

deBInfer logistic ODE example

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Preliminaries

First we install the deBInfer package. For this you need to install and load the devtools package first. You can do this from CRAN.

```
install.packages("devtools")
```

```
#Load the devtools package.  
library(devtools)
```

Then you install deBInfer from github

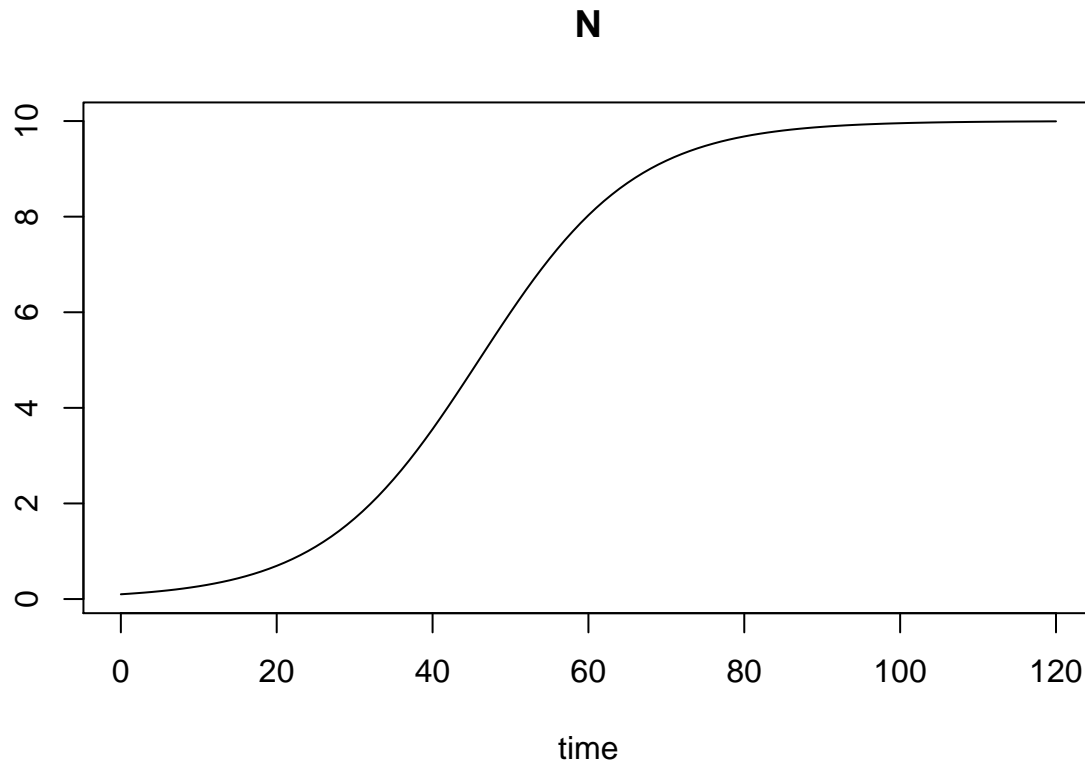
```
install_github("pboesu/debinfer")
```

Defining the DE model

We define a logistic growth ODE for deSolve.

```
library(deSolve)  
logistic_model <- function (time, y, parms) {  
  with(as.list(c(y, parms)), {  
    dN <- r * N * (1 - N / K)  
    list(dN)  
  })  
}  
y <- c(N = 0.1)  
parms <- c(r = 0.1, K = 10)  
times <- seq(0, 120, 1)  
out <- ode(y, times, logistic_model, parms, method='lsoda')
```

