The Tilings package: code

Andrew Stacey loopspace@mathforge.org

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1 Introduction

This is a TikZ library for drawing tiles, such as Penrose tiles (kite/dart, rhombus, and pentagon versions) and the aperiodical polykite tiles. It provides two methods of drawing: one in which an automatic pattern is built, and one where the tiles can be placed "by hand". The tiles can be shaped and (hopefully!) still fit together. For full user documentation, see the tilings.pdf file.

2 Implementation

1 (@@=tilings)

2.1 Initialisation

We use the spath3 library for manipulating the paths that will make up the tiles.

Now we move in to the realm of LATEX3.

9 \ExplSyntaxOn

Start with some basic paths (lines) for the sides of the tiles so that we know that we have well-defined tiles at the outset. These are globally defined as we will frequently want to define them in one tikzpicture and use them in another.

```
10 \tl_new:N \g__tilings_side_a_tl
11 \tl_new:N \g__tilings_side_b_tl
12 \tl_new:N \g__tilings_side_c_tl
```

```
13 tl_new:N \g_tilings_side_d_tl
      14 tl_new:N \g_tilings_side_e_tl
      _{15} \tl_new:N \g__tilings_side_A_tl
      _{16} \ \text{tl_new:N } \ \text{g\_tilings\_side\_B\_tl}
      17 \tilde{g}_t \approx \tilde{g}_t \sin g_s = \tilde{g}_t \sin g_s = \tilde{g}_t = \tilde{g}
      18 \tl_new:N \g_tilings_side_D_tl
      20 \tl_new:c {g__tilings_side_1_tl}
      21 \tl_new:c {g__tilings_side_2_tl}
      22 \tl_new:c {g__tilings_side_3_tl}
      23 \tl_gset:Nn \g__tilings_side_a_tl
      24 {
                      \pgfsyssoftpath@movetotoken{0pt}{0pt}
                      \pgfsyssoftpath@linetotoken{1pt}{0pt}
      27 }
      28 \tl_gset_eq:NN \g__tilings_side_b_tl \g__tilings_side_a_tl
      29 tl_gset_eq:NN \g_tilings_side_c_tl \g_tilings_side_a_tl
      30 \tl_gset_eq:NN \g__tilings_side_d_tl \g__tilings_side_a_tl
      31 \tl_gset_eq:NN \g__tilings_side_e_tl \g__tilings_side_a_tl
      32 \tl_gset_eq:NN \g__tilings_side_A_tl \g__tilings_side_a_tl
      33 \tl_gset_eq:NN \g__tilings_side_B_tl \g__tilings_side_a_tl
      34 tl_gset_eq:NN \g_tilings_side_C_tl \g_tilings_side_a_tl
      35 \tl_gset_eq:NN \g__tilings_side_D_tl \g__tilings_side_a_tl
      36 \tl_gset_eq:NN \g__tilings_side_E_tl \g__tilings_side_a_tl
      _{\mbox{\scriptsize 37}}\ \mbox{\tl}_{\mbox{\scriptsize get}}\ \mbox{\ensuremath{\mbox{\scriptsize g}}\_\mbox{\tl}}\ \mbox{\tl}_{\mbox{\scriptsize gl}}\ \mbox{\t
      _{\mbox{\scriptsize 38}} \tl_gset_eq:cN {g__tilings_side_2_tl} \g__tilings_side_a_tl
      We need a few temporary variables to hold intermediate calculations.
      40 \fp_new:N \l__tilings_tmpa_fp
      41 \fp_new:N \l__tilings_tmpb_fp
      42 \fp_new:N \l__tilings_tmpc_fp
      43 \fp_new:N \l__tilings_saved_x_fp
      44 \fp_new:N \l__tilings_saved_y_fp
      45 \str_new:N \l__tilings_tmpa_str
      46 \str_new:N \l__tilings_tmpb_str
      47 \seq_new:N \l__tilings_tmpa_seq
      48 \tl_new:N \l__tilings_tmpa_tl
      49 \tl_new:N \l__tilings_tmpb_tl
      50 \tl_new:N \l__tilings_tmpc_tl
      51 \tl_new:N \l__tilings_tmpd_tl
      52 \tl_new:N \l__tilings_tmp_tile_path_tl
      53 \tl_new:N \l__tilings_action_lms_tl
      54 \tl_new:N \l__tilings_parameters_lms_tl
      55 \int_new:N \l__tilings_tmpa_int
      56 \int_new:N \l__tilings_tmpb_int
      57 \fp_new:N \l__tilings_xa_fp
      58 \fp_new:N \l__tilings_ya_fp
      59 \fp_new:N \l__tilings_xb_fp
      60 \fp_new:N \l__tilings_yb_fp
      61 \dim_new:N \l__tilings_xa_dim
      62 \dim_new:N \l__tilings_ya_dim
      63 \dim_new:N \l__tilings_xb_dim
      64 \dim_new:N \l__tilings_yb_dim
      65 \dim_new:N \g__tilings_xa_dim
      66 \dim_new:N \g__tilings_ya_dim
      67 \dim_new:N \g__tilings_xb_dim
      68 \dim_new:N \g__tilings_yb_dim
      69 \prop_new:N \l__tilings_tmpa_prop
```

ngs_tmpa_fp
ngs_tmpb_fp

ngs_tmpc_fp

saved_x_fp

_saved_y_fp gs_tmpa_str

gs_tmpb_str

gs_tmpa_seq

ngs_tmpa_tl

ngs_tmpb_tl

ngs_tmpc_tl

ngs_tmpd_tl

gs_tmpa_int

gs_tmpb_int

ings_xa_dim

ings_ya_dim

ings_xb_dim

ings_yb_dim

ings_xa_dim

ings_ya_dim

ings_xb_dim

ings_yb_dim

s_tmpa_prop

ngs_cw_bool

pdate saved bool

Lative_bool

s_output_tl

70 \bool_new:N \l__tilings_cw_bool

71 \bool_new:N \l__tilings_update_saved_bool

```
72 \bool_new:N \l__tilings_relative_bool
73 \bool_new:N \l__tilings_edge_bool
74 \str_const:Nn \c__tilings_colon_str {:}
75 \str_const:Nn \c__tilings_comma_str {,}
76 \fp_const:Nn \c__tilings_cm_fp {\dim_to_fp:n {1cm}}
77 \tl_new:N \g_tilings_output_tl
78 \fp_new:N \g__tilings_output_a_fp
79 \fp_new:N \g__tilings_output_b_fp
80 \prop_new:N \g__tilings_tilenames_prop
81 \regex_const:Nn \c__tilings_anchor_regex {\s\w+\Z}
82 \cs_generate_variant:Nn \seq_set_split:Nnn {NVV}
83 \cs_generate_variant:Nn \regex_extract_once:NnNTF {NVNTF}
84 \cs_generate_variant:Nn \tl_if_eq:nnT {nVT}
85 \cs_generate_variant:Nn \tl_if_in:NnT {NVT}
86 \cs_generate_variant:Nn \prop_item:Nn {cV}
87 \cs_generate_variant:Nn \tl_if_head_is_group_p:n {V}
```

 $(End\ definition\ for\ \verb+\l_tilings_tmpa_fp\ and\ others.)$

2.2 Helpful Error Messages

```
%% \msg_new:nnn { tilings }{ not baked }
%% { Tile~ #1~ has~ not~ been~ baked. }
%% \msg_new:nnn { tilings }{ no tile }
%% \msg_new:nnn { tilings }{ no tile }
%% \msg_new:nnn { tilings }{ no side }
%% \msg_new:nnn { tilings }{ tile no edge }
%% \msg_new:nnn { tilings }{ tile no edge }
%% { Tile~ #1~ doesn't~ have~ an~ edge~ labelled~ #2;
%% ~ available~ edges~ are~ #3.}
%% \msg_new:nnn { tilings }{ no edge }
%% { Either~ tile~ #1~ doesn't~ exist
%% ~ or~ it~ doesn't~ have~ an~ edge~ labelled~ #2.}
```

2.3 Creating the Tiles

ise_path:Nn

When defining the path for a side, we normalise so that it starts at the origin and ends at (1pt, 0pt).

```
100 \cs_new_nopar:Npn \__tilings_normalise_path:Nn #1#2
```

Get the initial point of the path and convert to floating point.

```
\text{\group_begin:}
\text{\group_begin:}
\text{\group_begin:}
\text{\group_begin:}
\text{\group_tilings_tmpa_tl {\pmu2}}
\text{\pmu2}
\text{\pmu3} \text{\p
```

Get the final point of the path, and compute the difference of the final and initial points.

The resulting numbers, say a and b, will be put into a matrix to rotate and scale the path. The formula for the matrix is:

$$\frac{1}{a^2 + b^2} \begin{bmatrix} a & b \\ -b & a \end{bmatrix}$$

```
\spath_finalpoint:Nn \l__tilings_tmpa_tl {#2}

\fp_set:Nn \l__tilings_tmpa_fp

\ftl_head:N \l__tilings_tmpa_tl - \l__tilings_tmpa_fp}

\tl_set:Nx \l__tilings_tmpa_tl {\tl_tail:N \l__tilings_tmpa_tl}

\fp_set:Nn \l__tilings_tmpb_fp

\t\t\_head:N \l_tilings_tmpa_tl - \l_tilings_tmpb_fp}
```

Now compute the square of the length of the path for scaling.

```
\fp_set:Nn \l__tilings_tmpc_fp
{\l__tilings_tmpa_fp^2 + \l__tilings_tmpb_fp^2}
```

```
\fp_set:Nn \l__tilings_tmpa_fp {\l__tilings_tmpa_fp/\l__tilings_tmpc_fp}
                                      \fp_set:Nn \l__tilings_tmpb_fp {\l__tilings_tmpb_fp/\l__tilings_tmpc_fp}
                            116
                                      \fp_set:Nn \l__tilings_tmpc_fp {-\l__tilings_tmpb_fp}
                         Now construct the matrix.
                                      \tl_set:Nx \l__tilings_tmpb_tl
                            119
                                          {\fp_use:N \l__tilings_tmpa_fp}
                            120
                                          {\fp_use:N \l__tilings_tmpc_fp} % swapped
                                          {\fp_use:N \l__tilings_tmpb_fp} % swapped
                                          {\fp_use:N \l__tilings_tmpa_fp}
                            123
                            124
                         Get the initial point back again for the translation part.
                                      \spath_initialpoint:Nn \l__tilings_tmpa_tl {#2}
                         But we need to premultiply by the matrix because of how the transformations are applied.
                                      \fp_set:Nn \l__tilings_tmpa_fp
                            126
                            127
                                          (-1) * \label{local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_lo
                            128
                                         + (-1) * \l__tilings_tmpb_fp * \tl_tail:N \l__tilings_tmpa_tl
                            129
                            130
                                      \fp_set:Nn \l__tilings_tmpb_fp
                            131
                            132
                                          (-1) * \l__tilings_tmpa_fp * \tl_tail:N \l__tilings_tmpa_tl
                                              \l__tilings_tmpb_fp * \tl_head:N \l__tilings_tmpa_tl
                            135
                         Finally, we apply the transformation to the path.
                                      \tl_put_right:Nx \l__tilings_tmpb_tl {
                            136
                                          {\fp_to_dim:N \l__tilings_tmpa_fp}
                            137
                                          {\fp_to_dim:N \l__tilings_tmpb_fp}
                            138
                            139
                                      \spath_transform: NnV \l__tilings_tmpa_tl {#2} \l__tilings_tmpb_tl
                            140
                                      \tl_gset_eq:NN \g__tilings_output_tl \l__tilings_tmpa_tl
                                      \group_end:
                            142
                                      \tl_set_eq:NN #1 \g__tilings_output_tl
                            143
                                      \tl_gclear:N \g__tilings_output_tl
                            144
                            145 }
                            146 \cs_generate_variant:Nn \__tilings_normalise_path:Nn {NV, cn, cV}
                            \cs_new_protected_nopar:Npn \__tilings_normalise_path:N #1
                                      \__tilings_normalise_path:NV #1#1
                            149
                            150 }
                            \cs_generate_variant:Nn \__tilings_normalise_path:N {c}
                         (End\ definition\ for\ \_\_tilings\_normalise\_path:Nn.)
etTilingPath This sets the path corresponding to a particular side to the current path, and normalises it.
                            152 \cs_new_protected_nopar:Npn \__tilings_set_tiling_path:n #1
                                      \group_begin:
                            154
                                      \verb|\pgfsyssoftpath@getcurrentpath\l__tilings_tmpa_tl|
                            155
                                      \verb|\lines| tilings_normalise_path: N \ | l_tilings_tmpa_tl|
                                      \tl_gset_eq:cN {g__tilings_side_#1_tl} \l__tilings_tmpa_tl
                            157
                                      \group_end:
                            158
                            159 }
                            161 \NewDocumentCommand \SetTilingPath { m }
                                      \_tilings_set_tiling_path:n {#1}
                            164 }
```

```
can_point:n This is a wrapper around \tikz@scan@one@point to make it easier to use with LATEX3 variables.
               165 \cs_new_nopar:Npn \tikz_scan_point:n #1
                    \tikz@scan@one@point\pgfutil@firstofone#1\relax
               167
              168 }
              169 \cs_generate_variant:Nn \tikz_scan_point:n {V}
             (End definition for \tikz_scan_point:n.)
             This extracts the code that tests if a node is defined.
defined:TF
               170 \prg_new_conditional:Npnn \tikz_node_if_defined:n #1 {p,T,F,TF}
              171
                    \tl_if_exist:cTF {pgf@sh@ns@\use:c{tikz@pp@name}{#1}}
              173
              174
                      \prg_return_true:
               175
                      \tl_if_exist:cTF
               176
                      {pgf@sh@ns@not yet positionedPGFINTERNAL\use:c{tikz@pp@name}{#1}}
               177
               178
               179
                        \pgf_return_true:
               180
                      {
               181
                        \prg_return_false:
              182
              183
                    }
               184
              185 }
             (End\ definition\ for\ \verb+\tikz_node_if_defined:TF.)
ceys_get:Nn
             This is a wrapper around \pgfkeysgetvalue to make it easier to use with LATEX3 variables.
fkeys_get:n
               186 \cs_new_nopar:Npn \__tilings_keys_get:Nn #1#2
                    \pgfkeysgetvalue{/tikz/tiling/#2}{#1}
              189 }
                 \cs_new_nopar:Npn \__tilings_keys_get:n #1
               190
               191
                    \pgfkeysvalueof{/tikz/tiling/#1}
               192
               193 }
                 \cs_new_nopar:Npn \__tilings_tikz_keys_get:Nn #1#2
              194
               195
                    \pgfkeysgetvalue{/tikz/#2}{#1}
               196
               197 }
               198 \cs_new_nopar:Npn \__tilings_tikz_keys_get:n #1
               200
                    \pgfkeysvalueof{/tikz/#1}
              201
              202 \cs_new_nopar:Npn \__tilings_pgf_keys_get:Nn #1#2
              203 {
                    \pgfkeysgetvalue{#2}{#1}
              204
              205 }
                 \cs_new_nopar:Npn \__tilings_pgf_keys_get:n #1
               206
               207
                    \pgfkeysvalueof{#1}
              208
               209 }
             (End definition for \__tilings_keys_get:Nn and \pgfkeys_get:n.)
             This builds the tile path from its pieces. The arguments are the name of the tile, the descriptions of the sides,
ke_tile:nnn
             and a token list of the coordinates.
              210 \cs_new_nopar:Npn \__tilings_make_tile:nnn #1#2#3
```

