

$$1. \Pi_{PNAME} (PARTS \bowtie CATALOG)$$

$$2. T_1 \leftarrow PARTS \bowtie CATALOG$$

$$T_2 \leftarrow \sigma_{STREET = '1 Central Ave.'} (SUPPLIERS)$$

$$T_3 \leftarrow \Pi_{PNAME} (T_1 \bowtie T_2)$$

$$3. T_1 \leftarrow PARTS \bowtie CATALOG \bowtie SUPPLIERS$$

$$T_2 \leftarrow \Pi_{SNAME} (\sigma_{COLOR = 'red'} (T_1))$$

$$4. T_1 \leftarrow \sigma_{COLOR = 'red' \text{ OR } COLOR = 'GREEN'} (PARTS)$$

$$T_2 \leftarrow \Pi_{SID} (CATALOG \bowtie T_1)$$

$$5. T_1 \leftarrow \sigma_{COLOR = 'red'} (PARTS)$$

$$T_2 \leftarrow \sigma_{STREET = '221 Packer Street'} (SUPPLIERS)$$

$$T_3 \leftarrow T_1 \bowtie CATALOG$$

$$T_4 \leftarrow (\Pi_{SID}(T_2)) \cup (\Pi_{SID}(T_3))$$

$$6. T_1 \leftarrow CATALOG \bowtie (\sigma_{COLOR = 'red'} (PARTS))$$

$$T_2 \leftarrow CATALOG \bowtie (\sigma_{COLOR = 'green'} (PARTS))$$

$$T_3 \leftarrow (\Pi_{SID}(T_1)) \cap (\Pi_{SID}(T_2))$$

$$7. T_1 \leftarrow \sigma_{COLOR = 'red'} (PARTS)$$

$$T_2 \leftarrow \sigma_{CITY = 'Newark'} (SUPPLIERS) \bowtie \cancel{PARTS} \bowtie CATALOG$$

$$T_3 \leftarrow (\Pi_{PID}(T_1)) \cup (\Pi_{PID}(T_2))$$

$$\begin{aligned}
 8. \quad T_1 &\leftarrow (\sigma_{CITY='Newark'}(SUPPLIERS)) \times CATALOG \\
 T_2 &\leftarrow (\sigma_{CITY='Trenton'}(SUPPLIERS)) \times CATALOG \\
 T_3 &\leftarrow (\Pi_{PID}(T_1)) \cap (\Pi_{PID}(T_2))
 \end{aligned}$$

$$\begin{aligned}
 9. \quad T_1 &\leftarrow \Pi_{SID}(SUPPLIERS) \\
 T_2 &\leftarrow \Pi_{SID, PID}(CATALOG) \\
 T_3 &\leftarrow T_2 \div T_1
 \end{aligned}$$

$$\begin{aligned}
 10. \quad T_1 &\leftarrow \Pi_{SID}(CATALOG) \\
 T_2 &\leftarrow \Pi_{SID, PID}(CATALOG) \\
 T_3 &\leftarrow T_2 \div T_1
 \end{aligned}$$

$$\begin{aligned}
 11. \quad T_1 &\leftarrow \Pi_{SID}(\sigma_{CITY='Newark' \text{ OR } CITY='Trenton'}(SUPPLIERS)) \\
 T_2 &\leftarrow \Pi_{SID, PID}(CATALOG) \\
 T_3 &\leftarrow T_2 \div T_1
 \end{aligned}$$

$$\begin{aligned}
 12. \quad T_1 &\leftarrow \Pi_{SID, PID}(CATALOG) \div \Pi_{SID}(\sigma_{CITY='Newark'}(SUPPLIERS)) \\
 T_2 &\leftarrow \Pi_{SID, PID}(CATALOG) \div \Pi_{SID}(\sigma_{CITY='Trenton'}(SUPPLIERS)) \\
 T_3 &\leftarrow T_1 \cup T_2
 \end{aligned}$$

13. 11 is more restrictive. Because in 11, the parts are ~~both~~ supplied by the suppliers from newark and
 both

by the supplier from Trenton. In the 12, the parts only need to be supplied by one of these two cities.

14. $T_1 \leftarrow (\rho_{PID \rightarrow PIDS, COST \rightarrow COSTS}(CATALOG)) * CATALOG$
 $T_2 \leftarrow \Pi_{PID, PIDS} (\sigma_{COST > COSTS}(T_1))$

15. $T_1 \leftarrow \Pi_{SID, PID}(CATALOG)$
 $T_2 \leftarrow \Pi_{PID} \{PID \rightarrow PIDS(T_1)\}$
 $T_3 \leftarrow \sigma_{PID \neq PIDS}(T_1 * T_2)$
 $T_4 \leftarrow \Pi_{SID}(T_3)$

16. $T_1 \leftarrow \sigma_{SID} \tilde{f}_{COUNT(PID)}(CATALOG)$
 $T_2 \leftarrow \Pi_{SID} (\sigma_{COUNT(PID) \geq 2}(T_1))$

17. $T_1 \leftarrow \rho_{PID} \tilde{f}_{MAX(COST)}(CATALOG)$
 $T_2 \leftarrow \rho_{MAX(COST) \rightarrow COST}(T_1)$
 $T_3 \leftarrow \Pi_{SID, PID}(CATALOG * T_2)$
 $T_4 \leftarrow SUPPLIERS * T_3$
 $T_5 \leftarrow \sigma_{CITY = 'Newark'}(T_4)$
 $T_6 \leftarrow \Pi_{PID, SID, SNAME}(T_5)$

18. $T_1 \leftarrow \rho_{PID} \tilde{f}_{COUNT(SID)}(CATALOG)$
 $T_2 \leftarrow \Pi_{PID, PNAME}(PARTS)$
 $T_3 \leftarrow T_2 * T_1$

19. $T_1 \leftarrow \rho_{PID} \tilde{f}_{AVERAGE(COST)}(CATALOG)$
 $T_2 \leftarrow \Pi_{PID, PNAME}(PARTS)$
 $T_3 \leftarrow T_2 * T_1$

20. $T_1 \leftarrow \sigma_{\text{color} = 'red'}(\text{PARTS})$

$T_2 \leftarrow T_1 * \text{CATALOG}$

$T_3 \leftarrow \pi_{\text{average}(\text{cost})}(T_2)$

21. $T_1 \leftarrow \sigma_{\text{name} = 'Yosemite Sham'}(\text{SUPPLIERS})$

$T_2 \leftarrow T_1 * \text{CATALOG}$

$T_3 \leftarrow \pi_{\text{average}(\text{cost})}(T_2)$