Which gives us the numerical solution



Simulating observations

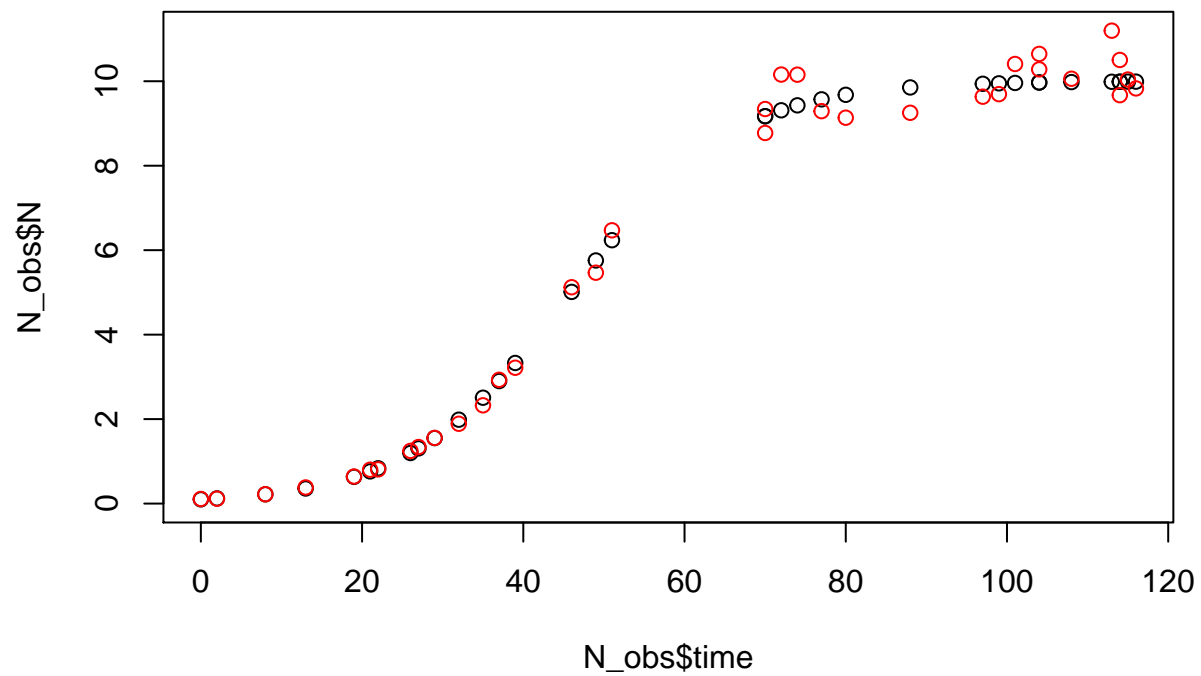
Now we simulate a noisy dataset from this equation. We sample a random subset from the integration output

```
set.seed(143)
N_obs <- as.data.frame(out[c(1,runif(35, 0, nrow(out))),]) #force include the first time-point (t=0)
```

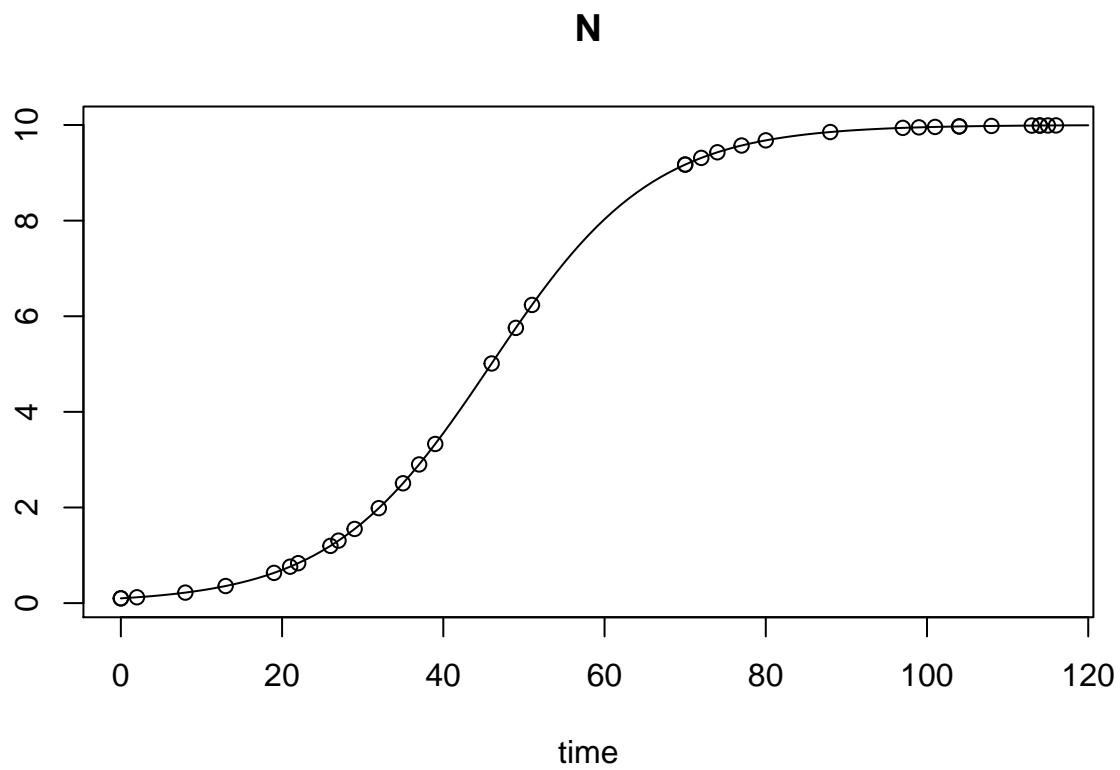
and we “add” lognormal noise

```
# add lognormal noise
parms['sdlog.N'] <- 0.05
N_obs$N_noisy <- rlnorm(nrow(N_obs), log(N_obs$N),parms['sdlog.N'])
#observations must be ordered for solver to work
N_obs <- N_obs[order(N_obs$time),]

plot(N_obs$time, N_obs$N, ylim=c(0, max(N_obs$N,N_obs$N_noisy)))
points(N_obs$time, N_obs$N_noisy, col="red")
```



```
out_obs <- ode(y, c(0,N_obs$time), logistic_model, parms, method='lsoda')
plot(out_obs, type="p")
lines(out)
```