Get the first coordinate and initialise the path with a move to this point.

```
\group_begin:
 213
      \tl_set:Nn \l__tilings_tmpa_tl {#3}
      \tl_set:Nx \l__tilings_tmpb_tl {\tl_head:N \l__tilings_tmpa_tl}
 214
      \tl_set:Nn \l__tilings_tmpa_tl {\pgfsyssoftpath@movetotoken}
      \tl_put_right:Nx \l__tilings_tmpa_tl
 216
      {
          \fp_to_dim:n
 219
          {(\tl_item:Nn \l__tilings_tmpb_tl {1}) * \c__tilings_cm_fp}
          \fp_to_dim:n
 223
          {(\tl_item:Nn \l__tilings_tmpb_tl {2}) * \c__tilings_cm_fp}
 224
 225
 226
      \tl_set_eq:NN \l__tilings_tmp_tile_path_tl \l__tilings_tmpa_tl
Now we have our path initialised, we can start appending the side paths according to the specification in the
second argument.
    We append the initial coordinate to the end of the list to make a closed cycle.
      \tl_set:Nn \l__tilings_tmpa_tl {#3}
      \tl_put_right:Nx \l__tilings_tmpa_tl {{\tl_head:N \l__tilings_tmpa_tl}}
Now we walk through the description of the sides, adding the specified paths to our tile path.
      \tl_map_inline:nn {#2} {
Clone the path for this side.
        \tl_set:Nx \l__tilings_tmpc_tl {\tl_head:n {##1}}
        \tl_if_exist:cF {g__tilings_side_ \tl_use:N \l__tilings_tmpc_tl _tl}
          \msg_error:nnx { tilings }{ no side } { \tl_use:N \l__tilings_tmpc_tl }
 234
          \tl gset eq:cc
 235
          {g_tilings_side_ \tl_use:N \l_tilings_tmpc_tl _tl}
          {g__tilings_side_a_tl}
 238
        \tl_set_eq:Nc \l__tilings_tmpd_tl
        {g__tilings_side_ \tl_use:N \l__tilings_tmpc_tl _tl}
Strip off the next coordinate, and convert it to a point.
        \tl_set:Nx \l__tilings_tmpb_tl {\tl_head:N \l__tilings_tmpa_tl}
        \tl_set:Nx \l__tilings_tmpa_tl {\tl_tail:N \l__tilings_tmpa_tl}
Store the resulting coordinate.
        \fp_set:Nn \l__tilings_tmpa_fp
 243
        { \tl_item: Nn \l__tilings_tmpb_tl {1} }
 244
        \fp_set:Nn \l__tilings_tmpb_fp
        { \tl_item: Nn \l__tilings_tmpb_tl {2} }
Now get the next coordinate.
        \tl_set:Nx \l__tilings_tmpb_tl {\tl_head:N \l__tilings_tmpa_tl}
We want the difference between the two coordinates.
        \fp_set:Nn \l__tilings_tmpa_fp
 248
        {\tl_item:Nn \l__tilings_tmpb_tl {1} - \l__tilings_tmpa_fp}
 249
        \fp_set:Nn \l__tilings_tmpb_fp
 250
        {\tl_item:Nn \l__tilings_tmpb_tl {2} - \l__tilings_tmpb_fp}
This is converted into a transformation matrix.
        \fp_set:Nn \l__tilings_tmpc_fp {-\l__tilings_tmpb_fp}
 252
        \tl_set:Nx \l__tilings_tmpb_tl
 253
 254
          {\fp_to_dim:n { \l__tilings_tmpa_fp * \c__tilings_cm_fp }}
 255
          256
```

```
{\fp_to_dim:n { \l__tilings_tmpc_fp * \c__tilings_cm_fp }}% not swapped
              257
                        {\fp_to_dim:n { \l__tilings_tmpa_fp * \c__tilings_cm_fp }}
              258
                        {0}
              250
                       {0}
              260
              261
             The transformation is applied to the cloned path.
                      \spath_transform:NV \l__tilings_tmpd_tl \l__tilings_tmpb_tl
             And this is welded to the tile path.
                      \spath_weld:NV \l__tilings_tmp_tile_path_tl \l__tilings_tmpd_tl
                   }
              264
             At the end we close the path.
                   \spath_close:N \l__tilings_tmp_tile_path_tl
                   \tl_gset_eq:NN \g__tilings_output_tl \l__tilings_tmp_tile_path_tl
              266
                   \group_end:
              267
                   \tl_gclear_new:c {g__tilings_tile_#1_tl}
              268
                   \tl_gset_eq:cN {g__tilings_tile_#1_tl} \g__tilings_output_tl
                   \tl_gclear:N \g__tilings_output_tl
              270
              271 }
             (End definition for \__tilings_make_tile:nnn.)
             A wrapper around the above which allows us to specify the second two arguments as two items in a token list.
ake_tile:nn
              272 \cs_new_nopar:Npn \__tilings_make_tile:nn #1#2
              273 {
              274
                    \__tilings_make_tile:nnn {#1} #2
              275 }
              276 \cs_generate_variant:Nn \__tilings_make_tile:nn {nV}
             (End definition for \__tilings_make_tile:nn.)
             2.4
                    Specifying the Tiles
             The tile specifications are contained in a prop.
              277 \prop_new:N \g__tilings_tiles_prop
             Process a coordinate through fp and adds it to a token list.
d_coordinate:Nnn
              278 \cs_new_nopar:Npn \__tilings_add_coordinate:Nnn #1#2#3 {
                   \group_begin:
              279
                   \fp_set:Nn \l__tilings_tmpa_fp {#2}
              280
                   \fp_set:Nn \l__tilings_tmpb_fp {#3}
              281
                   \bool_if:NT \l__tilings_relative_bool
              282
                      \fp_add:\n\\l__tilings_tmpa_fp {\l__tilings_saved_x_fp}
              284
                      \fp_add:\n\\l__tilings_tmpb_fp {\l__tilings_saved_y_fp}
              285
              286
                   \fp_gset_eq:NN \g__tilings_output_a_fp \l__tilings_tmpa_fp
              287
                   \fp_gset_eq:NN \g__tilings_output_b_fp \l__tilings_tmpb_fp
              288
                   \group_end:
              289
                   \tl_put_right:Nx #1
              290
              291
                       \{ \{ p_use: N \geq_tilings_output_a_fp \} \{ fp_use: N \leq_tilings_output_b_fp \} \} 
              292
              293
                   \bool_if:NT \l__tilings_update_saved_bool
```

ordinate:w

297 298

299

300 301 } \fp_set_eq:NN \l__tilings_saved_x_fp \g__tilings_output_a_fp \fp_set_eq:NN \l__tilings_saved_y_fp \g__tilings_output_b_fp

\fp_gzero:N \g__tilings_output_a_fp

\fp_gzero:N \g__tilings_output_b_fp

```
Wrapper around the add coordinate command to split at a comma.
 302 \cs_new_nopar:Npn \__tilings_add_xy_coordinate:w #1#2,#3 \q_stop
 303 {
       \__tilings_add_coordinate:Nnn #1 {#2}{#3}
 304
 305 }
    Wrapper around the add coordinate command to split at a colon.
 306 \cs_new_nopar:Npn \__tilings_add_rth_coordinate:w #1#2:#3 \q_stop
 307
      \__tilings_add_coordinate:Nnn #1 {(#3) * cosd(#2)}{(#3) * sind(#2)}
 308
 309 }
(\mathit{End \ definition \ for \ } \_\texttt{tilings\_add\_coordinate:Nnn} \ \ \mathit{and \ } \_\texttt{tilings\_add\_coordinate:w.})
Apply a transformation to make a given side lie on the x-axis. Second argument is the tile, third is the side,
first is whether to reverse the side.
 310 \cs_new_nopar:Npn \__tilings_transform_side_to_axis:Nnn #1#2#3
Get our tile data, checking if the tile exists.
      \group_begin:
      \prop_get:NnNTF \g__tilings_tiles_prop {#2} \l__tilings_tmpa_tl
Start with the edge list.
    Initialise the counter.
      \int_zero:N \l__tilings_tmpb_int
      \int_incr:N \l__tilings_tmpb_int
Get the path type list.
      \tl_set:Nx \l__tilings_tmpc_tl {\tl_head:N \l__tilings_tmpa_tl}
    Iterate through the path type list, looking for the requested path.
         \bool_set_false:N \l__tilings_edge_bool
 318
         \tl_map_inline:Nn \l__tilings_tmpc_tl {
 319
           \str_if_eq:nnT {##1} {#3} {
             \bool_set_true:N \l__tilings_edge_bool
             \tl_map_break:
           }
 323
 324
           \int_incr:N \l__tilings_tmpb_int
 325
         \bool_if:NTF \l__tilings_edge_bool
 326
 327
Get the coordinate list.
           \tl_set:Nx \l__tilings_tmpc_tl {\tl_tail:N \l__tilings_tmpa_tl}
Strip off the outer braces.
           \tl_set:Nx \l__tilings_tmpc_tl {\tl_item:Nn \l__tilings_tmpc_tl {1}}
Add the first coordinate at the end.
           \tl_put_right:Nx \l__tilings_tmpc_tl
 330
            \{ \{ tl_item: Nn \ l__tilings_tmpc_tl \ \{1\} \} \} 
 331
```

side_to_axis:Nnn

Get the coordinates for this edge.

334

\tl_set:Nx \l__tilings_tmpa_tl

\tl_set:Nx \l__tilings_tmpb_tl

{\tl_item:Nn \l__tilings_tmpc_tl {\int_use:N \l__tilings_tmpb_int}}

{\tl_item:Nn \l__tilings_tmpc_tl {\int_use:N \l__tilings_tmpb_int + 1}}

```
Possibly swap the ends.
  336
                     \bool_if:NT #1
                          \tl_set:NV \l__tilings_tmpc_tl \l__tilings_tmpa_tl
  338
                         \tl_set:NV \l__tilings_tmpa_tl \l__tilings_tmpb_tl
  339
                          \tl_set:NV \l__tilings_tmpb_tl \l__tilings_tmpc_tl
  340
  341
Get the coordinates of the first point, which will be the origin of the transformation.
                      \fp_set:Nn \l__tilings_xa_fp {\tl_item:Nn \l__tilings_tmpb_tl {1}}
                     \label{lem:nn loss} $$ \int_{-\infty} \int_{-\infty} \left( \sum_{i=1}^{\infty} \frac{1_{i+1} - 1_{i+1} - 
  343
Get the coordinates of the second point and adjust relative to the first.
                     \fp_set:Nn \l__tilings_xb_fp
                      345
                      \fp_set:Nn \l__tilings_yb_fp
  346
                     {\qquad \  } 1_{item:Nn \ l_tilings_tmpa_tl \ \{2\} \ - \ l_tilings_ya_fp}
  347
And normalise the vector along it.
  348 %
               \label{lem:local_state} $$ \int_{-\infty} xb_f  \left( -\frac{1}{1-tilings_xb_fp } / c_tilings_cm_fp \right) $$
               \fp_set:Nn \l__tilings_yb_fp {\l__tilings_yb_fp / \c__tilings_cm_fp}
  349 %
                      \fp_set:Nn \l__tilings_tmpa_fp
  350
                      {(\l_tilings_xb_fp)^2 + (\l_tilings_yb_fp)^2}
  351
                      \fp_set:Nn \l__tilings_xb_fp { \l__tilings_xb_fp / \l__tilings_tmpa_fp}
  352
                     \fp_set:\n \l__tilings_yb_fp { \l__tilings_yb_fp / \l__tilings_tmpa_fp}
  353
Now rotate so that the x-axis lies along the edge.
                     \tl_gset:Nx \g__tilings_output_tl
  354
                     {
  355
                          \exp_not:N \pgftransformtriangle
  356
                         {
  357
                              \exp_not:N \pgfpoint{0pt}{0pt}
  358
                         }
  359
                         {
                              \exp_not:N \pgfpoint
                              {\fp_to_dim:N \l__tilings_xb_fp}{\fp_to_dim:n {-\l__tilings_yb_fp}}
                         }
  363
                         {
  364
                              \exp_not:N \pgfpoint
  365
                              {\fp_to_dim:N \l__tilings_yb_fp}{\fp_to_dim:N \l__tilings_xb_fp}
  366
  367
                          \exp_not:N \pgftransformshift
  368
                         {
  369
                               \exp_not:N \pgfpoint
                                   \fp_to_dim:n {-\l__tilings_xa_fp * \c__tilings_cm_fp}
                              }
  374
                                   \fp_to_dim:n {-\l__tilings_ya_fp * \c__tilings_cm_fp}
  375
  376
                         }
  377
                     }
  378
                 }
  379
  380
                      \msg_error:nnxxx {tilings} {tile no edge} {#2} {#3}
  381
                      {\tl_use:N \l__tilings_tmpc_tl }
  382
                      \tl_gclear:N \g__tilings_output_tl
                 }
  384
            }
  385
  386
                 \msg_error:nnn {tilings} {no tile} {#2}
  387
                 \tl_gclear:N \g__tilings_output_tl
  388
```

```
\group_end:
                                                 390
                                                                  \tl_use:N \g__tilings_output_tl
                                                 391
                                                                  \tl_gclear:N \g__tilings_output_tl
                                                 392
                                                 393 }
                                             (End\ definition\ for\ \verb|\__tilings_transform_side_to_axis:Nnn.|)
                                                 394 \cs_generate_variant:Nn
                                                 395 \__tilings_transform_side_to_axis:Nnn {Nnx,NnV,NVV}
                                             Apply a transformation to make a given vertex sit at the origin. Second argument is the tile, third is the side,
ex to origin:Nnn
                                             first is a boolean to determine whether to use the start or end.
                                                 396 \cs_new_nopar:Npn \__tilings_translate_vertex_to_origin:Nnn #1#2#3
                                             Get our tile data, checking if the tile exists.
                                                                   \group_begin:
                                                                  \prop_get:NnNTF \g__tilings_tiles_prop {#2} \l__tilings_tmpa_tl
                                             Start with the edge list.
                                                            Initialise the counter.
                                                                   \int_zero:N \l__tilings_tmpb_int
                                                                  \int_incr:N \l__tilings_tmpb_int
                                             Get the path type list.
                                                                  \tl_set:Nx \l__tilings_tmpc_tl {\tl_head:N \l__tilings_tmpa_tl}
                                                            Iterate through the path type list, looking for the requested path.
                                                                          \bool_set_false:N \l__tilings_edge_bool
                                                                          \tl_map_inline:Nn \l__tilings_tmpc_tl {
                                                 405
                                                                                 \str_if_eq:nnT {##1} {#3} {
                                                 406
                                                                                        \bool_set_true:N \l__tilings_edge_bool
                                                 407
                                                                                        \tl_map_break:
                                                 408
                                                 409
                                                                                 \verb|\int_incr:N \ll_tillings_tmpb_int|
                                                 410
                                                 411
                                                                          \bool_if:NTF \l__tilings_edge_bool
                                             Get the coordinate list.
                                                                                 \tl_set:Nx \l__tilings_tmpc_tl {\tl_tail:N \l__tilings_tmpa_tl}
                                             Strip off the outer braces.
                                                                                 \tl_set:Nx \l__tilings_tmpc_tl {\tl_item:Nn \l__tilings_tmpc_tl {1}}
                                                415
                                             Add the first coordinate at the end.
                                                                                 \tl_put_right:Nx \l__tilings_tmpc_tl
                                                                                 {{\tl_item:Nn \l__tilings_tmpc_tl {1}}}
                                                 417
                                             Get the coordinates for this edge.
                                                                                 \tl_set:Nx \l__tilings_tmpa_tl
                                                                                  {\tl_item:Nn \l__tilings_tmpc_tl {\int_use:N \l__tilings_tmpb_int}}
                                                                                 \tl_set:Nx \l__tilings_tmpb_tl
                                                                                  \{ \exists : \mathbb{N}  \mid \exists
                                             Possibly swap the ends.
                                                                                 \bool_if:NT #1
                                                                                        \tl_set:NV \l__tilings_tmpc_tl \l__tilings_tmpa_tl
                                                                                        \tl_set:NV \l__tilings_tmpa_tl \l__tilings_tmpb_tl
                                                                                        \tl_set:NV \l__tilings_tmpb_tl \l__tilings_tmpc_tl
                                                 426
```

