The braids package: codebase

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Introduction 1

This is a package for drawing braid diagrams using PGF/TikZ. Its inspiration was a question and answer on the website http://tex.stackexchange.com.

$\mathbf{2}$ History

- v1.0 First public release.
- v1.1 Added ability to configure the gap size, the control points, and the "nudge". Added ability to add labels to strands between crossings.
- v2 Reimplemented as TikZ library rather than a standalone package.

3 Implementation

Issue a notice that this is a depreciated version of the braids package.

- \ProvidesPackage{braids}[2011/10/18 v1.1 Tikz/PGF commands for drawing braid diagrams (depre \newif\if@braids@warning@
- \@braids@warning@true
- 5 \DeclareOption{nowarning}{%

\NeedsTeXFormat{LaTeX2e}

- \@braids@warning@false
- 7 }
- 9 \ProcessOptions
- 11 \if@braids@warning@ 12 \PackageWarning{braids}{%
- This package is frozen at v1.1 from 2011/10/18 and has been reimplemented as a TikZ librar
- 14 }%

\ge@addto@macro

This is an expanded version of \g@addto@macro. Namely, it adds the expansion of the second argument to the first.

- 16 $\lceil \log \leq \frac{16}{2000}$
- \begingroup
- $\verb|\toks@\expandafter\expandafter| expandafter {\expandafter#1#2} % if the property of the pr$

```
19 \xdef#1{\the\toks@}%
```

20 \endgroup}

(End of definition for \ge@addto@macro.)

\braid This is the user command. We start a group to ensure that all our assignments are local, and then call our initialisation code. The optional argument is for any keys to be set.

```
21 \newcommand{\braid}[1][]{%
```

- 22 \begingroup
- 23 \braid@start{#1}}

(End of definition for \braid. This function is documented on page ??.)

\braid@process

This is the token swallower. This takes the next token on the braid specification and passes it to the handler command (in the macro \braid@token) which decides what to do next. (Incidentally, the code here is heavily influenced by TikZ. That's probably not very surprising.)

```
24 \def\braid@process{%
```

- 25 \afterassignment\braid@handle\let\braid@token=%
- 26 }

 $(End\ of\ definition\ for\ \verb+\braid@process.)$

\braid@process@start

This is a variant of \braid@process which is used at the start where we might have a few extra bits and pieces before the braid itself starts. Specifically, we test for the at and (name) possibilities.

- 27 \def\braid@process@start{%
- 28 \afterassignment\braid@handle@start\let\braid@token=%
- 29 }

(End of definition for \braid@process@start.)

\braid@handle@start

This is the handler in use at the start. It looks for the tokens a or (which (might) signal the start of an at (coordinate) or (name). If we get anything else (modulo spaces) we decide that we've reached the end of the initialisation stuff and it is time to get started on the braid itself.

- 30 \def\braid@handle@start{%
- let\braid@next=\braid@handle
- 32 \ifx\braid@token a

We got an a so we might have an at (coordinate)

- 33 \let\braid@next=\braid@maybe@locate
- 34 **\els**e
- 35 \ifx\braid@token(%)

We got an (so we have a name

- 36 \iffalse)\fi %Indentation hack!
- 37 \let\braid@next=\braid@assign@name
- 38 \else
- 39 \ifx\braid@token\@sptoken

Space; boring, redo from start

- 40 \let\braid@next=\braid@process@start
- 41 \fi
- 42 \fi
- 43 \fi
- 44 \braid@next%
- 45 }

(End of definition for \braid@handle@start.)

\braid@handle

This is the main handler for parsing the braid word. It decides what action to take depending on what the token is. We have to be a bit careful with catcodes, some packages set; and I to be active. We should probably also be careful with ^ and _.

- 46 \let\braid@semicolon=;
- 47 \let\braid@bar=|
- 48 \def\braid@handle{%
- 49 \let\braid@next=\braid@process

Start by checking our catcodes to see what we should check against

- 50 \ifnum\the\catcode'\;=\active
- 51 \expandafter\let\expandafter\braid@semicolon\tikz@activesemicolon
- 52 **\fi**
- 53 \ifnum\the\catcode'\|=\active
- 54 \expandafter\let\expandafter\braid@bar\tikz@activebar
- 55 \f:
- 56 \ifx\braid@token\braid@semicolon

Semicolon, means that we're done reading our braid. It's time to render it.

- 57 \let\braid@next=\braid@render
- 58 \else
- 59 \ifx\braid@token^

Superscript character, the next token tells us whether it's an over-crossing or an under-crossing.

- 60 \let\braid@next=\braid@sup
- 61 \else
- 62 \ifx\braid@token_

Subscript character, the next token tells us which strands cross.

- 63 \let\braid@next=\braid@sub
- 4 \else
- 65 \ifx\braid@token-

Hyphen, this is so that we can have more than one crossing on the same level.

- 66 \braid@increase@levelfalse
- 67 \else
- 68 \ifx\braid@token1%

 $1\!\!:$ this means the "identity" crossing, so no crossing here. Increase the level, unless overriden, and add to the label.

- 69 \ifbraid@increase@level
- 70 \stepcounter{braid@level}
- 71 \fi
- 72 \braid@increase@leveltrue
- 73 \ge@addto@macro\braid@label{\braid@token}%
- 74 \else
- 75 \ifx\braid@token[%

Open bracket, this means we have some more options to process.

- \let\braid@next=\braid@process@options
- \else
- \ifx\braid@token\braid@bar 78

Bar, this tells us that we want a "floor" at this point.

- $\verb|\def| braid@tmp{,\expandafter\the\value{braid@level}}| % $$ $ \expandafter\the\value{braid@level}| % $$ $$ $ \expandafter\the\value{braid@level}| % $$ $$ $\expandafter\the\value{braid@level}| % $$ $$ $\expandafter\the\value{braid@level}| % $$ $$ $\expandafter\the\value{braid@level}| % $$\expandafter\the\value{braid@level}| % $$ $\expandafter\the\value{braid@level}| % $$\expandafter\the\value{braid@level}| %$
- \ge@addto@macro\braid@floors\braid@tmp% 80
- \else 81
- \ifx\braid@token\bgroup 82

Begin group, which we reinterpret as begining a scope.

- \braid@beginscope
- \else
- \ifx\braid@token\egroup 85

End group, which ends the scope

- \braid@endscope
- 87 \else
- \ifx\braid@token\braid@olabel@strand 88
 - \let\braid@next=\braid@olabel@strand
- 90

89

- \ifx\braid@token\braid@clabel@strand 91
- \let\braid@next=\braid@clabel@strand 92
- \else 93

Otherwise, we add the token to the braid label.

- \ge@addto@macro\braid@label{\braid@token}%
- 95
- \fi 96
- \fi
- \fi
- \fi 100 \fi
- \fi
- \fi 102
- \fi 103 \fi
- 104
- \fi 105
- \braid@next% 106

107 }

(End of definition for \braid@handle.)

\braid@maybe@locate

If we got an a token in the \braid@handle@start then it might mean we're looking at at (coordinate) or it might mean that the user has decided to use a as the braid parameter. So we examine the next token for a t.

```
108 \def\braid@maybe@locate{%
```

110 }

(End of definition for \braid@maybe@locate.)

```
\braid@@maybe@locate This is where we test for t and act appropriately.
                          111 \def\braid@@maybe@locate{%
                               \let\braid@next=\braid@handle
                          112
                          113
                               \ifx\braid@token t
                          114
                                \let\braid@next=\braid@find@location
                          115
                               \fi
                          116
                               \braid@next%
                          117 }
                         (End of definition for \braid@@maybe@locate.)
 \braid@find@location This macro starts us looking for a coordinate.
                          118 \def\braid@find@location{%
                               \afterassignment\braid@@find@location\let\braid@token=%
                          120 }
                         (End of definition for \braid@find@location.)
                        This is the test for the start of a coordinate. If we get a (that means we've reached the
\braid@@find@location
                        coordinate. A space means "carry on". Anything else is a (non-fatal) error.
                          121 \def\braid@@find@location{%
                          122
                               \let\braid@next=\braid@location@error
                          123
                               \ifx\braid@token(%)
                                \let\braid@next=\braid@locate
                          124
                               \else
                          125
                               \ifx\braid@token\@sptoken
                                \let\braid@next=\braid@find@location
                          127
                               \fi
                          128
                               \fi
                          129
                          130
                               \braid@next%
                          131 }
                        (End of definition for \braid@Ofind@location.)
\braid@location@error This is our error message for not getting a location.
                          132 \def\braid@location@error{%
                               \PackageWarning{braids}{Could not figure out location for braid}%
                               \braid@process@start%
                          134
                         (End of definition for \braid@location@error.)
        \braid@locate If we reached a ( when looking for a coordinate, everything up to the next ) is that
                        coordinate. Then we parse the coordinate and call the relocation macro.
                          136 \def\braid@locate#1){%
                               \tikz@scan@one@point\braid@relocate(#1)%
                          138 }
                         (End of definition for \braid@locate.)
      \braid@relocate This is the macro that actually does the relocation.
                          139 \def\braid@relocate#1{%
                          140 #1\relax
                               \advance\pgf@x by -\braid@width
                          141
                               \pgftransformshift{\pgfqpoint{\pgf@x}{\pgf@y}}
                               \braid@process@start%
                          143
                          144 }
```

```
(End of definition for \braid@relocate.)
                         This macro saves our name.
    \braid@assign@name
                           145 \def\braid@assign@name#1){%
                                \def\braid@name{#1}%
                                \braid@process@start%
                           148 }
                          (End of definition for \braid@assign@name.)
                          The intention of this macro is to allow setting of style options mid-braid. (At present,
\braid@process@options
                          this wouldn't make a lot of sense.)
                           149 \def\braid@process@options#1]{%
                                  \tikzset{#1}%
                                \braid@process%
                           151
                           152 }
                          (End\ of\ definition\ for\ \verb+\braid@process@options.)
                              The next macros handle the actual braid elements. Everything has to have a sub-
                          script, but the superscript is optional and can come before or after the subscript.
                         This handles braid elements of the form a^{-1}_2.
            \braid@sup
                           153 \def\braid@sup#1_#2{%
                                \goadd to @macro\braid@label{_{#2}^{#1}}%
                                \braid@add@crossing{#2}{#1}%
                           156 }
                          (End of definition for \braid@sup.)
            \braid@sub
                           157 % This handles braid elements of the form \Verb+a_1+ or \Verb+a_1^{-1}+.
                           158 \def\braid@sub#1{%
                                \@ifnextchar^{\braid@@sub{#1}}%
                                {\g@addto@macro\braid@label{_{#1}}\braid@add@crossing{#1}{1}}%
                           161 }
                          (End of definition for \braid@sub.)
            \braid@@sub Helper macro for \braid@sub.
                           162 \def\braid@@sub#1^#2{%
                                \goadd to @macro\braid @label{_{#1}^{#2}}%
                                \braid@add@crossing{#1}{#2}%
                           164
                           165 }
                          (End of definition for \braid@@sub.)
              \braid@ne Remember what 1 looks like for testing against.
                           166 \def\braid@ne{1}
                          (End of definition for \braid@ne.)
                         This is the macro which adds the crossing to the current list of strands. The strands are
   \braid@add@crossing
                          stored as soft paths (see the TikZ/PGF documentation). So this selects the right strands
```

and then extends them according to the crossing type.

167 \def\braid@add@crossing#1#2{%

Our crossing type, which is #2, is one of 1 or -1. Our strands are #1 and #1+1.

- 168 \edef\braid@crossing@type{#2}%
- 169 \edef\braid@this@strand{#1}%
- 170 \pgfmathtruncatemacro{\braid@next@strand}{#1+1}

Increment the level counter, if requested. The controls whether the crossing is on the same level as the previous one or is one level further on.

- 171 \ifbraid@increase@level
- 172 \stepcounter{braid@level}
- 173 \fi

Default is to request increment so we set it for next time.