Defining an observation model and parameters for inference

We define an observation model. Note that we are sampling the log of the observation standard deviation, to ensure sampled values are strictly positive. We also use an epsilon correction for the meanlog, as the DE model can return values of 0 (or even less due to numerical precision).

```
# the observation model
logistic_obs_model<-function(data, sim.data, samp){

  llik.N<-sum(dlnorm(data$N_noisy, meanlog=log(sim.data[, "N"] + 1e-6),
                    sdlog=samp[['sdlog.N']], log=TRUE)
            )

  llik<-llik.N

  return(llik)
}
```

We declare the parameters for inference:

```
library(deBInfer)
r <- debinfer_par(name = "r", var.type = "de", fixed = FALSE,
                  value = 0.5, prior="norm", hypers=list(mean = 0, sd = 1),
                  prop.var=0.005, samp.type="rw")

K <- debinfer_par(name = "K", var.type = "de", fixed = FALSE,
                  value = 5, prior="lnorm", hypers=list(meanlog = 1, sdlog = 1),
                  prop.var=0.1, samp.type="rw")

sdlog.N <- debinfer_par(name = "sdlog.N", var.type = "obs", fixed = FALSE,
                        value = 0.1, prior="lnorm", hypers=list(meanlog = 0, sdlog = 1),
                        prop.var=c(3,4), samp.type="rw-unif")
```

and we also need to provide an initial condition for the differential equation:

```
N <- debinfer_par(name = "N", var.type = "init", fixed = TRUE, value = 0.1)
```

All declared parameters are collated using the `setup_debinfer` function

```
mcmc.pars <- setup_debinfer(r, K, sdlog.N, N)
```

