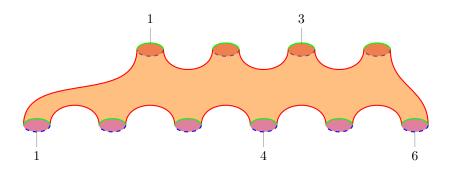
The tqft package: codebase

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? from ?



1 Introduction

This is a package for drawing TQFT diagrams using PGF/TikZ. Its inspiration was a question and answer on the website http://tex.stackexchance.com.

2 Implementation

2.1 Old Version: Node Shapes

- 1 \RequirePackage{pgfkeys}
- 2 \RequirePackage{pgf}

We can view the cobordisms from the input or output ends, the implementation of the choice is to draw an arc from 0 to 180 or from 0 to -180 so we just need to track minus signs. These macros are for that.

- 3 \def\pgf@tqft@minus{-}
- 4 \let\pgf@tqft@upper\@empty
- 5 \let\pgf@tqft@lower\pgf@tqft@minus

Some helpful extra functions.

- \tqftset is our equivalent of \tikzset.
- 6 \def\tqftset#1{\pgfkeys{/pgf/tqft/.cd,#1}}

\tqft@process This macro applies our flow transformation to the given coordinates, with the result stored in \pgf@x and \pgf@y.

- 7 \def\tqft@process#1#2{%
- 8 \edef\tqft@px{#1}
- 9 \edef\tqft@py{#2}
- 10 \pgf@process{

```
\pgftransformreset
        \let\tikz@transform=\pgfutil@empty
 12
        \expandafter\tikzset\expandafter{\tqft@transformation}
 13
        \tikz@transform
 14
        \pgfpointtransformed{\pgfqpoint{\tqft@px}{\tqft@py}}
 15
 16
 17 }
   Declare some dimension registers to hold the specifications of the cobordism.
 18 \newdimen\tqft@xa
 19 \newdimen\tqft@xb
 20 \newdimen\tqft@c
 21 \newdimen\tqft@ch
 22 \newdimen\tqft@h
 23 \newdimen\tqft@s
 24 \newdimen\tqft@w
 25 \newif\iftqft@within@node
Now we set up all the keys that we'll need in the course of this shape
 26 \pgfkeys{
Add a key to switch between the two versions.
      /tikz/tqft/use nodes/.is choice,
      /tikz/tqft/use nodes/true/.code={%
 28
 29
        \tikzset{
If using nodes, set the defaults
 30
          tqft/.style={%
 31
            /tikz/shape=tqft cobordism,
 32
            /pgf/tqft,
 33
            /tikz/every tqft/.try
          },
 34
Unknowns go to /pgf/tqft
 35
          tqft/.unknown/.code={%
            \let\tqft@searchname=\pgfkeyscurrentname%
 36
 37
            \pgfkeys{%
              /pgf/tqft/\tqft@searchname={##1}
 38
 39
 40
          },
 41
        }%
 42
      },
If not using nodes, set the defaults for the library
      /tikz/tqft/use nodes/false/.code={%
 44
        \tikzset{
          tqft/.style={%
 45
            pic type=cobordism,
 46
            tqft/.cd,
 47
            every tqft/.try,
 48
 49
          },
Pass unknown keys on to TikZ.
          tqft/.unknown/.code={%
 50
            \let\tqft@searchname=\pgfkeyscurrentname%
 51
 52
            \pgfkeys{%
```

```
/tikz/\tqft@searchname={##1}
 53
 54
          },
 55
        }%
 56
 57
      /tikz/tqft/use nodes=true,
 58
This deals with unknown keys, passing them on to TikZ.
 59
      /pgf/tqft/.unknown/.code={%
 60
        \let\tqft@searchname=\pgfkeyscurrentname%
        \pgfkeysalso{%
 61
          /tikz/\tqft@searchname={#1}
 62
 63
        }
 64
     },
Let's play happy families!
      /pgf/tqft/.is family,
     /pgf/tqft,
This sets our shape to be the boundary circle
 67
      boundary circle/.style={
 68
        /tikz/shape=tqft boundary circle
      },
 69
These set our number of boundary components
      incoming boundary components/.initial=5,
      outgoing boundary components/.initial=4,
This is the "horizontal" offset of the first outgoing component from the first in-
coming one.
     offset/.initial=0,
This is the "vertical" separation between boundary components.
      cobordism height/.initial=2cm,
This is the "horizontal" separation between boundary components.
      boundary separation/.initial=2cm,
These are the "horizontal" and "vertical" radii, respectively, of the boundary com-
ponents (perhaps poorly named!).
      circle width/.initial=10pt,
     circle depth/.initial=5pt,
These control the separation between the node and its anchors.
 77
      outer xsep/.initial=Opt,
 78
      outer ysep/.initial=0pt,
 79
      outer sep/.style={
        outer xsep=#1,
 80
 81
        outer ysep=#1
 82
      },
```

This is our flow control. The flow key installs a transformation to be applied to our node shape. The possible transformations are stored in the following keys. They aren't just rotations so that the numbering is always "top to bottom" or "left to right".

```
83 flow/.code={%
```

84 \pgfkeys{/pgf/tqft/flow transformation/.expand twice/.expand once=\pgfkeysvalueof{/pgf/t

```
},
 85
     flow transformation south/.initial={},
 86
      flow transformation north/.initial={%
 87
        xscale=-1,rotate=180
 88
 89
      flow transformation east/.initial={%
 90
        rotate=90,xscale=-1
 91
 92
     },
      flow transformation west/.initial={%
 93
       rotate=270
 94
 95
      flow transformation/.initial={},
 96
These control the direction from which we view the cobordism.
      view from/.is choice,
 97
      view from/incoming/.code={%
 98
        \let\pgf@tqft@upper\pgf@tqft@minus
 99
        \let\pgf@tqft@lower\@empty
 100
 101
      view from/outgoing/.code={%
 102
 103
      \let\pgf@tqft@lower\pgf@tqft@minus
 104
        \let\pgf@tqft@upper\@empty
 105
The next set of keys are for styling the different pieces of a cobordism.
      boundary lower style contents/.initial={},
 106
 107
      boundary lower style/.code={%
        \pgfkeys{/pgf/tqft/boundary lower style contents/.style={%
 108
 109
            /tikz/.cd,#1
 110
        }
 111
      },
 112
      boundary style contents/.initial={},
 113
      boundary style/.code={%
 114
        \pgfkeys{/pgf/tqft/boundary style contents/.style={%
 115
            /tikz/.cd,#1
 116
 117
        }
 118
      },
 119
      boundary upper style contents/.initial={},
 120
 121
      boundary upper style/.code={%
 122
        \pgfkeys{/pgf/tqft/boundary upper style contents/.style={%
 123
            /tikz/.cd,#1
 124
        }
 125
      },
 126
      cobordism style contents/.initial={},
 127
 128
      cobordism style/.code={%
        \pgfkeys{/pgf/tqft/cobordism style contents/.style={%
 129
            /tikz/.cd,#1%
 130
 131
        }
 132
 133
      },
```

The next set of keys define some default shapes.

```
pair of pants/.style={
134
       /tikz/tqft,
135
       incoming boundary components=1,
136
       outgoing boundary components=2,
137
       offset=-.5
138
     },
139
140
     /tikz/tqft pair of pants/.style={
141
       /pgf/tqft/pair of pants,
142
     reverse pair of pants/.style={
143
       /tikz/tqft,
144
       incoming boundary components=2,
145
       outgoing boundary components=1,
146
       offset=.5
147
148
     /tikz/tqft reverse pair of pants/.style={
149
       /pgf/tqft/reverse pair of pants,
150
151
     cylinder to prior/.style={
152
153
       /tikz/tqft,
       incoming boundary components=1,
154
       outgoing boundary components=1,
155
       offset=-.5
156
     },
157
     /tikz/tqft cylinder to prior/.style={
158
       /pgf/tqft/cylinder to prior,
159
160
     cylinder to next/.style={
161
162
       /tikz/tqft,
163
       incoming boundary components=1,
164
       outgoing boundary components=1,
       offset=.5
165
166
    },
     /tikz/tqft cylinder to next/.style={
167
       /pgf/tqft/cylinder to next,
168
169
     },
170
     cylinder/.style={
171
       /tikz/tqft,
172
       incoming boundary components=1,
173
       outgoing boundary components=1
174
175
     /tikz/tqft cylinder/.style={
       /pgf/tqft/cylinder,
176
     },
177
     cup/.style={
178
       /tikz/tqft,
179
180
       incoming boundary components=1,
       outgoing boundary components=0
181
182
183
     /tikz/tqft cup/.style={
184
       /pgf/tqft/cup,
185
     },
     cap/.style={
186
       /tikz/tqft,
187
```

```
outgoing boundary components=1
            189
                 }.
            190
                  /tikz/tqft cap/.style={
            191
                    /pgf/tqft/cap,
            192
            193
            194 }
tqft shape This is a generic cobordism shape
            195 \pgfdeclareshape{tqft cobordism}{
           Save our specifications: incoming and outgoing boundary components
                 \savedmacro{\tqft@incoming}{\edef\tqft@incoming{\pgfkeysvalueof{/pgf/tqft/incoming boundar
                 \savedmacro{\tqft@outgoing}{\edef\tqft@outgoing{\pgfkeysvalueof{/pgf/tqft/outgoing boundar
            197
           and the offset (in units of boundary components) between the leading incoming
           and outgoing components (regarded as a shift of the outgoing components relative
           to the incoming)
                 \savedmacro{\tqft@offset}{\edef\tqft@offset{\pgfkeysvalueof{/pgf/tqft/offset}}}
            198
           Now we save our dimensions: height, separation, the radii of the boundary circles,
           and outer seps, and the heights of the control points.
            199
                  \saveddimen{\tqft@height}{\pgf@x=\pgfkeysvalueof{/pgf/tqft/cobordism height}}
                 \saveddimen{\tqft@separation}{\pgf@x=\pgfkeysvalueof{/pgf/tqft/boundary separation}}
            200
            201
                  \saveddimen{\tqft@width}{\pgf@x=\pgfkeysvalueof{/pgf/tqft/circle width}}
            202
                 \saveddimen{\tqft@depth}{\pgf@x=\pgfkeysvalueof{/pgf/tqft/circle depth}}
                  \saveddimen{\tqft@outerxsep}{\pgf@x=\pgfkeysvalueof{/pgf/tqft/outer xsep}}
            203
                  \saveddimen{\tqft@outerysep}{\pgf@x=\pgfkeysvalueof{/pgf/tqft/outer ysep}}
            204
                  \saveddimen{\tqft@control}{
            205
                  \pgfkeysgetvalue{/pgf/tqft/cobordism height}{\tqft@tempa}
            206
                  \pgfkeysgetvalue{/pgf/tqft/circle depth}{\tqft@tempb}
            207
                  \pgfmathsetlength{\pgf@x}{.5 * \tqft@tempa - 4 * \tqft@tempb}
            208
            209 }
           This is the internal transformation that is in place
                   \savedmacro{\tqft@transformation}{%
            210
                  \pgfkeysgetvalue{/pgf/tqft/flow transformation}{\tqft@transformation}
            211
            212 }
           For the externally available anchors, we need to save a few things as well.
              Position of first incoming boundary in internal coordinates
            213
                   \savedanchor{\tqft@start@incoming}{%
                    \pgfmathsetlength{\pgf@x}{-(max(\pgfkeysvalueof{/pgf/tqft/incoming boundary components}
            214
                    \pgfmathsetlength{\pgf@y}{.5 * \pgfkeysvalueof{/pgf/tqft/cobordism height}}
            215
            216 }
           Position of first outgoing boundary in internal coordinates
                   \savedanchor{\tqft@start@outgoing}{%
            217
                    \pgfmathsetlength{\pgf@x}{-(max(\pgfkeysvalueof{/pgf/tqft/incoming boundary components}
            218
                    \pgfmathsetlength{\pgf@y}{-.5 * \pgfkeysvalueof{/pgf/tqft/cobordism height}}
            219
            220 }
           For completeness, we record the size of the text box (not that we expect any text,
           but you never know)
            221 \savedanchor{\tqft@textsize}{%
                 \pgf@y=-.5\ht\pgfnodeparttextbox%
```

