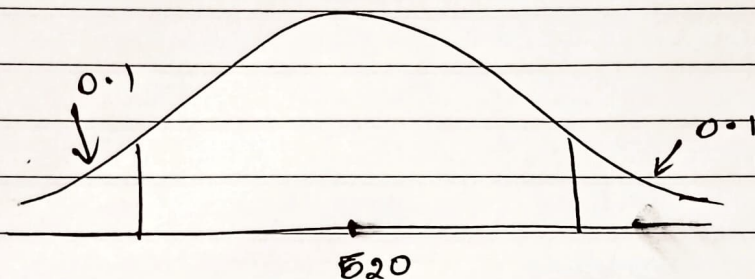


DEEPA SAHU

- 8) In the Quant test of CAT exam the population standard deviation is known to be 100. A sample of 25 test takers has a mean of 520. Construct a 80% confidence interval (CI) about mean?

Solⁿ Given, $\sigma = 100$, $n = 25$, $\bar{x} = 520$
 $\alpha = 1 - 0.8$
 $= \underline{\underline{0.2}}$



we know, $CI = \text{point estimate} \pm \text{margin of error}$
 $= \underline{\underline{\bar{x} \pm Z_{\alpha/2} \frac{\sigma}{\sqrt{n}}}}$

$$\begin{aligned} \text{Lower fence} &= \bar{x} - Z_{0.1} \frac{\sigma}{\sqrt{n}} \\ &= 520 - 1.29 \times \frac{100}{5} \\ &= 520 - 25.8 \\ &= \underline{\underline{494.2}} \end{aligned}$$

$$\left[\begin{aligned} Z_{\frac{\alpha}{2}} &= Z_{\frac{0.2}{2}} \\ &= Z_{0.1} \end{aligned} \right.$$

$$\begin{aligned} 1 - 0.1 &= 0.9 \\ \text{from Z score table} \\ &= 1.29 \end{aligned}$$

$$\begin{aligned} \text{Higher fence} &= 520 + 1.29 \times \frac{100}{5} \\ &= 520 + 25.8 \\ &= \underline{\underline{545.8}} \end{aligned}$$