389 }

427

```
\fp_set:Nn \l__tilings_xa_fp {\tl_item:Nn \l__tilings_tmpb_tl {1}}
 429
           \fp_set:Nn \l__tilings_ya_fp {\tl_item:Nn \l__tilings_tmpb_tl {2}}
Shift to place the selected vertex at the origin.
           \tl_gset:Nx \g__tilings_output_tl
             \exp_not:N \pgftransformshift
 432
             {
 433
               \exp_not:N \pgfpoint
 435
                 \fp_to_dim:n {-\l__tilings_xa_fp * \c__tilings_cm_fp}
 436
 437
 438
                 \fp_to_dim:n {-\l__tilings_ya_fp * \c__tilings_cm_fp}
             }
          }
        }
 443
 444
           \msg_error:nnxxx {tilings} {tile no edge} {#2} {#3}
 445
           {\tl_use:N \l__tilings_tmpc_tl }
 446
           \tl_gclear:N \g__tilings_output_tl
 447
 448
      }
 449
 450
         \msg_error:nnn {tilings} {no tile} {#2}
        \tl_gclear:N \g__tilings_output_tl
      }
 454
      \group_end:
      \tl_use:N \g__tilings_output_tl
 455
      \tl_gclear:N \g__tilings_output_tl
 456
 457 }
(End\ definition\ for\ \verb|\__tilings_translate_vertex_to_origin:Nnn.)
 458 \cs_generate_variant:Nn
 459 \__tilings_translate_vertex_to_origin:Nnn {Nnx,NnV,NVV}
Make this available outside the IATEX3 environment. The starred version allows for reversing the side.
 460 \DeclareDocumentCommand \TransformAlongSide {s m m}
 461 {
Store the star
      \IfBooleanTF {#1}
 462
      {
 463
         \bool_set_true:N \l__tilings_cw_bool
      }
      {
         \bool_set_false:N \l__tilings_cw_bool
 467
      }
      \__tilings_transform_side_to_axis:Nnx \l__tilings_cw_bool {#2}{#3}
 469
 470 }
(End\ definition\ for\ \verb|\TransformAlongSide|.)
This places TikZ coordinates at the vertices of the tile.
 471 \cs_new_nopar:Npn \__tilings_coordinates_at_vertices:n #1
 472 {
      \group_begin:
 473
Get our tile data
      \prop_get:NnN \g__tilings_tiles_prop {#1} \l__tilings_tmpa_tl
```

rmAlongSide

es at vertices:n

Get the coordinates of the first point, which will be the origin of the transformation.

```
Start with the edge list
      \tl_set:Nx \l__tilings_tmpb_tl {\tl_head:N \l__tilings_tmpa_tl}
Get the coordinate list
      \tl_set:Nx \l__tilings_tmpc_tl {\tl_tail:N \l__tilings_tmpa_tl}
Strip off the outer braces
      \tl_set:Nx \l__tilings_tmpc_tl
      478
Add the first coordinate at the end
      \tl_put_right:Nx \l__tilings_tmpc_tl
      {{\tl_item:Nn \l__tilings_tmpc_tl {1}}}
Get the first coordinate
      \tl_set:Nx \l__tilings_tmpa_tl {\tl_head:N \l__tilings_tmpc_tl}
      \tl_set:Nx \l__tilings_tmpc_tl {\tl_tail:N \l__tilings_tmpc_tl}
Iterate through the edge list, placing coordinates
      \tl_map_inline:Nn \l__tilings_tmpb_tl {
        \tl_set:Nx \l__tilings_tmpd_tl {
 484
 485
          \exp_not:N \coordinate
 486
          (-edge~ ##1~ start)~
 487
          at (
          \tl_item:Nn \l__tilings_tmpa_tl {1},
 488
          \tl_item:Nn \l__tilings_tmpa_tl {2}
 489
          );
 490
 491
        \tl_use:N \l__tilings_tmpd_tl
 492
        \tl_set:Nx \l__tilings_tmpa_tl {\tl_head:N \l__tilings_tmpc_tl}
 493
        \tl_set:Nx \l__tilings_tmpc_tl {\tl_tail:N \l__tilings_tmpc_tl}
        \tl_set:Nx \l__tilings_tmpd_tl {
          \exp_not:N \coordinate
          (-edge~ ##1~ end)~
 497
          at (
 498
          \tl_item:Nn \l__tilings_tmpa_tl {1},
 499
          \tl_item:Nn \l__tilings_tmpa_tl {2}
 500
 501
 502
        \tl_use:N \l__tilings_tmpd_tl
 503
      }
 504
      \group_end:
 506 }
(End definition for \__tilings_coordinates_at_vertices:n.)
User-accessible wrapper around the above.
 507 \DeclareDocumentCommand \CoordinatesAtVertices {m}
 508 €
 509
       \__tilings_coordinates_at_vertices:n {#1}
 510 }
(End definition for \CoordinatesAtVertices.)
 511 \tikzset{
      transform~ to~ tile/.code~ args={#1~ along~ #2}{%
 512
        \group_begin:
 513
        \tl_if_in:nnTF {#1} {back}
 514
 515
          \tikzset{
 516
            tiling/alignment~ set~ location=#1,
 517
 518
            tiling/alignment~ direction={backwards}
          }
        }
```

AtVertices

```
\tikzset{
          tiling/alignment~ location=#1,
          tiling/alignment~ direction={forewards}
524
526
      \tl_if_in:nnTF {#2} {using}
527
528
        \tikzset{
529
          tiling/alignment~ set~ edges=#2,
      7
        \tikzset{
534
          tiling/alignment~ edge=#2,
536
      \tikz_scan_point:n {
538
        (\__tilings_keys_get:n {alignment~ location}
539
        -edge~ \__tilings_keys_get:n {alignment~ edge}~ start)
541
      \dim_set_eq:Nc \l__tilings_xa_dim {pgf@x}
542
      \dim_set_eq:Nc \l__tilings_ya_dim {pgf@y}
      \tikz_scan_point:n {
544
        (\__tilings_keys_get:n {alignment~ location}
545
        -edge~ \__tilings_keys_get:n {alignment~ edge}~ end)
546
547
      \dim_set_eq:Nc \l__tilings_xb_dim {pgf@x}
548
      \dim_set_eq:Nc \l__tilings_yb_dim {pgf@y}
549
      \__tilings_keys_get:Nn \l__tilings_tmpb_tl {alignment~ direction}
      \tl_if_eq:NnTF \l__tilings_tmpb_tl {forewards}
        553
        \dim_gset_eq:NN \g__tilings_ya_dim \l__tilings_ya_dim
        \dim_gset_eq:NN \g__tilings_xb_dim \l__tilings_xb_dim
        \dim_gset_eq:NN \g__tilings_yb_dim \l__tilings_yb_dim
556
557
        \dim_gset_eq:NN \g__tilings_xa_dim \l__tilings_xb_dim
        \dim_gset_eq:NN \g__tilings_ya_dim \l__tilings_yb_dim
        \dim_gset_eq:NN \g__tilings_xb_dim \l__tilings_xa_dim
561
        \dim_gset_eq:NN \g__tilings_yb_dim \l__tilings_ya_dim
563
      \dim_gsub:Nn \g__tilings_xb_dim {\g__tilings_xa_dim}
564
      \dim_gsub:Nn \g__tilings_yb_dim {\g__tilings_ya_dim}
565
      \dim_gset:Nn \g__tilings_xb_dim
566
      {\g__tilings_xb_dim * \dim_ratio:nn {1pt}{1cm}}
567
      568
      {\g_tilings_yb_dim * \dim_ratio:nn {1pt}{1cm}}
569
      \group_end:
```

We store the initial points in \pgf@xa and \pgf@ya but we want \pgf@xb and \pgf@yb to be a vector along the edge.

We shift to the start of the edge.

Now rotate so that the x-axis lies along the edge.

```
\pgftransformtriangle
{\pgfpoint{0pt}{0pt}}
{\pgfpoint{\g_tilings_xb_dim}{\g_tilings_yb_dim}}
{\pgfpoint{-\g_tilings_yb_dim}{\g_tilings_xb_dim}}
```

```
},
576
     align~ with/.code~ args={#1~ along~ #2}{%
577
       \tl_if_in:nnTF {#1} {back}
578
579
         \tikzset{
580
           tiling/alignment~ set~ location=#1,
581
           tiling/alignment~ direction={backwards}
582
583
       }
584
         \tikzset{
           tiling/alignment~ location=#1,
587
           tiling/alignment~ direction={forewards}
589
590
       \tl_if_in:nnTF {#2} {using}
591
592
         \tikzset{
593
           tiling/alignment~ set~ edges=#2,
594
         }
595
       }
597
598
         \tikzset{
599
           tiling/alignment~ edge=#2,
         }
600
601
       \tikz_node_if_defined:nTF
602
603
         \__tilings_keys_get:n {alignment~ location}
605
         -edge~ \__tilings_keys_get:n {alignment~ edge}~ start
       }
         \tikzset{
           tiling/alignment~ start/.expanded={
             (\__tilings_keys_get:n {alignment~ location}
             -edge~ \__tilings_keys_get:n {alignment~ edge}~ start)
611
           },
612
           tiling/alignment~ end/.expanded={
613
             (\__tilings_keys_get:n {alignment~ location}
614
             -edge~ \__tilings_keys_get:n {alignment~ edge}~ end)
615
616
         }
617
618
       }
619
         \__tilings_keys_get:Nn \l__tilings_tmpa_tl {alignment~ location}
         \tl_set:Nx \l__tilings_tmpa_tl {\tl_use:N \l__tilings_tmpa_tl}
621
         \prop_get:NVNTF \g__tilings_tilenames_prop
         \l__tilings_tmpa_tl \l__tilings_tmpb_tl
624
           \prop_get:NVN \g__tilings_tiles_prop
           \l__tilings_tmpb_tl \l__tilings_tmpc_tl
626
           \msg_error:nnxxx { tilings }{ tile no edge }
             \tl_use:N \l__tilings_tmpa_tl \c_space_tl
             (type~ \tl_use:N \l__tilings_tmpb_tl)
631
           {\__tilings_keys_get:n {alignment~ edge} }
           { \tl_item:Nn \l__tilings_tmpc_tl {1} }
634
635
           \msg_error:nnx { tilings }{ no tile }
```

```
{\__tilings_keys_get:n {alignment~ location} }
 637
 638
       }
 639
     },
 640
     tiling/.is~ family,
641
     tiling/alignment~ set~ location/.code~ args={#1~ back}{
642
       \tikzset{
643
         tiling/alignment~ location=#1,
 644
     },
     tiling/alignment~ set~ edges/.code~ args={#1~ using~ #2}{
       \tikzset{
         tiling/alignment~ edge=#1,
         tiling/alignment~ new~ edge=#2
 650
       }
 651
     },
 652
     align~ between/.code~ args={#1~ and~ #2~ using~ #3}{
653
654
         tiling/alignment~ start={#1},
655
         tiling/alignment~ end={#2},
 658
       \str_set:Nn \l__tilings_tmpa_str {#3}
       \str_set:Nx \l__tilings_tmpb_str {\str_tail:N \l__tilings_tmpa_str}
 659
       \tikzset{
 660
         tiling/alignment~ new~ edge/.expanded={\str_use:N \l__tilings_tmpb_str}
 661
 662
       663
       \str_set:Nx \l__tilings_tmpb_str {\str_lowercase:f { \l__tilings_tmpa_str}}
 664
       \str_if_eq:NNT \l__tilings_tmpa_str \l__tilings_tmpb_str
 665
         \str_set:Nx \l__tilings_tmpb_str
         {\str_uppercase:f { \l__tilings_tmpa_str}}
       \tikzset{
         tiling/alignment~ edge/.expanded={\str_use:N \l__tilings_tmpb_str},
 671
 672
     },
 673
     tiling/alignment~ location/.initial={},
674
     tiling/alignment~ edge/.initial=a,
675
     tiling/alignment~ new~ edge/.initial={},
     tiling/alignment~ direction/.initial={forewards},
     tiling/alignment~ start/.initial={},
     tiling/alignment~ end/.initial={},
     tiling/anchor/.initial={},
Default clipping style.
     every~ tile~ clip/.style={clip}
682 }
```

\DefineTile This is the user function for defining a tile.

```
OB3 \DeclareDocumentCommand \DefineTile { s m m m }
```

Clear the temporary variable.

```
\tl_clear:N \l__tilings_tmpa_tl
```

The 3rd parameter is a list of coordinates at vertices, iterate through them and add them to the list.

```
\int_zero:N \l__tilings_tmpa_int
    fp_zero:N l__tilings_saved_x_fp
687
688
    \tl_map_inline:nn {#4} {
689
       \str_set:Nn \l__tilings_tmpa_str {##1}
690
       \str_if_eq:VnTF \l__tilings_tmpa_str {+}
691
692
         \int_incr:N \l__tilings_tmpa_int
693
694
         \int_case:nn {\l__tilings_tmpa_int}
           {0} {
             \bool_set_false:N \l__tilings_relative_bool
             \bool_set_true:N \l__tilings_update_saved_bool
700
           }
701
           {1} {
702
             \bool_set_true:N \l__tilings_relative_bool
703
             \bool_set_false:N \l__tilings_update_saved_bool
704
           }
705
           {2} {
             \bool_set_true:N \l__tilings_relative_bool
             \bool_set_true:N \l__tilings_update_saved_bool
708
709
         \str_if_in:NnTF \l__tilings_tmpa_str {:}
712
           \seq_set_split:NVV \l__tilings_tmpa_seq \c__tilings_colon_str \l__tilings_tmpa_str
714
           \__tilings_add_coordinate:Nnn \l__tilings_tmpa_tl
715
             (\seq_item:Nn \l__tilings_tmpa_seq {2}) * cosd (\seq_item:Nn \l__tilings_tmpa_seq {1})
           }
           {
             (\seq_item:Nn \l__tilings_tmpa_seq {2}) * sind (\seq_item:Nn \l__tilings_tmpa_seq {1})
           }
        }
723
           \seq set split:NVV \1 tilings tmpa seq \c tilings comma str \1 tilings tmpa str
724
           \__tilings_add_coordinate:Nnn \l__tilings_tmpa_tl
725
             (\seq_item: Nn \l__tilings_tmpa_seq {1})
           }
           {
729
             (\seq_item:Nn \l__tilings_tmpa_seq {2})
         \int_zero:N \l__tilings_tmpa_int
734
735
```

Now we make a list of the edge types (from the 2nd parameter), using a prop to keep track of whether an edge is repeated.

```
\prop_clear:N \l__tilings_tmpa_prop
     \t: map_inline:nn {#3} {
       \prop_if_in:NnTF \l__tilings_tmpa_prop {##19}
738
       {
739
         \prop_put:Nnn \l__tilings_tmpa_prop {##1} {1}
740
741
742
         \prop_put:Nnn \l__tilings_tmpa_prop {##1} {0}
743
```

\BakeTile This is the user wrapper around the tile creation macros.

```
903 \cs_new_protected_nopar:Npn \__tilings_bake_tile:n #1
904 {
905    \prop_get:NnN \g__tilings_tiles_prop {#1} \l__tilings_tmpa_tl
906    \__tilings_make_tile:nV {#1} \l__tilings_tmpa_tl
907 }
908
909 \NewDocumentCommand \BakeTile {m}
910 {
911   \__tilings_bake_tile:n {#1}
912 }
```

\UseTile This is the command that actually places a tile on the page. The first argument is optional and is for styling.

```
913 \cs_new_protected_nopar:Npn \__tilings_use_tile:nn #1#2
```

We need to transform the tile to correspond to the current transformation matrix. To ensure that we only transform the current tile, we clone it first.

```
915 \tl_if_exist:cTF {g__tilings_tile_#2_tl}
916 {
917 \tl_set_eq:Nc \l_tilings_tmp_tile_path_tl {g__tilings_tile_#2_tl}
```

We get the current transformation to apply to this path.

```
918 \pgfgettransform \l__tilings_tmpa_tl
```

Apply the transformation, protocol the path, and render it.