incoming boundary components=0,

```
\pgf@x=-.5\wd\pgfnodeparttextbox%
224 }
  These are our externally available anchors
     \anchor{centre}{\pgfpointorigin}
    \anchor{center}{\pgfpointorigin}
227 \anchor{text}{
228
    \tqft@textsize
229 }
230 \anchor{north}{%
     \pgf@ya=\tqft@height\relax
231
     \pgf@yb=.5\pgf@ya
232
     \advance\pgf@yb by \tqft@outerysep\relax
233
234
     \tqft@process{Opt}{\the\pgf@yb}
235 }
236 \anchor{south}{%
237
    \pgf@yb=\tqft@height\relax
238
     \pgf@ya=.5\pgf@yb
     239
    \pgf@yb=-\pgf@ya
240
     \tqft@process{Opt}{\the\pgf@yb}
241
242 }
243 \anchor{west}{%
     \tqft@start@incoming
244
245
     \pgf@xa=\pgf@x
     \advance\pgf@xa by -\tqft@width
246
247
     \pgf@ya=\pgf@y
248
     \tqft@start@outgoing
249
     \pgf@xb=\pgf@x
     \advance\pgf@xb by -\tqft@width
250
     \pgf@yb=\pgf@y
251
     \pgf@xc=.5\pgf@xa
252
     \advance\pgf@xc by .5\pgf@xb
253
     \pgf@yc=.5\pgf@ya
254
255
     \advance\pgf@yc by .5\pgf@yb
     \advance\pgf@xc by -\tqft@outerxsep\relax
256
257
     \tqft@process{\the\pgf@xc}{\the\pgf@yc}
258 }
259 \anchor{east}{%
260
    \tqft@start@incoming
261
     \pgf@xa=\pgf@x
     \pgfmathsetlength{\pgf@xa}{\pgf@xa + (\tqft@incoming - 1) * \tqft@separation}
262
     263
     \pgf@ya=\pgf@y
264
     \tqft@start@outgoing
265
266
     \pgf@xb=\pgf@x
     \pgfmathsetlength{\pgf@xb}{\pgf@xb + (\tqft@outgoing - 1) * \tqft@separation}
267
268
     \advance\pgf@xb by \tqft@width\relax
269
     \pgf@yb=\pgf@y
270
     \pgf@xc=.5\pgf@xa
     \advance\pgf@xc\ by\ .5\pgf@xb
271
272
     \pgf@yc=.5\pgf@ya
273
     \advance\pgf@yc by .5\pgf@yb
274
     \advance\pgf@xc by \tqft@outerxsep\relax
275
    \tqft@process{\the\pgf@xc}{\the\pgf@yc}
```

```
276 }
 277 \anchor{north west}{
           \tqft@start@incoming
 278
            \pgf@xc=\pgf@x
 279
            \pgf@yc=\pgf@y
 280
            \advance\pgf@xc by -\tqft@width\relax
 281
            \advance\pgf@yc by \tqft@outerysep\relax
 282
            \advance\pgf@xc by -\tqft@outerxsep\relax
 284
            \tqft@process{\the\pgf@xc}{\the\pgf@yc}
 285 }
 286 \anchor{south west}{
 287
            \tqft@start@outgoing
            \pgf@xc=\pgf@x
 288
            \pgf@yc=\pgf@y
 289
            \advance\pgf@xc by -\tqft@width\relax
 290
            \advance\pgf@yc by -\tqft@outerysep\relax
 291
            \advance\pgf@xc by -\tqft@outerxsep\relax
 292
            \tqft@process{\the\pgf@xc}{\the\pgf@yc}
 293
 294 }
 295 \anchor{north east}{
 296
           \tqft@start@incoming
 297
            \pgf@xc=\pgf@x
            298
 299
            \pgf@yc=\pgf@y
            \advance\pgf@xc by \tqft@width\relax
 300
 301
            \advance\pgf@yc by \tqft@outerysep\relax
            \advance\pgf@xc by \tqft@outerxsep\relax
 302
 303
            \tqft@process{\the\pgf@xc}{\the\pgf@yc}
 304 }
 305 \anchor{south east}{
 306
           \tqft@start@outgoing
 307
            \pgf@xc=\pgf@x
            \pgfmathsetlength{\pgf@xc}{\pgf@xc + (\tqft@outgoing - 1)*\tqft@separation}
 308
 309
            \pgf@yc=\pgf@y
            \advance\pgf@xc by \tqft@width\relax
 310
            \advance\pgf@yc by -\tqft@outerysep\relax
 311
            \advance\pgf@xc by \tqft@outerxsep\relax
 312
 313
            \tqft@process{\the\pgf@xc}{\the\pgf@yc}
 314 }
To define anchors at the boundary components requires a bit of trickery borrowed
from the "regular polygon" shape.
 315 \expandafter\pgfutil@g@addto@macro\csname pgf@sh@s@tqft cobordism\endcsname{%
           \c@pgf@counta\tqft@incoming\relax%
 316
            \pgfmathloop%
 317
            \ifnum\c@pgf@counta>0\relax%
 318
            \verb|\pgfutil@ifundefined{pgf@anchor@tqft| cobordism@incoming| boundary\space\\the\\c@pgf@counta}{%| boundary\space\\the\\counta}{%| boundary\space\\the\\counta}{%
 319
                \expandafter\xdef\csname pgf@anchor@tqft cobordism@incoming boundary\space\the\c@pgf@cou
 320
            \noexpand\tqft@start@incoming
 321
            \noexpand\pgfmathsetlength{\noexpand\pgf@y}{\noexpand\pgf@y + \noexpand\tqft@outerysep}
 322
            \label{loss} $$\operatorname{noexpand}\left(x + (\theta - 1) * \right) = 0. $$\operatorname{noexpand}\left(x + (\theta - 2) + (\theta - 1) * \right) $$
 323
            324
           }
 325
           }{\c@pgf@counta0\relax}%
 326
```

```
327
            \advance\c@pgf@counta-1\relax%
            \repeatpgfmathloop%
 328
 329 }
 330 \expandafter\pgfutil@g@addto@macro\csname pgf@sh@s@tqft cobordism\endcsname{%
             \c@pgf@counta\tqft@outgoing\relax%
 331
 332
             \pgfmathloop%
             \ifnum\c@pgf@counta>0\relax%
 333
             \pgfutil@ifundefined{pgf@anchor@tqft cobordism@outgoing boundary\space\the\c@pgf@counta}{%
 334
                 \expandafter\xdef\csname pgf@anchor@tqft cobordism@outgoing boundary\space\the\c@pgf@cou
 335
 336
             \noexpand\tqft@start@outgoing
             \noexpand\pgfmathsetlength{\noexpand\pgf@y}{\noexpand\pgf@y - \noexpand\tqft@outerysep}
 337
             338
             \label{loss} $$\operatorname{noexpand} \endpercel{loss} {\noexpand} \endpercel{loss} $$\operatorname{noexpand} \endpercel{loss} $$\operatorname{noexpand} \end{loss} $$\end{loss} $$\operatorname{noexpand} \end{loss} $$\end{loss} $$\end{loss} $$\operatorname{noexpand} \end{loss} $$\end{loss} $$\end{loss} $$\end{loss} $$\end{loss} $$\end{loss} $$\end{loss} $$\end{loss} $$\end{loss} $$\end{loss} \end{loss} $$\end{loss} $$\end{loss} $$\end{loss} $$\end{lo
 339
 340
            }
            }{\c@pgf@counta0\relax}%
 341
             \advance\c@pgf@counta-1\relax%
 342
 343
             \repeatpgfmathloop%
 344 }
 345 \expandafter\pgfutil@g@addto@macro\csname pgf@sh@s@tqft cobordism\endcsname{\%}
             \c@pgf@counta\tqft@incoming\relax%
 346
 347
             \advance\c@pgf@counta-1\relax
 348
             \pgfmathloop%
 349
            \ifnum\c@pgf@counta>0\relax%
             \pgfutil@ifundefined{pgf@anchor@tqft cobordism@after incoming boundary\space\the\c@pgf@cou
 350
                 \expandafter\xdef\csname pgf@anchor@tqft cobordism@after incoming boundary\space\the\c@r
 351
 352
             \noexpand\tqft@start@incoming
             \noexpand\pgfmathsetlength{\noexpand\pgf@y}{.25 * \noexpand\pgf@y +.75 * \noexpand\tqft@cc
 353
             \noexpand\pgfmathsetlength{\noexpand\pgf@x}{\noexpand\pgf@x + (\the\c@pgf@counta - .5) * \
 354
             \noexpand\tqft@process{\noexpand\the\noexpand\pgf@x}{\noexpand\the\noexpand\pgf@y}
 355
 356
            }{\c@pgf@counta0\relax}%
 357
 358
             \advance\c@pgf@counta-1\relax%
             \repeatpgfmathloop%
 359
 360 }
 361 \expandafter\pgfutil@g@addto@macro\csname pgf@sh@s@tqft cobordism\endcsname{%
             \c@pgf@counta\tqft@outgoing\relax%
 362
             \advance\c@pgf@counta-1\relax
 363
 364
             \pgfmathloop%
 365
             \ifnum\c@pgf@counta>0\relax%
 366
             \pgfutil@ifundefined{pgf@anchor@tqft cobordism@after outgoing boundary\space\the\c@pgf@cou
 367
                 \expandafter\xdef\csname pgf@anchor@tqft cobordism@after outgoing boundary\space\the\c@p
 368
             \noexpand\tqft@start@outgoing
             \noexpand\pgfmathsetlength{\noexpand\pgf@y}{.25 * \noexpand\pgf@y -.75 * \noexpand\tqft@cc
 369
             \n0 \noexpand\pgfmathsetlength{\noexpand\pgf@x}{\noexpand\pgf@x + (\the\c@pgf@counta - .5) * \
 370
             \noexpand\tqft@process{\noexpand\the\noexpand\pgf@x}{\noexpand\the\noexpand\pgf@y}
 371
 372
 373
            }{\c@pgf@counta0\relax}%
 374
             \advance\c@pgf@counta-1\relax%
 375
             \repeatpgfmathloop%
 376 }
Now we define the background path. This is the upper part of the cobordism.
            \backgroundpath{
```

