



Assignment-I

B.Tech. / Semester: III/V  
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SET-12

Q1. The second order extension of a DMS  $X$ , denoted by  $X^2$ , is formed by taking the source symbols two at a time. The coding of this extension has been shown in Table 1. Find the efficiency  $\eta$  and the redundancy  $\gamma$  of this extension code. [CO2, BL3]

$a_i$	$P(a_i)$	Code
$a_1 = x_1 x_1$	0.81	0
$a_2 = x_1 x_2$	0.09	10
$a_3 = x_2 x_1$	0.09	110
$a_4 = x_2 x_2$	0.01	111

Q2. Prove that the upper bound on Entropy is given as  $H_{\max} \leq \log_2 m$ . Here  $m$  is the number of messages emitted by the source. [CO1, BL3]

Q3. Consider a BSC with  $P(x_1) = \alpha$ . Show that the mutual information  $I(X;Y)$  is given by:

$$I(X;Y) = H(Y) + p \log_2 p + (1-p) \log_2 (1-p).$$

Also calculate  $I(X;Y)$  for  $\alpha=0.5$  and  $p = 0.1$  [CO2, BL3]

Q4. A DMS  $X$  has five symbols  $x_1, x_2, x_3, x_4$  and  $x_5$  with  $P(x_1)=0.2$ ,  $P(x_2)=0.15$ ,  $P(x_3)=0.05$ ,  $P(x_4)=0.10$  and  $P(x_5)=0.50$

(a) Construct a Shannon Fano code for  $X$ , and calculate the efficiency of the code.

(b) Repeat for the Huffman code and compare the results. [CO2, BL3]