Conduct inference

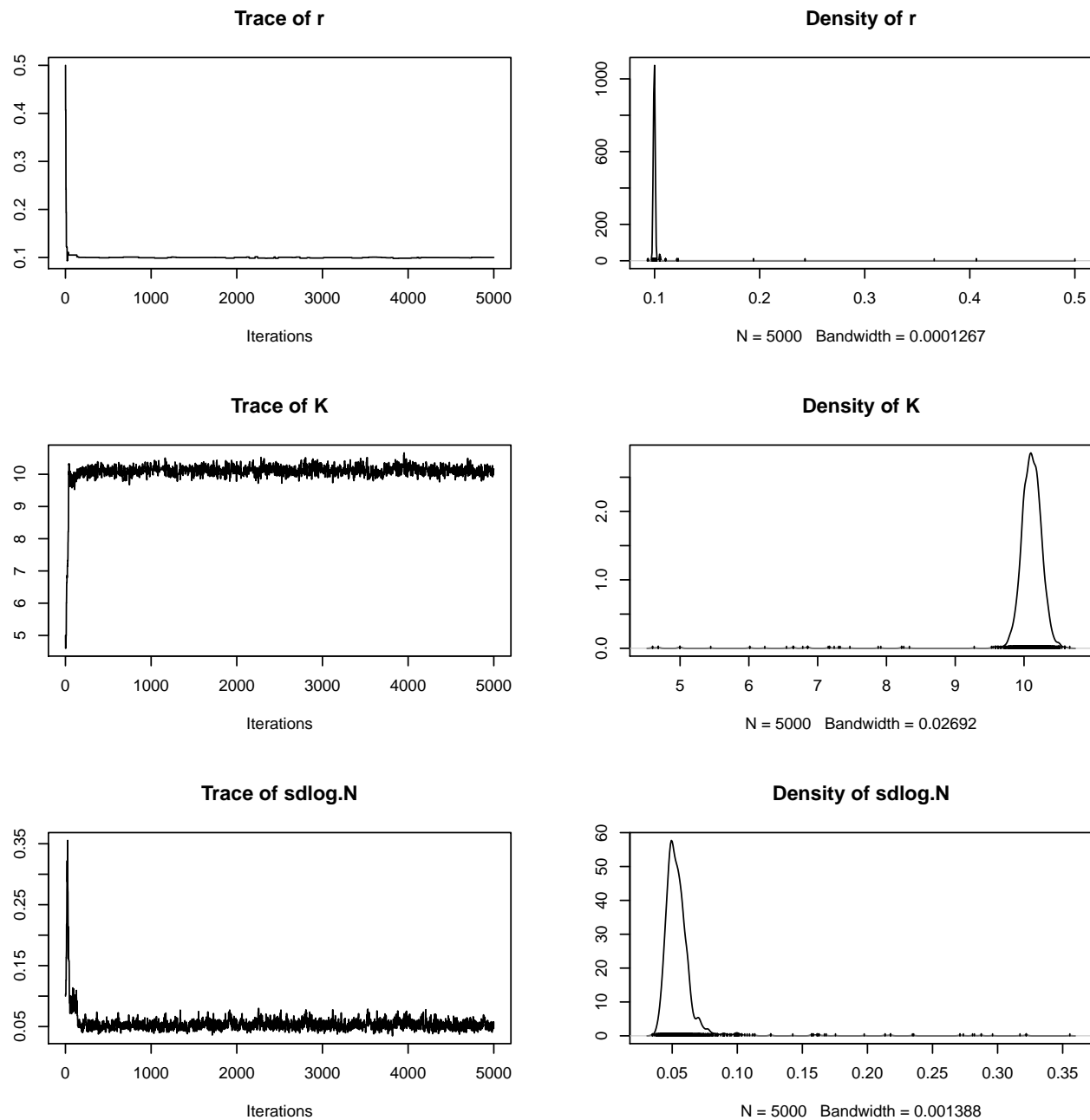
Finally we use `deBInfer` to estimate the parameters of the original model.

```
# do inference with deBInfer
# MCMC iterations
iter = 5000
# inference call
mcmc_samples <- de_mcmc(N = iter, data=N_obs, de.model=logistic_model,
```

```
obs.model=logistic_obs_model, all.params=mcmc.pars,
Tmax = max(N_obs$time), data.times=N_obs$time, cnt=iter+1,
plot=FALSE, sizestep=0.1, solver="ode")
```