Apply the internal transformation

```
Compute the starting position of the incoming boundary components so that we
get the centre anchor on the centre of the cobordism
383 \tqft@start@incoming
384 \tqft@xa=\pgf@x
       \advance\tqft@xa by -.5\tqft@w\relax
386 \tqft@h=\pgf@y
387
       \tqft@xb=\tqft@xa
       \advance\tqft@xb by \tqft@w\relax
388
389 \tqft@c=\tqft@control\relax
Do we have any incoming boundary components at all?
       \ifnum\tqft@incoming>0
Yes, so move to the position of the first and draw it
391
       \pgfpathmoveto{\pgfqpoint{\tqft@xa}{\tqft@h}}
392
         \pgfpatharc{\pgf@tqft@upper180}{0}{\tqft@width and \tqft@depth}
Do we have any more incoming boundary components?
      \ifnum\tqft@incoming>1
393
Yes, so iterate over the remaining incoming boundary components
       \foreach \tqft@k in {2,...,\tqft@incoming} {
394
        \advance\tqft@xa by \tqft@k\tqft@s
395
        396
        \advance\tqft@xb by -2\tqft@s
397
        \advance\tqft@xa by -\tqft@s
398
        \pgfpathcurveto{\pgfqpoint{\tqft@xb}{\tqft@c}}{\pgfqpoint{\tqft@xa}{\tqft@c}}{\pgfqpoir
399
400
        \pgfpatharc{\pgf@tqft@upper180}{0}{\tqft@width and \tqft@depth}
401
402
       \fi
If we don't have any outgoing boundary components, may as well close up now.
403
       \ifnum\tqft@outgoing=0
        404
        \advance\tqft@xb by -\tqft@s
405
        \pgfmathsetlength{\tqft@ch}{min(0,max(-\tqft@h,\tqft@h - (\tqft@h - \tqft@c) * ((abs(\t
406
407
         \pgfpathcurveto{\pgfqpoint{\tqft@xb}{\tqft@ch}}{\pgfqpoint{\tqft@xa}{\tqft@ch}}{\pgfqpc
       \fi
408
       \fi
409
Shift down to the outgoing components, if we have any
       \ifnum\tqft@outgoing>0
410
411
         \advance\tqft@xb by \tqft@incoming\tqft@s
        \advance\tqft@xb by -\tqft@s
412
        \pgfmathsetlength{\tqft@xa}{\tqft@xa + (\tqft@outgoing - 1 + \tqft@offset) * \tqft@sepa
413
If we had incoming boundaries, this is a curveto, otherwise it's a moveto
```

378

379

380

381

382

\let\tikz@transform=\pgfutil@empty

Convert the boundary separation and width to lengths

\pgfmathsetlength{\tqft@s}{\tqft@separation}

\pgfmathsetlength{\tqft@w}{2*\tqft@width}

\tikz@transform

\expandafter\tikzset\expandafter{\tqft@transformation}

 $\left\langle \frac{1}{2}\right\rangle$

414

```
\pgfpathcurveto{\pgfqpoint{\tqft@xb}{\tqft@ch}}{\pgfqpoint{\tqft@xa}{-
 416
        \tqft@ch}}{\pgfqpoint{\tqft@xa}{-\tqft@h}}
                \else
 417
                  \pgfpathmoveto{\pgfqpoint{\tqft@xa}{-\tqft@h}}
 418
 419
                  \tqft@xb=\tqft@xa
 420
                  \advance\tqft@xb by -\tqft@w
 421
Now draw the lower components
 422
                  \pgfpatharc{0}{\pgf@tqft@upper180}{\tqft@width and \tqft@depth}
Now iterate over the remaining outgoing boundary components
                \ifnum\tqft@outgoing>1
 423
                \foreach \tqft@k in {2,...,\tqft@outgoing} {
 424
                  \advance\tqft@xa by -\tqft@k\tqft@s
 425
                  \advance\tqft@xb by -\tqft@k\tqft@s
 426
 427
                  \advance\tqft@xb by 2\tqft@s
                  \advance\tqft@xa by \tqft@s
 428
                  \pgfpathcurveto{\pgfqpoint{\tqft@xb}{-\tqft@c}}{\pgfqpoint{\tqft@xa}{-
 429
        \tqft@c}{\pgfqpoint{\tqft@xa}{-\tqft@h}}
 430
                  \pgfpatharc{0}{\pgf@tqft@upper180}{\tqft@width and \tqft@depth}
                }
 431
 432
                \fi
Shift back up to the incoming components, if we had any, otherwise arc back to
our starting point
                  \advance\tqft@xb by -\tqft@outgoing\tqft@s
 433
                  \advance\tqft@xb by \tqft@s
 434
                \ifnum\tqft@incoming>0
 435
                  \pgfmathsetlength{\tqft@xa}{\tqft@xa - (\tqft@outgoing -1 + \tqft@offset) * \tqft@separ
 436
                  \label{thm:local_max} $$ \operatorname{length}(tqft@ch)_{min(0,max(-\tqft@h,\tqft@h - (\tqft@h - \tqft@c) * ((abs(\tqft@h,\tqft@h - \tqft@c) + (\tqft@h - \tqft@h - \tqft@c) + (\tqft@h - \tqft@h - \tqft@h - \tqft@h - \tqft@c) + (\tqft@h - \tqft@h - \tqft@
 437
                  \pgfpathcurveto{\pgfqpoint{\tqft@xb}{-\tqft@ch}}{\pgfqpoint{\tqft@xa}{\tqft@ch}}{\pgfqp
 438
 439
                \else
                  440
                  \pgfpathcurveto{\pgfqpoint{\tqft@xb}{-\tqft@ch}}{\pgfqpoint{\tqft@xa}{-
 441
        \tqft@ch}}{\pgfqpoint{\tqft@xa}{-\tqft@h}}
 442
                \fi
 443
Close the path
                  \pgfpathclose
 444
 445
End of background path Now we define the behind background path. This is the
lower part of the boundary circles.
          \behindbackgroundpath{
Apply the internal transformation
                \let\tikz@transform=\pgfutil@empty
 447
                \expandafter\tikzset\expandafter{\tqft@transformation}
 448
                \tikz@transform
 449
Convert the boundary separation and width to lengths
                \pgfmathsetlength{\tqft@s}{\tqft@separation}
 450
 451
                \pgfmathsetlength{\tqft@w}{2*\tqft@width}
```

```
Compute the starting position of the incoming boundary components so that we
get the centre anchor on the centre of the cobordism
        \pgfmathsetlength{\tqft@xa}{-(max(\tqft@incoming - 1,\tqft@outgoing - 1 + \tqft@offset)
452
        \pgfmathsetlength{\tqft@h}{.5 * \tqft@height}
453
This section draws the boundary circles
Initialise the TikZ path settings and read in the style options for the boundary
455
          \tikz@mode@fillfalse%
          \tikz@mode@drawfalse%
456
          \let\tikz@mode=\pgfutil@empty
457
          \let\tikz@options=\pgfutil@empty
458
459
          \tqftset{boundary style contents}
460
          \tikz@mode
          \tikz@options
461
Do we have any incoming boundary components at all?
        \ifnum\tqft@incoming>0
Yes, so iterate over them
463
        \foreach \tqft@k in {1,...,\tqft@incoming} {
         \advance\tqft@xa by \tqft@k\tqft@s
464
         \pgfpathellipse{\pgfqpoint{\tqft@xa}{\tqft@h}}{\pgfqpoint{\tqft@width}{0pt}}{\pgfqpoint
465
        }
466
467
        \fi
Now iterate over the outgoing boundary components, if we have any
        \ifnum\tqft@outgoing>0
468
         \pgfmathsetlength{\tqft@xa}{\tqft@xa + (\tqft@outgoing + \tqft@offset + 1) * \tqft@sepa
469
        \foreach \tqft@k in {1,...,\tqft@outgoing} {
470
         \advance\tqft@xa by -\tqft@k\tqft@s
471
472 %
          \advance\tqft@xa by \tqft@s
         \pgfpathellipse{\pgfqpoint{\tqft@xa}{-\tqft@h}}{\pgfqpoint{\tqft@width}{0pt}}{\pgfqpoir
473
        }
474
        \fi
475
476
          \edef\tikz@temp{\noexpand\pgfusepath{%
477
              \iftikz@mode@fill fill,\fi%
478
              \iftikz@mode@draw draw\fi%
479
          }}%
480
          \tikz@temp
481
This section draws the lower parts of the boundary circles
482
Initialise the TikZ path settings and read in the style options for the boundary
          \tikz@mode@fillfalse%
483
484
          \tikz@mode@drawfalse%
485
          \let\tikz@mode=\pgfutil@empty
486
          \let\tikz@options=\pgfutil@empty
          \tqftset{boundary lower style contents}
487
          \tikz@mode
488
          \tikz@options
489
          \advance\tqft@xa by .5\tqft@w
490
```

```
Do we have any incoming boundary components at all?
        \ifnum\tqft@incoming>0
491
Yes, so iterate over them
        \foreach \tqft@k in {1,...,\tqft@incoming} {
492
         \advance\tqft@xa by \tqft@k\tqft@s
493
494
         \pgfpathmoveto{\pgfqpoint{\tqft@xa}{\tqft@h}}
         \pgfpatharc{0}{\pgf@tqft@lower180}{\tqft@width and \tqft@depth}
495
496
497
        \fi
Now iterate over the outgoing boundary components, if we have any
        \ifnum\tqft@outgoing>0
498
         \pgfmathsetlength{\tqft@xa}{\tqft@xa + (\tqft@outgoing + \tqft@offset + 1) * \tqft@sepa
499
        \foreach \tqft@k in {1,...,\tqft@outgoing} {
500
501
         \advance\tqft@xa by -\tqft@k\tqft@s
          \advance\tqft@xa by \tqft@s
502 %
503
         \pgfpathmoveto{\pgfqpoint{\tqft@xa}{-\tqft@h}}
504
         \pgfpatharc{0}{\pgf@tqft@lower180}{\tqft@width and \tqft@depth}
505
        \fi
506
          \edef\tikz@temp{\noexpand\pgfusepath{%
507
              \iftikz@mode@fill fill,\fi%
508
              \iftikz@mode@draw draw\fi%
509
          ት ጉ %
510
511
          \tikz@temp
        }
512
      }
513
End of behind background path.
   Now we define the before background path. This is the upper part of the
boundary circles and the cobordism edge.
     \beforebackgroundpath{
We don't apply the internal transformation as it is already in place from the
\backgroundpath. Convert the boundary separation and width to lengths
        \pgfmathsetlength{\tqft@s}{\tqft@separation}
515
516
        \pgfmathsetlength{\tqft@w}{2*\tqft@width}
Compute the starting position of the incoming boundary components so that we
get the centre anchor on the centre of the cobordism
517
        \pgfmathsetlength{\tqft@xa}{-(max(\tqft@incoming - 1,\tqft@outgoing - 1 + \tqft@offset)
        \tqft@xb=\tqft@xa
518
        \advance\tqft@xb by \tqft@w
519
520 \neq 0 
        \pgfmathsetlength{\tqft@h}{.5 * \tqft@height}
This section draws the non-boundary part of the cobordism.
522
Initialise the TikZ path settings and read in the style options for the boundary
          \tikz@mode@fillfalse%
523
          \tikz@mode@drawfalse%
524
          \let\tikz@mode=\pgfutil@empty
525
          \let\tikz@options=\pgfutil@empty
526
527
          \tqftset{cobordism style contents}
```

```
528
         \tikz@mode
529
         \tikz@options
530 % Do we have any incoming boundary components at all?
531 %
        \begin{macrocode}
       \ifnum\tqft@incoming>0
532
Do we have more than one?
      \ifnum\tqft@incoming>1
533
Yes, so iterate over the remaining incoming boundary components
       \foreach \tqft@k in {2,...,\tqft@incoming} {
535
        \advance\tqft@xa by \tqft@k\tqft@s
        \advance\tqft@xb by \tqft@k\tqft@s
536
        537
        \advance\tqft@xa by -\tqft@s
538
       \pgfpathmoveto{\pgfqpoint{\tqft@xb}{\tqft@h}}
539
        540
       }
541
       \fi
542
If we don't have any outgoing boundary components, may as well close up now.
543
       \ifnum\tqft@outgoing=0
544
        \advance\tqft@xb by \tqft@incoming\tqft@s
        \advance\tqft@xb by -\tqft@s
545
        \pgfmathsetlength{\tqft@ch}{min(0,max(-\tqft@h,\tqft@h - (\tqft@h - \tqft@c) * ((abs(\t
546
       \pgfpathmoveto{\pgfqpoint{\tqft@xb}{\tqft@h}}
547
548
        \pgfpathcurveto{\pgfqpoint{\tqft@xb}{\tqft@ch}}{\pgfqpoint{\tqft@xa}{\tqft@ch}}{\pgfqpc
549
550
       \fi
Shift down to the outgoing components, if we have any
       \ifnum\tqft@outgoing>0
552
        \advance\tqft@xb by \tqft@incoming\tqft@s
553
        \advance\tqft@xb by -\tqft@s
        \label{tqft0xa} $$ \operatorname{tqft0xa} + (\operatorname{tqft0outgoing} - 1 + \operatorname{tqft0offset}) * \operatorname{tqft0separate} $$
554
If we had incoming boundaries, this is a curveto, otherwise it's a moveto
       \ifnum\tqft@incoming>0
555
        556
557
        \pgfpathmoveto{\pgfqpoint{\tqft@xb}{\tqft@h}}
        558
   \tqft@ch}}{\pgfqpoint{\tqft@xa}{-\tqft@h}}
       \else
559
        \pgfpathmoveto{\pgfqpoint{\tqft@xa}{-\tqft@h}}
560
561
562
        \tqft@xb=\tqft@xa
563
        \advance\tqft@xb\ by\ -\tqft@w
Now draw the lower components
        564
Now iterate over the remaining outgoing boundary components
       \ifnum\tqft@outgoing>1
565
       \foreach \tqft@k in {2,...,\tqft@outgoing} {
566
        \advance\tqft@xa by -\tqft@k\tqft@s
567
        \advance\tqft@xb by -\tqft@k\tqft@s
568
```