174 \braid@increase@leveltrue

Now we figure out the coordinates of the crossing. (\braid@tx,\braid@ty) is the top-left corner (assuming the braid flows down the page). (\braid@nx,\braid@ny) is the bottom-right corner (assuming the braid flows down the page). We start by setting (\braid@tx,\braid@ty) according to the level and strand number, then shift \braid@ty by \braid@eh which is the "edge height" (the little extra at the start and end of each strand). Then from these values, we set (\braid@nx,\braid@ny) by adding on the appropriate amount. The heights \braid@cy and \braid@dy are for the control points for the strands as they cross. They're actually the same height, but using two gives us the possibility of changing them independently in a later version of this package. Lastly, we bring \braid@ty and \braid@ny towards each other just a little so that there is "clear water" between subsequent crossings (makes it look a bit better if the same strand is used in subsequent crossings).

- 175 \braid@tx=\braid@this@strand\braid@width
- 176 \braid@ty=\value{braid@level}\braid@height
- \advance\braid@ty by \braid@eh
- 178 \braid@nx=\braid@tx
- 179 \braid@ny=\braid@ty
- l80 \advance\braid@nx by \braid@width
- lal \advance\braid@ny by \braid@height
- ls2 \advance\braid@ty by \braid@nf\braid@height
- \advance\braid@ny by -\braid@nf\braid@height
- 184 \braid@cy=\braid@ty
- 185 \braid@dy=\braid@ny
- \advance\braid@cy by \braid@cf\braid@height
- \advance\braid@dy by -\braid@cf\braid@height

Now we try to find a starting point for the strand ending here. We might not have used this strand before, so it might not exist.

- \expandafter\let\expandafter\braid@this@path@origin%
- \csname braid@strand@\braid@this@strand @origin\endcsname

If we haven't seen this strand before, that one will be \relax.

190 \ifx\braid@this@path@origin\relax

Haven't seen this strand before, so initialise it. Record the initial position of the strand.

let\braid@this@path@origin\braid@this@strand

Start a new soft path.

- 92 \pgfsyssoftpath@setcurrentpath{\@empty}
- 193 \pgfpathmoveto{\pgfpoint{\braid@tx}{0pt}}

Save the path as \braid@this@path.

- 194 \pgfsyssoftpath@getcurrentpath{\braid@this@path}
- 195 \else

We have seen this before, so we simply copy the associated path in to \braid@this@path.

- 196 \expandafter\let\expandafter\braid@this@path%
- \csname braid@strand@\braid@this@path@origin\endcsname
- 198 \fi

Now we do the same again with the other strand in the crossing.

- \expandafter\let\expandafter\braid@next@path@origin%
- 200 \csname braid@strand@\braid@next@strand @origin\endcsname
- 201 \ifx\braid@next@path@origin\relax
- 202 \let\braid@next@path@origin\braid@next@strand
- 203 \pgfsyssoftpath@setcurrentpath{\@empty}
- 204 \pgfpathmoveto{\pgfpoint{\braid@nx}{0pt}}
- 205 \pgfsyssoftpath@getcurrentpath{\braid@next@path}
- 206 \else
- 207 \expandafter\let\expandafter\braid@next@path%
- \csname braid@strand@\braid@next@path@origin\endcsname
- 209 \f:

Now that we have the paths for our two strands, we extend them to the next level. We start by selecting the first path.

pgfsyssoftpath@setcurrentpath{\braid@this@path}

Draw a line down to the current level, note that this line is always non-trivial since we shifted the corners of the crossing in a little.

https://pgfpathlineto{\pgfqpoint{\braid@tx}{\braid@ty}}

Curve across to the next position. Depending on the crossing type, we either have a single curve or we have to break it in two. Our gap is to interrupt at times determined by the gap key.

- ${\tt 212 pgfmathsetmacro{\braid@gst}{0.5 pgfkeysvalueof{/pgf/braid/gap}}}\%$
- ${\tt 213 pgfmathsetmacro{\braid@gend}{0.5 + pgfkeysvalueof{/pgf/braid/gap}}} \%$
- 214 \ifx\braid@crossing@type\braid@over@cross

We're on the overpass, so just one curve needed.

- \pgfpathcurveto{\pgfqpoint{\braid@tx}{\braid@cy}}%
- 216 {\pgfqpoint{\braid@nx}{\braid@dy}}%
- 217 {\pgfqpoint{\braid@nx}{\braid@ny}}
- 218 **\else**

We're on the underpass, so we need to interrupt our path to allow the other curve to go past.

- 219 \pgfpathcurvebetweentimecontinue{0}{\braid@gst}%
- 220 {\pgfqpoint{\braid@tx}{\braid@ty}}%
- 221 {\pgfqpoint{\braid@tx}{\braid@cy}}%
- 222 {\pgfqpoint{\braid@nx}{\braid@dy}}%
- {\pgfqpoint{\braid@nx}{\braid@ny}}%
- \pgfpathcurvebetweentime{\braid@gend}{1}%
- 225 {\pgfqpoint{\braid@tx}{\braid@ty}}%
- 226 {\pgfqpoint{\braid@tx}{\braid@cy}}%
- 27 {\pgfqpoint{\braid@nx}{\braid@dy}}%
- 228 {\pgfqpoint{\braid@nx}{\braid@ny}}
- 229 **\fi**

```
We're done with this path, so now we save it.
      \pgfsyssoftpath@getcurrentpath{\braid@this@path}
Now do the same with the second path.
      \pgfsyssoftpath@setcurrentpath{\braid@next@path}
 231
      \pgfpathlineto{\pgfqpoint{\braid@nx}{\braid@ty}}
    \ifx\braid@crossing@type\braid@over@cross
 233
      \pgfpathcurvebetweentimecontinue{0}{\braid@gst}%
 234
      {\pgfqpoint{\braid@nx}{\braid@ty}}%
 235
      {\pgfqpoint{\braid@nx}{\braid@cy}}%
 236
      {\pgfqpoint{\braid@tx}{\braid@dy}}%
      {\pgfqpoint{\braid@tx}{\braid@ny}}
 238
      \pgfpathcurvebetweentime{\braid@gend}{1}%
 239
      {\pgfqpoint{\braid@nx}{\braid@ty}}%
      {\pgfqpoint{\braid@nx}{\braid@cy}}%
      {\pgfqpoint{\braid@tx}{\braid@dy}}%
 242
      {\pgfqpoint{\braid@tx}{\braid@ny}}
 243
    \else
 244
      \pgfpathcurveto{\pgfqpoint{\braid@nx}{\braid@cy}}%
 245
      {\pgfqpoint{\braid@tx}{\braid@dy}}%
 246
      {\pgfqpoint{\braid@tx}{\braid@ny}}
 247
    \fi
 248
      \pgfsyssoftpath@getcurrentpath{\braid@next@path}
 249
Now save the paths to their proper macros again.
      \expandafter\let%
 250
      \csname braid@strand@\braid@this@path@origin \endcsname%
 251
      \braid@this@path
 252
      \expandafter\let%
 253
      \csname braid@strand@\braid@next@path@origin \endcsname%
      \braid@next@path
 255
Now update the origins
      \expandafter\let%
 256
      \csname braid@strand@\braid@this@strand @origin\endcsname%
 257
      \braid@next@path@origin
 258
      \expandafter\let%
 259
      \csname braid@strand@\braid@next@strand @origin\endcsname%
 260
      \braid@this@path@origin
 261
increment the strand counter, if necessary
      \pgfmathparse{\value{braid@strands} < \braid@next@strand ?</pre>
        "\noexpand\setcounter{braid@strands}{\braid@next@strand}" : ""}
 263
      \pgfmathresult
 264
And merrily go on our way with the next bit of the braid specification.
      \braid@process%
 266 }
```

\braid@olabel@strand

This macro allows us to label a strand just before a crossing. The first argument is the strand number at that particular crossing and the second is the label. We also save the current height. This version takes the strand number as meaning the *original* ordering.

```
267 \newcommand{\braid@olabel@strand}[3][]{%
268 \edef\braid@tmp{{\the\value{braid@level}}}%
```

(End of definition for \braid@add@crossing.)

```
\expandafter\ifx\csname braid@strand@#2@origin\endcsname\relax
                                       \g@addto@macro\braid@tmp{{#2}}%
                                 271
                                       \edef\braid@tmpa{{\csname braid@strand@#2@origin\endcsname}}%
                                       \ge@addto@macro\braid@tmp{\braid@tmpa}%
                                 273
                                 274
                                       \g@addto@macro\braid@tmp{{#3}{#1}}%
                                       \ge@addto@macro{\braid@strand@labels}{\braid@tmp}%
                                       \braid@process%
                                 277
                                 278 }
                                (End\ of\ definition\ for\ \braidColabelCstrand.)
                                This macro allows us to label a strand just before a crossing. The first argument is the
        \braid@clabel@strand
                                strand number at that particular crossing and the second is the label. We also save the
                                current height. This version takes the strand number as meaning the current ordering.
                                    \newcommand{\braid@clabel@strand}[3][]{%
                                       \edef\braid@tmp{{\the\value{braid@level}}}%
                                       \g@addto@macro\braid@tmp{{#2}{#3}{#1}}%
                                 281
                                       \ge@addto@macro{\braid@strand@labels}{\braid@tmp}%
                                       \braid@process%
                                 284 }
                                (End of definition for \braid@clabel@strand.)
          \braid@floors@trim The list of floors, if given, will start with a superfluous comma. This removes it.
                                 285 \def\braid@floors@trim,{}
                                (End of definition for \braid@floors@trim.)
         \braid@render@floor This is the default rendering for floors: it draws a rectangle.
                                 286 \def\braid@render@floor{%
                                         \draw (\floorsx,\floorsy) rectangle (\floorex,\floorey);
                                 288 }
                                (End of definition for \braid@render@floor.)
 \braid@render@strand@labels
                                This starts rendering the labels on the strands at the crossings.
                                 289 \def\braid@render@strand@labels#1{%
                                       \def\braid@tmp{#1}%
                                 290
                                       \ifx\braid@tmp\pgfutil@empty
                                 291
                                       \let\braid@next=\pgfutil@gobble
                                 292
                                       \let\braid@next=\braid@@render@strand@labels
                                       \fi
                                       \braid@next{#1}%
                                 297 }
                                (End\ of\ definition\ for\ \ braid@render@strand@labels.)
                                This is the actual renderer.
\braid@@render@strand@labels
                                 298 \def\braid@@render@strand@labels#1#2#3#4{%
                                       \begingroup
                                 299
                                       \pgfscope
                                 300
                                       \let\tikz@options=\pgfutil@empty
                                 301
```

```
\let\tikz@mode=\pgfutil@empty
302
     \let\tik@transform=\pgfutil@empty
303
     \let\tikz@fig@name=\pgfutil@empty
304
     \tikzset{/pgf/braid/strand label,#4}%
305
     \braid@nx=#2\braid@width
306
     \braid@ny=#1\braid@height
307
     \advance\braid@ny by \braid@eh
308
     \advance\braid@ny by \braid@height
309
     \pgftransformshift{\pgfqpoint{\braid@nx}{\braid@ny}}%
310
     \tikz@options
311
     \setbox\pgfnodeparttextbox=\hbox%
312
     \bgroup%
313
     \tikzset{every text node part/.try}%
314
     \ifx\tikz@textopacity\pgfutil@empty%
315
316
     \pgfsetfillopacity{\tikz@textopacity}%
317
     \pgfsetstrokeopacity{\tikz@textopacity}%
318
     \fi%
319
     \pgfinterruptpicture%
     \tikz@textfont%
     \ifx\tikz@text@width\pgfutil@empty%
322
     \else%
323
     \begingroup%
324
     \pgfmathsetlength{\pgf@x}{\tikz@text@width}%
325
     \pgfutil@minipage[t]{\pgf@x}\leavevmode\hbox{}%
326
     \tikz@text@action%
327
     \fi%
328
     \tikz@atbegin@node%
329
     \bgroup%
330
     \aftergroup\unskip%
331
     \ifx\tikz@textcolor\pgfutil@empty%
332
     \else%
333
     \pgfutil@colorlet{.}{\tikz@textcolor}%
334
     \fi%
335
     \pgfsetcolor{.}%
336
     \setbox\tikz@figbox=\box\pgfutil@voidb@x%
337
     \tikz@uninstallcommands%
338
339
     \tikz@halign@check%
340
     \ignorespaces%
341
     #3
342
     \egroup
     \tikz@atend@node%
     \ifx\tikz@text@width\pgfutil@empty%
344
     \else%
345
     \pgfutil@endminipage%
346
     \endgroup%
347
     \fi%
348
     \endpgfinterruptpicture%
349
350
351
      \ifx\tikz@text@width\pgfutil@empty%
352
       \else%
         \pgfmathsetlength{\pgf@x}{\tikz@text@width}%
353
         \wd\pgfnodeparttextbox=\pgf@x%
354
```