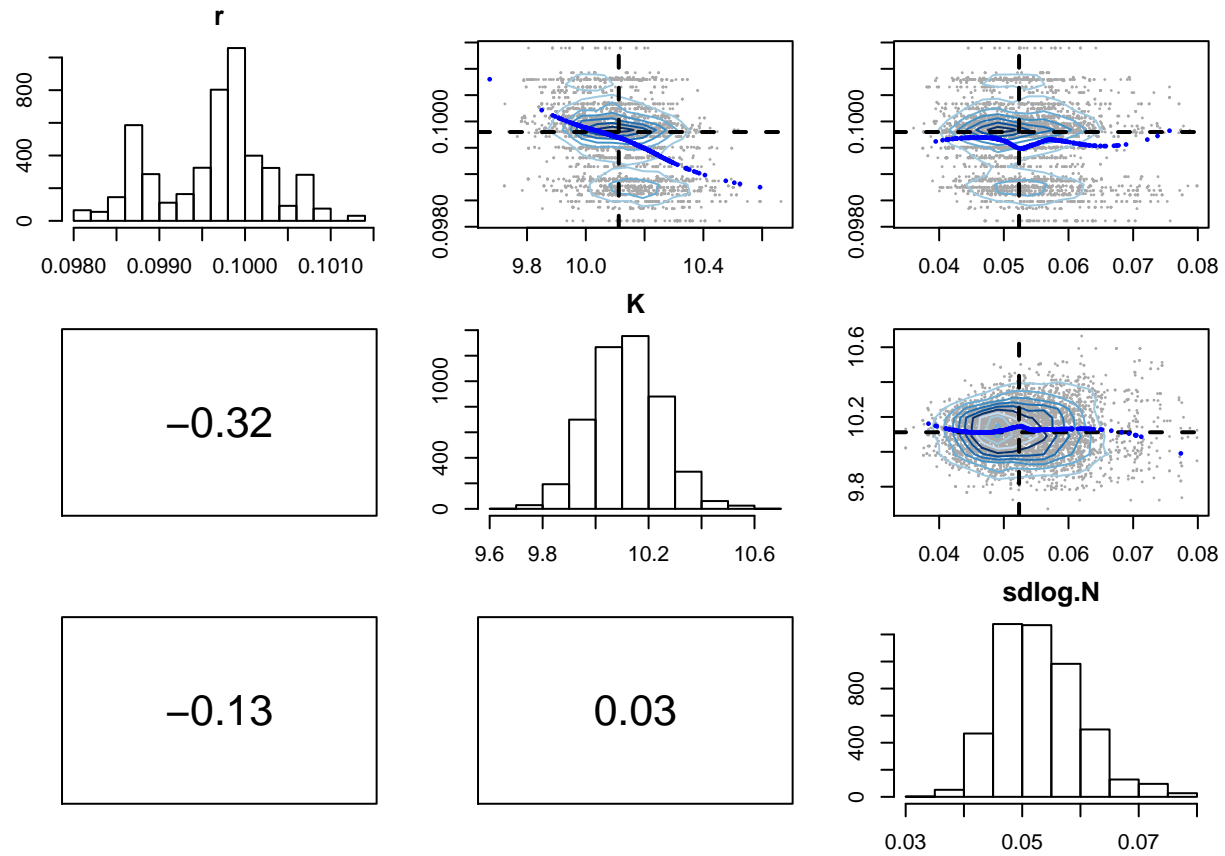
We plot and summarize the MCMC chains

```
plot(mcmc_samples)
```

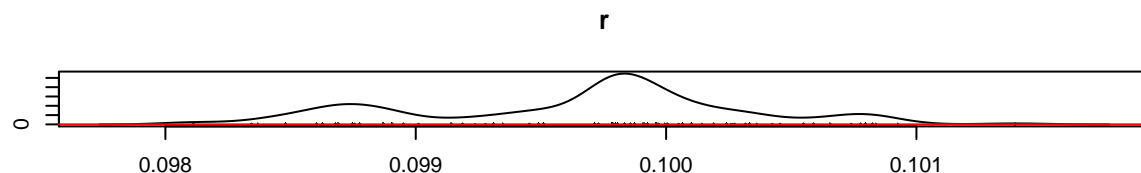


From the traceplot we can see that the burnin period is about 200 samples. We can remove the burnin and have a look at parameter correlations, and the overlap between the posterior and prior densities.

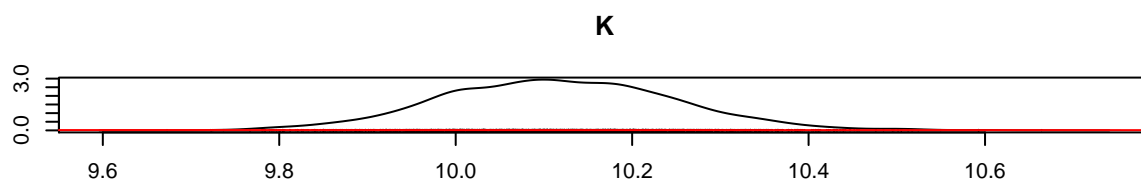
```
burnin = 200
pairs(mcmc_samples, burnin = burnin, scatter=TRUE, trend=TRUE)
```



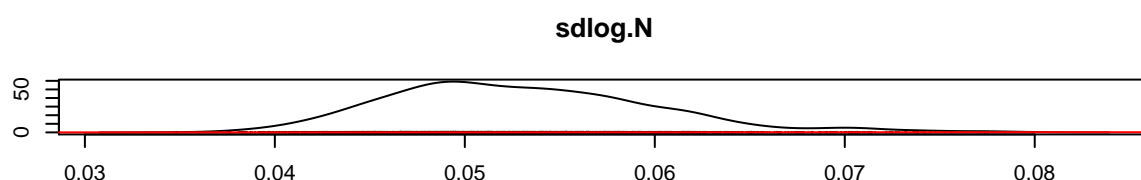
```
post_prior_densplot(mcmc_samples, burnin = burnin)
```