\advance\tqft@xb by 2\tqft@s

```
\advance\tqft@xa by \tqft@s
570
         \pgfpathcurveto{\pgfqpoint{\tqft@xb}{-\tqft@c}}{\pgfqpoint{\tqft@xa}{-
571
    \tqft@c}}{\pgfqpoint{\tqft@xa}{-\tqft@h}}
         \advance\tqft@xa by -\tqft@w
572
573
         \pgfpathmoveto{\pgfqpoint{\tqft@xa}{-\tqft@h}}
574
575
Shift back up to the incoming components, if we had any, otherwise arc back to
our starting point
         \advance\tqft@xb by -\tqft@outgoing\tqft@s
576
         \advance\tqft@xb by \tqft@s
577
578
        \ifnum\tqft@incoming>0
579
         \pgfmathsetlength{\tqft@xa}{\tqft@xa - (\tqft@outgoing -1 + \tqft@offset) * \tqft@separ
         \pgfmathsetlength{\tqft@ch}{min(0,max(-\tqft@h,\tqft@h - (\tqft@h - \tqft@c) * ((abs(\t
580
         \pgfpathcurveto{\pgfqpoint{\tqft@xb}{-\tqft@ch}}{\pgfqpoint{\tqft@xa}{\tqft@ch}}{\pgfqp
581
582
         \pgfmathsetlength{\tqft@ch}{min(0,max(-\tqft@h,\tqft@h - (\tqft@h - \tqft@c) * ((abs(\t
583
         584
    \tqft@ch}}{\pgfqpoint{\tqft@xa}{-\tqft@h}}
585
586
          \edef\tikz@temp{\noexpand\pgfusepath{%
587
              \iftikz@mode@fill fill,\fi%
588
              \iftikz@mode@draw draw\fi%
589
590
          }}%
          \tikz@temp
This section draws the upper parts of the boundary circles
593
Initialise the TikZ path settings and read in the style options for the boundary
594 \let\tqft@bdry@path=\pgfutil@empty
595 \verb|\let\tqft@bdry@node@path=\pgfutil@empty|
596 \pgfsyssoftpath@setcurrentpath{\tqft@bdry@path}
          \tikz@mode@fillfalse%
597
          \tikz@mode@drawfalse%
598
599
          \let\tikz@mode=\pgfutil@empty
600
          \let\tikz@options=\pgfutil@empty
601
          \tqftset{boundary upper style contents}
602
          \tikz@mode
603
          \tikz@options
604
          \advance\tqft@xa by -\tqft@s
          \verb|\advance|| tqft@xa by \tqft@w|
605
Do we have any incoming boundary components at all?
        \ifnum\tqft@incoming>0
606
Yes, so iterate over them
607
        \foreach \tqft@k in {1,...,\tqft@incoming} {
         \advance\tqft@xa by \tqft@k\tqft@s
608
609
         \pgfpathmoveto{\pgfqpoint{\tqft@xa}{\tqft@h}}
610
         \pgfpatharc{0}{\pgf@tqft@upper180}{\tqft@width and \tqft@depth}
611
      \ifx\tikz@fig@name\pgfutil@empty
```

\else

```
613
                               \advance\tqft@xa by -\tqft@width
                        614
                               \pgftransformshift{\pgfqpoint{\tqft@xa}{\tqft@h}}
                        615
                               \tqft@within@nodetrue
                        616
                               \pgfsyssoftpath@getcurrentpath{\tqft@bdry@path}
                        617
                               \pgfsyssoftpath@setcurrentpath{\tqft@bdry@node@path}
                        618
                               \pgfnode{tqft boundary circle}{centre}{}\tikz@fig@name\space incoming \tqft@k}{}
                        619
                               \pgfsyssoftpath@getcurrentpath{\tqft@bdry@node@path}
                        620
                        621
                               \pgfsyssoftpath@setcurrentpath{\tqft@bdry@path}
                        622
                        623
                             \fi
                               }
                        624
                               \fi
                        625
                       Now iterate over the outgoing boundary components, if we have any
                               \ifnum\tqft@outgoing>0
                        626
                                \pgfmathsetlength{\tqft@xa}{\tqft@xa + (\tqft@outgoing + \tqft@offset + 1) * \tqft@sepa
                        627
                               \foreach \tqft@k in {1,...,\tqft@outgoing} {
                        628
                                \advance\tqft@xa by -\tqft@k\tqft@s
                        629
                                 \advance\tqft@xa by \tqft@s
                        630 %
                        631
                                \pgfpathmoveto{\pgfqpoint{\tqft@xa}{-\tqft@h}}
                                 \pgfpatharc{0}{\pgf@tqft@upper180}{\tqft@width and \tqft@depth}
                        632
                        633
                             \ifx\tikz@fig@name\pgfutil@empty
                        634
                             \else
                        635
                               \pgfmathtruncatemacro{\tqft@l}{\tqft@outgoing + 1 - \tqft@k}
                        636
                               \advance\tqft@xa by -\tqft@width
                        637
                               \pgftransformshift{\pgfqpoint{\tqft@xa}{-\tqft@h}}
                        638
                               \tqft@within@nodetrue
                        639
                               \pgfsyssoftpath@getcurrentpath{\tqft@bdry@path}
                        640
                               \pgfsyssoftpath@setcurrentpath{\tqft@bdry@node@path}
                        641
                        642
                               \pgfnode{tqft boundary circle}{centre}{}\tikz@fig@name\space outgoing \tqft@l}{}
                        643
                               \pgfsyssoftpath@getcurrentpath{\tqft@bdry@node@path}
                               \pgfsyssoftpath@setcurrentpath{\tqft@bdry@path}
                        644
                        645
                             }
                        646
                             \fi
                               }
                        647
                        648
                                  \edef\tikz@temp{\noexpand\pgfusepath{%
                        649
                        650
                                      \iftikz@mode@fill fill,\fi%
                        651
                                      \iftikz@mode@draw draw\fi%
                                 }}%
                        652
                        653
                                  \tikz@temp
                        654
                        655
                             }
                        656 }
boundary circle shape This is a the shape of the boundary circles
                        657 \pgfdeclareshape{tqft boundary circle}{
                       Now we save our dimensions: height, separation, and the radii of the boundary
                       circles
                             \saveddimen{\tqft@height}{\pgf@x=\pgfkeysvalueof{/pgf/tqft/cobordism height}}
                        658
```

\saveddimen{\tqft@separation}{\pgf@x=\pgfkeysvalueof{/pgf/tqft/boundary separation}}

```
660 \saveddimen{\tqft@width}{\pgf@x=\pgfkeysvalueof{/pgf/tqft/circle width}}
661 \saveddimen{\tqft@depth}{\pgf@x=\pgfkeysvalueof{/pgf/tqft/circle depth}}
```

For the externally available anchors, we need to save the declared transformation; we save the actual transformation, not the macro that points to it. If we're called within the main cobordism shape, the transformation is already applied so we ignore it.

```
\savedmacro{\tqft@transformation}{%
662
      \iftqft@within@node
663
      \let\tqft@transformation=\pgfutil@empty
664
665
      \pgfkeysgetvalue{/pgf/tqft/flow transformation}{\tqft@transformation}
666
667
668 }
       \savedanchor{\tqft@centre}{%
669
      \pgfpointorigin}
670
For completeness, we record the size of the text box (not that we expect any text,
but you never know)
671 \savedanchor{\tqft@textsize}{%
      \verb|\pgf@y=-.5\ht\pgfnodeparttextbox||
673
      \pgf@x=-.5\wd\pgfnodeparttextbox%
674 }
These are our externally available anchors
      \anchor{centre}{\tqft@centre}
675
      \anchor{center}{\tqft@centre}
676
677 \anchor{text}{
      \tqft@textsize
678
679 }
      \anchor{next}{%
680
      \tqft@process{\tqft@separation}{Opt}}%
681
      \anchor{prior}{%
682
      \tqft@process{-\tqft@separation}{0pt}}%
683
      \anchor{above}{%
684
      \tqft@process{Opt}{\tqft@height}}%
685
      \anchor{below}{%
686
      \tqft@process{Opt}{-\tqft@height}}%
```

The anchor border is the ellipse, but we need to take into account the possible transformation. (This isn't right if the origin is shifted.) At the moment, '0 degrees' is interpreted in the transformed coordinate system. Should provide a system whereby that can be interpreted in the main coordinate system.

