

**Problem 9:** We wish to compute the laziest way to dial given n-digit number on a standard pushbutton telephone using two fingers. We assume that the two fingers start out on the star and hash keys, and that the effort required to move a finger from one button to another is proportional to the Euclidean distance between them. Design and analyze an efficient algorithm that computes in time of dialing that involves moving your fingers the smallest amount of total distance.

**PSEUDOCODE :**

Def distance(p1, p2):

    Return Euclidean distance between p1 and p2

Def dialing(input\_number):

    total\_dist, finger1\_position, finger2\_position

    For each digit i in input\_number:

        Calculate dist1, dist2

        If dist1 <= dist2:

            total\_dist += dist1  
            Update finger1\_position

        Else:

            total\_dist += dist2  
            Update finger2\_position

    Return total\_dist

Input input\_number

Print "Total distance moved:" followed by dialing(input\_number)

**CODE :**

```
import math
keypad = {
    '1': (0, 0), '2': (0, 1), '3': (0, 2),
    '4': (1, 0), '5': (1, 1), '6': (1, 2),
    '7': (2, 0), '8': (2, 1), '9': (2, 2),
    '0': (3, 1), '*' : (3, 0), '#' : (3, 2)
}

def distance(p1, p2):
    return math.sqrt((p1[0] - p2[0])**2 + (p1[1] - p2[1])**2)

def dialing(input_number):
    total_dist = 0
    finger1_position = keypad['*']
    finger2_position = keypad['#']
```

```

for i in input_number:
    i_position = keypad[i]

    dist1 = distance(finger1_position, i_position)
    dist2 = distance(finger2_position, i_position)

    if dist1 <= dist2:
        total_dist += dist1
        finger1_position = i_position
    else:
        total_dist += dist2
        finger2_position = i_position

return total_dist

input_number = input()
print("Total distance moved:", dialing(input_number))

```

#### ALGORITHM ANALYSIS :

**Time Complexity:**  $O(n)$

#### Problem 7:

##### PSEUDOCODE :

##### CODE :

#### ALGORITHM ANALYSIS :

**Time Complexity:**  $O(n^2)$

**Problem 10:** There are  $N$  floors and  $N$  persons each one is tagged with some random unique number between 1 to  $N$  (represents floor number). We have a lift which can accommodate one person at a time. Every person is in some random floor. Initially lift is at floor 1 and all floors have single person. Design an algorithm to move the persons to their corresponding floor with minimum number of lift movements. [Restriction: Lift can have at most one person at a time. While moving persons, at some point of time, we can keep more than one person at one floor. ]

##### PSEUDOCODE :

Def min\_movement( $N$ , persons):

Sort persons based on their tagged floor numbers

```

movements = 0
current_floor = 1

```

For each person in persons:

```

    movements += abs(current_floor - person[1])

```

```
movements += abs(person[0] - person[1])
```

```
current_floor = person[1]
```

Return movements

#### CODE :

```
def min_movement(N, persons):
    persons.sort(key=lambda x: x[1])
    movements = 0
    current_floor = 1

    for person in persons:
        movements += abs(current_floor - person[1])
        movements += abs(person[0] - person[1])
        current_floor = person[1]
    return movements

N = int(input('number of floor: '))
persons = []
for i in range(N):
    person_floor = int(input('person floor: '))
    persons.append((i+1, person_floor))
print(min_movement(N, persons))
```

#### ALGORITHM ANALYSIS :

**Time Complexity:**  $O(n \log n)$

## Assignment - 5 (Dynamic Programming)

**Problem 1: Given 3 strings of all having length  $\leq 100$ , write a program to find the longest common sub-sequence in all three given sequences.**

### PSEUDOCODE :

Function Lcs(s1, s2, s3, i, j, k, dict):

    If  $i = 0$  or  $j = 0$  or  $k = 0$ :

        Return // Base case: One of the strings is empty

    If (i, j, k) is already in dict:

        Return dict[(i, j, k)]