 $ciling_{\sqcup}path$

This is a style for a user to take a path and make it into the path for one of the sides. It needs to store both that side and the reverse.

```
931 \tikzset{
932    save~ tiling~ path/.code={
933    \tikz@addmode{

Get the current path.

934    \pgfsyssoftpath@getcurrentpath\l__tilings_tmpa_tl

Normalise the path and save.

935    \__tilings_normalise_path:N \l__tilings_tmpa_tl
```

```
vtl_gclear_new:c {g__tilings_side_#1_tl}
vtl_gset_eq:cN {g__tilings_side_#1_tl} \l__tilings_tmpa_tl
```

Now create the reverse path. The name is the upper case version.

Reverse the path, and relocate to the interval [0, 1].

```
spath_reverse:N \l__tilings_tmpa_tl
spath_transform:Nnnnnn \l__tilings_tmpa_tl {-1} {0} {0} {-1} {1} {0}
tl_gclear_new:c {g__tilings_side_ \tl_use:N \l__tilings_tmpb_tl _tl}
```

```
\tl_gset_eq:cN {g__tilings_side_ \tl_use:N \l__tilings_tmpb_tl _tl} \l__tilings_tmpa_tl
942
       }
943
    },
044
     clone~ tiling~ side~ path/.style~ 2~ args={
945
       spath/set~ name=tiling~ side,
946
       spath/clone~ global={#1}{#2}
947
     },
948
     flip~ tile/.code={
949
       \tl_set:Nn \l__tilings_tmpa_tl {#1}
       \tl_set:Nn \l__tilings_tmpb_tl {true}
951
       \bool_set:Nn \l__tilings_cw_bool {\tl_if_eq_p:NN \l__tilings_tmpa_tl \l__tilings_tmpb_tl}
    },
953
     flip~ tile/.default={true},
05/
     spath/prefix/tiling~side/.style={
955
       spath/set~ prefix=g__tilings_side_,
956
    },
957
     spath/suffix/tiling~side/.style={
958
       spath/set~ suffix=_tl,
959
    },
960
     clone~ tile~ path/.style~ 2~ args={
961
       spath/set~ name=tiling~tile,
       spath/clone~ global={#1}{#2}
963
    },
964
     spath/prefix/tiling~tile/.style={
965
       spath/set~ prefix=g__tilings_tile_,
966
    ٦.
967
     spath/suffix/tiling~tile/.style={
968
       spath/set~ suffix=_tl,
969
970
971
     expand~ key/.code={
       \exp_args:NV \pgfkeysalso #1
973
974 }
```

(End definition for save tiling path. This function is documented on page ??.)

2.5 Lindenmayer System

This is an implementation of the Lindenmayer System description of Penrose and other tilings as a way of generating tilings from a specific starting seed.

The implementation uses props to store *rules* and *actions*. The rules are used to expand the starting seed to a certain level, after which the actions are carried out. The syntax is based on the PGF library, but as we're already using LATEX3 it is reimplemented in that.

ce_lms:Nnnn

This creates the token list of actions, starting with the seed. The arguments are: a token list to store the result in, the name of the system, the number of iterations, and the initial state.

```
975 \cs_new_nopar:Npn \__tilings_make_lms:Nnnn #1#2#3#4
976 {
977  \group_begin:
On the first time round, we start with the given seed.
978  \tl_set:Nn \l__tilings_tmpb_tl {#4}
We repeat the specified number of times.
979  \prg_replicate:nn {#3} {
Duplicate the current state.
980  \tl_set_eq:NN \l__tilings_tmpa_tl \l__tilings_tmpb_tl
Clear the receiving token list.
981  \tl_clear:N \l__tilings_tmpb_tl
```

```
Walk through the current list, appending to the receiving list according to the rules.
        \tl_map_inline:Nn \l__tilings_tmpa_tl
 983
If a rule exists, copy that.
          \tl_set:Nx \l__tilings_action_lms_tl {\tl_head:n {##1}}
          \tl_set:Nx \l__tilings_parameters_lms_tl {\tl_tail:n {##1}}
 985
           \prop_if_in:cVTF {g__tilings_#2_lms_rule_prop} \l__tilings_action_lms_tl
 987
             \prop_get:cVN {g__tilings_#2_lms_rule_prop} \l__tilings_action_lms_tl \l__tilings_tmpc_tl
 988
            \tl_put_right:Nx \l__tilings_tmpb_tl {\tl_use:N \l__tilings_tmpc_tl}
 989
 990 %
              {\prop_item:cn {g_tilings_#2_lms_rule_prop} {##1} }
          }
 991
          {
 992
Otherwise, just copy the token.
             \tl_if_single:nTF {##1}
 993
            {
 994
               \tl_put_right:Nn \l__tilings_tmpb_tl {##1}
 995
            }
            {
               \tl_put_right:Nn \l__tilings_tmpb_tl {{##1}}
            }
 aga
1000
1001
1002
We've done all this inside a group, now pass the result outside.
      \tl_set:Nn \l__tilings_tmpa_tl {
1003
        \group_end:
1004
        \tl_set:Nn #1
1005
      \tl_put_right:Nx \l__tilings_tmpa_tl {{\tl_use:N \l__tilings_tmpb_tl}}
1007
      \tl_use:N \l__tilings_tmpa_tl
1008
1009
    \cs_generate_variant:Nn \__tilings_make_lms:Nnnn {Nnnx}
(End\ definition\ for\ \_\_tilings\_make\_lms:Nnnn.)
This carries out the actions specified by the resulting rules.
1011 \cs_new_nopar:Npn \__tilings_invoke_lms:nn #1#2
1012
      \group_begin:
1013
Walk through the given list, carrying out the corresponding action if it exists. If not, look at the default.
Otherwise, just do nothing.
1014
      \tl_map_inline:nn {#1} {
        \tl_set:Nx \l__tilings_action_lms_tl {\tl_head:n {##1}}
1015
```

oke_lms:nn

```
\tl_set:Nx \l__tilings_parameters_lms_tl {\tl_tail:n {##1}}
1016
        \prop_if_in:cVTF {g__tilings_#2_lms_action_prop} \l__tilings_action_lms_tl
1017
1018
          \prop_item:cV {g__tilings_#2_lms_action_prop} \l__tilings_action_lms_tl
1019
        }
1021
          \prop_if_in:cVT {g__tilings_default_lms_action_prop} \l__tilings_action_lms_tl
            \prop_item:cV {g__tilings_default_lms_action_prop} \l__tilings_action_lms_tl
1025
       }
1026
     }
1027
1028
     \group_end:
1029 }
1030 \cs_generate_variant:Nn \__tilings_invoke_lms:nn {Vn}
```

```
(End definition for \__tilings_invoke_lms:nn.)
    We need some parameters.
1031 \dim_new:N \l__tilings_step_dim
1032 \dim_set:Nn \l__tilings_step_dim {1cm}
    These are the defaults, which will be used in all the rule sets.
1033 \prop_new:N \g__tilings_default_lms_action_prop
1034 \prop_gput:Nnn \g__tilings_default_lms_action_prop {[]} {\group_begin:}
1035 \prop_gput:Nnn \g__tilings_default_lms_action_prop {]} {\group_end:}
1036 \prop_gput:Nnn \g_tilings_default_lms_action_prop {f}
1037 {\pgftransformxshift{\l__tilings_step_dim}}
1038 \prop_gput:Nnn \g__tilings_default_lms_action_prop {b}
1039 {\pgftransformxshift{-\l__tilings_step_dim}}
    Holds a list of the tiles that actually draw for each tile set
1040 \prop_new:N \g__tilings_drawables_lms_prop
    We keep track of the number of tiles.
1041 \int_new:N \g__tilings_tile_int
1042 \int_new:N \g__tilings_tiles_int
```

This is the user macro to invoke the decomposition. The arguments are: optional styles, the name, number of iterations, and starting seed.

```
1043 \cs_new_protected_nopar:Npn \__tilings_tiling_decomposition:nnnn #1#2#3#4
1044 {
1045
      \group_begin:
      \tikzset{
1046
        every~ #2~ decomposition/.try,
1047
1048
1049
      \__tilings_make_lms:Nnnx \l__tilings_tmpa_tl {#2} {#3} {#4}
      \__tilings_count_lms:Vn \l__tilings_tmpa_tl {#2}
1051
      \int_gzero:N \g__tilings_tile_int
1052
      \__tilings_invoke_lms:Vn \l__tilings_tmpa_tl {#2}
      \group_end:
1055 }
    \cs_new_protected_nopar:Npn \__tilings_tiling_decomposition:nnn #1#2#3
1056
1057
         _tilings_tiling_decomposition:nnnn {}{#1}{#2}{#3}
1058
1059 }
    \cs_generate_variant:Nn \__tilings_tiling_decomposition:nnn {VVV}
1060
1061
    \NewDocumentCommand \TilingDecomposition { O{} m m m }
1062
        _tilings_tiling_decomposition:nnnn {#1}{#2}{#3}{#4}
    }
1065
1066
    \tikzset{
1067
      pics/decomposition/.style~ n~ args={3}{
1068
        code={
1069
             _tilings_tiling_decomposition:nnn {#1}{#2}{#3}
1070
1071
1072
1073 }
This counts the number of tiles in the string.
1074 \cs_new_nopar:Npn \__tilings_count_lms:nn #1#2
1075
```

ount_lms:nn

1076

\group_begin:

\int_gzero:N \g__tilings_tiles_int

20

```
\prop_get:NnNT \g__tilings_drawables_lms_prop {#2} \l__tilings_tmpa_tl
1078
1079
        \tl_map_variable:nNn {#1} \l__tilings_tmpb_tl
1080
1081
           \tl_set:Nx \l__tilings_tmpb_tl {\tl_head:N \l__tilings_tmpb_tl}
1082
           \bool_do_while:nn
1083
           {
1084
             !\tl_if_empty_p:N \l__tilings_tmpb_tl
1085
             \tl_if_head_is_group_p:V \l__tilings_tmpb_tl
          }
           {
             \tl_set:Nx \l__tilings_tmpb_tl {\tl_head:N \l__tilings_tmpb_tl}
          }
1091
           \tl_if_in:NVT \l__tilings_tmpa_tl \l__tilings_tmpb_tl
1092
1093
             \int_gincr:N \g__tilings_tiles_int
1094
1095
        }
1096
      }
1097
      \group_end:
1098
1099 }
1100 \cs_generate_variant:Nn \__tilings_count_lms:nn {Vn}
(End definition for \__tilings_count_lms:nn.)
    This is a \tikzset mechanism for setting the dimensions of the tiling.
1101 \tikzset{
      tiling~ step/.code={
1102
        \dim_set:Nn \l__tilings_step_dim {#1}
1103
1104
1105 }
1106 \ExplSyntaxOff
1107 \RequirePackage{tikz}
1108 \usetikzlibrary{tilings}
1109 \ProvidesFile {tikzlibrarytilings.penrose.code.tex}
1110 [2023/06/01 v2.0 TikZ pics for Penrose tiles]
    Create the pre-defined tile shapes.
   • Thin Rhombus.
          \DefineTile{thin rhombus}{a A B b}
          {
1112
           {0,0}
1113
           \{cosd(18), sind(18)\}
1115
           \{2*\cos d(18), 0\}
           \{cosd(18), -sind(18)\}
1116
          }
1117
    Thick Rhombus.
          \DefineTile{thick rhombus}{B a A b}
1118
          {
1119
           {0,0}
           \{\cos d(36), \sin d(36)\}
1121
           \{2*\cos d(36), 0\}
           \{\cos d(36), -\sin d(36)\}
1124
```

```
• Dart.
```

```
\DefineTile{dart}{c a A C}
1126
          {0 , 0}
1127
          \{2*sind(18)*cosd(108), 2*sind(18)*sind(108)\}
1128
          \{2*sind(18), 0\}
1129
          \{2*sind(18)*cosd(108), -2*sind(18)*sind(108)\}
1130
  • Kite.
         \DefineTile{kite}{a c C A}
1132
1133
         {
          {0 , 0}
1134
          \{cosd(36), sind(36)\}
          {1 , 0}
1136
          \{\cos d(36), -\sin d(36)\}
1138
  • Golden Triangle.
         \DefineTile{golden triangle}{a c b}
         {
1141
          {0 , 0}
          \{cosd(18), sind(18)\}
1142
          \{cosd(18), -sind(18)\}
1144
  • Reverse Golden Triangle.
         \DefineTile {reverse golden triangle}{B C A}
         {
          {0 , 0}
          \{\cos d(18), \sin d(18)\}
          \{\cos d(18), -\sin d(18)\}
1149
1150
  • Golden Gnomon
         \DefineTile {golden gnomon}{C b A}
1152
          {0 , 0}
1153
          \{cosd(36), sind(36)\}
1155
          \{2*\cos d(36), 0\}
1156
  • Reverse Golden Gnomon
         \DefineTile {reverse golden gnomon}{a B c}
1158
          {0, 0}
1159
          \{2*\cos d(36), 0\}
1160
          \{cosd(36), -sind(36)\}
1162
  • Primary Pentagon (pentagon 5)
         \DefineTile {pentagon 5}{a a a a}
1163
1164
```

```
{0 , 0}
1165
           \{\cos d(108), \sin d(108)\}
1166
           \{1+\cos d(72)+\cos d(144), \sin d(72)+\sin d(144)\}
1167
           \{1+\cos d(72), \sin d(72)\}
1168
           {1 , 0}
1169
1170
   • Secondary Pentagon (pentagon 3)
          \DefineTile {pentagon 3}{A b a a b}
1171
          {
1172
           {0, 0}
1173
           \{\cos d(108), \sin d(108)\}
1174
           \{1+\cos d(72)+\cos d(144), \sin d(72)+\sin d(144)\}
1175
           \{1+\cos d(72) \text{ , } \sin d(72)\}
1176
           {1 , 0}
1178
   • Tertiary Pentagon (pentagon 2)
          \DefineTile {pentagon 2}{d A e c A}
1179
          {
           {0 , 0}
1181
           \{\cos d(108), \sin d(108)\}
1182
           \{1+\cos d(72)+\cos d(144) , \sin d(72)+\sin d(144)\}
1183
           \{1+\cos d(72) , \sin d(72)\}
1184
           {1 , 0}
1185
1186
   • Pentagram
          \DefineTile {pentagram}{C E C E C E C E C E}
          {
             {1 , 0}
             \{1-\cos d(36), -\sin d(36)\}
1190
             \{1-\cos d(36)-\cos d(108), -\sin d(36)-\sin d(108)\}
1191
             \{\cos d(108), -\sin d(108)\}
1192
             \{-1+3*\cos d(108)+\cos d(36), -\sin d(36)-\sin d(108)\}
1193
             \{-1+2*\cos d(108)+\cos d(36), -\sin d(36)\}
1194
             \{-1+2*cosd(108), 0\}
1195
             {2*cosd(108), 0}
1196
             \{\cos d(108), \sin d(108)\}
1197
             {0,0}
          }
1199
   • Boat
          \DefineTile {boat}{C E C E B D B}
1200
          {
1201
           {-1+2*cosd(108) , 0}
1202
           \{2*cosd(108), 0\}
1203
           \{\cos d(108), \sin d(108)\}
1204
           {0, 0}
1205
           {1 , 0}
1206
           \{1-\cos d(36), -\sin d(36)\}
           \{-1+2*\cos d(108)+\cos d(36), -\sin d(36)\}
1208
1209
```