688 \anchorborder{

This next \pgf@process makes the angles absolute. Comment it out to make the angles relative.

```
689 \tqft@process{\the\pgf@x}{\the\pgf@y}
690 \edef\tqft@marshal{%
691 \noexpand\pgfpointborderellipse
692 {\noexpand\pgfqpoint{\the\pgf@x}{\the\pgf@y}}
693 {\noexpand\pgfqpoint{\tqft@width}{\tqft@depth}}
694 }%
```

```
\tqft@marshal
695
      696
697 }
Now we define the background path. This is the upper part of the cobordism.
     \backgroundpath{
698
Apply the internal transformation if we're not within a node
        \let\tikz@transform=\pgfutil@empty
700
        \expandafter\tikzset\expandafter{\tqft@transformation}
        \tikz@transform
701
Draw the boundary circle
      \pgfpathellipse{\pgfqpoint{0pt}}{\pgfqpoint{\tqft@width}{0pt}}{\pgfqpoint{0pt}{\tqft@
703
     }
We draw the upper and lower arcs again with the appropriate styles
     \beforebackgroundpath{
705
      \iftqft@within@node
706
      \else
707
        \tikz@mode@fillfalse%
708
        \tikz@mode@drawfalse%
709
        \let\tikz@mode=\pgfutil@empty
        \let\tikz@options=\pgfutil@empty
710
711
        \pgfsys@beginscope
712
          \tqftset{boundary lower style contents}
713
          \tikz@mode
714
715
          \tikz@options
          \pgfpathmoveto{\pgfqpoint{\tqft@width}{0pt}}
716
          \pgfpatharc{0}{\pgf@tqft@lower180}{\tqft@width and \tqft@depth}
717
718
          \edef\tikz@temp{\noexpand\pgfusepath{%
719
              \iftikz@mode@fill fill,\fi%
              \iftikz@mode@draw draw\fi%
720
          }}%
721
          \tikz@temp
722
          \pgfsys@endscope
723
       }
724
725
          \pgfsys@beginscope
726
727
          \tqftset{boundary upper style contents}
728
          \tikz@mode
729
          \tikz@options
          \pgfpathmoveto{\pgfqpoint{\tqft@width}{0pt}}
730
          \pgfpatharc{0}{\pgf@tqft@upper180}{\tqft@width and \tqft@depth}
731
          \edef\tikz@temp{\noexpand\pgfusepath{%
732
              \iftikz@mode@fill fill,\fi%
733
              \iftikz@mode@draw draw\fi%
734
          }}%
735
          \tikz@temp
736
          \pgfsys@endscope
737
       }
738
739
        \fi
740
     }
```

741 }

2.2 New Version: Picture Shapes

Issue a warning if the pic syntax is not available.

```
742 \ifcsname pgfk@/handlers/.pic/.@cmd\endcsname
743 \else
744 \pgfwarning{This library only works with TikZ 3.0 or later; for earlier versions of TikZ use
745 \fi
```

For the boundaries, we need elliptical node shapes.

```
746 \usetikzlibrary{shapes.geometric}
```

We can view the cobordisms from the *input* or *output* ends, the implementation of the choice is to draw an arc from 0 to 180 or from 0 to -180 so we just need to track minus signs. These macros are for that.

```
747 \def\pgf@tqft@minus{-}
748 \let\pgf@tqft@upper\@empty
749 \let\pgf@tqft@lower\pgf@tqft@minus
```

Should we twist the cobordism?

```
750 \newif\iftqft@twisted
```

Split an anchoring coordinate. The y-value is simply multiplied by the cobordism height (but pointing downwards, so that 1 is level with the outgoing boundary). The x-value is multiplied by the boundary separation, but is shifted so that at the incoming boundary level, or above, then it is in line with the incoming boundaries and similarly at the outgoing boundary level, or below, it is in line with the outgoing boundaries.

```
751 \def\tqft@split(#1,#2){%
752 \pgfmathsetmacro\tqft@y{#2 * (-\tqft@val{cobordism height})}%
753 \pgfmathsetmacro\tqft@x{(#1 - 1 + max(min(#2,1),0)*\tqft@val{offset}) * \tqft@val{boundary}
754 \def\tqft@shift{(\tqft@x pt, \tqft@y pt)}%
755 }%
```

Now we set up all the keys that we'll need in the course of this shape

```
756 \tikzset{
```

Fix for the fact that the alias key doesn't use the prefix and suffix.

This key is our basic installer key, setting the pic and putting us in the right key family.

```
761
      tqft/.style={%
762
        pic type=cobordism,
763
        every tqft/.try,
764
        tqft/.cd,
765
     },
This deals with unknown keys, passing them on to TikZ.
      tqft/.unknown/.code={%
766
        \let\tqft@searchname=\pgfkeyscurrentname%
767
        \pgfkeysalso{%
768
          /tikz/\tqft@searchname={#1}
769
770
        }
771
     },
```

```
Let's play happy families!
 772 tqft/.cd,
These set our number of boundary components and genus.
      incoming boundary components/.initial=5,
      outgoing boundary components/.initial=4,
      skip incoming boundary components/.initial={},
 775
      skip outgoing boundary components/.initial={},
 776
      genus/.initial = 0,
This is the "horizontal" offset of the first outgoing component from the first in-
coming one.
778
     offset/.initial=0,
This is the "vertical" separation between boundary components.
      cobordism height/.initial=2cm,
This is the "horizontal" separation between boundary components.
      boundary separation/.initial=2cm,
These are the "horizontal" and "vertical" radii, respectively, of the boundary com-
ponents.
      circle x radius/.initial=10pt,
     circle y radius/.initial=5pt,
These control the direction from which we view the cobordism.
 783
      view from/.is choice,
 784
      view from/incoming/.code={%
        \let\pgf@tqft@upper\pgf@tqft@minus
 785
        \let\pgf@tqft@lower\@empty
 786
 787
      view from/outgoing/.code={%
 788
      \let\pgf@tqft@lower\pgf@tqft@minus
 789
        \let\pgf@tqft@upper\@empty
 790
 791
     },
Should we twist the cobordism?
     twisted/.is if=tqft@twisted,
We simulate node placement using the following key.
      anchor/.initial = none,
The next set of keys define some default shapes.
 794
      pair of pants/.style={
 795
        /tikz/tqft,
 796
        incoming boundary components=1,
 797
        outgoing boundary components=2,
        offset=-.5
 798
 799
      /tikz/tqft pair of pants/.style={
 800
        /tikz/tqft/pair of pants,
 801
     },
 802
     reverse pair of pants/.style={
 803
        /tikz/tqft,
 804
        incoming boundary components=2,
 805
```

outgoing boundary components=1,

806 807

offset=.5

```
808
     /tikz/tqft reverse pair of pants/.style={
809
       /tikz/tqft/reverse pair of pants,
810
811
     cylinder to prior/.style={
812
       /tikz/tqft,
813
       incoming boundary components=1,
814
815
       outgoing boundary components=1,
       offset=-.5
816
     },
817
     /tikz/tqft cylinder to prior/.style={
818
       /tikz/tqft/cylinder to prior,
819
820
     },
     cylinder to next/.style={
821
       /tikz/tqft,
822
       incoming boundary components=1,
823
824
       outgoing boundary components=1,
825
       offset=.5
     },
826
     /tikz/tqft cylinder to next/.style={
827
       /tikz/tqft/cylinder to next,
828
     },
829
     cylinder/.style={
830
       /tikz/tqft,
831
832
       incoming boundary components=1,
       outgoing boundary components=1
833
     },
834
     /tikz/tqft cylinder/.style={
835
836
       /tikz/tqft/cylinder,
837
     },
     cup/.style={
838
       /tikz/tqft,
839
840
       incoming boundary components=1,
       outgoing boundary components=0
841
     },
842
843
     /tikz/tqft cup/.style={
844
       /tikz/tqft/cup,
845
     },
846
     cap/.style={
847
       /tikz/tqft,
848
       incoming boundary components=0,
849
       outgoing boundary components=1
     },
850
     /tikz/tqft cap/.style={
851
852
       /tikz/tqft/cap,
     },
853
854 }
  This is a little helper macro for getting the values of tqft keys.
855 \ensuremath{\def \tqft@val\#1{\pgfkeysvalueof{\tikz/tqft/\#1}}}
  Now we define the code for the actual cobordism shape.
856 \tikzset{
    cobordism/.pic={
857
```

Defining the cobordism paths. This holds the full boundary path of the cobordism shape.

```
858 \gdef\tqft@fullpath{}%
```

This is a list of the edge pieces without the boundary circles.

```
859 \global\let\tqft@blist\pgfutil@gobble%
```

This punches the holes (if there are any) in the cobordism shape.

```
860 \gdef\tqft@gclip{}%
```

This is a list of the paths for drawing the holes.

```
%861 \global\let\tqft@glist\pgfutil@gobble%
```

This collects any coordinates that are to be defined (it appears to be difficult to define them as we go along).

```
862 \global\let\tqft@clist\pgfutil@gobble%
```

This collects any coordinates that can be used to shift the shape that aren't to be defined using \tqft@clist.

```
863 \global\let\tqft@alist\pgfutil@gobble
```

These will be lists of the boundary components, divided into sets as to whether or not they are rendered. For the outgoing ones, we need two lists because they are rendered in the opposite order to how they are labelled.

```
864 \global\let\tqft@ibdrylist=\pgfutil@gobble
865 \global\let\tqft@cibdrylist=\pgfutil@gobble
866 \global\let\tqft@cobdrylist=\pgfutil@gobble
867 \global\let\tqft@cobdrylist=\pgfutil@gobble
868 \global\let\tqft@robdrylist=\pgfutil@gobble
869 \global\let\tqft@rcobdrylist=\pgfutil@gobble
```

Is the cobordism twisted? If so, we need to reverse the order of the outgoing boundary components.

```
870 \iftqft@twisted
871 \pgfmathsetmacro\tqft@outgoing@end{0}%
872 \pgfmathsetmacro\tqft@outgoing@dir{-1}%
873 \else
874 \pgfmathsetmacro\tqft@outgoing@end{1}%
875 \pgfmathsetmacro\tqft@outgoing@dir{1}%
876 \fi
```

The first stage is to iterate over the incoming boundary components (if there are any), building up the various paths.

```
877 \ifnum\tqft@val{incoming boundary components}>0\relax
```

We have some so draw the half circle for the first component. Note that we use \pgf@tqft@upper to flip the sign of the start angle depending on the view from setting.