    If  $s1[i - 1] = s2[j - 1] = s3[k - 1]$ :

        lcs = Lcs(s1, s2, s3, i - 1, j - 1, k - 1, dict) +  $s1[i - 1]$

        dict[(i, j, k)] = lcs

    Return lcs

Else:

    lcs1 = Lcs(s1, s2, s3, i - 1, j, k, dict)

    lcs2 = Lcs(s1, s2, s3, i, j - 1, k, dict)

    lcs3 = Lcs(s1, s2, s3, i, j, k - 1, dict)

    lcs = Longest of lcs1, lcs2, lcs3 // Find the longest subsequence

    dict[(i, j, k)] = lcs

    Return lcs

Function lcs(s1, s2, s3):

    dict = Empty dictionary

    Return Lcs(s1, s2, s3, Length of s1, Length of s2, Length of s3, dict)

### CODE :

```
def Lcs(s1, s2, s3, i, j, k, dict):
    if i == 0 or j == 0 or k == 0:
        return ""

    if (i, j, k) in dict:
        return dict[(i, j, k)]

    if s1[i - 1] == s2[j - 1] == s3[k - 1]:
        lcs = Lcs(s1, s2, s3, i - 1, j - 1, k - 1, dict) + s1[i - 1]
```

```

        dict[(i, j, k)] = lcs
        return lcs
    else:
        lcs1 = Lcs(s1, s2, s3, i - 1, j, k, dict)
        lcs2 = Lcs(s1, s2, s3, i, j - 1, k, dict)
        lcs3 = Lcs(s1, s2, s3, i, j, k - 1, dict)
        lcs = max(lcs1, lcs2, lcs3, key=len)
        dict[(i, j, k)] = lcs
        return lcs

def lcs(s1, s2, s3):
    dict = {}
    return Lcs(s1, s2, s3, len(s1), len(s2), len(s3), dict)

s1 = input("first string: ")
s2 = input("second string: ")
s3 = input("third string: ")
print("Longest common subsequence:", lcs(s1, s2, s3))

```

#### ALGORITHM ANALYSIS :

Time Complexity:  $O(n^3)$

**Problem 3: A subsequence is palindromic if it is the same whether read left to right or right to left. For instance, the sequence A;C; G; T; G; T;C; A; A; A; A; T;C;G has many palindromic subsequences, including A;C; G;C;A and A; A; A;A (on the other hand, the subsequence A;C; T is not palindromic). Devise an algorithm that takes a sequence  $x[1 : : n]$  and returns the (length of the) longest palindromic subsequence. Its running time should be  $O(n^2)$ .**

#### PSEUDOCODE :

Function lps(S):

R = ReverseString(S)

length = Length(S)

dp = initialize 2\*2 matrix with 0

for i from 1 to length:

for j from 1 to length:

if  $S[i - 1] == R[j - 1]$ : If the characters at positions i and j are equal

$dp[i][j] = 1 + dp[i - 1][j - 1]$

else:

$dp[i][j] = \max(dp[i][j - 1], dp[i - 1][j])$

return  $dp[length][length]$

**CODE :**

```
def lps(S):
    R = S[::-1]
    length = len(S)
    dp = [[0] * (length + 1) for i in range(length + 1)]

    for i in range(1, length + 1):
        for j in range(1, length + 1):
            if S[i - 1] == R[j - 1]:
                dp[i][j] = 1 + dp[i - 1][j - 1]
            else:
                dp[i][j] = max(dp[i][j - 1], dp[i - 1][j])

    return dp[length][length]
```

```
s = input()
print(lps(s))
```

**ALGORITHM ANALYSIS :**

**Time Complexity:**  $O(n^2)$

**Problem 7:** Write a program that calculates the highest sum of numbers passed on a route that starts at the top and ends somewhere on the base.  $n = 0$  7  $n = 1$  3 , 8  $n = 2$  8 ,1, 0  $n = 3$  2, 7, 4, 4  $n = 4$  4, 5, 2, 6, 5 For the above figure shows a number triangle and its output is 30(7,3,8,7,5). Each step can go either diagonally down to the left or diagonally down to the right.