• Diamond.

```
\DefineTile {diamond}{D B B D}
                      {0, 0}
                      \{cosd(18), sind(18)\}
 1213
                      {2*cosd(18) , 0}
 1214
                      \{\cos d(18), -\sin d(18)\}
 1215
 1216
         Place the arcs
       \tikzset{
            every thin rhombus before path/.code={
 1218
                 \path[every circle arc/.try] (-edge a end) circle[radius=1/4];
                 \path[every long arc/.try] (-edge b start) circle[radius=1/4];
            },
            every thick rhombus before path/.code={
                 \path[every circle arc/.try] (-edge a end) circle[radius=1/4];
                 \path[every long arc/.try] (-edge B start) circle[radius=3/4];
 1224
            every kite before path/.code={
 1226
                 \path[every circle arc/.try] (-edge a start) circle[radius=2/(sqrt(5)+1)];
                 \path[every long arc/.try] (-edge c end) circle[radius=2/(3+sqrt(5))];
 1228
 1229
            every dart before path/.code={
 1230
                 \path[every circle arc/.try] (-edge a end) circle[radius=1 - 2/(sqrt(5)+1)];
                  \path[every long arc/.try] (-edge c start) circle[radius=2/(sqrt(5)+1) - 2/(3+sqrt(5))];
 1234 }
         Now bake the tiles.
 1235 \BakeTile {thin rhombus}
 1236 \BakeTile {thick rhombus}
 1237 \BakeTile {dart}
 1238 \BakeTile {kite}
 1239 \BakeTile {golden triangle}
 1240 \BakeTile {reverse golden triangle}
 1241 \BakeTile {golden gnomon}
 1242 \BakeTile {reverse golden gnomon}
 1243 \BakeTile {pentagon 5}
 1244 \BakeTile {pentagon 3}
 1245 \BakeTile {pentagon 2}
 1246 \BakeTile {pentagram}
 1247 \BakeTile {boat}
 1248 \BakeTile {diamond}
             Lindenmayer System
2.6
 1249 \ExplSyntaxOn
         These are the rules for generating rhombus tilings with the Lindenmayer System procedure.
 1250 \prop_new:N \g__tilings_rhombus_lms_rule_prop
 \label{local_prop_gput:Nnn g_tilings_rhombus_lms_rule_prop {T} {[f*sT][f>g]} % \end{substitute} % \begin{substitute} \begin{s
 1252 \prop_gput:Nnn \g_tilings_rhombus_lms_rule_prop {t} {[f_st][f>G]}
 1253 \prop_gput:Nnn \g__tilings_rhombus_lms_rule_prop {G} {[f+sG][sf>g][sf*sT]}
 1254 \prop_gput:Nnn \g__tilings_rhombus_lms_rule_prop {g} {[f-sg][sf>G][sf_st]}
         These are the rules for generating kite and dart tilings.
```

1255 \prop_new:N \g__tilings_kite_lms_rule_prop

These are the rules for generating pentagon tilings.