N = 4801 Bandwidth = 0.0001253



N = 4801 Bandwidth = 0.02562



N = 4801 Bandwidth = 0.001354

```
summary(mcmc_samples)
```

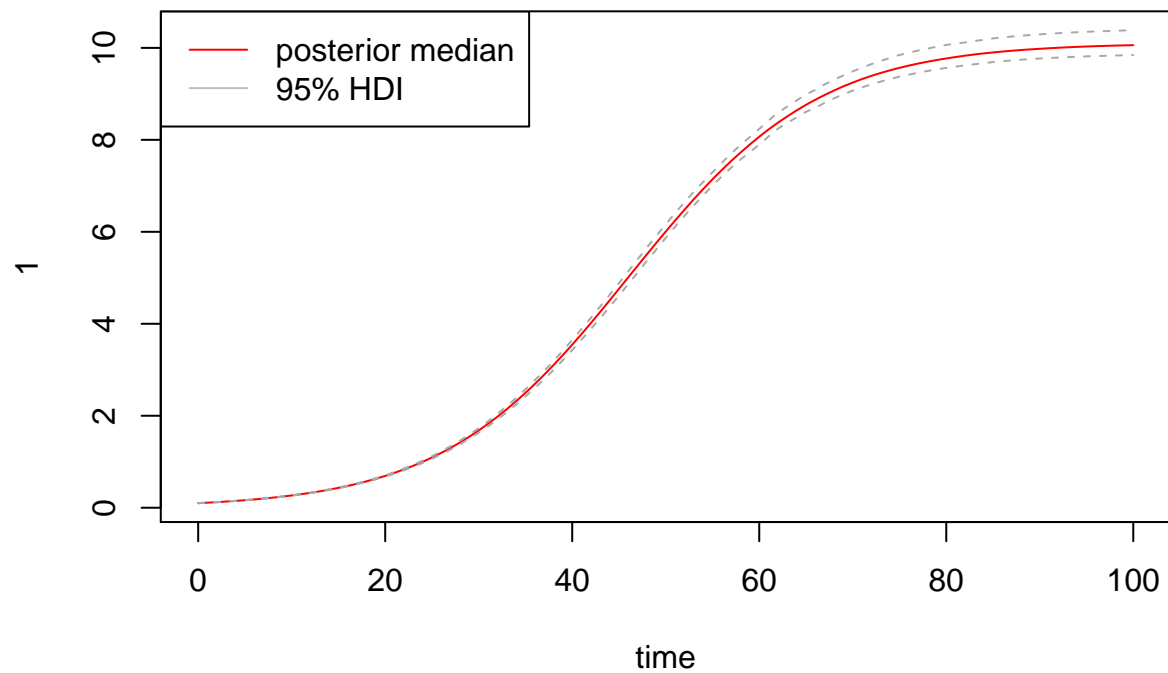
```
##
## Iterations = 1:5000
## Thinning interval = 1
## Number of chains = 1
## Sample size per chain = 5000
##
## 1. Empirical mean and standard deviation for each variable,
##    plus standard error of the mean:
##
##           Mean      SD Naive SE Time-series SE
## r          0.10025 0.01087 0.0001537      0.0004989
## K          10.08557 0.34547 0.0048857      0.0292687
## sdlog.N     0.05499 0.01767 0.0002499      0.0018154
##
## 2. Quantiles for each variable:
##
##           2.5%      25%      50%      75%      97.5%
## r          0.09837 0.09919 0.09980 0.10007 0.10504
## K          9.81885 10.01341 10.10725 10.20032 10.37755
## sdlog.N     0.04149 0.04818 0.05255 0.05782 0.07771
```

We simulate DE model trajectories from the posterior and calculate the HPD interval for the deterministic part of the model.

```
post_traj <- post_sim(mcmc_samples, n=200, times=0:100, burnin=burnin, output = 'all')
```

We can visualise the median posterior trajectory and the associated highest posterior density interval using

```
#median and HDI
plot(post_traj, plot.type = "medianHDI")
legend("topleft", legend=c("posterior median", "95% HDI"), lty=1, col=c("red","grey"))
```



Alternatively we can plot an ensemble of posterior trajectories

```
plot(post_traj, plot.type = "ensemble", col = "#FF000040")
```


N