**PSEUDOCODE :**

```
high_sum(triangle):
n = length of triangle
dp = Last row of triangle
for row in range(n - 2, -1, -1):
// Iterate over elements in the current row
    for i in range(length of triangle[row]):
dp[i] = triangle[row][i] + maximum of (dp[i], dp[i + 1])
print(dp)

// Return the maximum sum from the top of the triangle
return dp[0]
```

**CODE :**

```
def high_sum(triangle):

    n = len(triangle)

    dp = triangle[-1][:]

    for row in range(n - 2, -1, -1):

        for i in range(len(triangle[row])):

            dp[i] = triangle[row][i] + max(dp[i], dp[i + 1])

    print(dp)

    return dp[0]

triangle = []
n = int(input("Enter the number of rows: "))
print("Enter the elements:")
for i in range(n):
    row = list(map(int, input().split()))
    triangle.append(row)

result = high_sum(triangle)
print(" maximum sum :", result)
```

**ALGORITHM ANALYSIS :**

**Time Complexity:**  $O(n^2)$

**Problem 10:** In the art gallery guarding problem, a line  $L$  represents a long art gallery hallway. We are given a set of location points on it  $X=x_0, x_1, \dots, x_{n-1}$  of real numbers that specify the positions of the paintings along the hallway. A single guard can guard paintings standing at most 1 meter from each painting on either side. Design an algorithm that finds the optimal number of guards to guard all the paintings along the hallway.

**PSEUDOCODE :**

min\_guards(locations):

- Sort the locations list
- Initialize a list  $dp$  with  $n$  elements, each set to positive infinity
- Set  $dp[0]$  to 1 (as the base case)
- For each location from the second one to the last:
- For each previous location:
- If the distance between the current location and the previous one is less than or equal to 1:
  - Update  $dp[i]$  to be the minimum of its current value and  $dp[j] + 1$

- Return the last element of dp, which represents the optimal number of guards needed

#### CODE :

```
def min_guards(locations):
    locations.sort()
    n = len(locations)
    dp = [float('inf')] * n
    dp[0] = 1

    for i in range(1, n):
        for j in range(i):
            if locations[i] - locations[j] <= 1:
                dp[i] = min(dp[i], dp[j] + 1)

    return dp[-1]

n = int(input("Enter the number of location points: "))
locations = []
print("Enter the location points:")
for i in range(n):
    location = float(input())
    locations.append(location)
print("Optimal number of guards:", min_guards(locations))
```

#### ALGORITHM ANALYSIS :

**Time Complexity:**  $O(n^2)$

**Problem 4 :** A list of  $n$  positive integers  $a_1; a_2; \dots; a_n$ ; and a positive integer  $t$  is given. Write a program to find subset of the  $a_i$ 's add up to  $t$ ? (You can use each  $a_i$  at most once.)

#### PSEUDOCODE :

Function subset\_sum(nums, target):

$n = \text{length of nums}$

    Initialize a 2D array dp with dimensions  $(n+1) \times (\text{target}+1)$

    Set  $\text{dp}[i][0] = \text{true}$  for all  $i$  from 0 to  $n$  // Base case: subset with sum 0 exists for all subsets

    Set  $\text{dp}[0][j] = \text{false}$  for all  $j$  from 1 to target // Base case: subset with non-zero sum doesn't exist for an empty set

    for  $i$  from 1 to  $n$ :

        for  $j$  from 1 to target:

            if  $\text{nums}[i-1] \leq j$ :



```
dp[i][j] = dp[i-1][j] or dp[i-1][j-nums[i-1]]
```

else:

```
dp[i][j] = dp[i-1][j]
```

Initialize an empty list subset

```
i = n, j = target
```

```
while i > 0 and j > 0:
```

```
    if dp[i][j] and not dp[i-1][j]:
```

```
        Append nums[i-1] to subset
```

```
        j = j - nums[i-1]
```

```
    Decrement i
```

Return subset

**CODE :**

```
def subset_sum(nums, target):
    n = len(nums)
    dp = [[False] * (target + 1) for i in range(n + 1)]

    for i in range(n + 1):
        dp[i][0] = True

    for i in range(1, n + 1):
        for j in range(1, target + 1):
            if nums[i - 1] <= j:
                dp[i][j] = dp[i - 1][j - nums[i - 1]] or dp[i - 1][j]
            else:
                dp[i][j] = dp[i - 1][j]

    subset = []
    i, j = n, target
    while i > 0 and j > 0:
        if dp[i][j] and not dp[i - 1][j]:
            subset.append(nums[i - 1])
            j -= nums[i - 1]
        i -= 1

    return subset[::-1]

nums = list(map(int, input('enter the list').split()))
target = int(input('enter the target'))
print("Subset with sum equal to", target, ":", subset_sum(nums, target))
```

**ALGORITHM ANALYSIS :**

**Time Complexity:**  $O(n^2)$