1256 \prop_gput:Nnn \g__tilings_kite_lms_rule_prop {T} {[f*sT][f*st][+sg]}
1257 \prop_gput:Nnn \g__tilings_kite_lms_rule_prop {t} {[f_st][f*sT][-sG]}
1258 \prop_gput:Nnn \g__tilings_kite_lms_rule_prop {G} {[f*+sG][sT]}
1259 \prop_gput:Nnn \g__tilings_kite_lms_rule_prop {g} {[f-_sg][st]}

```
1260 \prop_new:N \g__tilings_pentagon_lms_rule_prop
1261 \prop_gput:Nnn \g_tilings_pentagon_lms_rule_prop {P}
1262 {[s>P][1sF+Q][1+sF+Q][1*sF+Q][1-sF+Q][1_sF+Q]} % pentagon 5
\prop_gput:Nnn \g__tilings_pentagon_lms_rule_prop {Q}
\{[s>P][1+sFR][1*sF*R][1-sF+Q][1_sF+Q][1sF+Q][->fsD]\} % pentagon 3
1265 \prop_gput:Nnn \g__tilings_pentagon_lms_rule_prop {R}
1266 {[s>P] [1-sF+Q] [1+sF*R] [1*sFR] [1 sF*R] [1sFR] [_>fsD] [>fsD]} % pentagon 2
1267 \prop_gput:Nnn \g__tilings_pentagon_lms_rule_prop {G}
1268
     [s>G]
     [se[>d+R][e1B]]
     [+se[>d+R][e1B]]
1271
     [-se[>d+R][e1B]]
     [*se[>d+R][e1B]]
     [se[>d+R][e1B]]
1274
1275 } % pentagram
1276 \prop_gput:Nnn \g_tilings_pentagon_lms_rule_prop {B}
1277
1278
     [s>G]
     [se[>d+R][e1B]]
1279
     [+se[>d+R][e1B]]
     [-se[>d+R][e1B]]
1282 } % boat
1283 \prop_gput:Nnn \g__tilings_pentagon_lms_rule_prop {D}
1284 {[s>d+R][s>eG][se1B]} % diamond
    Each of the standard tilings can also be drawn using triangles using the same rules.
1285 \prop_gset_eq:NN \g__tilings_rtriangle_lms_rule_prop
1286 \g__tilings_rhombus_lms_rule_prop
1287 \prop_gset_eq:NN \g__tilings_ktriangle_lms_rule_prop
1288 \g__tilings_kite_lms_rule_prop
    These are the lists of tokens that actually draw things
1289 \prop_gput:Nnn \g__tilings_drawables_lms_prop {rhombus} {TG}
1290 \prop_gput:Nnn \g__tilings_drawables_lms_prop {kite} {Tg}
\prop_gput:Nnn \g_tilings_drawables_lms_prop {rtriangle} {TtGg}
\prop_gput:Nnn \g__tilings_drawables_lms_prop {pentagon} {PQRGBD}
    These hold the various actions.
1294 \prop_new:N \g__tilings_rhombus_lms_action_prop
1295 \prop_new:N \g__tilings_kite_lms_action_prop
1296 \prop_new:N \g__tilings_rtriangle_lms_action_prop
\label{local_prop_new} $$ \operatorname{prop\_new:N \ \g_tilings_ktriangle_lms_action\_prop } $$
1298 \prop_new:N \g__tilings_pentagon_lms_action_prop
    The rhombus rules need a variety of turns.
1299 \prop_gput:Nnn \g__tilings_rhombus_lms_action_prop {+}
1300 {\pgftransformrotate{144}}
1301 \prop_gput:Nnn \g__tilings_rhombus_lms_action_prop {*}
1302 {\pgftransformrotate{108}}
1303 \prop_gput:Nnn \g__tilings_rhombus_lms_action_prop {-}
1304 {\pgftransformrotate{216}}
1305 \prop_gput:Nnn \g__tilings_rhombus_lms_action_prop {_}
1306 {\pgftransformrotate{252}}
1307 \prop_gput:Nnn \g_tilings_rhombus_lms_action_prop {>}
1308 {\pgftransformrotate{180}}
\label{limin_limit} $$1309 \simeq \prop_gput:Nnn $$ g_tilings_rhombus_lms_action_prop $$ {s} $$ {}
     \fp_set:Nn \l__tilings_tmpa_fp { 2 * sind(18) * \l__tilings_step_dim }
     \label{lem:normalized} $$\dim_{set:Nn \l_tilings_step_dim {\phi_dim:N \l_tilings_tmpa_fp}$} $$
1311
1312 }
   Up to now, the actions for the rhombus and its triangle replacement are the same.
1313 \prop_gset_eq:NN \g__tilings_rtriangle_lms_action_prop
```

```
1314 \g__tilings_rhombus_lms_action_prop
    Now we do the actions that actually draw something.
    \prop_gput:Nnn \g__tilings_rhombus_lms_action_prop {T} {
      \group_begin:
As we go through, we keep track of how many tiles we've drawn.
      \int_gincr:N \g__tilings_tile_int
Set up the position, size, and angle correctly.
      \pgftransformrotate{198}
1318
      \fp_set:\n \l__tilings_tmpa_fp {\l__tilings_step_dim*2*cosd(18)}
      \pgftransformxshift{-\fp_to_dim:N \l__tilings_tmpa_fp}
      \fp_set:Nn \l__tilings_tmpa_fp {\l__tilings_step_dim/(1cm)}
      \pgftransformscale{\fp_use:N \l__tilings_tmpa_fp}
Now we draw the thin rhombus, applying every style we can possibly imagine. The tile style gets the current
tile and total tile numbers passed to it.
      \tl_set:Nx \l__tilings_tmpc_tl
1323
      {
1324
        {\int_use:N \g__tilings_tile_int}
        {\int_use:N \g__tilings_tiles_int}
1326
      }
1327
      \UseTile[
1328
        every~ tile/.try,
        every~ thin~ rhombus/.try,
        tile~ \int_use:N \g__tilings_tile_int/.try,
1331
        tile/.try/.expand~ once=\l__tilings_tmpc_tl
      []{thin~rhombus}
      \group_end:
1334
1335
    Same for the thick rhombus.
    \prop_gput:Nnn \g__tilings_rhombus_lms_action_prop {G} {
1336
      \group_begin:
      \int_gincr:N \g__tilings_tile_int
1338
      \fp_set:Nn \l__tilings_tmpa_fp {\l__tilings_step_dim/(1cm)/(2*cosd(36))}
      \pgftransformscale{\fp_use:N \l__tilings_tmpa_fp}
1340
      \tl_set:Nx \l__tilings_tmpc_tl
1341
        {\int_use:N \g__tilings_tile_int}
        {\int_use:N \g__tilings_tiles_int}
1344
      7
1345
      \UseTile[
1346
1347
        every~ tile/.try,
        every~ thick~ rhombus/.try,
1348
        tile~ \int_use:N \g__tilings_tile_int/.try,
1349
        tile/.try/.expand~ once=\l__tilings_tmpc_tl
1350
      ]{thick~rhombus}
1351
      \group_end:
1352
1353 }
    Now we do the same for the kite and dart tiling.
1354 \prop_gput:Nnn \g__tilings_kite_lms_action_prop {+} {\pgftransformrotate{36}}
1355 \prop_gput:Nnn \g_tilings_kite_lms_action_prop {*} {\pgftransformrotate{108}}
1356 \prop_gput:Nnn \g_tilings_kite_lms_action_prop {-} {\pgftransformrotate{-36}}
1357 \prop_gput:Nnn \g_tilings_kite_lms_action_prop {_}
1358 {\pgftransformrotate{-108}}
1359 \prop_gput:Nnn \g_tilings_kite_lms_action_prop {>} {\pgftransformrotate{180}}
   \prop_gput:Nnn \g__tilings_kite_lms_action_prop {s} {
      \fp_set:Nn \l__tilings_tmpa_fp { 2 * sind(18) * \l__tilings_step_dim }
1361
      \dim_set:Nn \l__tilings_step_dim {\fp_to_dim:N \l__tilings_tmpa_fp}
1362
1363
1364 \prop_gset_eq:NN \g__tilings_ktriangle_lms_action_prop
1365 \g__tilings_kite_lms_action_prop
```

```
\prop_gput:Nnn \g__tilings_kite_lms_action_prop {T} {
     \group_begin:
1367
     \int_gincr:N \g__tilings_tile_int
1368
     \pgftransformrotate{36}
1369
     \fp_set:Nn \l__tilings_tmpa_fp {\l__tilings_step_dim/(1cm)}
     \pgftransformscale{\fp_use:N \l__tilings_tmpa_fp}
     \tl_set:Nx \l__tilings_tmpc_tl
1372
1373
        {\int_use:N \g__tilings_tile_int}
        {\int_use:N \g__tilings_tiles_int}
     \UseTile[
1377
       every~ tile/.try,
1378
       every~ kite/.try,
       tile~ \int_use:N \g__tilings_tile_int/.try,
1380
       tile/.try/.expand~ once=\l__tilings_tmpc_tl
1381
     ]{kite}
1382
1383
     \group_end:
1384 }
1385
   \prop_gput:Nnn \g__tilings_kite_lms_action_prop {g} {
1386
     \group_begin:
1387
     \int_gincr:N \g__tilings_tile_int
     \pgftransformrotate{144}
1388
     \pgftransformxshift{-\l__tilings_step_dim * 2 * sin(18)}
1389
     \fp_set:Nn \l__tilings_tmpa_fp {\l__tilings_step_dim/(1cm)}
1390
     \pgftransformscale{\fp_use:N \l__tilings_tmpa_fp}
1391
     \tl_set:Nx \l__tilings_tmpc_tl
1392
1393
        {\int_use:N \g__tilings_tile_int}
       {\int_use:N \g__tilings_tiles_int}
1395
     }
     \UseTile[
1397
       every~ tile/.try,
1398
       every~ dart/.try,
1399
       1400
       tile/.try/.expand~ once=\l_tilings_tmpc_tl
1401
1402
     \group_end:
1403
1404 }
    Now we set up the actions for the triangle variations.
   \prop_gput:Nnn \g_tilings_rtriangle_lms_action_prop {T} {
     \group_begin:
1407
     \int_gincr:N \g__tilings_tile_int
1408
     \pgftransformrotate{18}
     \fp_set:Nn \l__tilings_tmpa_fp {\l__tilings_step_dim/(1cm)}
1409
     \pgftransformscale{\fp_use:N \l__tilings_tmpa_fp}
1410
     \tl_set:Nx \l__tilings_tmpc_tl
1411
1412
        {\int_use:N \g__tilings_tile_int}
1413
        {\int_use:N \g__tilings_tiles_int}
1414
     \UseTile[
       every~ tile/.try,
1417
       every~ reverse~ golden~ triangle/.try,
1418
       tile~ \int_use:N \g__tilings_tile_int/.try,
1419
       tile/.try/.expand~ once=\l__tilings_tmpc_tl
1420
     ]{reverse~ golden~ triangle}
1421
     \group_end:
1422
1423 }
1424 \prop_gput:Nnn \g__tilings_rtriangle_lms_action_prop {t} {
```

```
1425
           \group_begin:
           \int_gincr:N \g__tilings_tile_int
1426
           \pgftransformrotate{-18}
1427
           \fp_set:Nn \l__tilings_tmpa_fp {\l__tilings_step_dim/(1cm)}
1428
           \pgftransformscale{\fp_use:N \l__tilings_tmpa_fp}
1429
           \tl_set:Nx \l__tilings_tmpc_tl
1430
1431
               {\int_use:N \g__tilings_tile_int}
1432
               {\int_use:N \g__tilings_tiles_int}
1433
1434
           \tl_set:Nx \l__tilings_tmpc_tl
1436
               {\int_use:N \g__tilings_tile_int}
1437
               1438
           }
1439
           \UseTile[
1440
               every~ tile/.try,
1441
               every~ golden~ triangle/.try,
1442
               tile~ \int_use:N \g__tilings_tile_int/.try,
1443
               tile/.try/.expand~ once=\l__tilings_tmpc_tl
           ]{golden~ triangle}
           \group_end:
1446
1447 }
      \prop_gput:Nnn \g__tilings_rtriangle_lms_action_prop {G} {
1448
1449
           \group_begin:
           \int_gincr:N \g__tilings_tile_int
1450
           \pgftransformrotate{180}
1451
           \pgftransformxshift{-\l__tilings_step_dim}
1452
           \fp_set:Nn \l__tilings_tmpa_fp {\l__tilings_step_dim/(1cm)/(2*cosd(36))}
1453
           \pgftransformscale{\fp_use:N \l__tilings_tmpa_fp}
1454
           \tl_set:Nx \l__tilings_tmpc_tl
1455
1456
               {\int_use:N \g__tilings_tile_int}
1457
               {\int_use:N \g__tilings_tiles_int}
1458
           }
1459
           \UseTile[
1460
               every~ tile/.try,
1461
               every~ reverse~ golden~ gnomon/.try,
1462
               tile~ \int_use:N \g__tilings_tile_int/.try,
1463
               tile/.try/.expand~ once=\l__tilings_tmpc_tl
1464
           ]{reverse~ golden~ gnomon}
1465
1466
           \group_end:
1467 }
\prop_gput:\nn \g_tilings_rtriangle_lms_action_prop \{g\} \{
           \group_begin:
           \int_gincr:N \g__tilings_tile_int
1470
           \pgftransformrotate{180}
1471
           \pgftransformxshift{-\l__tilings_step_dim}
1472
           1473
           \position{ line of the line 
1474
1475
           \tl_set:Nx \l__tilings_tmpc_tl
1476
               {\int_use:N \g__tilings_tile_int}
1477
               {\int_use:N \g__tilings_tiles_int}
1478
           }
1479
           \UseTile[
1480
               every~ tile/.try,
1481
               every~ golden~ gnomon/.try,
1482
               tile~ \int_use:N \g__tilings_tile_int/.try,
1483
               tile/.try/.expand~ once=\l__tilings_tmpc_tl
1484
          ]{golden~ gnomon}
```

```
\group_end:
1486
1487
   \prop_gput:Nnn \g__tilings_ktriangle_lms_action_prop {T} {
1488
      \group_begin:
1489
     \int_gincr:N \g__tilings_tile_int
1490
      \pgftransformrotate{18}
1491
      \fp_set:Nn \l__tilings_tmpa_fp {\l__tilings_step_dim/(1cm)}
      \pgftransformscale{\fp_use:N \l__tilings_tmpa_fp}
      \tl_set:Nx \l__tilings_tmpc_tl
        {\int_use:N \g__tilings_tile_int}
1496
        {\int_use:N \g__tilings_tiles_int}
1497
     }
1498
     \UseTile[
1499
       every~ tile/.try,
1500
        every~ reverse~ golden~ triangle/.try,
1501
1502
       tile~ \int_use:N \g__tilings_tile_int/.try,
        tile/.try/.expand~ once=\l__tilings_tmpc_tl
1503
     ]{reverse~ golden~ triangle}
      \group_end:
1505
1506 }
   \prop_gput:Nnn \g__tilings_ktriangle_lms_action_prop {t} {
1507
      \group_begin:
1508
     \int_gincr:N \g__tilings_tile_int
1509
     \pgftransformrotate{-18}
      \fp_set:Nn \l__tilings_tmpa_fp {\l__tilings_step_dim/(1cm)}
      \pgftransformscale{\fp_use:N \l__tilings_tmpa_fp}
      \tl_set:Nx \l__tilings_tmpc_tl
1513
1514
        {\int_use:N \g__tilings_tile_int}
1515
        {\int_use:N \g__tilings_tiles_int}
1516
     }
1517
     \UseTile[
       every~ tile/.try,
1519
        every~ golden~ triangle/.try,
       tile~ \int_use:N \g__tilings_tile_int/.try,
        tile/.try/.expand~ once=\l__tilings_tmpc_tl
     ]{golden~ triangle}
      \group_end:
1524
1525
1526 \prop_gput:Nnn \g__tilings_ktriangle_lms_action_prop {G} {
      \group_begin:
1527
     \verb|\int_gincr:N \g__tilings_tile_int| \\
1528
1529
      \pgftransformrotate{180}
      \pgftransformxshift{-\l__tilings_step_dim}
      \fp_set:Nn \l__tilings_tmpa_fp {\l__tilings_step_dim/(1cm)/(2*cosd(36))}
      \pgftransformscale{\fp_use:N \l__tilings_tmpa_fp}
1533
     \tl_set:Nx \l__tilings_tmpc_tl
1534
        {\int_use:N \g__tilings_tile_int}
        {\int_use:N \g__tilings_tiles_int}
1536
     }
1537
     \UseTile[
1538
       every~ tile/.try,
1539
1540
        every~ reverse~ golden~ gnomon/.try,
       tile~ \int_use:N \g__tilings_tile_int/.try,
        tile/.try/.expand~ once=\l__tilings_tmpc_tl
     ]{reverse~ golden~ gnomon}
     \group_end:
1544
1545 }
```

```
\prop_gput:Nnn \g__tilings_ktriangle_lms_action_prop {g} {
      \group_begin:
1547
      \int_gincr:N \g__tilings_tile_int
1548
      \pgftransformrotate{180}
1549
      \pgftransformxshift{-\l__tilings_step_dim}
1550
      \fp_set:Nn \l__tilings_tmpa_fp {\l__tilings_step_dim/(1cm)/(2*cosd(36))}
      \pgftransformscale{\fp_use:N \l__tilings_tmpa_fp}
1552
      \tl_set:Nx \l__tilings_tmpc_tl
1553
        {\int_use:N \g__tilings_tile_int}
        {\int_use:N \g__tilings_tiles_int}
      ļ
1557
      \UseTile[
1558
        every~ tile/.try,
1559
        every~ golden~ gnomon/.try,
1560
        tile~ \int_use:N \g__tilings_tile_int/.try,
1561
        tile/.try/.expand~ once=\l__tilings_tmpc_tl
1562
      ]{golden~ gnomon}
1563
1564
      \group_end:
1565 }
    Now we do the same for the pentagonal tilings.
    The rules need a variety of turns.
1566 \int_new:N \l__tilings_pentagon_parity_int
1567 \seq_new:N \l__tilings_pentagon_parity_seq
\seq_set_from_clist:Nn \l__tilings_pentagon_parity_seq {odd,even}
   \prop_gput:Nnn \g__tilings_pentagon_lms_action_prop {1} {
      \int_set:Nn \l__tilings_pentagon_parity_int
1571
      {3 - \l_tilings_pentagon_parity_int}
1572 }
1573 \tikzset{
      every~ pentagon~ decomposition/.code={%
1574
        \int_set:Nn \l__tilings_pentagon_parity_int {2}
1575
1576
1577 }
1578 \prop_gput:Nnn \g__tilings_pentagon_lms_action_prop {+}
1579 {\pgftransformrotate{72}}
\prop_gput:Nnn \g_tilings_pentagon_lms_action_prop {*}
1581 {\pgftransformrotate{144}}
1582 \prop_gput:Nnn \g__tilings_pentagon_lms_action_prop {-}
1583 {\pgftransformrotate{288}}
\prop_gput:Nnn \g_tilings_pentagon_lms_action_prop {_}
1585 {\pgftransformrotate{216}}
1586 \prop_gput:Nnn \g_tilings_pentagon_lms_action_prop {>}
1587 {\pgftransformrotate{180}}
1588 \prop_gput:Nnn \g__tilings_pentagon_lms_action_prop {|}
1589 {\pgftransformxscale{-1}}
The scale factor is different.
   \prop_gput:Nnn \g__tilings_pentagon_lms_action_prop {s} {
      \fp_set:Nn \l__tilings_tmpa_fp
1591
        1/(2 + 2 * cosd(72) ) * \l__tilings_step_dim
      \dim_set:Nn \l__tilings_step_dim {\fp_to_dim:N \l__tilings_tmpa_fp}
1595
1596 }
And we tend to work better vertically.
    \prop_gput:Nnn \g__tilings_pentagon_lms_action_prop {f} {
      \fp_set:Nn \l__tilings_tmpa_fp { tand(54)/2 * \l__tilings_step_dim }
      \pgftransformyshift{\fp_to_dim:N \l__tilings_tmpa_fp}
1600 }
\prop_gput:Nnn \g__tilings_pentagon_lms_action_prop {F} {
```

```
\fp_set:\n \l__tilings_tmpa_fp { tand(54) * \l__tilings_step_dim }
1602
      \pgftransformyshift{\fp_to_dim:N \l__tilings_tmpa_fp}
1603
1604
   \prop_gput:Nnn \g__tilings_pentagon_lms_action_prop {d} {
1605
      \fp_set:Nn \l__tilings_tmpa_fp
1606
1607
        (tand(54)/2 - tand(72)/2 + sind(36)) * \l_tilings_step_dim
1608
1609
      \pgftransformyshift{\fp_to_dim:N \l__tilings_tmpa_fp}
1610
1611 }
   \prop_gput:Nnn \g__tilings_pentagon_lms_action_prop {e} {
     \fp_set:Nn \l__tilings_tmpa_fp
1613
1614
       tand(54) * cosd(36) * \l__tilings_step_dim
1615
     }
1616
     \pgftransformyshift{\fp_to_dim:N \l__tilings_tmpa_fp}
1617
1618 }
   \prop_gput:Nnn \g__tilings_pentagon_lms_action_prop {P} {
1619
      \group_begin:
      \int_gincr:N \g__tilings_tile_int
      \fp_set:Nn \l__tilings_tmpa_fp {\l__tilings_step_dim/2}
      \pgftransformxshift{-\fp_to_dim:N \l__tilings_tmpa_fp}
1623
      \fp_set:\n \l__tilings_tmpa_fp {\l__tilings_step_dim*tand(54)/2}
1624
      \pgftransformyshift{-\fp_to_dim:N \l__tilings_tmpa_fp}
1625
     \fp_set:Nn \l__tilings_tmpa_fp {\l__tilings_step_dim/(1cm)}
1626
      \pgftransformscale{\fp_use:N \l__tilings_tmpa_fp}
1627
     \tl_set:Nx \l__tilings_tmpc_tl
1628
1629
        {\int_use:N \g__tilings_tile_int}
1630
        {\int_use:N \g__tilings_tiles_int}
1631
     }
1632
     \UseTile[
1633
        every~ tile/.try,
1634
        every~ pentagon/.try,
1635
        everv~
1636
        \seq_item:Nn \l__tilings_pentagon_parity_seq
1637
        {\l__tilings_pentagon_parity_int}
1638
        \space pentagon/.try,
1639
        every~ pentagon~ 5/.try,
        tile~ \int_use:N \g__tilings_tile_int/.try,
        tile/.try/.expand~ once=\l__tilings_tmpc_tl
1643
     ]{pentagon~5}
      \group_end:
1644
1645
\label{local_local_prop_gput:Nnn g_tilings_pentagon_lms_action_prop {Q} {\ } \\
1647
      \group_begin:
     \int_gincr:N \g__tilings_tile_int
1648
     \fp_set:Nn \l__tilings_tmpa_fp {\l__tilings_step_dim/2}
1649
      \pgftransformxshift{-\fp_to_dim:N \l__tilings_tmpa_fp}
1650
      \fp_set:\n \l__tilings_tmpa_fp {\l__tilings_step_dim*tand(54)/2}
1651
1652
      \pgftransformyshift{-\fp_to_dim:N \l__tilings_tmpa_fp}
      \fp_set:Nn \l__tilings_tmpa_fp {\l__tilings_step_dim/(1cm)}
      \pgftransformscale{\fp_use:N \l__tilings_tmpa_fp}
      \tl_set:Nx \l__tilings_tmpc_tl
        {\int_use:N \g__tilings_tile_int}
1657
        {\int_use:N \g__tilings_tiles_int}
1658
     }
1659
     \UseTile[
1660
       every~ tile/.try,
1661
        every~ pentagon/.try,
1662
```

```
1663
       everv~
       \seq_item:Nn \l__tilings_pentagon_parity_seq
1664
       {\l_tilings_pentagon_parity_int}
1665
       \space pentagon/.try,
1666
       every~ pentagon~ 3/.try,
1667
       tile~ \int_use:N \g__tilings_tile_int/.try,
1668
       tile/.try/.expand~ once=\l__tilings_tmpc_tl
1669
     ]{pentagon~3}
1670
     \group_end:
1671
1672 }
   \prop_gput:Nnn \g__tilings_pentagon_lms_action_prop {R} {
1673
     \group_begin:
1674
     \int_gincr:N \g__tilings_tile_int
1675
     \fp_set:\n \l__tilings_tmpa_fp {\l__tilings_step_dim/2}
1676
     \pgftransformxshift{-\fp_to_dim:N \l__tilings_tmpa_fp}
1677
     \fp_set:Nn \l__tilings_tmpa_fp {\l__tilings_step_dim*tand(54)/2}
1678
1679
     \pgftransformyshift{-\fp_to_dim:N \l__tilings_tmpa_fp}
1680
     \fp_set:Nn \l__tilings_tmpa_fp {\l__tilings_step_dim/(1cm)}
     \pgftransformscale{\fp_use:N \l__tilings_tmpa_fp}
     \tl_set:Nx \l__tilings_tmpc_tl
1682
1683
1684
       {\int_use:N \g__tilings_tile_int}
       {\int_use:N \g__tilings_tiles_int}
1685
1686
     \UseTile[
1687
       every~ tile/.try,
1688
       every~ pentagon/.try,
1689
       \seq_item:Nn \l__tilings_pentagon_parity_seq
       {\l_tilings_pentagon_parity_int}
       \space pentagon/.try,
       every~ pentagon~ 2/.try,
1694
       tile~ \int_use:N \g__tilings_tile_int/.try,
1695
       tile/.try/.expand~ once=\l__tilings_tmpc_tl
1696
     ]{pentagon~2}
1697
     \group_end:
1698
1699 }
   \prop_gput:Nnn \g__tilings_pentagon_lms_action_prop {G} {
     \group_begin:
     \int_gincr:N \g__tilings_tile_int
1702
1703 % \pgftransformrotate{198}
     \fp_set:\n \l__tilings_tmpa_fp {\l__tilings_step_dim*cosd(72)}
1704
     \pgftransformxshift{\fp_to_dim:N \l__tilings_tmpa_fp}
     1706
     \pgftransformyshift{\fp_to_dim:N \l__tilings_tmpa_fp}
1707
     \fp_set:Nn \l__tilings_tmpa_fp {\l__tilings_step_dim/(1cm)}
     \pgftransformscale{\fp_use:N \l__tilings_tmpa_fp}
     \tl_set:Nx \l__tilings_tmpc_tl
1711
       {\int_use:N \g__tilings_tile_int}
       {\int_use:N \g__tilings_tiles_int}
     ļ
1714
     \UseTile[
       every~ tile/.try,
1716
       every~ pentagram/.try,
1717
       tile~ \int_use:N \g__tilings_tile_int/.try,
1718
       tile/.try/.expand~ once=\l__tilings_tmpc_tl
     ]{pentagram}
     \group_end:
1722 }
```

```
1723 \prop_gput:Nnn \g__tilings_pentagon_lms_action_prop {B} {
     \group_begin:
     \int_gincr:N \g__tilings_tile_int
1725
1726 % \pgftransformrotate{198}
     \fp_set:Nn \l__tilings_tmpa_fp {\l__tilings_step_dim*cosd(72)}
     \pgftransformxshift{\fp_to_dim:N \l__tilings_tmpa_fp}
1728
     1729
     \pgftransformyshift{\fp_to_dim:N \l__tilings_tmpa_fp}
1730
     \fp_set:Nn \l__tilings_tmpa_fp {\l__tilings_step_dim/(1cm)}
     \pgftransformscale{\fp_use:N \l__tilings_tmpa_fp}
     \tl_set:Nx \l__tilings_tmpc_tl
1733
1734
       {\int_use:N \g__tilings_tile_int}
1735
       1736
     }
     \UseTile[
1738
       every~ tile/.try,
1739
       every~ boat/.try,
1740
       tile~ \int_use:N \g__tilings_tile_int/.try,
1741
       tile/.try/.expand~ once=\l__tilings_tmpc_tl
     ]{boat}
1744
     \group_end:
1745 }
1746 \prop_gput:Nnn \g__tilings_pentagon_lms_action_prop {D} {
     \group_begin:
1747
     \verb|\int_gincr:N \g__tilings_tile_int| \\
1748
     \pgftransformrotate{90}
1749
     \fp_set:\n \l__tilings_tmpa_fp {\l__tilings_step_dim*cosd(18)}
     \pgftransformxshift{-\fp_to_dim:N \l__tilings_tmpa_fp}
     \fp_set:Nn \l__tilings_tmpa_fp {\l__tilings_step_dim/(1cm)}
     \pgftransformscale{\fp_use:N \l__tilings_tmpa_fp}
     \tl_set:Nx \l__tilings_tmpc_tl
1754
1755
       {\int_use:N \g__tilings_tile_int}
1756
       {\int_use:N \g__tilings_tiles_int}
1757
1758
     \UseTile[
1759
       every~ tile/.try,
1760
       every~ diamond/.try,
1761
       tile~ \int_use:N \g__tilings_tile_int/.try,
       tile/.try/.expand~ once=\l__tilings_tmpc_tl
1763
     ]{diamond}
1764
     \group_end:
1765
1766 }
1767 \ExplSyntaxOff
1768 \RequirePackage{tikz}
1769 \usetikzlibrary{tilings}
1770 \ProvidesFile {tikzlibrarytilings.polykite.code.tex}
   [2023/06/01 v2.0 TikZ pics for Aperiodical Polykite tiles]
```