And add the centre to the list for available shifts.

```
\xdef\tqft@alist{%

883 \tqft@alist,-incoming boundary 1/{(0,0)},-incoming boundary/{(0,0)}%

884 }%
```

If there are more than one then for each subsequent one we add the curve between them and the corresponding arc of the boundary circle.

```
\ifnum\tqft@val{incoming boundary components}>1\relax
885
        \foreach \k in {2,...,\tqft@val{incoming boundary components}} {
886
          \edef\tqft@temp{\noexpand\pgfutil@in@{,\k,}{,\tqft@val{skip incoming boundary componer
887
          \tqft@temp
888
          \ifpgfutil@in@
889
          \xdef\tqft@cibdrylist{\tqft@cibdrylist,\k}
890
          \else
891
892
          \xdef\tqft@ibdrylist{\tqft@ibdrylist,\k}
893
894
        }
895
        \ifx\tqft@ibdrylist\pgfutil@gobble
896
        \else
        \foreach \k [
897
          remember=\k as \kmo (initially 1),
898
            evaluate=\k as \xpos using (\k-1)*\tqft@val{boundary} separation} -
899
    \tqft@val{circle x radius},
900
        ] in \tqft@ibdrylist {
          \pgfmathsetmacro\xppos{(\kmo - 1)*\tqft@val{boundary separation} + \tqft@val{circle x
901
          \pgfmathsetmacro\cpos{(\xpos + \xppos)/2}
902
Add the curve and the arc.
903
            \xdef\tqft@fullpath{%
904
              \tqft@fullpath
                .. controls +(0,-\tqft@val{cobordism height}/3) and +(0,-\tqft@val{cobordism height}
905
          }%
906
But for the edge path, just add the curve to the list.
907
            \xdef\tqft@blist{%
908
              \tqft@blist,incoming boundary \k/incoming/{%
          (\xppos pt,0) .. controls +(0,-)tqft@val{cobordism height}/3) and +(0,-)
909
    \tqft@val{cobordism height}/3) .. (\xpos pt,0)}%
910
We add a coordinate at the midpoint of the curve.
911
          \xdef\tqft@clist{%
            \tqft@clist,-between incoming \kmo\space and \k/{(\cpos pt,-\tqft@val{cobordism heig
912
913
And add the centre to the list for available shifts.
          \xdef\tqft@alist{%
914
915
            \tqft@alist,-incoming boundary \k/{(\kmo * \tqft@val{boundary separation},0)}%
916
        }%
917
        \fi
918
          \fi
919
```

We're at the edge of the last incoming boundary component. What we do now depends on whether or not there are outgoing boundary components.

```
\verb| 920 | \texttt{ \frum\tqft@val{outgoing boundary components}}>0\\ | \\
```

There are.

We start by adding a curve from the end of the last incoming to the last outgoing component to the full path,

```
921 \pgfmathsetmacro\xppos{%
```

```
+ \tqft@val{offset}) * \tqft@val{boundary separation}
923
          + \tqft@outgoing@dir * \tqft@val{circle x radius}}%
924
          925
          \pgfmathsetmacro\tqft@ht{1/3 + 2/3*\tqft@ht/(\tqft@ht + 1)}%
926
927
          \xdef\tqft@fullpath{%
928
            \tqft@fullpath
            .. controls +(0,-\tqft@ht*\tqft@val{cobordism height}) and +(0,\tqft@ht*\tqft@val{co
    \tqft@val{cobordism height})
         }%
930
and the edge path.
          \xdef\tqft@blist{%
931
            \tqft@blist,between last incoming and last outgoing/incoming and outgoing/{%
932
            (\tqft@val{incoming boundary components} * \tqft@val{boundary separation} + \tqft@va
933
            .. controls +(0,-\tqft@ht*\tqft@val{cobordism height}) and +(0,\tqft@ht*\tqft@val{co
934
    \tqft@val{cobordism height})}%
         ጉ%
935
In addition, we add a coordinate at the midpoint.
          \pgfmathsetmacro\xppos{(\xppos + (\tqft@val{incoming boundary components} -
         \tqft@val{boundary separation} +\tqft@val{circle x radius})/2}%
937
          \xdef\tqft@clist{%
            \tqft@clist,-between last incoming and last outgoing/{(\xppos pt,-
938
    \tqft@val{cobordism height}/2)}%
          }%
939
          \else
940
There aren't any outgoing boundary components so we loop back to the start. We
adjust the height of the control points to take into account the overall width.
          \pgfmathsetmacro\tqft@ht{1/3 + 2/3*(\tqft@val{incoming boundary components} - 1)/\tqft
941
          \xdef\tqft@fullpath{%
942
            \tqft@fullpath
943
            .. controls +(0,-)tqft@ht*\dotqft@val{cobordism height}) and +(0,-)tqft@ht*\dotqft@val{cobordism height})
944
    \tqft@ht*\tqft@val{cobordism height}) .. (-\tqft@val{circle x radius},0)
945
          }%
Same for the edge path.
          \xdef\tqft@blist{%
946
947
            \tqft@blist,between first and last incoming/incoming and outgoing/{%
            (\tqft@val{incoming boundary components} * \tqft@val{boundary separation} + \tqft@va
948
            .. controls +(0,-\tqft@ht*\tqft@val{cobordism height}) and +(0,-\tqft@ht*\tqft@val{cobordism height})
949
    \tqft@ht*\tqft@val{cobordism height}) .. (-\tqft@val{circle x radius},0)}
950
          ጉ%
Add a coordinate at the midpoint.
          \pgfmathsetmacro\xppos{(\tqft@val{incoming boundary components} -1) * \tqft@val{bounda
951
952
          \xdef\tqft@clist{%
953
            \tqft@clist,-between first and last incoming/{(\xppos pt,-\tqft@ht*\tqft@val{cobordi
   between first incoming and last incoming/{(\xppos pt,-\tqft@th*\tqft@val{cobordism height}*3
954
          \fi
955
          \else
956
```

(\tqft@outgoing@end * (\tqft@val{outgoing boundary components} -1)

922

There weren't any incoming boundary components, so we test to see if there were any outgoing ones and move to the start of them.

```
\ifnum\tqft@val{outgoing boundary components}>0\relax
            \pgfmathsetmacro\xppos{( \tqft@outgoing@end * (\tqft@val{outgoing boundary component
958
   1)+\tqft@val{offset}) * \tqft@val{boundary separation} + \tqft@outgoing@dir * \tqft@val{circ
Add a move to the full path,
          \xdef\tqft@fullpath{%
959
            \tqft@fullpath
960
            (\xppos pt, -\tqft@val{cobordism height})
961
962
          }%
963
          \fi
964
          \fi
We're done with the incoming boundary components, now we're set up for the
outgoing ones. However we got there, if we have outgoing boundary components
then we're now located at the start of them, although we might be counting
backwards.
965
        \ifnum\tqft@val{outgoing boundary components}>0\relax
966
        \pgfmathsetmacro\xppos{%
967
          ( \tqft@outgoing@end * (\tqft@val{outgoing boundary components} -1)
968
          + \tqft@val{offset}) * \tqft@val{boundary separation}
969
          - \tqft@outgoing@dir * \tqft@val{circle x radius}}%
Draw the arc for the first (well, last actually) boundary component.
          \xdef\tqft@fullpath{%
970
971
            \tqft@fullpath
972
            arc[end angle=\pgf@tqft@upper180, start angle=0, x radius=\tqft@outgoing@dir * \tqft
973
          }%
And add the centre to the list for available shifts.
974
          \xdef\tqft@alist{%
975
            \tqft@alist,-outgoing boundary \tqft@val{outgoing boundary components}/{(\xppos pt +
    \tqft@val{cobordism height})},-outgoing boundary/{(\tqft@val{offset}*\tqft@val{boundary sepa
    \tqft@val{cobordism height})}%
976
          }%
Do we have more than one boundary component?
          \ifnum\tqft@val{outgoing boundary components}>1\relax
977
Yes, so add a curve and arc for each.
        \foreach \k [evaluate=\k as \ok using int(\tqft@outgoing@end * (\tqft@val{outgoing bound
978
          \edef\tqft@temp{\noexpand\pgfutil@in@{,\ok,}{,\tqft@val{skip outgoing boundary compone
979
980
          \tqft@temp
981
          \ifpgfutil@in@
          \xdef\tqft@cobdrylist{\tqft@cobdrylist,\k}
982
983
          \xdef\tqft@obdrylist{\tqft@obdrylist,\k}
984
985
986
        \ifx\tqft@obdrylist\pgfutil@gobble
987
        \else
988
        \foreach \k [
989
          remember=\k as \kmo (initially 1),
990
991
            evaluate=\k as \xpos using ( \tqft@outgoing@end * (\tqft@val{outgoing boundary compo
992
        ] in \tqft@obdrylist {
          \pgfmathsetmacro\xppos{(\tqft@outgoing@end * (\tqft@val{outgoing boundary components}
```