\fi%

```
\ifx\tikz@text@height\pgfutil@empty%
 356
        \else%
 357
           \pgfmathsetlength{\pgf@x}{\tikz@text@height}%
 358
           \ht\pgfnodeparttextbox=\pgf@x%
 359
 360
        \ifx\tikz@text@depth\pgfutil@empty%
 361
 362
           \pgfmathsetlength{\pgf@x}{\tikz@text@depth}%
 363
           \dp\pgfnodeparttextbox=\pgf@x%
        \fi%
 365
      \pgfmultipartnode{\tikz@shape}{\tikz@anchor}{\tikz@fig@name}{%
 366
        {\begingroup\tikz@finish}%
 367
 368
      \endpgfscope
 369
      \endgroup
 370
      \braid@render@strand@labels%
 371
(End\ of\ definition\ for\ \ braid@@render@strand@labels.)
```

\braid@render

This is called at the end of the braid and it renders the braids and floors according to whatever has been built up up to now.

```
373 \def\braid@render{
```

Check for floors since we do them first.

```
\ifx\braid@floors\@empty
374
       \else
375
```

Have some floors, start a scope and prepare to render them.

```
\pgfsys@beginscope
```

Clear the path (just to be sure).

```
\pgfsyssoftpath@setcurrentpath{\empty}
```

Trim the initial comma off the list of floors.

\edef\braid@floors{\expandafter\braid@floors@trim\braid@floors}

Initialise our horizontal coordinates.

```
\braid@tx=\braid@width
       \advance\braid@tx by \braid@eh
380
       \braid@nx=\value{braid@strands}\braid@width
381
       \advance\braid@nx by -\braid@eh
```

Loop over the list of floors.

```
\foreach \braid@f in \braid@floors {
383
         \pgfsys@beginscope
```

Figure out the vertical coordinates for the current floor.

```
\braid@ty=\braid@f\braid@height
         \advance\braid@ty by \braid@eh
386
         \advance\braid@ty by \braid@height
387
         \braid@ny=\braid@ty
388
         \advance\braid@ny by \braid@height
389
```

Save the coordinates for use in the floor rendering macro.

393 \edef\floorey{\the\braid@ny}
394 \let\tikz@options=\pgfutil@empty

Load general floor style options.

\expandafter\tikzset\expandafter{\braid@floors@style}

Load any style options specific to this floor. We're actually offset by 2 from what the user thinks the floor level is.

>pgfmathtruncatemacro{\braid@ff}{\braid@f+2}

Load the relevant floor style, if it exists.

```
\expandafter\let\expandafter\braid@floor@style%

\csname braid@options@floor@\braid@ff\endcsname
\ifx\braid@floor@style\relax
```

400 \else

There is a floor style for this level, so process it.

```
\verb|\expandafter\tikzset\expandafter{\tikzset}| when the constraint of the constrain
```

402 \fi

The \tikzset just parses the options, we need to call \tikz@options to actually set them.

403 \tikz@options

Now we call the rendering code.

404 \braid@render@floor

Done! End the scope for this floor and go again.

```
405 \pgfsys@endscope
406 }
```

Done rendering floors, end the scope.

```
407 \pgfsys@endscope
```

408 \fi

Finished with floors (if we had them), now get on with the strands.

```
409 \stepcounter{braid@level}
```

Start a local scope to ensure we don't mess with other braids

11 \pgfsys@beginscope

Default is to draw each braid

- 412 \tikz@mode@drawtrue%
- 413 \let\tikz@mode=\pgfutil@empty
- 414 \let\tikz@options=\pgfutil@empty

(x,y) coordinates of bottom of strand

- 415 \braid@tx=\braid@k\braid@width
- $\verb|\braid@ty=\value{braid@level}\braid@height|$
- 417 \advance\braid@ty by 2\braid@eh

```
Try to find the starting point of this strand
        \expandafter\let\expandafter\braid@path@origin%
        \csname braid@strand@\braid@k @origin\endcsname
 419
        \ifx\braid@path@origin\relax
 420
If that doesn't exist, we'll just draw a straight line so we move to the top of the current
position
        \pgfsyssoftpath@setcurrentpath{\@empty}
        \pgfpathmoveto{\pgfqpoint{\braid@tx}{0pt}}
 422
        \let\braid@path@origin\braid@k
 423
        \else
 424
If the path does exist, we load it
        \expandafter\let\expandafter\braid@path%
        \csname braid@strand@\braid@path@origin\endcsname
 426
        \pgfsyssoftpath@setcurrentpath{\braid@path}
 427
 428
Extend the path to the bottom
        \pgflineto{\pgfqpoint{\braid@tx}{\braid@ty}}
Load common style options
        \expandafter\tikzset\expandafter{\braid@style}
 430
Load any style options specific to this strand
        \expandafter\let\expandafter\braid@style%
        \csname braid@options@strand@\braid@path@origin\endcsname
 432
        \ifx\braid@style\relax
 433
 434
        \expandafter\tikzset\expandafter{\braid@style}
 435
        \fi
 436
    \braid@options
        \tikz@mode
 438
        \tikz@options
 439
This is the command that actually draws the strand.
          \edef\tikz@temp{\noexpand\pgfusepath{%
               \iftikz@mode@draw draw\fi%
 441
          }}%
 442
          \tikz@temp
If our braid has a name, we label the ends of the strand.
 444 \ifx\braid@name\pgfutil@empty
 445 \else
Label the ends of the strand.
 446 \coordinate (\braid@name-\braid@path@origin-e) at (\braid@tx,\braid@ty);
 447 \coordinate (\braid@name-rev-\braid@k-e) at (\braid@tx,\braid@ty);
 448 \braid@nx=\braid@path@origin\braid@width
 449 \coordinate (\braid@name-\braid@path@origin-s) at (\braid@nx,0pt);
 450 \coordinate (\braid@name-rev-\braid@k-s) at (\braid@nx,Opt);
Done with this strand, close the scope and do the next one.
       \pgfsys@endscope
 453
```

If our braid has a name, we also want to label the centre.

Now we label the strands if needed.

- 464 \ifx\braid@strand@labels\pgfutil@empty
- 465 **\els**e
- \expandafter\braid@render@strand@labels\braid@strand@labels{}%
- 467 \fi

All done now, close the scope and end the group (which was opened right at the start).

- 468 \pgfsys@endscope
- 469 \endgroup}

(End of definition for \braid@render.)

\braid@start

This starts off the braid, initialising a load of stuff. We start a PGF scope, set the level to -1, the label, floors, and name to empty, process any options we're given, and save certain lengths for later use.

- 470 \def\braid@start#1{%
- 471 \pgfsys@beginscope
- 472 \setcounter{braid@level}{-1}%
- 473 \let\braid@label\@empty
- 474 \let\braid@strand@labels\@empty
- 475 \let\braid@floors\@empty
- 476 \let\braid@name\empty
- 477 \let\clabel=\braid@clabel@strand
- 478 \let\olabel=\braid@olabel@strand
- 479 \pgfkeys{/pgf/braid/.cd,#1}%
- 480 \ifbraid@strand@labels@origin
- 481 \let\label=\braid@olabel@strand
- 482 **\else**
- 483 \let\label=\braid@clabel@strand
- 484 **\fi**
- 486 \tikz@transform
- 487 \setcounter{braid@strands}{%
- \pgfkeysvalueof{/pgf/braid/number of strands}}%
- 489 \braid@width=\pgfkeysvalueof{/pgf/braid/width}%
- 490 \braid@height=\pgfkeysvalueof{/pgf/braid/height}%
- 491 \braid@eh=\pgfkeysvalueof{/pgf/braid/border height}%
- 492 \pgfkeysgetvalue{/pgf/braid/control factor}{\braid@cf}%
- 493 \pgfkeysgetvalue{/pgf/braid/nudge factor}{\braid@nf}%
- 494 \braid@height=-\braid@height
- 495 \braid@eh=-\braid@eh
- 496 \braid@increase@leveltrue
- 497 \braid@process@start

```
498 }
(End of definition for \braid@start.)
    These are the lengths we'll use as we construct the braid
 499 \newdimen\braid@width
 500 \newdimen\braid@height
 501 \newdimen\braid@tx
 502 \newdimen\braid@ty
 503 \newdimen\braid@nx
 504 \newdimen\braid@ny
 505 \newdimen\braid@cy
 506 \newdimen\braid@dy
 507 \newdimen\braid@eh
    An if to decide whether or not to step to the next level or not
 508 \newif\ifbraid@increase@level
An if to decide whether label indices should be absolute or not
 509 \newif\ifbraid@strand@labels@origin
    Some initial values
 510 \let\braid@style\pgfutil@empty
 511 \let\braid@floors@style\pgfutil@empty
 512 \def\braid@over@cross{1}
    Counters to track the strands and the levels.
 513 \newcounter{braid@level}
 514 \newcounter{braid@strands}
    All the keys we'll use.
 515 \pgfkeys{
Handle unknown keys by passing them to pgf and tikz.
        /tikz/braid/.search also={/pgf},
        /pgf/braid/.search also={/pgf,/tikz},
 517
Our "namespace" is /pgf/braid.
        /pgf/braid/.cd,
 518
        number of strands/.initial=0,
 519
        height/.initial=1cm,
        width/.initial=1cm,
        gap/.initial=.1,
        border height/.initial=.25cm,
        control factor/.initial=.5,
        nudge factor/.initial=.05,
 525
        name/.code={%
 526
          \def\braid@name{#1}%
 527
        },
 528
        at/.code={%
 529
          \braid@relocate{#1}%
 530
 531
        floor command/.code={%
 532
          \def\braid@render@floor{#1}%
 533
```

style strands/.code 2 args={%

\braidset{style each strand/.list={#1}}%

\def\braid@temp{#2}%

534

535

536

```
538
                     style each strand/.code={%
             539
                       \expandafter\edef%
             540
                       \csname braid@options@strand@#1\endcsname{\braid@temp}%
             541
             542
                     style floors/.code 2 args={%
             543
                       \def\braid@temp{#2}%
                       \braidset{style each floor/.list={#1}}%
                     style each floor/.code={%
             547
             548
                        \expandafter\edef%
                       \csname braid@options@floor@#1\endcsname{\braid@temp}%
             549
             550
                     style all floors/.code={%
             551
                        \def\braid@floors@style{#1}
             552
             553
                     strand label/.style={},
                     strand label by origin/.is if=braid@strand@labels@origin,
             556 }
\braidset Shorthand for setting braid-specific keys.
             557 \def\braidset#1{%
                   \pgfkeys{/pgf/braid/.cd,#1}}
            (\mathit{End}\ of\ definition\ for\ \verb|\braidset|.\ \mathit{This}\ \mathit{function}\ \mathit{is}\ \mathit{documented}\ \mathit{on}\ \mathit{page}\ \ref{eq:constraint}.)
             559 (*library)
             560 (@@=braid)
                  Reimplementation as a TikZ Library
            Life is so much easier with LATEX3.
             561 \ProvidesFile{tikzlibrarybraids.code.tex}[%
                   2024/01/09 v2.3 Tikz/PGF library for drawing braid diagrams%
             563
             564 \RequirePackage{expl3}
             565 \ExplSyntaxOn
            Define all the variables we'll be using.
             566 \tl_new:N \l__braid_tmpa_tl
             567 \tl_new:N \l__braid_tmpb_tl
             568 \tl_new:N \l__braid_tmpc_tl
             569 \tl_new:N \l__braid_tmpd_tl
             570 \tl_new:N \l__braid_anchor_strand_tl
             _{571} \tl_new:N \l__braid_anchor_level_tl
             572 \fp_new:N \l__braid_height_fp
             573 \fp_new:N \l__braid_width_fp
             ^{574} fp_new:N l_braid_nudge_fp
             575 \fp_new:N \l__braid_control_fp
             576 \fp_new:N \l__braid_ctrlax_fp
             577 \fp_new:N \l__braid_ctrlay_fp
             578 \fp_new:N \l__braid_ctrlbx_fp
             579 \fp_new:N \l__braid_ctrlby_fp
```