PolykiteTile Define one of the family of polykite tiles. Needs a name and length parameters. A star option switches the side labels to enable the hat-turtle pairing of a tile with its "opposite".

```
\DeclareDocumentCommand \DefinePolykiteTile {s m m m}
   {
1773
      \IfBooleanTF {#1}
1774
      {
1775
         \DefineTile {#2} {2 2 1 1 2 2 1 1 1 1 2 2 1 1}
1776
      }
1777
1778
         \DefineTile {#2} {1 1 2 2 1 1 2 2 2 2 1 1 2 2}
1779
      }
1780
      {
1781
         {0 : #4}
1782
        ++{90 : #3}
1783
        ++{150 : #3}
1784
        ++{240 : #4}
1785
        ++{180 : #4}
1786
        ++{-90 : #3}
1787
         ++{210 : #3}
1788
         ++{-60 : #4}
1789
        ++{0 : #4}
         ++{0 : #4}
         ++{60 : #4}
1792
        ++{-30 : #3}
        ++{30 : #3}
1794
         ++{120 : #4}
1795
      }
1796
1797 }
```

Some predefined tiles. The aperiodical hat and turtle can be swapped in for each other as they use the same edge definitions. The spectral hat and turtle are designed to be used in the same diagram. Technically, the spectral and aperiodical hats are the same, but I figured it better to have two names for the two uses. The spectre uses the alternating edge scheme.

• Aperiodical and Spectral Hat.

```
\DefinePolykiteTile{aperiodical hat}{sqrt(3)/2}{1/2}
1798
        \DefinePolykiteTile{spectral hat}{sqrt(3)/2}{1/2}
```

Aperiodical and Spectral Turtles.

```
\DefinePolykiteTile{aperiodical turtle}{1/2}{sqrt(3)/2}
1800
         \DefinePolykiteTile*{spectral turtle}{1/2}{sqrt(3)/2}
1801
```

Aperiodical Spectre.

```
\DefineTile {spectre} {a A a A a A a A a A a A }
1802
1803
              \{0 : 1\}
1804
              ++{90 : 1}
1805
              ++{150 : 1}
1806
              ++{240 : 1}
1807
              ++{180 : 1}
1808
              ++{-90 : 1}
              ++{210 : 1}
              ++{-60 : 1}
1811
              ++{0 : 1}
1812
              ++{0 : 1}
1813
              ++{60 : 1}
1814
              ++{-30 : 1}
1815
              ++{30 : 1}
1816
```

```
1817 ++{120 : 1}
1818 }
```

• Meta Clusters

The mapping between the notation in the https://arxiv.org/abs/2303.10798 is:

$$A^{+}, A^{-} \mapsto a, A$$

$$B^{+}, B^{-} \mapsto b, B$$

$$F^{+}, F^{-} \mapsto c, C$$

$$X^{+}, X^{-} \mapsto d, D$$

$$L \mapsto 1$$

```
\DefineTile{meta cluster T}{A A b}
1819
1820
         \{-1.5, -sqrt(3)/2\}
         \{ 1.5, -sqrt(3)/2 \}
         { 0 , sqrt(3) }
1824
         \DefineTile{meta cluster P}{1 D d A 1 D d b}
1825
1826
         \{ -2.5, sqrt(3)/2 \}
1827
         { -2, 0 }
1828
         \{-1.5, -sqrt(3)/2\}
1829
         \{ -0.5, -sqrt(3)/2 \}
1830
         \{ 2.5, -sqrt(3)/2 \}
1831
         { 2,0}
1832
         { 1.5 , sqrt(3)/2 }
         \{ .5 , sqrt(3)/2 \}
1834
1835
         \DefineTile{meta cluster F}{1 D d 1 D c C d b}
1836
         ₹
1837
         \{ -2.5, sqrt(3)/2 \}
1838
         { -2, 0 }
1839
         \{-1.5, -sqrt(3)/2\}
1840
         \{ -0.5, -sqrt(3)/2 \}
1841
         \{ .5 , -sqrt(3)/2 \}
         \{ 1.5, -sqrt(3)/2 \}
         { 2,0}
         { 1.5 , sqrt(3)/2 }
         \{ .5 , sqrt(3)/2 \}
1846
1847
         \DefineTile{meta cluster H}{B D d B D d a D d}
1848
         {
1849
         { -2, -sqrt(3) }
1850
         { 1, -sqrt(3) }
1851
         { 2, -sqrt(3) }
1852
         \{ 2.5, -sqrt(3)/2 \}
1853
         { 1, sqrt(3)}
         \{ .5, 3*sqrt(3)/2 \}
         \{ -.5 , 3*sqrt(3)/2 \}
         { -2, 0 }
1857
         \{ -2.5, -sqrt(3)/2 \}
1858
1859
```

• Super Clusters

DefineTile{super cluster T}{A A b}

```
1861
         { -30 : 3 * (1 + sqrt(5))/2 / sqrt(3) }
1862
         {90:3*(1+sqrt(5))/2/sqrt(3)}
1863
         { 210 : 3 * (1 + sqrt(5))/2 / sqrt(3) }
1864
         }
1865
         % 1 + 3phi, 1 + 2phi
1866
         \DefineTile{super cluster P}{1 D d A 1 D d b}
1867
1868
         \{-1.75 - \text{sqrt}(5), (\text{sqrt}(5)/2 + 1) * \text{sqrt}(3)/2\}
         ++{ -60 : 1 + sqrt(5) }
         ++{ -60 : 1}
         ++{ 1, 0}
         ++{3*(1 + sqrt(5))/2, 0}
         ++{ 120 : 1 + sqrt(5) }
1874
         ++{ 120 : 1 }
1875
         ++{ -1, 0 }
1876
1877
         \DefineTile{super cluster F}{1 D d 1 D c C d b}
1878
1879
         \{-1.75 - \text{sqrt}(5), (\text{sqrt}(5)/2 + 1) * \text{sqrt}(3)/2\}
1880
         ++{ -60 : 1 + sqrt(5) }
         ++{ -60 : 1}
1882
         ++{ 1, 0}
1883
         ++{ 1 + sqrt(5), 0 }
1884
         ++{ 1, 0 }
1885
         +\{ -.75 + (2 + sqrt(5)) * sqrt(3)/4 * sqrt(3)/3,
1886
            (2 + sqrt(5)) * sqrt(3)/4 + 3/4 * sqrt(3)/3 }
1887
         ++{\{ -1.5, (2 + sqrt(5)) * sqrt(3)/2 \}}
1888
         ++{ -1, 0 }
1889
         \DefineTile{super cluster H}{B D d B D d a D d}
         {1.75 + 3*sqrt(5)/4, -(1 + sqrt(5))*sqrt(3)/4}
         ++{120 : 3*(1+sqrt(5))/2 }
         ++{120 : 1 }
1895
         ++{-1,0}
1896
         ++{240 : 3*(1+sqrt(5))/2}
1897
         ++{240 : 1}
1898
         ++{300 : 1}
1899
         ++{3*(1+sqrt(5))/2, 0}
         ++{1, 0}
1901
         ++{60 : 1}
1903

    Subclusters

         \DefineTile{subcluster H}{B B a}
1904
1905
           { 0, 0 }
1906
           { 3, 0 }
1907
            { 60 : 3 }
1908
1909
         \DefineTile{subcluster T}{A A b}
1910
            { 0, 0 }
           { 3, 0 }
1913
            { 60 : 3 }
1914
1915
         \DefineTile{subcluster P}{ 1 A 1 b }
1916
1917
            { 0, 0 }
1918
```

```
{ 1, 0 }
1919
                        { 4, 0 }
1920
                        { 3, 0 }
1921
1922
                    \DefineTile{subcluster F}{ 1 1 f F b }
1923
1924
                        { 0, 0 }
1925
                        { 1, 0 }
1926
                        +{ 60 : 1 }
                        { 2, 0 }
                        { 3, 0 }
1930
        The P and F subclusters have no area, so clipping against them is not helpful.
1931 \tikzset{
           no clip/.code={%
                \tikz@addmode{\tikz@mode@clipfalse}%
1933
            },
1934
            every subcluster P clip/.style={no clip},
1935
            every subcluster F clip/.style={no clip},
1936
1937 }
1938 \BakeTile {aperiodical hat}
1939 \BakeTile {aperiodical turtle}
1940 \BakeTile {spectral hat}
1941 \BakeTile {spectral turtle}
1942 \BakeTile {spectre}
1943 \BakeTile {meta cluster T}
1944 \BakeTile {meta cluster P}
1945 \BakeTile {meta cluster F}
1946 \BakeTile {meta cluster H}
1947 \BakeTile {super cluster T}
1948 \BakeTile {super cluster P}
1949 \BakeTile {super cluster F}
1950 \BakeTile {super cluster H}
        The subclusters are deformed by default.
1951 \ExplSyntaxOn
       \clist_map_inline:nn {a,A,b,B,f,F}
1952
1953
            \tl_new:c {g__tilings_side_polykite_#1_tl}
1954
            \tl_if_exist:cF {g__tilings_side_#1_tl}
1955
1956
                 \tl_new:c {g__tilings_side_#1_tl}
            }
       }
1959
       \tl_gset:cn {g__tilings_side_polykite_A_tl}
1961
1962
            \pgfsyssoftpath@movetotoken {Opt}{-0.3333332942822268pt}
1963
            \pgfsyssoftpath@linetotoken {0.0833331478405773pt}{-0.1889954840909892pt}
1964
             \pgfsyssoftpath@linetotoken {0.3333332942822268pt}{-0.3333332942822268pt}
1965
             \pgfsyssoftpath@linetotoken {0.5833333235705567pt}{-0.1889954840909892pt}
1966
             \protect{\protect} \protect{\p
1967
             \pgfsyssoftpath@linetotoken {1pt}{-0.3333332942822268pt}
1968
1969 }
       \tl_gset:cn {g__tilings_side_polykite_a_tl}
1970
1971
            \pgfsyssoftpath@movetotoken {0pt}{0.33333pt}
1972
            \pgfsyssoftpath@linetotoken {0.33333pt}{0.33333pt}
1973
            \pgfsyssoftpath@linetotoken {0.41667pt}{0.189pt}
```

1974

```
\pgfsyssoftpath@linetotoken {0.66667pt}{0.33333pt}
1975
     \pgfsyssoftpath@linetotoken {0.91667pt}{0.189pt}
1976
     \pgfsyssoftpath@linetotoken {1pt}{0.33333pt}
1977
1978
   \tl_gset:cn {g__tilings_side_polykite_B_tl}
1979
1980
      \pgfsyssoftpath@movetotoken {0pt}{0pt}
1981
      \pgfsyssoftpath@linetotoken {0.3333332942822268pt}{0pt}
1982
      \protect{pgfsyssoftpath@linetotoken {0.4166665592761237pt}{0.1443378101912376pt}}
     \pgfsyssoftpath@linetotoken {0.6666667057177732pt}{0pt}
      \pgfsyssoftpath@linetotoken {0.9166666178527835pt}{0.1443378101912376pt}
      \pgfsyssoftpath@linetotoken {1pt}{0pt}
1987 }
   \tl_gset:cn {g__tilings_side_polykite_b_tl}
1988
1989
     \pgfsyssoftpath@movetotoken {0pt}{0pt}
1990
     \pgfsyssoftpath@linetotoken {0.08333pt}{-0.14433pt}
1991
     \pgfsyssoftpath@linetotoken {0.33333pt}{0pt}
1992
     \pgfsyssoftpath@linetotoken {0.58333pt}{-0.14433pt}
1993
     \pgfsyssoftpath@linetotoken {0.66667pt}{0pt}
1994
     \pgfsyssoftpath@linetotoken {1pt}{0pt}
1995
1996
   \tl_gset:cn {g__tilings_side_polykite_F_tl}
1997
1998 {
     \pgfsyssoftpath@movetotoken {Opt}{-2.00000070292pt}
1999
     \pgfsyssoftpath@linetotoken {0.74999982427pt}{-1.566987221617321pt}
2000
      \pgfsyssoftpath@linetotoken {1pt}{-2.00000070292pt}
2001
2002 }
   \tl_gset:cn {g__tilings_side_polykite_f_tl}
2003
2004
      \pgfsyssoftpath@movetotoken {0pt}{2pt}
     \pgfsyssoftpath@linetotoken {0.25pt}{1.56699pt}
2007
      \pgfsyssoftpath@linetotoken {1pt}{2pt}
2008 }
2000
   \clist_map_inline:nn {a,A,b,B,f,F}
2010
2011
     \tl_gclear_new:c {g__tilings_side_backup_#1_tl}
2012
     \tl_gset_eq:cc {g__tilings_side_backup_#1_tl} {g__tilings_side_#1_tl}
2013
     \tl_gclear_new:c {g__tilings_side_#1_tl}
     \tl_gset_eq:cc {g__tilings_side_#1_tl}{g__tilings_side_polykite_#1_tl}
2016 }
2017
2018 \BakeTile{subcluster~ H}
2019 \BakeTile{subcluster~ T}
2020 \BakeTile{subcluster~ P}
2021 \BakeTile{subcluster~ F}
2022
2023 \clist_map_inline:nn {a,A,b,B,f,F}
2024 {
     \tl_gset_eq:cc {g__tilings_side_#1_tl} {g__tilings_side_backup_#1_tl}
2025
2026 }
```

2.7 Lindenmayer System

cluster tile:nn

These are the rules for generating the super cluster tilings with the Lindenmayer System procedure.

