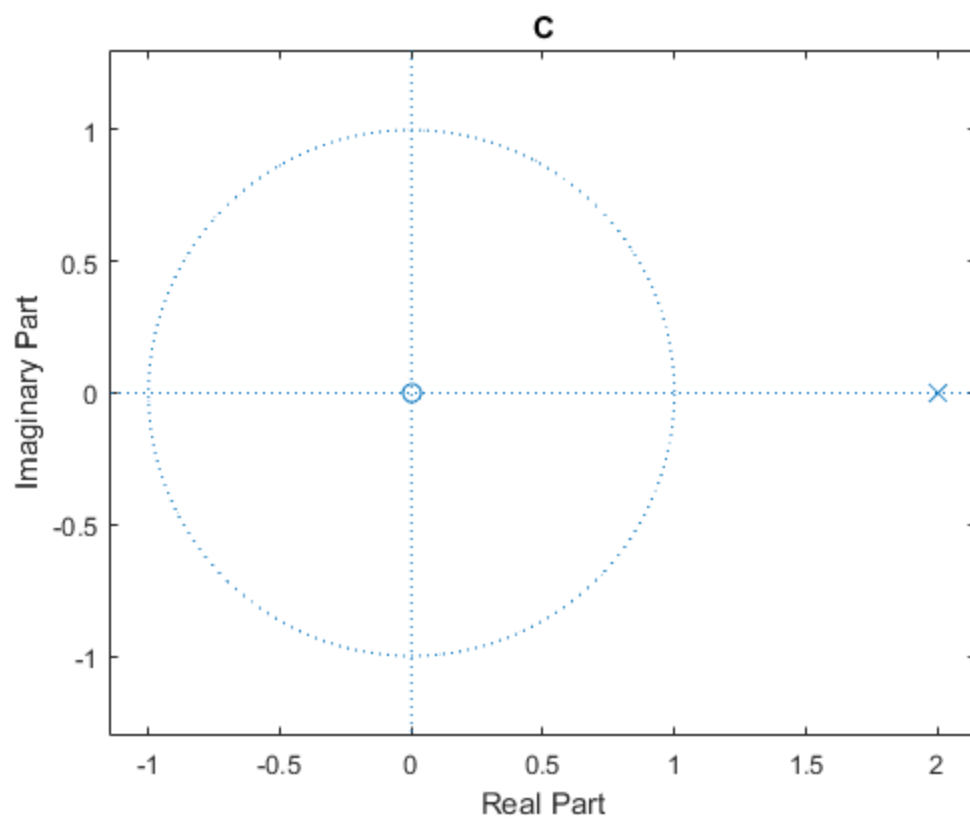
% (b)
syms z n a;

f(n) = ((-1/3)^n) - (2^n);
X = collect(ztrans(f(n),n,z));
[n, d] = numden(X);
figure;
zplane(sym2poly(n),sym2poly(d));
title('B');

% (c)
syms z n a;
f(n) = (2^(n+1));
X = collect(ztrans(f(n),n,z));
[n, d] = numden(X);
figure;
zplane(sym2poly(n),sym2poly(d));
title('C');

% (d)
syms z n a;
f(n) = mod(n,2) - 1;
X = collect(ztrans(f(n),n,z));
[n, d] = numden(X);
figure;
zplane(sym2poly(n),sym2poly(d));
title('D');
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3).

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% Use MATLAB to obtain Symbolic Inverse Z-Transform of some basic signals.
% a.  $X(z) = ((1+3*(z^{-1}))/ (1-3*(z^{-1})+2*(z^{-2})))$ 
% b.  $X(z) = ((1+2*(z^{-1}))/ (1+(z^{-2})))$ 
% c.  $X(z) = ((1+2*(z^{-1})+(z^{-2}))/ (1+4*(z^{-1})+4*(z^{-2})))$ 

% clc;
clear;

syms z n;

% (a)
X(z) = (1+3*z^(-1))/(1-3*z^(-1)+2*z^(-2));
out=iztrans(X, z, n);
disp('A:');
disp(out);

% (b)
X(z) = (1+2*z^(-1))/(1 + z^(-2));
out=iztrans(X, z, n);
disp('B:');
disp(out);

% (c)
X(z) = (1+2*z^(-1)+z^(-2))/(1+4*z^(-1)+4*z^(-2));
out=iztrans(X, z, n);
disp('C:');
disp(out);
```

A:

$$5 \cdot 2^n - 4$$

B:

$$(-1i)^{(n-1)} \cdot (1 - 1i/2) + 1i^{(n-1)} \cdot (1 + 1i/2)$$

C:

$$(-2)^n + ((-2)^n \cdot (n-1))/4$$

4).

```
% 1). Use MATLAB to obtain impulse response & step response of the systems specified below
% 2). Use MATLAB to obtain pole-zero plot of the systems specified in (a), (b), (c)
%      a.  $Y(n) = 0.75 y(n-1) - 0.125 y(n-2) + x(n)$ 
%      b.  $Y(n) = y(n-1) + x(n)$ 
%      c.  $Y(n) = 0.7 y(n-1) - 0.1 y(n-2) + 2 x(n) - x(n-2)$ 

clc;
clear;

syms n z;

% (a)

z_1 = 1/(1 - 0.75*z^(-1) + 0.125*z^(-2)); % Z-Transform (a)
disp('Impulse Response of (a): ')
ir_1 = iztrans(z_1,z,n); % Impulse Response
disp(ir_1);

sz1 = z_1*(z/(z - 1)); % For Step Response, Multiplying in Z
domain
disp('Step Response of (a): ')
sr_1 = iztrans(sz1,z,n); % Step Response
disp(sr_1);

x = 1; % Numerator Coefficients (Zeros)
y = [1,-0.75,0.125]; % Denominator Coefficients (Poles)

figure;
zplane(x,y);
title('(A)');

% (b)

z_1 = 1/(1 - (z^(-1))); % Z-Transform of (b)
disp('Impulse Response of (b): ')
ir_1 = iztrans(z_1,z,n); % Impulse Response
disp(ir_1);

sz1 = z_1*(z/(z - 1)); % For Step Response, Multiplying
in Z domain
disp('Step Response of (b): ')
sr_1 = iztrans(sz1,z,n); % Step Response
disp(sr_1);

x = 1; % Numerator Coefficients (Zeros)
y = [1,-1]; % Denominator Coefficients (Poles)
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figure;
zplane(x,y);
title(' (B) ');

% (c)

z_1 = (2 - (z^(-2)))/(1 - 0.7*(z^(-1)) + 0.1*z^(-2)); % Z-Transform of (c)
disp('Impulse Response of (c): ')
ir_1 = iztrans(z_1,z,n); % Impulse Response
disp(ir_1);

sz1 = z_1*(z/(z - 1)); % For Step Response,
Multiplying in Z domain
disp('Step Response of (c): ')
sr_1 = iztrans(sz1,z,n); % Step Response
disp(sr_1);

x = [2,0,-1]; % Numerator Coefficients
(Zeros)
y = [1,-0.75,0.125]; % Denominator Coefficients
(Poles)

figure;
zplane(x,y);
title(' (C) ');

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Impulse Response of (a):

$$2*(1/2)^n - (1/4)^n$$

Step Response of (a):

$$(1/4)^n/3 - 2*(1/2)^n + 8/3$$

Impulse Response of (b):

$$1$$

Step Response of (b):

$$n + 1$$

Impulse Response of (c):

$$(46*(1/5)^n)/3 - (10*(1/2)^n)/3$$

Step Response of (c):

$$(10*(1/2)^n)/3 - (23*(1/5)^n)/6 + 5/2$$