580 \fp_new:N \l__braid_endx_fp

```
581 \fp_new:N \l__braid_endy_fp
 582 fp_new:N l_braid_anchor_x_fp
 583 \fp_new:N \l__braid_anchor_y_fp
 584 \int_new:N \l__braid_tmpa_int
 585 \int_new:N \l__braid_tmpb_int
 586 \int_new:N \l__braid_length_int
 587 \int_new:N \l__braid_strands_int
 588 \int_new:N \l__braid_crossing_int
 589 \int_new:N \l__braid_crossing_start_int
 590 \int_new:N \l__braid_crossing_end_int
 591 \int_new:N \l__braid_crossing_width_int
 \mbox{\cite{thm}} \int_new:N \l__braid_crossing_start_factor_int
 ^{594} \int_new:N \l__braid_crossing_end_factor_int
 595 \int_new:N \l__braid_anchor_level_int
 596 \int_new:N \l__braid_floor_int
 597 \seq_new:N \l__braid_tmpa_seq
 598 \seq_new:N \l__braid_word_seq
 599 \seq_new:N \l__braid_crossing_seq
 600 \seq_new:N \l__braid_anchor_seq
 601 \seq_new:N \l__braid_floors_seq
 602 \str_new:N \l__braid_tmpa_str
 603 \bool_new:N \l__braid_step_level_bool
 604 \bool_new:N \l__braid_swap_crossing_bool
 605 \bool_new:N \l__braid_default_crossing_bool
 \verb|\bool_new:N \l_\_braid_default_symbol_bool|\\
 607 \bool_set_true:N \l__braid_default_crossing_bool
 608 \bool_set_true:N \l__braid_default_symbol_bool
 609 \bool_new:N \l__braid_floor_bool
 610 \bool_new:N \l__braid_height_bool
 {\tt 611} \verb|\bool_new:N \ll_braid_crossing_height_bool\\
 {\tiny \texttt{612}} \  \, \texttt{\braid\_strands\_prop}
 {\tiny \texttt{613}} \  \, \textbf{\formula} = \texttt{N} \  \, \textbf{\formula} = \texttt{permutation\_prop}
 614 \prop_new:N \l__braid_crossing_permutation_prop
 _{615} \prop_new:N \l_braid_inverse\_prop
 616 \prop_new:N \l__braid_anchor_prop
 617 \msg_new:nnn {braids} {height} {The~ keys~ "height"~ and~ "crossing~ height"~ shouldn't~ be~
 618 \cs_generate_variant:Nn \seq_set_split:Nnn {NVn}
 619 \cs_generate_variant:Nn \str_compare:nNnTF {VNnTF}
Our interface is through a TikZ pic.
 620 \tikzset{
       braid/.pic={
 621
         \begin{scope}[every~ braid/.try]
 622
         \__braid_parse_word:n {#1}
 623
         \__braid_count:
 624
         \__braid_render:
 625
         \end{scope}
 626
       },
 627
       floor/.pic={
 628
         \path[pic~ actions, draw=none] (0,0) rectangle (1,1);
 629
         \path[pic~ actions, fill=none] (0,0) -- (1,0) (0,1) -- (1,1);
 630
       },
 631
       /tikz/braid/.search~ also={/tikz},
 632
       braid/.cd,
 633
```

The various TikZ parameters for the braid.

The anchor determines which part of the braid is located at the position specified by the pic. It can be of the form n-m where n is a strand number and +m+ is a crossing level. The strand number can be either a number or rev-n to use the ending numbering of the strands. The crossing level can also be s or e which means the actual start or end of the strand (including the border).

```
anchor/.initial=1-s,
```

number of strands sets a minimum for the number of strands in the braid (otherwise, it is set by the strands used in the specified crossings).

```
number~ of~ strands/.initial=0,
```

These keys determine whether crossings are over or under by default.

```
crossing~ convention/.is~choice,
636
      crossing~ convention/over/.code={
637
638
        \bool_set_true:N \l__braid_default_crossing_bool
      crossing~ convention/down/.code={
640
        \bool_set_true:N \l__braid_default_crossing_bool
641
      },
642
      crossing~ convention/under/.code={
643
        \bool_set_false:N \l__braid_default_crossing_bool
644
      },
645
      crossing~ convention/up/.code={
646
        \bool_set_false:N \l__braid_default_crossing_bool
647
648
      crossing~ convention/.default=over,
649
      flip~ crossing~ convention/.code={
650
        \verb|\bool_set_inverse:N \ll_braid_default_crossing_bool|
651
652
```

These keys determine whether elements should be inverted by default.

```
set~ symbols/.is~choice,
653
      set~ symbols/over/.code={
654
        \bool_set_true:N \l__braid_default_symbol_bool
655
656
      set~ symbols/down/.code={
657
        \bool_set_true:N \l__braid_default_symbol_bool
658
      },
659
      set~ symbols/under/.code={
660
        \bool_set_false:N \l__braid_default_symbol_bool
661
662
      set~ symbols/up/.code={
663
        \bool_set_false:N \l__braid_default_symbol_bool
664
      },
665
      set~ symbols/.default=over,
666
      flip~ symbols/.code={
        \bool_set_inverse:N \l__braid_default_symbol_bool
669
```

The next two keys are used to control the separation between the crossings. The original braid package used the height as part of how it determined the direction of the braid on the page. In particular, the height could be negative, and indeed the

default is for it to be so since a vertical braid usually flows from top to bottom. Now that the drawing is reimplemented as a pic then the direction is better controlled using transformations. So then height should be simply to set the gap between crossings in whatever orientation. In particular, height should be a positive length.

To avoid backwards incompatibility, the original (counter-intuitive) version of height is retained but a new key, crossing height, is introduced which can only be positive (rather, the code will take its absolute value so you can *declare* it to be negative but the code will laugh at you and ignore the sign).

To ensure that **crossing height** wins, we use a boolean to see if it has been invoked by the user.

```
height/.initial=-1cm,
 670
 671
       height/.code={
         \bool_if:NTF \l__braid_crossing_height_bool
 672
 673
 674
            \msg_term:nn {braids} {height}
         }
 675
 676
            \pgfkeyssetvalue{/tikz/braid/height}{#1}
 677
            \bool_set_true:N \l__braid_height_bool
 678
 679
       },
       crossing~ height/.code={
         \bool_if:NT \l__braid_height_bool
 683
            \msg_term:nn {braids} {height}
 684
 685
         \exp_args:Nnx \pgfkeyssetvalue {/tikz/braid/height}
 686
         {\dim_{eval:n} {-\dim_{abs:n{#1}}}}
 687
         \bool_set_true:N \l__braid_crossing_height_bool
 688
 689
       },
width is the distance between strands (can be negative).
       width/.initial=1cm,
gap is for determining the gap in the under-strand of a crossing.
       gap/.initial=.05,
 691
border height is a length added at the start and end of each strand.
       border~ height/.initial=.25cm,
floor border is added to the width of any floors
       floor~ border/.initial=.25cm,
floors is a list of floors to draw, specified as a cslist of coordinates as (x,y,w,h,a) in which
the units are numbers of strands and crossing levels. The parameters are: coordinates of
lower left corner, width, height, (optional) name for styling.
       add~ floor/.code={
 694
         \seq_push:Nn \l__braid_floors_seq {#1}
 695
       },
 696
control factor determines the proportion of the height used for the control points.
       control~ factor/.initial=.5,
nudge factor is used to compress each crossing slightly within its rectangle.
       nudge~ factor/.initial=.05
 698
 699 }
```

__braid_parse_word: Nn Parse the braid word as a token list and convert it into a sequence.

```
700 \cs_new_nopar:Npn \__braid_parse_word:n #1
701 {
702    \seq_clear:N \l__braid_word_seq
703    \tl_clear:N \l__braid_tmpa_tl
704    \tl_set:Nn \l__braid_tmpb_tl {#1}
705
706    \bool_until_do:nn { \tl_if_empty_p:N \l__braid_tmpb_tl }
707    {
```

We step through the braid specification, looking for special characters. To avoid catcode issues, the comparison is as strings. Some actions may involve consuming more tokens from the list so we can't do a simple map_inline but have to keep stripping off the head token.

The idea is to store information about the current crossing in a token list (noting that it may be specified in a variety of orders) and then when we're sure we have all the information we add it to our sequence of crossings.

```
708 \str_set:Nx \l__braid_tmpa_str {\tl_head:N \l__braid_tmpb_tl}
709 \tl_set:Nx \l__braid_tmpb_tl {\tl_tail:N \l__braid_tmpb_tl}
710 \str_case_e:nnTF {\l__braid_tmpa_str}
711 {
```

Underscore introduces the crossing numbers

Power is used to indicate inverse.

Bar is for floors.

```
{ | }
728
729
         \tl_if_empty:NF \l__braid_tmpa_tl
730
           \seq_put_right:NV \l__braid_word_seq \l__braid_tmpa_tl
           \tl_clear:N \l__braid_tmpa_tl
733
734
735
736
         \tl_set:Nn \l__braid_tmpa_tl {
           \bool_set_false:N \l__braid_step_level_bool
737
           \bool_set_true:N \l__braid_floor_bool
738
```

```
739     }
740     \seq_put_right:NV \l__braid_word_seq \l__braid_tmpa_tl
741     \tl_clear:N \l__braid_tmpa_tl
742     }
```

Hyphen says the next crossing is on the same level as the current one.

1 is for the identity (i.e., no crossing but still have a level). We put a nop token on the list so that it is no longer empty.

Ignore spaces.

```
759 {~}
760 {
761 }
762 }
763 {
764 }
765 {
```

If we get an unrecognised token, it's our trigger to start accumulating information for the next crossing.