993

994

\pgfmathsetmacro\cpos{(\xpos + \xppos)/2}

```
\pgfmathsetmacro\nk{int(\tqft@val{outgoing boundary components} - \k + 1)}
995
            \pgfmathsetmacro\nkpo{int(\tqft@val{outgoing boundary components} - \kmo + 1)}
996
Both are added to the full path.
            \xdef\tqft@fullpath{%
997
              \tqft@fullpath
998
               .. controls +(0,\tqft@val{cobordism height}/3) and +(0,\tqft@val{cobordism height}
999
    \tqft@val{cobordism height}) arc[end angle=\pgf@tqft@upper180, start angle=0, x radius=\tqft
1000
         ጉ%
Just the arc for the edge paths.
            \xdef\tqft@blist{%
1001
              \tqft@blist,between outgoing \nk\space and \nkpo/outgoing/{%
1002
     (\xppos pt,-\tqft@val{cobordism height})
1003
               .. controls +(0,\tqft@val{cobordism height}/3) and +(0,\tqft@val{cobordism height
1004
    \tqft@val{cobordism height}) ++(-2*\tqft@val{circle x radius},0)}%
1005
And a coordinate at the midpoint.
          \xdef\tqft@clist{%
1006
1007
            \tqft@clist,-between outgoing \nk\space and \nkpo/{(\cpos pt,-3*\tqft@val{cobordism
1008
         ጉ%
And add the centre to the list for available shifts.
          \xdef\tqft@alist{%
1009
            \tqft@alist,-outgoing boundary \nk/{(\xpos pt - \tqft@val{circle x radius},-
1010
    \tqft@val{cobordism height})}%
         }%
1011
1012
         }%
1013
        \fi
Now we're at the end of the outgoing boundary components (well, the start ac-
tually). What we do now depends on whether or not there are any incoming
boundary components.
1015
          \ifnum\tqft@val{incoming boundary components}>0\relax
There are, so we draw the path back up.
1016
          1017
          \xdef\tqft@fullpath{%
1018
            \tqft@fullpath
            .. controls +(0,\tqft@ht*\tqft@val{cobordism height}) and +(0,-\tqft@ht*\tqft@val{co
1019
    \tqft@val{circle x radius},0)
1020
         }%
And the edge path does the same.
1021
          \xdef\tqft@blist{%
1022
            \tqft@blist,between first incoming and first outgoing/incoming and outgoing/{%
1023
        ({ ((1 - \tqft@outgoing@end) * (\tqft@val{outgoing boundary components} - 1) + \tqft@va
    \tqft@val{cobordism height})
            .. controls +(0,\tqft@ht*\tqft@val{cobordism height}) and +(0,-\tqft@ht*\tqft@val{cobordism height})
1024
    \tqft@val{circle x radius},0)}%
         }%
1025
Add a coordinate at the midpoint.
         \xdef\tqft@clist{%
1026
```

```
\tqft@clist,-between first incoming and first outgoing/{({ ( (1 - \tqft@outgoing@end
1027
    \tqft@val{cobordism height}/2)}%
1028
          ጉ%
          \else
1029
No incoming boundary components so loop back to the other end of the outgoing
boundary components.
          \pgfmathsetmacro\xppos{(\tqft@val{outgoing boundary components} -1+\tqft@val{offset})
1030
          \pgfmathsetmacro\tqft@ht{1/3 + 2/3*(\tqft@val{outgoing boundary components} - 1)/\tqft
1031
Full path.
1032
          \xdef\tqft@fullpath{%
1033
            \tqft@fullpath
1034
            .. controls +(0,\tqft@ht*\tqft@val{cobordism height}) and +(0,\tqft@ht*\tqft@val{cob
    \tqft@val{cobordism height})
1035
          }%
Edge path.
1036
          \xdef\tqft@blist{%
1037
            \tqft@blist,between first and last outgoing/incoming and outgoing/{%
        (\tqft@val{offset} * \tqft@val{boundary separation} - \tqft@val{circle x radius},-
    \tqft@val{cobordism height})
            .. controls +(0,\tqft@ht*\tqft@val{cobordism height}) and +(0,\tqft@ht*\tqft@val{cobordism height})
1039
    \tqft@val{cobordism height})}%
          ጉ%
1040
Add a coordinate at the midpoint.
          \pgfmathsetmacro\xppos{(\tqft@val{outgoing boundary components}/2 + \tqft@val{offset}
    1/2) * \tqft@val{boundary separation}}%
          \pgfmathsetmacro\tqft@ht{1 -\tqft@ht*3/4}%
1042
          \xdef\tqft@clist{%
1043
            \tqft@clist,-between first and last outgoing/{(\xppos pt,-\tqft@ht*\tqft@val{cobordi
1044
    between first outgoing and last outgoing/{(\xppos pt,-\tqft@th*\tqft@val{cobordism height}))
1045
          }%
1046
          \fi
1047
          \fi
Now we define the clip path for the genus holes. We start with a big rectangle
that ought to be big enough to contain the whole shape. We start with the top
left corner.
1048
          \pgfmathsetmacro\xpos{%
1049
            (
            \tqft@val{outgoing boundary components} > 0 ?
1050
1051
            \tqft@val{incoming boundary components} > 0 ?
1052
            min(0,\tqft@val{offset}) : \tqft@val{offset}
1053
1054
            ): 0
1055
            )
1056
            *\tqft@val{boundary separation} - 2*\tqft@val{circle x radius}}%
          \xdef\tqft@gclip{(\xpos pt,2*\tqft@val{circle y radius}) rectangle }%
1057
Now the bottom right.
1058
          \pgfmathsetmacro\xpos{%
1059
1060
            \tqft@val{outgoing boundary components} > 0 ?
1061
```

```
\tqft@val{incoming boundary components} > 0 ?
1062
            max(\tqft@val{incoming boundary components},\tqft@val{outgoing boundary components}
1063
            ) : \tqft@val{incoming boundary components}
1064
1065
            )-1)
            *\tqft@val{boundary separation} + 2*\tqft@val{circle x radius}}%
1066
Together, these make a rectangle.
1067
          \xdef\tqft@gclip{\tqft@gclip (\xpos pt,-\tqft@val{cobordism height} - 2*\tqft@val{circ
Are there any holes?
1068
          \ifnum\tqft@val{genus}>0\relax
Yes, so first we need to figure out where to place them. We work out the left-hand
edge of the cobordism.
1069
          \pgfmathsetmacro\xpos{%
1070
1071
            \tqft@val{outgoing boundary components} > 0 ?
1072
            \tqft@val{incoming boundary components} > 0 ?
1073
            \tqft@val{offset}/2 : \tqft@val{offset}
1074
            ) : 0
1075
1076
            *\tqft@val{boundary separation} - \tqft@val{circle x radius}}%
1077
Work out the height that the holes should be punched at.
          \pgfmathsetmacro\ypos{%
1078
1079
            (
            \tqft@val{outgoing boundary components} > 0 ?
1080
1081
            \tqft@val{incoming boundary components} > 0 ?
1082
            -\tqft@val{cobordism height}/2 : -1 + \tqft@val{cobordism height}/3
1083
            ) : - \tqft@val{cobordism height}/3
1084
            ) }%
1085
Start our clip path at this point
          \xdef\tqft@gclip{%
1086
1087
            \tqft@gclip
1088
             (\xpos pt,\ypos pt)
1089
          }%
Now work out the width of the cobordism, in units of circle half-widths. This may
not be very accurate if there aren't any boundary components of a given type.
1090
          \pgfmathsetmacro\gsize{%
1091
            ((
            \tqft@val{outgoing boundary components} > 0 ?
1092
1093
1094
            \tqft@val{incoming boundary components} > 0 ?
            (\tqft@val{incoming boundary components} + \tqft@val{outgoing boundary components})/
1095
1096
            ) : \tqft@val{incoming boundary components}
            )-1)
1097
            \verb| * tqft@val{boundary separation}/ tqft@val{circle x radius} + 2} %
1098
```

Each hole should take up three half-widths, but we want a little extra on the edges so the total number of half-widths we want is 3g+1. Do we need to scale down the holes (we never scale up)? If so, \gscale holds the overall scale factor and \gxscale and gyscale are the resulting horizontal and vertical measurements. The baseline is the size of the boundary circles.

```
\pgfmathsetmacro\gxscale{\tqft@val{circle x radius}*\gscale}%
1101
Each hole should take up 2 half widths, modulo scaling, so the total width used
by the holes is 2gs leaving w-2gs left for the gaps which is divided in to g+1
          \pgfmathsetmacro\gsep{((\gsize - 2*\tqft@val{genus}*\gscale)/(\tqft@val{genus} + 1)*\t
1102
We shift in by half of one unit of excess separation.
          \xdef\tqft@gclip{%
1103
1104
            \tqft@gclip
1105
            ++(\gsep/2 pt,0)
1106
Some useful quantities.
1107
          \pgfmathsetmacro\omrstwo{1 - 1/sqrt(2)}%
1108
          \pgfmathsetmacro\sqrtwo{sqrt(2)}%
Now we iterate over the holes.
          \foreach[
1109
            evaluate=\k as \kmo using int(2 * \k-1)
1110
          ] \k in {1,...,\tqft@val{genus}} {
1111
For the clipping path, we just want the bare hole.
1112
            \xdef\tqft@gclip{%
1113
              \tqft@gclip
Move in by half an excess separation unit and move to the left-hand extent of the
hole.
              ++(\gsep/2 pt + \omrstwo*\gxscale pt,0)
1114
Now curve up over the hole,
1115
              .. controls +(\gxscale*\sqrtwo/3 pt,4/3*\gyscale pt) and +(-\gxscale*\sqrtwo/3 pt,
1116
              .. ++(\sqrtwo*\gxscale pt,0)
and return on the underside.
              .. controls +(-\gxscale*\sqrtwo/3 pt,-4/3*\gyscale pt) and +(\gxscale*\sqrtwo/3 pt
    4/3*\gyscale pt)
              .. ++(-\sqrtwo*\gxscale pt,0)
1118
Lastly, move to the right-hand edge of the space taken up by this hole.
              ++(2*\gxscale pt -\omrstwo*\gxscale pt + \gsep/2 pt,0)
1119
1120
For the genus path we want to add the little "tails" which means that the two
curves are different, and we need to take into acount the view from direction.
            \xdef\tqft@glist{%
1121
1122
              \tqft@glist,%
                hole \k/lower/{%
1123
Move to the starting point of the smaller curve and add that.
                (\xpos pt + \k * \gsep pt + \kmo * \gxscale pt + \gxscale pt -
    \omrstwo*\gxscale pt,\ypos pt)
1125
              .. controls +(-\gxscale pt*\sqrtwo/3,\pgf@tqft@upper4/3*\gyscale pt) and +(\gxscal
1126
              .. ++(-\sqrt{\sqrt{2}}),%
1127 % Move to the left-hand corner of the path, with the upper or lower chosen by the \verb+view
              hole \k/upper/{(\xpos pt + \k * \gsep pt + \kmo * \gxscale pt - \gxscale pt,\ypos
```