At the end, we also put our current token list on the word sequence.

```
773 \tl_if_empty:NF \l_braid_tmpa_tl
774 {
775 \seq_put_right:NV \l_braid_word_seq \l_braid_tmpa_tl
776 \tl_clear:N \l_braid_tmpa_tl
777 }
778 }
```

 $(End\ of\ definition\ for\ \verb|_braid_parse_word:Nn.|)$

__braid_parse_index:n Parse an index, saving it in a sequence with the two indices such that the first goes over the second. 779 \cs_new_nopar:Npn __braid_parse_index:n #1 780 { \seq_clear:N \l__braid_crossing_seq 781 \clist_map_inline:nn {#1} 782 783 \tl_if_in:nnTF {##1} {-} 784 785 \seq_set_split:Nnn \l__braid_tmpa_seq {-} {##1} 786 \int_compare:nTF {\seq_item:Nn \l__braid_tmpa_seq {1} < \seq_item:Nn \l__braid_tmpa_se 787 \int_set:Nn \l__braid_tmpa_int {1} } { \int_set:Nn \l__braid_tmpa_int {-1} 793 \int_step_inline:nnnn {\seq_item:Nn \l__braid_tmpa_seq {1}} {\l__braid_tmpa_int} {\sec_item:Nn \l__braid_tmpa_seq {1}} 794 { 795 \seq_put_right: Nn \l__braid_crossing_seq {####1} 796 797 } 798 { \seq_put_right:Nn \l__braid_crossing_seq {##1} 801 802 } \int_compare:nT {\seq_count:N \l__braid_crossing_seq == 1} 803 804 \seq_put_right:Nx \l__braid_crossing_seq {\int_eval:n {#1 + 1} } 805 806 \bool_xor:nnT {\l__braid_swap_crossing_bool} {\l__braid_default_symbol_bool} 807 808 \seq_reverse:N \l__braid_crossing_seq } 810 811 } $(End\ of\ definition\ for\ \verb|__braid_parse_index:n.|)$ Parse an exponent, basically testing to see if it is -1 in which case our crossing numbers __braid_parse_exponent:n should be reversed. 812 \cs_new_nopar:Npn __braid_parse_exponent:n #1 813 { $\int \int d^2 r dr dr$ 814 815 { \bool_set_true:N \l__braid_swap_crossing_bool 816

__braid_do_identity:

817 }

{

818

\bool_set_false:N \l__braid_swap_crossing_bool

(End of definition for __braid_parse_exponent:n.)

```
822 \cs_new_nopar:Npn \__braid_do_identity:
823 {
824 }
(End of definition for \__braid_do_identity:.)
```

__braid_count:NNN

Work out how big the braid is by counting strands and levels. We also figure out the permutation from the start to end of the strands. This is useful for labelling various parts of the braid.

```
825 \cs_new_nopar:Npn \__braid_count:
 826 {
 827
      \int_zero:N \l__braid_length_int
      \int_set:Nn \l__braid_strands_int {\__braid_value:n {number~of~strands}}
 828
      \prop_clear:N \l__braid_permutation_prop
 829
      \prop_clear:N \l__braid_crossing_permutation_prop
 830
      \prop_clear:N \l__braid_anchor_prop
 831
      \prop_clear:N \l__braid_inverse_prop
 832
 833
      \seq_map_inline: Nn \l__braid_word_seq
 834
 835
Clear the crossing sequence and assume we're going to step the level.
        \seq_clear:N \l__braid_crossing_seq
 836
        \bool_set_true:N \l__braid_step_level_bool
 837
        \bool_set_false:N \l__braid_swap_crossing_bool
 838
Run the details of this crossing.
If we're increasing the level (no hyphen), do so.
        \bool_if:NT \l__braid_step_level_bool
 840
 841
           \int_incr:N \l__braid_length_int
 842
 843
If we have a crossing, check we have enough strands to cover it.
        \seq_if_empty:NF \l__braid_crossing_seq
 844
 845
           \seq_map_inline: Nn \l__braid_crossing_seq
 846
 847
             \int_set:Nn \l__braid_strands_int
 848
               \int_max:nn {\l__braid_strands_int} {###1}
             }
 851
 852
          }
        }
 853
 854
```

Now that we know how many strands we have, we can initialise our permutation props. One will hold the overall permutation, the other will keep track of our current permutation.

```
% \int_step_inline:nnnn {1} {1} {\l__braid_strands_int}
% {
% \prop_put:Nnn \l__braid_permutation_prop {##1} {##1}
% \prop_put:Nnn \l__braid_anchor_prop {##1} {##1}
% \prop_put:Nnn \l__braid_crossing_permutation_prop {##1} {##1}
% }
% }
```

Now we step through the braid word again and record the permutations so that we can calculate the overall permutation defined by the braid.

We will also figure out our shift from the anchor, so first we need to get some information about the anchor.

If the anchor specification has a hyphen then it is of the form strand-level, otherwise it is an anchor as if the whole braid were contained in a rectangular node.

```
\tl_set:Nx \l__braid_tmpa_tl {\__braid_value:n {anchor}}
     \tl_if_in:NnTF \l__braid_tmpa_tl {-}
862
     {
       \seq_set_split:NnV \l__braid_anchor_seq {-} \l__braid_tmpa_tl
865
       \tl_set:Nx \l__braid_tmpa_tl {\seq_item:Nn \l__braid_anchor_seq {1}}
866
       \tl_if_eq:VnTF \l__braid_tmpa_tl {rev}
867
868
         \tl_set:Nx \l__braid_anchor_strand_tl {\seq_item:Nn \l__braid_anchor_seq {2}}
869
         \tl_set:Nx \l__braid_anchor_level_tl {\seq_item:Nn \l__braid_anchor_seq {3}}
870
      }
871
872
         \tl_set:Nx \l__braid_anchor_strand_tl {\seq_item:Nn \l__braid_anchor_seq {1}}
873
         \tl_set:Nx \l__braid_anchor_level_tl {\seq_item:Nn \l__braid_anchor_seq {2}}
874
875
```

The important information is as to the level at which the requested anchor resides. If it is at the end or start of a strand, we set the level to -1 so that it never matches a level number.

```
\tl_if_eq:VnTF \l__braid_anchor_level_tl {s}
876
877
          \int_set:Nn \l__braid_anchor_level_int {-1}
878
       }
879
880
          \tl_if_eq:VnTF \l__braid_anchor_level_tl {e}
882
            \int_set:Nn \l__braid_anchor_level_int {-1}
883
         3
884
885
            \int_set:Nn \l__braid_anchor_level_int
886
            {\tl_use:N \l__braid_anchor_level_tl}
887
888
       }
889
     }
890
891
```

There wasn't a hyphen in the anchor specification, so assume it's an anchor on a node surrounding the entire braid. For now, set the anchor strand and level to -1.

```
892  \int_set:Nn \l__braid_anchor_level_int {-1}
893  \tl_set:Nn \l__braid_anchor_strand_tl {-1}
894  }
895
896  \int_zero:N \l__braid_crossing_int
897  \int_incr:N \l__braid_crossing_int
898  \seq_map_inline:Nn \l__braid_word_seq
899  {
900  \bool_set_true:N \l__braid_step_level_bool
```

```
\seq_clear:N \l__braid_crossing_seq
 901
        \bool_set_false:N \l__braid_swap_crossing_bool
 902
 903
        \seq_if_empty:NF \l__braid_crossing_seq
 904
 905
          \int_step_inline:nnn {2} {\seq_count:N \l__braid_crossing_seq}
 906
 907
            \int_set:Nn \l__braid_tmpa_int {###1}
            \int_set:Nn \l__braid_tmpb_int {####1 - 1}
            \prop_get:NxN \l__braid_permutation_prop
 911
            {
 912
              \seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int}
 913
            } \l__braid_tmpa_tl
 914
            \prop_get:NxN \l__braid_permutation_prop
 915
 916
            {
              \seq_item: Nn \l__braid_crossing_seq {\l__braid_tmpb_int}
 917
            } \l__braid_tmpb_tl
 918
            \prop_put:NxV \l__braid_permutation_prop
              \seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpb_int}
            } \l__braid_tmpa_tl
 923
            \prop_put:NxV \l__braid_permutation_prop
 924
 925
              \seq_item: Nn \l__braid_crossing_seq {\l__braid_tmpa_int}
 926
 927
            } \l__braid_tmpb_tl
          }
 928
        }
 929
See if the current level is what was requested by the anchor.
        \int_compare:nT {\l__braid_crossing_int = \l__braid_anchor_level_int}
 930
 931
 932
          \prop_set_eq:NN \l__braid_anchor_prop \l__braid_permutation_prop
        }
 933
        \bool_if:NT \l__braid_step_level_bool
 934
 935
          \int_incr:N \l__braid_crossing_int
 936
 937
 938
This inverts the anchor permutation.
      \int_step_inline:nnnn {1} {1} {\l_braid_strands_int}
 939
 940
        \prop_get:NnN \l__braid_anchor_prop {##1} \l__braid_tmpa_tl
 941
        \prop_put:NVn \l__braid_inverse_prop \l__braid_tmpa_tl {##1}
 942
 943
      \prop_set_eq:NN \l__braid_anchor_prop \l__braid_inverse_prop
 944
This inverts the full permutation.
      \int_step_inline:nnnn {1} {1} {\l__braid_strands_int}
 945
 946
        \prop_get:\nn \l_braid_permutation_prop {##1} \l_braid_tmpa_tl
 947
 948
        \prop_put:NVn \l__braid_inverse_prop \l__braid_tmpa_tl {##1}
 949
      }
```

Now that we have the inverse, we can figure out our anchor. If the strand was recorded as -1, then we want to figure out the position from the braid as a whole so we don't bother with processing.

```
\tl_if_eq:VnF \l__braid_anchor_strand_tl {-1}
                              {
                         951
                       Now, see if we requested a strand by its position at the end of the braid.
                                \tl_set:Nx \l__braid_tmpa_tl {\seq_item:Nn \l__braid_anchor_seq {1}}
                                \tl_if_eq:VnT \l__braid_tmpa_tl {rev}
                         953
                         954
                                  \prop_get:NVN \l__braid_permutation_prop
                         955
                                  \l_braid_anchor_strand_tl \l_braid_anchor_strand_tl
                         956
                         957
                                \tl_if_eq:VnF \l__braid_anchor_level_tl {s}
                         958
                         959
                                  \tl_if_eq:VnTF \l__braid_anchor_level_tl {e}
                         960
                         961
                                     \prop_get:NVN \l__braid_inverse_prop
                         962
                                     \l__braid_anchor_strand_tl \l__braid_anchor_strand_tl
                         963
                                  }
                                     \prop_get:NVN \l__braid_anchor_prop
                                    \l__braid_anchor_strand_tl \l__braid_anchor_strand_tl
                         967
                         968
                         969
                              }
                         970
                       (End of definition for \__braid_count:NNN.)
\__braid_dim_value:n
                       Extract a length or a value from a PGF key.
    \__braid_value:n
                        972 \cs_new_nopar:Npn \__braid_dim_value:n #1
                        973 {
                              \dim_to_fp:n {\pgfkeysvalueof{/tikz/braid/#1}}
                         974
                        975 }
                         976 \cs_new_nopar:Npn \__braid_value:n #1
                         977 {
                              \pgfkeysvalueof{/tikz/braid/#1}
                        978
                        979 }
                       (End\ of\ definition\ for\ \_braid\_dim\_value:n\ and\ \_braid\_value:n.)
    \__braid_render:
                       This is the macro that converts the braid word into TikZ paths.
                         980 \cs_generate_variant:Nn \prop_get:NnN {NxN}
                        981 \cs_generate_variant:Nn \prop_put:Nnn {NxV}
                         982 \cs_generate_variant:Nn \tl_if_eq:nnTF {VnTF}
                         983 \cs_generate_variant:Nn \tl_if_eq:nnF {VnF}
                        984 \cs_generate_variant:Nn \tl_if_eq:nnT {VnT}
                        985
                        986 \cs_new_nopar:Npn \__braid_render:
                        987 {
                       Start by figuring out our anchor.
                             \tl_if_eq:VnTF \l__braid_anchor_strand_tl {-1}
                         988
                              {
                         989
```

The strand is -1 then we're working with the braid as if a node. We'll redefine this node later anyway.

```
\tl_set:cn {pgf@sh@ns@temporary braid node}{rectangle}
 990
        \tl_set:cx {pgf@sh@np@temporary braid node}{%
 991
          \exp_not:N\def
 992
          \exp_not:N\southwest
 993
 994
             \exp_not:N\pgfqpoint
 995
            {Opt}
 996
            {Opt}
 997
 998
          \exp_not:N\def
          \exp_not:N\northeast
            \exp_not:N\pgfqpoint
            {
1003
               \fp_to_dim:n
1004
               {
1005
                 (\l_braid_strands_int - 1)
1006
1007
                 abs(\__braid_dim_value:n {width})
1008
               }
1009
            }
             {
1012
               \fp_to_dim:n
1013
                 \l__braid_length_int * abs(\__braid_dim_value:n {height})
1014
                 + 2 * \__braid_dim_value:n {border~ height}
1015
1016
            }
1017
          }
1018
1019
        \pgfgettransform\l__braid_tmpa_tl
        \tl_set:cV {pgf@sh@nt@temporary braid node} \l__braid_tmpa_tl
        \tl_set:cV {pgf@sh@pi@temporary braid node} \pgfpictureid
        \pgfpointanchor{temporary braid node} {\__braid_value:n {anchor}}
1023
Adjustments due to the possibility of negative widths/heights
        \fp_set:Nn \l__braid_anchor_x_fp {
1024
          - \dim_use:c {pgf@x}
          - (1 - sign(\_braid_dim_value:n {width})) / 2
          * (\l_braid_strands_int - 1)
          * \__braid_dim_value:n {width}
1028
1029
        \fp_set:Nn \l__braid_anchor_y_fp {
1030
          - \dim_use:c {pgf@y}
1031
          - (1 - sign(\__braid_dim_value:n {height})) / 2
1032
1033
          \l__braid_length_int * abs(\__braid_dim_value:n {height})
1034
1035
          + 2 * \__braid_dim_value:n {border~ height}
          ) * sign(\__braid_dim_value:n {height})
1037
        }
      }
1038
      {
1039
```

```
The strand is not -1 so we're setting the anchor via strand and level numbers.
        \fp_set:Nn \l__braid_anchor_x_fp { - 1 * (\tl_use:N \l__braid_anchor_strand_tl - 1) * \_
1040
1041
        \tl_if_eq:VnTF \l__braid_anchor_level_tl {s}
1042
1043
1044
           \fp_set:Nn \l__braid_anchor_y_fp {0}
        }
        {
           \tl_if_eq:VnTF \l__braid_anchor_level_tl {e}
1048
             \fp_set:Nn \l__braid_anchor_y_fp {
1049
               -1 * \l__braid_length_int * \__braid_dim_value:n {height}
1050
               - sign(\__braid_dim_value:n {height})
1051
               * 2 * \__braid_dim_value:n {border~ height}
1052
             }
1053
          }
1054
1055
             \fp_set:Nn \l__braid_anchor_y_fp {
               -1 * \l__braid_anchor_level_tl * \__braid_dim_value:n {height}
1058
               - sign(\__braid_dim_value:n {height})
1059
               * \__braid_dim_value:n {border~ height}
1060
1061
1062
1063
1064
      \begin{scope}[
1065
        shift={
           (\fp_to_decimal:N \l__braid_anchor_x_fp pt,
           \fp_to_decimal:N \l__braid_anchor_y_fp pt
1069
        }
1070
      ]
1071
Initialise a prop for the individual strands.
      \prop_clear:N \l__braid_strands_prop
Initialise some lengths.
      \fp_zero:N \l__braid_height_fp
1073
      \fp_zero:N \l__braid_nudge_fp
1074
      \fp_zero:N \l__braid_control_fp
1075
This holds our current height of our strands.
      \fp_set:Nn \l__braid_height_fp
1076
1077
        sign(\__braid_dim_value:n {height})
1078
          \__braid_dim_value:n {border~ height}
1079
1080
This holds the total width of our strands.
      \fp_set:Nn \l__braid_width_fp
1082
      {
        (\l_braid_strands_int - 1) * \_braid_dim_value:n {width}
1083
```

+ 2 * sign(__braid_dim_value:n{width})

__braid_dim_value:n {floor~ border}

1084

Each crossing actually starts a little bit into the crossing space, as defined by the nudge factor.

```
\fp_set:Nn \l__braid_nudge_fp
1087
1088
        \__braid_value:n {nudge~ factor} * \__braid_dim_value:n {height}
1089
1090
This sets where the control points for the crossing curves will be.
      \fp_set:Nn \l__braid_control_fp
1092
        \__braid_value:n {control~ factor} * \__braid_dim_value:n {height}
1093
1094
      \fp_sub:\n\\l_braid_control_fp {\l_braid_nudge_fp}
1095
Initialise our strand paths with a \draw.
      \int_step_inline:nnnn {1} {1} {\l__braid_strands_int}
1096
1097
        \prop_get:NnN \l__braid_inverse_prop {##1} \l__braid_tmpa_tl
1098
        \prop_put:Nnx \l__braid_strands_prop {##1}
1099
1100
          \exp_not:N \draw[
            braid/every~ strand/.try,
            braid/strand~ ##1/.try
1104
1105
          \exp_not:N \__braid_moveto:nn {
            \fp_eval:n {(##1 - 1) * \__braid_dim_value:n {width} }
          } {0}
          \exp_not:N \__braid_lineto:nn {
            \fp_eval:n {(##1 - 1) * \__braid_dim_value:n {width} }
1109
            { \fp_to_decimal:N \l__braid_height_fp}
Add a load of coordinates at the start of each strand, indexed by both forward and
backward strand numbers.
1112
        \__braid_coordinate:xxxx {-##1-s} {-rev-\l__braid_tmpa_tl-s}
        {\phi_0} {\phi_0} = {\phi_0} * \phi_0
1113
1114
        \_braid_coordinate:xxxx {-##1-0} {-rev-\l_braid_tmpa_tl-0}
1115
        {\phi = {\phi = 1} * -1} * _braid_dim_value:n {width} }
1116
        { \fp_to_decimal:N \l__braid_height_fp}
1117
1118
    Run through any extra floors requested.
      \seq_map_inline: Nn \l__braid_floors_seq
1119
1120
        \tl_set:Nx \l__braid_tmpa_tl {\clist_item:nn {##1} {5}}
        \__braid_do_floor: Vxxxx \l__braid_tmpa_tl
1122
        {\fp_eval:n
          {
1124
            -1*sign(\__braid_dim_value:n{width})
1125
1126
            * \__braid_dim_value:n {floor~ border}
            + (\__braid_dim_value:n {width}) * (\clist_item:nn {##1} {1} - 1)
1128
          }
1129
```

}

```
{\sigma: \{ p_eval: n \}}
          ₹
                _braid_height_fp + ( \__braid_dim_value:n {height} ) * (\clist_item:nn {##1} {2})
1134
1135
          pt
        }
1136
        {\fp_eval:n {
             ((\clist_item:nn {##1} {3}) * \__braid_dim_value:n {width}
1138
             + 2 * sign(\__braid_dim_value:n{width})
1139
             * \__braid_dim_value:n {floor~ border} ) / \dim_to_fp:n {1cm}
1140
1141
        }
1142
        {\fp_eval:n {
1143
             (\clist_item:nn {##1} {4}) * ( \__braid_dim_value:n {height} ) / \dim_to_fp:n {1cm}
1144
1145
1146
1147
    Keep track of the crossing level for the floor.
      \int_zero:N \l__braid_crossing_int
1148
      \int_incr:N \l__braid_crossing_int
1149
1150
1151
      \seq_map_inline:Nn \l__braid_word_seq
Clear the flags for this segment of the braid word
        \seq_clear:N \l__braid_crossing_seq
        \bool_set_true: N \l__braid_step_level_bool
1154
        \bool_set_false:N \l__braid_floor_bool
        \bool_set_false:N \l__braid_swap_crossing_bool
        ##1
1157
If we're drawing a floor, do so straightaway.
        \bool_if:NT \l__braid_floor_bool
1158
            _braid_do_floor:Vxxxx \l__braid_crossing_int
           {\fp_eval:n
1162
               -1*sign(\__braid_dim_value:n{width})
1163
                 \__braid_dim_value:n {floor~ border}
1164
            }
            pt
1166
1167
           {\fp_to_decimal:N \l__braid_height_fp pt}
1168
           {\fp_eval:n { \l__braid_width_fp / \dim_to_fp:n {1cm} }}
1169
           {\fp_eval:n { ( \__braid_dim_value:n {height} ) / \dim_to_fp:n {1cm}}}
1170
1171
If we have a crossing, process it.
        \seq_if_empty:NF \l__braid_crossing_seq
           \int_set:Nn \l__braid_crossing_long_int
1174
1175
           ₹
                       \seq_item:Nn \l__braid_crossing_seq {\seq_count:N \l__braid_crossing_seq}
1176
             \seq_item:Nn \l__braid_crossing_seq {1}
1178
```

```
\int_set:Nn \l__braid_crossing_start_int
1179
          {
1180
1181
            \int_min:nn
            {
1182
              \seq_item: Nn \l__braid_crossing_seq {1}
            }
1184
            {
1185
              \seq_item:Nn \l__braid_crossing_seq {\seq_count:N \l__braid_crossing_seq}
1186
            }
          }
1188
1189
          \int_set:Nn \l__braid_crossing_end_int
1190
          {
1191
            \int_max:nn
1192
            ₹
              \seq_item: Nn \l__braid_crossing_seq {1}
1194
            {
1195
              \seq_item:Nn \l__braid_crossing_seq {\seq_count:N \l__braid_crossing_seq}
1196
          \int_set:Nn \l__braid_crossing_width_int
            \l__braid_crossing_end_int
1203
            \l__braid_crossing_start_int
1204
          }
1205
Step through the crossing
          \int_step_inline:nnn {2} {\seq_count:N \l__braid_crossing_seq}
1206
1207
            \bool_if:NTF \l__braid_default_crossing_bool
1208
              \int_set:Nn \l__braid_tmpa_int {###1}
              \int_set:Nn \l__braid_tmpb_int {####1 - 1}
            }
1214
              \int_set:Nn \l__braid_tmpa_int {####1 - 1}
              \int_set:Nn \l__braid_tmpb_int {###1}
1216
Keep track of the current permutation.
          \prop_get:NxN \l__braid_crossing_permutation_prop
1217
          1218
          \prop_get:NxN \l__braid_crossing_permutation_prop
1219
          {\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpb_int}} \l__braid_tmpb_tl
1220
1221
          \prop_put:NxV \l__braid_crossing_permutation_prop
          {\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpb_int}} \l__braid_tmpa_tl
          \prop_put:NxV \l__braid_crossing_permutation_prop
1224
          {\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int}} \l__braid_tmpb_tl
1225
Now get the strands corresponding to the ones involved in the crossing.
          \prop_get:NxN \l__braid_strands_prop
1226
          {\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int}} \l__braid_tmpa_tl
1227
```

```
\prop_get:NxN \l__braid_strands_prop
1228
           \{\ensuremath{\verb|l_braid_crossing_seq {l_braid_tmpb_int}}\} \ensuremath{\verb|l_braid_tmpb_tl|} \\
1229
The over-strand is easy as that's a single curve.
            \int_set:Nn \l__braid_crossing_start_factor_int {1}
1231 %
          \int_set:Nn \l__braid_crossing_end_factor_int {1}
1232 %
            \int_compare:nT {
1233 %
              \seq_item: Nn \l__braid_crossing_seq {\l__braid_tmpa_int}
1234 %
1235 %
              \l__braid_crossing_long_int
           }
1236 %
1237 %
             \int_set:Nn \l__braid_crossing_start_factor_int {0}
1238
             \int_set:Nn \l__braid_crossing_end_factor_int {0}
1239
1240
             \int_compare:nT {
1241
               ####1 = \seq_count:N \l__braid_crossing_seq
             }
             {
1244
1245
               \int_set:Nn \l__braid_crossing_end_factor_int {1}
             }
1246
             \int_compare:nT {
1247
               ####1 = 2
1248
1249
             {
1250
               \int_set:Nn \l__braid_crossing_start_factor_int {1}
1251
            }
1253 %
1254
1255
          \tl_put_right:Nx \l__braid_tmpa_tl
1256
             \exp_not:N \__braid_lineto:nn
1257
1258
             {\fp_eval:n
1259
               {
1260
                 (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int} - 1)
1261
                   \__braid_dim_value:n {width}
1262
               }
            }
             {\fp_eval:n { \l__braid_height_fp + \l__braid_nudge_fp * \l__braid_crossing_start_fa
1265
                 + \__braid_dim_value:n {height} * (####1 - 2)/(\seq_count:N \l__braid_crossing_s
     } }
1267
1268
             \exp_not:N \__braid_curveto:nnnnn
1269
1271
             {\fp_eval:n { \l_braid_control_fp
1273 %
                  * \l__braid_crossing_start_factor_int
                 * 1/(\seq_count:N \l__braid_crossing_seq - 1)}}
1274
1275
             {0}
1276
             {\fp_eval:n {- \l__braid_control_fp
1277
                  * \l__braid_crossing_end_factor_int
1278 %
                 * 1/(\seq_count:N \l__braid_crossing_seq - 1)}}
1279
```

```
1282
               ₹
                 (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpb_int} - 1)
1283
                   \__braid_dim_value:n {width}
1284
1285
             }
1286
             {\fp_eval:n
1287
1288
                 \l__braid_height_fp
                 + \__braid_dim_value:n {height} * (####1 - 1)/(\seq_count:N \1__braid_crossing_s
                 - \l__braid_nudge_fp * \l__braid_crossing_end_factor_int
               }
1292
            }
1293
1294
The under-strand is a bit more complicated as we need to break it in the middle.
            \int_set:Nn \l__braid_crossing_start_factor_int {1}
            \int_set:Nn \l__braid_crossing_end_factor_int {1}
    %
    %
1297
            \int_compare:nT {
    %
              \seq_item: Nn \l__braid_crossing_seq {\l__braid_tmpb_int}
1298
    %
1299
1300 %
              \label{local_loss} $$ l_beautiful crossing_long_int $$
           }
1301 %
1302 %
            {
             \int_set:Nn \l__braid_crossing_start_factor_int {0}
1303
             \int_set:Nn \l__braid_crossing_end_factor_int {0}
1304
1305
             \int_compare:nT {
               ####1 = \seq_count:N \l__braid_crossing_seq
1308
1309
             {
               \int_set:Nn \l__braid_crossing_end_factor_int {1}
1311
             \int_compare:nT {
1312
               ####1 = 2
               \int_set:Nn \l__braid_crossing_start_factor_int {1}
1316
            }
1317
           }
1318 %
1319
          \tl_put_right:Nx \l__braid_tmpb_tl
1321
             \exp_not:N \__braid_lineto:nn
1322
1323
             {\fp_eval:n
1324
               {
1325
                 (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpb_int} - 1)
1326
                   \__braid_dim_value:n {width}
1327
               }
            }
1329
             {\fp_eval:n { \l__braid_height_fp + \l__braid_nudge_fp * \l__braid_crossing_start_fa
1330
                 + \_braid_dim_value:n {height} * (####1 - 2)/(\seq_count:N \l_braid_crossing_s
1332
            } }
```