 $\pgfmathsetmacro\gscale\{min(1,\gsize/(3*\tqft@val\{genus\}+1))\}\%$

\pgfmathsetmacro\gyscale{\tqft@val{circle y radius}*\gscale*.707}%

1099

```
Add the larger of the two curves.
                                        .. controls +(\gxscale pt*2/3,\pgf@tqft@lower8/3*\gyscale pt) and +(-
            \gxscale pt*2/3,\pgf@tqft@lower8/3*\gyscale pt)
1130
                                        .. ++(2*\gxscale pt,0)}%
1131
Add a coordinate at the centre of the hole.
1132
                                  \xdef\tqft@clist{%
                                        \tqft@clist,-hole \k/{(\xpos pt + \k * \gsep pt + \kmo * \gxscale pt,\ypos pt)}%
1133
1134
                                  ጉ%
1135
                            }%
1136
                             \fi
Now we start to lay out the cobordism Were we given a shift? If so, shift.
1137 \neq 0
1138 \edef\tqft@anchor{\tqft@val{anchor}}%
\label{limiting lambda} $$139 \exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp{\text{liming}e}\exp
1140 \ifpgfutil@in@
1141 \expandafter\tqft@split\tqft@anchor\relax
1142 \else
1143 \edef\tqft@anchor{-\tqft@val{anchor}}%
1144 \xdef\tqft@alist{\tqft@clist,\tqft@alist}%
1145 \foreach \anchor/\coord in \tqft@alist
1146 {
                 \ifx\anchor\tqft@anchor\relax
1147
                \global\let\tqft@shift\coord
1148
1149 \fi
1150 }%
1151 \fi
1152 \tikz@scan@one@point\pgfutil@firstofone\tqft@shift\relax
1153 \begin{scope}[shift={(-\pgf@x,-\pgf@y)}]
At each incoming boundary component we place an elliptical node of the right
size.
1154 \ifnum\tqft@val{incoming boundary components}>0\relax
1155 \ifx\tqft@ibdrylist\pgfutil@gobble
1156 \xdef\tqft@ibdrylist{1}
1157 \else
1158 \xdef\tqft@ibdrylist{1,\tqft@ibdrylist}
1159 \fi
1160
                             \foreach[evaluate=\k as \xpos using (\k-1)*\tqft@val{boundary separation}] \k in \tqft
1161
1162
                      transform shape,
                                       node contents={},
1163
                                        ellipse,
1164
                                        inner sep=Opt,
1165
                                        outer sep=0pt,
1166
1167
                                       minimum width=2*\tqft@val{circle x radius},
                                       minimum height=2*\tqft@val{circle y radius},
1168
1169
                                        at=\{(xpos pt,0)\},\
                                       name=-incoming boundary \k,
1170
1171
                                        /tikz/tqft/every boundary component/.try,
1172
                                       /tikz/tqft/every incoming boundary component/.try,
1173
                                        /tikz/tqft/incoming boundary component \k/.try
```

];

```
ጉ%
1175
1176 \ifx\tqft@cibdrylist\pgfutil@gobble
1177 \else
         1178
1179
     \node[
       transform shape,
1180
            node contents={},
1181
             ellipse,
1182
1183
             inner sep=0pt,
1184
             outer sep=0pt,
             minimum width=2*\tqft@val{circle x radius},
1185
             minimum height=2*\tqft@val{circle y radius},
1186
             at=\{(xpos pt,0)\},\
1187
            name=-incoming boundary \k,
1188
             /tikz/tqft/every skipped boundary component/.try,
1189
             /tikz/tqft/every skipped incoming boundary component/.try,
1190
             /tikz/tqft/skipped incoming boundary component \k/.try,
1191
1192
           ];
1193 }%
1194 \fi
Add an alias for the first.
         \path node also[pic alias=-incoming boundary] (-incoming boundary 1);
1196
Same for the outgoing boundary components.
         \ifnum\tqft@val{outgoing boundary components}>0\relax
1198 \ifx\tqft@obdrylist\pgfutil@gobble
1199 \xdef\tqft@obdrylist{1}
1200 \else
1201 \xdef\tqft@obdrylist{1,\tqft@obdrylist}
1202 \fi
1203 \foreach \k [evaluate=\k as \ok using int(\tqft@outgoing@end * (\tqft@val{outgoing boundary
     \xdef\tqft@robdrylist{\tqft@robdrylist,\ok}
1204
1205 }
1206
         \foreach[
           1207
1208
         ] \k in \tqft@robdrylist {
1209
     \node[
       transform shape,
1210
1211
            node contents={},
1212
             ellipse,
1213
            inner sep=0pt,
             outer sep=0pt,
1214
             minimum width=2*\tqft@val{circle x radius},
1215
             minimum height=2*\tqft@val{circle y radius},
1216
1217
             at={(\xpos pt,-\tqft@val{cobordism height})},
1218
             name=-outgoing boundary \k,
             /tikz/tqft/every boundary component/.try,
1219
1220
             /tikz/tqft/every outgoing boundary component/.try,
1221
             /tikz/tqft/outgoing boundary component \k/.try
1222
           ];
1223 }%
1224 \ifx\tqft@cobdrylist\pgfutil@gobble
1225 \else
```

```
1226 \foreach \k[evaluate=\k as \ok using int(\tqft@outgoing@end * (\tqft@val{outgoing boundary of tqft@val{outgoing boutgoing boundary of tqft@val{outgoing boutgoing boundary of tqft@va
1227 in \tqft@cobdrylist {
            \xdef\tqft@rcobdrylist{\tqft@rcobdrylist,\ok}
1228
1229 }
1230
                        evaluate=\k as \xpos using (\k-1+\tqft@val{offset})*\tqft@val{boundary separation}
1231
                    ] \k in \tqft@rcobdrylist {
1232
            \node[
1233
1234
                transform shape,
1235
                            node contents={},
1236
                            ellipse,
                            inner sep=Opt,
1237
                            outer sep=0pt,
1238
                            minimum width=2*\tqft@val{circle x radius},
1239
                            minimum height=2*\tqft@val{circle y radius},
1240
                            at={(\xpos pt,-\tqft@val{cobordism height})},
1241
1242
                            name=-outgoing boundary \k,
                            /tikz/tqft/every skipped boundary component/.try,
1243
1244
                            /tikz/tqft/every skipped outgoing boundary component/.try,
1245
                            /tikz/tqft/skipped outgoing boundary component \k/.try
1246
                        ];
                    }%
1247
1248 \fi
Add an alias for the first.
                    \path node also[pic alias=-outgoing boundary] (-outgoing boundary 1);
1249
1250
Now we draw the lower paths of the incoming boundary components.
                    \ifnum\tqft@val{incoming boundary components}>0\relax
1251
                    \foreach[evaluate=\k as \xpos using (\k-1)*\tqft@val{boundary separation}] \k in \tqft
1252
1253
                            /tikz/tqft/every lower boundary component/.try,
1254
1255
                            /tikz/tqft/every incoming lower boundary component/.try,
                            /tikz/tqft/incoming lower boundary component \k/.try
1256
1257
                        ] (\xpos pt - \tqft@val{circle x radius},0) arc[start angle=\pgf@tqft@lower180,end a
                    }%
1258
                    \fi
1259
Same for the outgoing boundary components.
1260
                    \ifnum\tqft@val{outgoing boundary components}>0\relax
1261
                    \foreach[
                        evaluate=\k as \xpos using (\k-1+\tqft@val{offset})*\tqft@val{boundary
1262
                    ] \k in \tqft@robdrylist {
1263
1264
                        \path[
1265
                            /tikz/tqft/every lower boundary component/.try,
1266
                            /tikz/tqft/every outgoing lower boundary component/.try,
1267
                            /tikz/tqft/outgoing lower boundary component \k/.try
                        ] (\xpos pt - \tqft@val{circle x radius},-\tqft@val{cobordism height}) arc[start ang
1268
                        }%
1269
1270
Full outer path, clipped against the genus holes in case it is filled.
                    \begin{scope}
1271
                    \path[overlay,clip] \tqft@gclip;
1272
1273
                    \path[
```

```
1274 /tikz/tqft/cobordism/.try,
1275 pic actions,
1276 /tikz/tqft/cobordism outer path/.try,
1277 ] \tqft@fullpath;
1278 \end{scope}
```

Now we draw the genus path, outside the clip. We view this as part of the full cobordism path so try to apply the same style as for the full path, but if that is filled then we turn the fill off. It can be turned back on again using the styles cobordism edge or genus style. We also apply the cobordism edge style as it could be thought of as part of the non-boundary edge. Finally, it has its own style to enable overrides if the other two get confused.

```
1279 \ifx\tqft@glist\pgfutil@gobble
1280 \else
1281 \foreach \tqft@gstyle/\tqft@gside/\tqft@gpath in \tqft@glist {
1282
          \path[
1283
            /tikz/tqft/cobordism/.try,
1284
            pic actions,
1285
            fill=none,
1286
            shade=none,
1287
            /tikz/tqft/cobordism edge/.try,
1288
            /tikz/tqft/genus style/.try,
1289
            /tikz/tqft/genus \tqft@gside/.try,
1290
            /tikz/tqft/\tqft@gstyle/.try,
1291
            /tikz/tqft/\tqft@gstyle\space\tqft@gside/.try,
          ] \tqft@gpath;
1292
1293 }
1294 \fi
Now we redraw the non-boundary paths.
1295 \ifx\tqft@blist\pgfutil@gobble
1296 \ensuremath{\setminus} \texttt{else}
1298
          \path[
1299
            /tikz/tqft/cobordism edge/.try,
1300
            /tikz/tqft/cobordism outer edge/.try,
            /tikz/tqft/between \tqft@btype/.try,
1301
            /tikz/tqft/\tqft@bstyle/.try,
1302
1303
          ] \tqft@bpath;
1304 }
1305 \fi
There were various coordinates that we wanted to define but couldn't. Here, we
put those in place.
1306
          \ifx\tqft@clist\pgfutil@gobble
1307
          \foreach \name/\coord in \tqft@clist {
1308
1309
            \path \coord node[coordinate, node contents={}, name=\name];
```

The last task is to draw the upper paths of the boundary components. First, incoming.

1310

}

```
1312 \ifnum\tqft@val{incoming boundary components}>0\relax
1313 \foreach[evaluate=\k as \xpos using (\k-1)*\tqft@val{boundary separation}] \k in \tqft
```

```
\path[
1314
                                                \verb|/tikz/tqft/every upper boundary component/.try|,
1315
                                                 /tikz/tqft/every incoming upper boundary component/.try,
1316
                                                 /tikz/tqft/incoming upper boundary component \k/.try
1317
                                         ] (\xpos pt - \tqft@val{circle x radius},0) arc[start angle=\pgf@tqft@upper180,end and arc [start angle=\pgf@tqft@upper180,end arc [start angle=\pgf@tqft@to@toper180,end arc [start angle=\pgf@tqft@toper180,end arc [start angle=\pgf@toper180,end arc [start angle=\pgf@top
1318
1319
1320
                                  \fi
Next, outgoing.
1321
                                  1322
                                         evaluate = \  \  \  (\k-1+\tqft@val{offset})* \tqft@val{boundary}
1323
1324
                                  ] \k in \tqft@robdrylist {
1325
1326
                                                 /tikz/tqft/every upper boundary component/.try,
                                                 /tikz/tqft/every outgoing upper boundary component/.try,
1327
                                                /tikz/tqft/outgoing upper boundary component \k/.try
1328
                                         ] (\xpos pt - \tqft@val{circle x radius},-\tqft@val{cobordism height}) arc[start ang
1329
                                  }
1330
                                  \fi
1331
1332 \end{scope}
We're done! Phew.
                }
1333
1334 }
```