 ${\sigma: n}$

```
1334
            \exp_not:N \__braid_curveto:nnnnn
1335
1336
            {0}
1338
              \fp_eval:n {
1339
                 \l__braid_control_fp * (.5 - \__braid_value:n {gap} * (\seq_count:N \l__braid_c
1340
1341
                  * \l__braid_crossing_start_factor_int
              }
            }
1343
            {
1345
              \fp_eval:n {
1346
                 - (.5 - \__braid_value:n {gap} * (\seq_count:N \l__braid_crossing_seq - 1) ) / 3
1347
                \__braid_bezier_tangent:nnnnn
1348
                \{.5 - \_ braid\_value:n \{gap\} * (\seq\_count:N \l__braid\_crossing\_seq - 1) \}
1349
                {0}
1350
                {0}
1351
                {
                   (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int}
                  - \seq_item: Nn \l__braid_crossing_seq {\l__braid_tmpb_int})
                   * \__braid_dim_value:n {width}
1355
                }
1356
                {
1357
                   (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int}
1358
                    \seq_item: Nn \l__braid_crossing_seq {\l__braid_tmpb_int})
1359
                    \__braid_dim_value:n {width}
1360
1361
              }
1362
            }
            {
              \fp_eval:n {
                -(.5 - \_braid_value:n {gap} * (\seq_count:N \l_braid_crossing_seq - 1) ) / 3
1366
1367
                \__braid_bezier_tangent:nnnnn
                {.5 - \_braid_value:n {gap} * (\seq_count:N \l_braid_crossing_seq - 1) }
1368
                {0}
1369
                {
1370
                   \l_braid_control_fp * 1/(\seq_count:N \l_braid_crossing_seq - 1)
1371
1372
                    * \l_braid_crossing_start_factor_int
                }
                {
                   \__braid_dim_value:n {height} * 1/(\seq_count:N \l__braid_crossing_seq - 1)
1376
                  - \l__braid_nudge_fp * \l__braid_crossing_start_factor_int
                  - \l_braid_nudge_fp * \l_braid_crossing_end_factor_int
1377
                   - \l__braid_control_fp * 1/(\seq_count:N \l__braid_crossing_seq - 1)
1378
                   * \l__braid_crossing_end_factor_int
1379
                }
1380
1381
                   \__braid_dim_value:n {height} * 1/(\seq_count:N \l__braid_crossing_seq - 1)
1382
                   - \l__braid_nudge_fp * \l__braid_crossing_start_factor_int
1383
                   - \l__braid_nudge_fp * \l__braid_crossing_end_factor_int
                }
              }
1386
            }
```

```
1388
            {
1389
              \fp_eval:n {
1390
                (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpb_int} - 1)
1391
                 * \__braid_dim_value:n {width} +
1392
                \__braid_bezier_point:nnnnn
1393
                {.5 - \_braid_value:n {gap} * (\seq_count:N \l_braid_crossing_seq - 1) }
1394
                {0}
1395
                {0}
                {
                   (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int}
                  - \seq_item: Nn \l__braid_crossing_seq {\l__braid_tmpb_int})
1399
                    \__braid_dim_value:n {width}
1400
                }
1401
                {
1402
                   (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int}
1403
                    \seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpb_int})
1404
                    \__braid_dim_value:n {width}
              }
            }
            {
              \fp_eval:n {
1410
                \l_braid_height_fp
1411
                + \l__braid_nudge_fp * \l__braid_crossing_start_factor_int
1412
                  \_braid_dim_value:n {height} * (####1 - 2)/(\seq_count:N \l__braid_crossing_s
1413
1414
1415
                \__braid_bezier_point:nnnnn
                {.5 - \_braid_value:n {gap} * (\seq_count:N \l_braid_crossing_seq - 1) }
1416
                {0}
                  \l_braid_control_fp * 1/(\seq_count:N \l_braid_crossing_seq - 1)
1420 %
                   * \l__braid_crossing_start_factor_int
                }
1421
                {
1422
                   \_braid_dim_value:n {height} * 1/(\seq_count:N \l_braid_crossing_seq - 1)
1423
                   - \l__braid_nudge_fp * \l__braid_crossing_start_factor_int
1424
                    \verb|\label{locality} $$ \line 1_braid_nudge_fp * \line 1_braid_crossing_end_factor_int $$
1425
                  - \l_braid_control_fp * 1/(\seq_count:N \l_braid_crossing_seq - 1)
1426
                   * \l__braid_crossing_end_factor_int
                }
                {\_braid_dim_value:n {height} * 1/(\seq_count:N \l_braid_crossing_seq - 1)
1430
                  - \l__braid_nudge_fp * \l__braid_crossing_start_factor_int
                   - \l__braid_nudge_fp * \l__braid_crossing_end_factor_int
1431
                }
1432
              }
1433
            }
1434
1435
            \exp_not:N \__braid_moveto:nn
1436
1437
              \fp_eval:n {
                (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpb_int} - 1)
1440
                * \__braid_dim_value:n {width} +
                \__braid_bezier_point:nnnnn
1441
```

```
{.5 + \__braid_value:n {gap} * (\seq_count:N \l__braid_crossing_seq - 1) }
                {0}
1443
                {0}
1444
                {
1445
                  (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int}
1446
                  - \seq_item: Nn \l__braid_crossing_seq {\l__braid_tmpb_int})
                    \__braid_dim_value:n {width}
                }
                {
                  (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int}
                  - \seq_item: Nn \l__braid_crossing_seq {\l__braid_tmpb_int})
                    \__braid_dim_value:n {width}
1453
1454
             }
1455
           }
1456
            {
1457
              \fp_eval:n {
1458
                \l__braid_height_fp
                + \l__braid_nudge_fp * \l__braid_crossing_start_factor_int
                + \_braid_dim_value:n {height} * (###1 - 2)/(\seq_count:N \l_braid_crossing_s
                \__braid_bezier_point:nnnnn
                {.5 + \__braid_value:n {gap} * (\seq_count:N \l__braid_crossing_seq - 1) }
1464
                {0}
1465
                {
1466
                  \l__braid_control_fp * 1/(\seq_count:N \l__braid_crossing_seq - 1)
1467
1468 %
                   * \l__braid_crossing_start_factor_int
                }
1469
1470
                  \__braid_dim_value:n {height} * 1/(\seq_count:N \l__braid_crossing_seq - 1)
                  - \l__braid_nudge_fp * \l__braid_crossing_start_factor_int
                  - \l__braid_nudge_fp * \l__braid_crossing_end_factor_int
1473
                  - \l_braid_control_fp * 1/(\seq_count:N \l_braid_crossing_seq - 1)
1474
                   * \l__braid_crossing_end_factor_int
1475
1476
                {\_braid_dim_value:n {height} * 1/(\seq_count:N \l_braid_crossing_seq - 1)
1477
                   \l__braid_nudge_fp * \l__braid_crossing_start_factor_int
1478
                    \l__braid_nudge_fp * \l__braid_crossing_end_factor_int
1479
1480
             }
           }
           \exp_not:N \__braid_curveto:nnnnnn
1485
1486
              \fp_eval:n {
1487
                (.5 - \_braid_value:n {gap} * (\seq_count:N \l_braid_crossing_seq - 1) ) / 3 *
1488
                \__braid_bezier_tangent:nnnnn
                {.5 + \__braid_value:n {gap} * (\seq_count:N \l__braid_crossing_seq - 1) }
                {0}
                {0}
                {
1494
                  (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int}
```

- \seq_item: Nn \l__braid_crossing_seq {\l__braid_tmpb_int})

```
\__braid_dim_value:n {width}
                }
1497
                {
                  (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int}
1499
                    \seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpb_int})
1500
                    \__braid_dim_value:n {width}
1501
1502
              }
1503
           }
            {
              \fp_eval:n {
                (.5 - \_braid_value:n {gap} * (\seq_count:N \l_braid_crossing_seq - 1) ) / 3 *
1507
                \__braid_bezier_tangent:nnnnn
1508
                \{.5 + \_braid\_value:n \{gap\} * (\seq\_count:N \l__braid\_crossing\_seq - 1) \}
1509
                {0}
1510
                {
1511
                      _braid_control_fp * 1/(\seq_count:N \l__braid_crossing_seq - 1)
1512
                    * \l__braid_crossing_start_factor_int
1513
                }
                {
                     _braid_dim_value:n {height} * 1/(\seq_count:N \l__braid_crossing_seq - 1)
                  - \l_braid_nudge_fp * \l_braid_crossing_start_factor_int
1517
                  - \l_braid_nudge_fp * \l_braid_crossing_end_factor_int
1518
                  - \l_braid_control_fp * 1/(\seq_count:N \l_braid_crossing_seq - 1)
1519
                   * \l__braid_crossing_end_factor_int
1520 %
1521
                {\_braid_dim_value:n {height} * 1/(\seq_count:N \l_braid_crossing_seq - 1)
1522
                  - \l__braid_nudge_fp * \l__braid_crossing_start_factor_int
1523
                  - \l__braid_nudge_fp * \l__braid_crossing_end_factor_int
1524
              }
           }
1528
            {0}
1529
            {\fp_eval:n {
1530
                 - \l__braid_control_fp * (.5 - \__braid_value:n {gap} * (\seq_count:N \l__braid
1531
                 * \l_braid_crossing_end_factor_int
1532 %
                * 1/(\seq_count:N \l__braid_crossing_seq - 1)}
1533
1534
            {\sigma: n}
1538
                (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int} - 1)
                  \__braid_dim_value:n {width}
1539
              }
1540
           }
1541
            {\fp_eval:n
1542
              {
1543
                \l__braid_height_fp
1544
                  \_braid_dim_value:n {height} * (####1 - 1)/(\seq_count:N \l__braid_crossing_s
1545
                 - \l__braid_nudge_fp * \l__braid_crossing_end_factor_int
              }
           }
1548
```

```
Now put those new strands back in the prop.
          \prop_put:NxV \l__braid_strands_prop
          {\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpb_int}} \l__braid_tmpa_tl
1552
          \prop_put:NxV \l__braid_strands_prop
1553
          1554
If the strands are more than one apart, the intermediate strands need to be broken as
well.
          \int_compare:nT
1555
1556
            \int_max:nn
            {
              \seq_item: Nn \l__braid_crossing_seq {####1 - 1}
            }
            {
1561
              \seq_item: Nn \l__braid_crossing_seq {####1}
1562
            }
1563
1564
            \int_min:nn
1565
            {
1566
              \seq_item:Nn \l__braid_crossing_seq {####1 - 1}
1567
            }
            {
1570
              \seq_item: Nn \l__braid_crossing_seq {####1}
            }
1571
1572
            > 1
          }
1573
1574
            \int_step_inline:nnnn
1575
            {
1576
              \int_min:nn
1577
              {
                \seq_item:Nn \l__braid_crossing_seq {####1 - 1}
              }
              {
                \seq_item: Nn \l__braid_crossing_seq {####1}
1582
              }
1583
              + 1}
1584
            {1}
1585
            {
1586
              \int_max:nn
1587
              {
1588
                \seq_item:Nn \l__braid_crossing_seq {####1 - 1}
              }
              {
1591
                \seq_item: Nn \l__braid_crossing_seq {####1}
1592
              }
1593
              - 1
1594
            }
1595
            {
1596
1597
              \prop_get:NnN \l_braid_strands_prop {#######1} \l_braid_tmpa_tl
1598
```

}

1550

\tl_put_right:Nx \l__braid_tmpa_tl

```
\exp_not:N \__braid_lineto:nn
1601
                   {\phi_0} {\phi_0} 
                   {\sigma: p_eval: n}
1603
1604
                       \l__braid_height_fp + \l__braid_nudge_fp
1605
                       + .5 * \l__braid_control_fp / (\seq_count:N \l__braid_crossing_seq - 1)
1606
                       + \__braid_dim_value:n {height} * (###1 - 2)/(\seq_count:N \l__braid_cros
                   }
                   \verb|\exp_not:N \  \  | \_braid_moveto:nn|
                   {p_eval:n {(#######1 - 1) * \_braid_dim_value:n {width} }}
1611
                   {\fp_eval:n
1612
1613
                     {
                       \l__braid_height_fp
1614
                       - \l_braid_nudge_fp - .5 * \l_braid_control_fp / (\seq_count:N \l_braid
1615
                       + \_braid_dim_value:n {height} * (####1 - 1)/(\seq_count:N \l__braid_cros
1616
1617
                   }
                }
                 \prop_put:NnV \l__braid_strands_prop {#######1} \l__braid_tmpa_tl
1621
              }
1622
          }
1623
Reset the current long
          \int_compare:nTF
            \seq_item: Nn \l__braid_crossing_seq {\l__braid_tmpa_int}
1626
1627
            \l__braid_crossing_long_int
1628
1629
1630
             \int_set:Nn \l__braid_crossing_long_int {\seq_item:Nn \l__braid_crossing_seq {\l__br
1631
1632
1633
          \int_compare:nT
1635
          {
            \seq_item: Nn \l__braid_crossing_seq {\l__braid_tmpb_int}
1637
             \l__braid_crossing_long_int
1638
1639
1640
             \int_set:Nn \l__braid_crossing_long_int {\seq_item:Nn \l__braid_crossing_seq {\l__br
1641
1642
          }
          }
1645
1646
If we're to step the level, increase the height and add a load of coordinates.
        \bool_if:NT \l__braid_step_level_bool
1647
1648
          \fp_add:\n \l__braid_height_fp { \__braid_dim_value:n {height} }
1649
```

```
1650
          \int_step_inline:nnnn {1} {1} {\l__braid_strands_int}
1651
1652
             \prop_get:NnN \l__braid_crossing_permutation_prop
1653
            {####1} \l__braid_tmpb_tl
1654
             \prop_get:NVN \l__braid_inverse_prop
1655
             \l__braid_tmpb_tl \l__braid_tmpa_tl
1656
1657
            \__braid_coordinate:xxxx
            {-\l_braid_tmpb_tl-\int_use:N \l_braid_crossing_int}
            {-rev-\l_braid_tmpa_tl-\int_use:N \l_braid_crossing_int }
            {\phi_0 * \ (\#\#\#1 - 1) * \_braid_dim_value:n {width} }}
1661
             {\fp_to_decimal:N \l__braid_height_fp}
1662
1663
1664
           \int_incr:N \l__braid_crossing_int
1665
1666
      }
1667
      fp_add:Nn l_braid_height_fp
        sign(\__braid_dim_value:n {height})
1671
          \__braid_dim_value:n {border~ height}
1672
1673
Add a little bit to the end of each strand, together with some coordinates.
      \int_step_inline:nnnn {1} {1} {\l__braid_strands_int}
1675
        \prop_get:NxN \l__braid_strands_prop {##1} \l__braid_tmpa_tl
1676
        \prop_get:NxN \l__braid_permutation_prop {##1} \l__braid_tmpb_tl
1677
1678
        \tl_put_right:Nx \l__braid_tmpa_tl {
1679
          \exp_not:N \__braid_lineto:nn
1680
          {\fp_eval:n { (##1 - 1) * \__braid_dim_value:n {width} }}
1681
          {\fp_to_decimal:N \l__braid_height_fp}
          coordinate (-rev-##1-e)
          coordinate (-\l__braid_tmpb_tl-e)
1685
        }
1686
1687
        \prop_put:NnV \l__braid_strands_prop {##1} \l__braid_tmpa_tl
1688
1689
This is where we actually carry out the drawing commands.
      \int_step_inline:nnnn {1} {1} {\l__braid_strands_int}
1690
1691
        \prop_get:NnN \l__braid_strands_prop {##1} \l__braid_tmpa_tl
1692
        \tl_use:N \l__braid_tmpa_tl
1693
1694
Finally, put a node around the whole braid if it's been named
      \tl_if_empty:cF {tikz@fig@name}
1695
1696
        \tl_gset:cn {pgf@sh@ns@ \tl_use:c{tikz@fig@name} }{rectangle}
1697
        \tl_gset:cx {pgf@sh@np@ \tl_use:c{tikz@fig@name} }{%
1698
```

```
\exp_not:N\def
1699
          \verb|\exp_not:N\southwest|
1700
1701
            \exp_not:N\pgfqpoint
            {
1703
               \fp_to_dim:n
1704
               {
1705
                 min(0,
                 (\l__braid_strands_int - 1)
                 (\__braid_dim_value:n {width})
1710
              }
            }
1712
            {
1713
               fp_{to\_dim:n}
                 min(0,
1716
                 \l__braid_length_int * (\__braid_dim_value:n {height})
                 + 2 * sign(\_braid_dim_value:n {height}) *
                 \__braid_dim_value:n {border~ height}
1720
              }
            }
1723
          \exp_not:N\def
1724
          \exp_not:N\northeast
1725
1726
            \exp_not:N\pgfqpoint
1727
               \fp_to_dim:n
               {
1731
                 max(0.
                 (\l__braid_strands_int - 1)
1733
                 (\__braid_dim_value:n {width})
1734
1735
              }
1736
            }
1737
            {
               \fp_to_dim:n
               {
                 max(0,
1741
                 \l__braid_length_int * (\__braid_dim_value:n {height})
1742
                 + 2 * sign(\__braid_dim_value:n {height}) *
1743
                 \__braid_dim_value:n {border~ height}
1744
1745
              }
1746
            }
1747
1748
          }
1749
        }%
1750
        \pgfgettransform\l__braid_tmpa_tl
        \tl_gset:cV {pgf@sh@nt@ \tl_use:c{tikz@fig@name} } \l__braid_tmpa_tl
1751
        \tl_gset:cV {pgf@sh@pi@ \tl_use:c{tikz@fig@name} } \pgfpictureid
1752
```

```
1753
                                      \end{scope}
                                1754
                                1755 }
                                (End of definition for \__braid_render:.)
                               These are our interfaces to the TikZ code.
         \__braid_moveto:nn
         \__braid_lineto:nn
                                1756 \cs_new_nopar:Npn \__braid_moveto:nn #1#2
    \_braid_curveto:nnnnnn
                                1757 {
   \__braid_coordinate:nnnn
                                      (#1 pt, #2 pt)
                                1758
                                1759 }
                                    \cs_new_nopar:Npn \__braid_lineto:nn #1#2
                                1760
                                1761
                                      -- (#1 pt, #2 pt)
                                1762
                                1763 }
                                    \cs_new_nopar:Npn \__braid_curveto:nnnnnn #1#2#3#4#5#6
                                1764
                                       -- +(5 pt, 0) -- +(0 pt, 0pt)
                                1767 % -- +(#1 pt, #2 pt) -- (#5 pt + #3 pt, #6 pt + #4 pt) -- (#5 pt, #6 pt)
                                      .. controls +(#1 pt, #2 pt) and +(#3 pt, #4 pt)
                                      .. (#5 pt, #6 pt)
                                1770 }
                                    \cs_new_nopar:Npn \__braid_coordinate:nnnn #1#2#3#4
                                1771
                                1772
                                      \coordinate[alias=#2] (#1) at (#3 pt,#4 pt);
                                1773
                                1774 }
                                1775 \cs_generate_variant:Nn \__braid_coordinate:nnnn {xxxx}
                                (End of definition for \__braid_moveto:nn and others.)
                               Used to calculate intermediate points and tangents on a bezier curve.
\__braid_bezier_point:nnnnn
        \ braid bezier tangent:nnnnn
                                1776 \cs_new_nopar:Npn \__braid_bezier_point:nnnnn #1#2#3#4#5
                                1777 {
                                      \fp_eval:n
                                1778
                                      {
                                1779
                                        (1 - (#1)) * (1 - (#1)) * (1 - (#1)) * (#2)
                                1780
                                1781
                                        3 * (1 - (#1)) * (1 - (#1)) * (#1) * (#3)
                                        3 * (1 - (#1)) * (#1) * (#1) * (#4)
                                1784
                                        (#1) * (#1) * (#1) * (#5)
                                1786
                                1787
                                1788 }
                                    \cs_new_nopar:Npn \__braid_bezier_tangent:nnnnn #1#2#3#4#5
                                1789
                                1790 {
                                      \fp_eval:n
                                1791
                                        3 * (1 - (#1)) * (1 - (#1)) * (#3 - (#2))
                                        6 * (1 - (#1)) * (#1) * (#4 - (#3))
                                1795
                                1796
                                        3 * (#1) * (#1) * (#5 - (#4))
                                1798
                                1799 }
```

```
1800 \cs_new_nopar:Npn \__braid_do_floor:nnnnn #1#2#3#4#5
1801 {
       \pic[pic~ type=floor,
1802
         xscale=#4,
1803
         yscale=#5,
1804
         at={(#2,#3)},
1805
         braid/every~ floor/.try,
1806
         braid/floor~#1/.try,
      ];
1808
1809 }
1810 \cs_generate_variant:Nn \__braid_do_floor:nnnnn {Vxxxx}
(\mathit{End}\ of\ definition\ for\ \verb|\_\_braid\_bezier\_point:nnnnn\ \mathit{and}\ \verb|\_\_braid\_bezier\_tangent:nnnnn.|)
1811 \ExplSyntaxOff
```