Useful auxiliary for placing a cluster tile from a particular set

```
2027 \cs_new_protected_nopar:Npn \__tilings_place_cluster_tile:nn #1#2
2028 {
2029 \group_begin:
```

```
\int_gincr:N \g__tilings_tile_int
 2030
              \fp_set:Nn \l__tilings_tmpa_fp {\l__tilings_step_dim/(1cm)}
 2031
               \pgftransformscale{\fp_use:N \l__tilings_tmpa_fp}
 2032
              \tl_set:Nx \l__tilings_tmpc_tl
 2033
 2034
                    {\int_use:N \g__tilings_tile_int}
 2035
                    {\int_use:N \g__tilings_tiles_int}
 2036
 2037
              \UseTile[
 2038
                    every~ tile/.try,
                    every~ #1~#2/.try,
                   tile~ \int_use:N \g__tilings_tile_int/.try,
                   tile/.try/.expand~ once=\l__tilings_tmpc_tl
 2042
              1{#1~ #2}
 2043
               \group_end:
 2044
 2045 }
 2046 \cs_generate_variant:Nn \__tilings_place_cluster_tile:nn {Vn}
(End definition for \__tilings_place_cluster_tile:nn.)
 2049 {
 2050
               [s H]
 2051 }
 2052 \prop_gput:Nnn \g__tilings_supercluster_lms_rule_prop {H}
               [s {r{-60}} T]
 2054
               [s {x{\phi_t}_{1}} {y{\phi_t}_{1}} 
 2055
 2056
                    {x{\phi_c=2-3*\c_tilings\_phi_fp}}
 2057
                    {y{\fp_to_decimal:n{-\c_tilings_phi_fp}}}
 2058
 2059
               [s
 2060
                    {x{\fp_to_decimal:n{1+3*\c__tilings_phi_fp}}}
 2061
                    {y{\fp_to_decimal:n{-1-\c__tilings_phi_fp}}}
 2062
                    \{r\{-120\}\}
 2063
                   НΊ
              ſs
                    {x{\phi_{-1.5-3.5*}c_tilings_phi_fp}}
                    {y(fp_to_decimal:n{2.5*\c_tilings_phi_fp+1.5})}
 2067
                    {r{-120}}
 2068
                   P]
 2069
               [s
 2070
                    {x{\fp_to_decimal:n{-1.5-2*\c__tilings_phi_fp}}}
 2071
                     \{y\{\fp\_to\_decimal:n\{-1.5-3*\c\_tilings\_phi\_fp\}\}\} 
 2072
                    {r{180}}
 2073
                   PΊ
 2074
 2075
               Гs
                    {x{\fp_to_decimal:n{3+5.5*\c__tilings_phi_fp}}}
                    {y{\fp_to_decimal:n{.5*\c__tilings_phi_fp}}}
 2077
                    {r{120}}
 2078
                   P]
 2079
 2080
                    {x\{\fp_to_decimal:n\{-4.5-6.5*\c_tilings_phi_fp\}\}}
 2081
                    {y{\fp_to_decimal:n{.5-.5*\c_tilings_phi_fp}}}
 2082
                    {r{-120}}
 2083
                   Fl
                    {x{\phi_1.5+4*\c_tilings\_phi_fp}}
                    {y{\fp_to_decimal:n{-2.5-3*\c__tilings_phi_fp}}}
                   F٦
 2088
```

```
ſs
2089
        {x{\phi_{a}: n{3+2.5*}c_tilings_phi_fp}}
2090
         \{y \{ f_{to\_decimal:n\{2+3.5* c\_tilings\_phi\_fp\}} \} 
2091
        {r{120}}
2092
2093
2094 }
   \prop_gput:Nnn \g__tilings_supercluster_lms_rule_prop {P}
2095
2096 {
      [s {r{60}} P]
     ſs
        {x{\phi_1:n{2.5+3.5*}c_tilings_phi_fp}}
        {y{\fp_to_decimal:n{-.5-.5*\c__tilings_phi_fp}}}
        \{r\{-120\}\}
       Н٦
      Γs
        {x{\phi_1:n{-2.5-3.5*}c_tilings\_phi_fp}}
2104
        {y{\fp_to_decimal:n{.5+.5*\c_tilings_phi_fp}}}
        {r{180}}
2106
       H]
      [s
2108
        {x{\phi_{x}(x_{-tilings_phi_fp})}}
2109
        {y{\fp_to_decimal:n{.5+\c__tilings_phi_fp}}}
        {r{120}}
2111
       FΊ
2112
      Γs
2113
        {x{\phi_c}_{-4.5-6*\c_tilings\_phi_fp}}
2114
        {y(fp_to_decimal:n\{-.5-\c_tilings_phi_fp\})}
        \{r\{-60\}\}
2116
       F]
2117
2118 }
2119
   \prop_gput:Nnn \g__tilings_supercluster_lms_rule_prop {F}
      [s {r{60}} P]
2121
     [s
         \{x\{\fp\_to\_decimal:n\{2.5+3.5*\c\__tilings\_phi\_fp\}\}\} 
2123
         \{y\{\fp\_to\_decimal:n\{-.5-.5*\c\__tilings\_phi\_fp\}\}\} 
2124
        \{r\{-120\}\}
       Н٦
2126
2127
        {x\{\fp_to_decimal:n\{-2.5-3.5*\c_tilings_phi_fp\}\}}
2128
        {y{\fp_to_decimal:n{.5+.5*\c__tilings_phi_fp}}}
2129
        {r{180}}
2130
      Гs
        {x{\phi_1}, x{\phi_2} = x{\phi_1}, x{\phi_2}}
        {y{\fp_to_decimal:n{.5+\c__tilings_phi_fp}}}
2134
        {r{120}}
2135
       F٦
2136
        {x{\fp_to_decimal:n{-4.5-6*\c__tilings_phi_fp}}}
2138
        {y{\fp_to_decimal:n{-.5-\c__tilings_phi_fp}}}
2139
        \{r\{-60\}\}
       Fl
2142
      Гs
        {x{\phi_{a+4.5*}c_tilings_phi_fp}}
        {y(fp_to_decimal:n\{-2-2.5*\c_tilings_phi_fp\})}
2144
2145
2146 }
2147 \prop_gput:Nnn \g__tilings_drawables_lms_prop {supercluster} {HTPF}
2148 \fp_const:Nn \c__tilings_phi_fp {(1 + sqrt(5))/2}
2149 \prop_new:N \g__tilings_supercluster_lms_action_prop
```

```
2150
   \prop_gput:Nnn \g__tilings_supercluster_lms_action_prop {r}
2151
2152
      \pgftransformrotate{\l__tilings_parameters_lms_tl}
2154
   \prop_gput:Nnn \g__tilings_supercluster_lms_action_prop {x}
2155
2156 {
      \pgftransformxshift{
2157
        \fp_to_dim:n
2158
        {.5 * (\l_tilings_parameters_lms_tl) * \l_tilings_step_dim}
2159
     }
2160
2161 }
   \prop_gput:Nnn \g__tilings_supercluster_lms_action_prop {y}
2162
   Ł
2163
      \pgftransformyshift{
2164
        \fp_to_dim:n
2165
        {.5 * sqrt(3) * (\l__tilings_parameters_lms_tl) * \l__tilings_step_dim}
2166
     }
2167
2168 }
2169
   \prop_gput:Nnn \g__tilings_supercluster_lms_action_prop {s}
2170
2171 {
     \fp_set:Nn \l__tilings_tmpa_fp {
2172
        \l__tilings_step_dim
2173
2174
        \c__tilings_phi_fp
2176
        \c__tilings_phi_fp
2177
2178
2179
     \dim_set:Nn \l__tilings_step_dim {\fp_to_dim:N \l__tilings_tmpa_fp}
2180 }
2181
   \prop_gput:Nnn \g__tilings_supercluster_lms_action_prop {H}
2182 {
      \__tilings_place_cluster_tile:nn {super~ cluster}{H}
2183
2184 }
   \prop_gput:Nnn \g__tilings_supercluster_lms_action_prop {T}
2185
   {
2186
        _tilings_place_cluster_tile:nn {super~ cluster}{T}
2187
2188 }
   \prop_gput:Nnn \g__tilings_supercluster_lms_action_prop {P}
2189
2190
      \__tilings_place_cluster_tile:nn {super~ cluster}{P}
2191
2192 }
   \prop_gput:Nnn \g__tilings_supercluster_lms_action_prop {F}
2194 {
      \__tilings_place_cluster_tile:nn {super~ cluster}{F}
2195
2196 }
   Parameters:
```

- 1. Cluster type (super cluster, meta cluster, subcluster)
- 2. This tile type (H, T, P, F)
- 3. This tile's name
- 4. Alignment tile's name
- 5. Edge to align along
- 6. Edge to align with

```
\cs_new_protected_nopar:Npn \__tilings_place_cluster_tile_as_pic:nnnnnn #1#2#3#4#5#6
2198 {
     \group_begin:
2199
     2200
     \fp_set:Nn \l__tilings_tmpa_fp {\l__tilings_step_dim/(1cm)}
2201
     \tl_set:Nx \l__tilings_tmpc_tl
2202
2203
        {\int_use:N \g__tilings_tile_int}
2204
        {\int_use:N \g__tilings_tiles_int}
2205
     \tl_clear:N \l__tilings_tmpa_tl
     \tl_put_right:Nn \l__tilings_tmpa_tl
2209
     {
       \pic[
         every~ tile/.try,
2211
         every~ #1~#2/.try,
2212
2213
       \tl_put_right:Nx \l__tilings_tmpa_tl
2214
2215
       tile~ \int_use:N \g__tilings_tile_int/.try,
2216
       tile/.try=\l__tilings_tmpc_tl,
       scale=\fp_use:N \l__tilings_tmpa_fp,
2218
2219
       \tl_put_right:Nn \l__tilings_tmpa_tl
2220
2221
         name=#3.
2222
2223
       \tl_if_empty:nTF {#4}
2224
2225
         \tl_put_right:Nn \l__tilings_tmpa_tl
            first~ tile/.try,
         }
2229
       }
2230
2231
          \tl_put_right:Nn \l__tilings_tmpa_tl
            align~ with=#4~along~#5
2234
         }
         \tl_if_single:nF {#6}
            \tl_put_right:Nx \l__tilings_tmpa_tl
              \c_space_tl using~\tl_tail:n {#6}
2241
         }
2242
          \tl_put_right:Nn \l__tilings_tmpa_tl {,}
2243
2244
       \tl_put_right:Nn \l__tilings_tmpa_tl
2245
       {
2246
         #1~ #2
       ];
     \tl_use:N \l__tilings_tmpa_tl
2251
     \group_end:
2252 }
   \cs_generate_variant:\n\__tilings_place_cluster_tile_as_pic:nnnnnn {
2253
     Vnnnnn, VnVnnn, VnVVnn
2254
2255 }
2256 \tikzset{
     cluster~ type/.initial=super~ cluster,
```

```
2258 first~ file/.style={transform~ shape}
2259 }
2260 \prop_new:N \g__tilings_cluster_lms_rule_prop
```

The first set of rules govern when the tile being replaced is a root tile, in which case one of the new tiles becomes the new root and all others are placed with respect to them.

It's convenient for code readability to have aliases for the labels for the parent and adjoining tiles, which are stored in the \l_@@_parameters_lms_tl token list.

```
\cs_new_nopar:Npn \__tilings_tile_label:
2262 {
     \tl_item: Nn \l__tilings_parameters_lms_tl {1}
2263
2264
   \cs_new_nopar:Npn \__tilings_adjoint_label:
2266
     \tl_item:Nn \l__tilings_parameters_lms_tl {2}
2267
2268 }
    A single T tile is replaced by a single H tile
   \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {T}
2269
2271
      [s {H{\__tilings_tile_label:0}{}}]
2272 }
    An H tile is replaced by 10 tiles, consisting of a T tile and 3 each of H, P, and F.
   \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {H}
2274
      [s \{r\{-60\}\}\ \{T\{\_tilings_tile_label:0\}\{\}\}\]
     [{ {HTa{A1}} {\__tilings_tile_label:1} {\__tilings_tile_label:0} }]
     [{ {HTa{A2}} {\__tilings_tile_label:2} {\__tilings_tile_label:0} }]
     [{ {HT{B1}b} {\__tilings_tile_label:3} {\__tilings_tile_label:0} }]
     [{ {PHb{B2}} {\_tilings_tile_label:4} {\_tilings_tile_label:1} }]
     [{ {PHb{B2}} {\_tilings_tile_label:5} {\_tilings_tile_label:2} }]
     [{ {PHAa} {\_tilings_tile_label:6} {\_tilings_tile_label:3} }]
2281
2282
     [{ {FHb{B1}} {\_tilings_tile_label:7} {\_tilings_tile_label:1} }]
2283
     [{ {FHb{B1}} {\_tilings_tile_label:8} {\_tilings_tile_label:2} }]
2284
     [{ {FHb{B2}} {\_tilings_tile_label:9} {\_tilings_tile_label:3} }]
2285 }
    Lastly, the P and F tile substitutions.
   \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {P}
2286
2287 {
      [s \{r\{60\}\}\ \{P\{\setminus\_tilings\_tile\_label:0\}\{\}\}\]
2288
     [{ {HPaA} {\_tilings_tile_label:1} {\_tilings_tile_label:0} }]
2289
     [{ {HP{B2}b} {\__tilings_tile_label:2} {\__tilings_tile_label:0} }]
     [{ {FHb{B2}} {\__tilings_tile_label:3} {\__tilings_tile_label:1} }]
     [{ {FHb{B1}} {\__tilings_tile_label:4} {\__tilings_tile_label:2} }]
2292
2293
   \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {F}
2294
   {
2295
     [s \{r\{60\}\}\ \{P\{\__tilings_tile_label:0\}\}\}]
2296
     [{ {HPaA} {\_tilings_tile_label:1} {\_tilings_tile_label:0} }]
     [{ {HP{B2}b} {\__tilings_tile_label:2} {\__tilings_tile_label:0} }]
      [{ {FHb{B2}} {\__tilings_tile_label:3} {\__tilings_tile_label:1} }]
      [{ {FHb{B1}} {\__tilings_tile_label:4} {\__tilings_tile_label:2} }]
      [{ {FHb{B1}} {\_tilings_tile_label:5} {\__tilings_tile_label:1} }]
2301
2302 }
```

The rest of the rules are for when the tile being replaced was itself positioned by aligning it with another tile. For these tiles, one of its edge tiles will be its root and positioned alongside one of the edge tiles of the replacement of the original tile's alignment tile. Then all the other tiles are positioned out from that root. The labelling has to be the same regardless of the order of drawing the tiles.

Not every edge pairing is necessary to generate a pattern as the edges that can be created are all between A^{\pm} edges and between B^{\pm} edges. However, to avoid errors in case they are part of the seed then for now we create blank substitution rules that will effectively remove any such rogue elements.

```
2303 \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {TH{A1}a} {}
2304 \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {TH{A2}a} {}
2305 \prop_gput:Nnn \g_tilings_cluster_lms_rule_prop {THb{B1}} {}
2306 \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {THb{B2}} {}
2307 \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {HTa{A1}}
2308 \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {HTa{A2}} {}
2309 \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {HT{B1}b} {}
2310 \prop_gput:Nnn \g_tilings_cluster_lms_rule_prop {HT{B2}b} {}
2311 \prop_gput:\nn \g__tilings_cluster_lms_rule_prop {HPaA} {}
2312 \prop_gput:Nnn \g_tilings_cluster_lms_rule_prop {HP{B1}b} {}
2313 \prop_gput:Nnn \g_tilings_cluster_lms_rule_prop {HP{B2}b} {}
2314 \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {HF{B1}b} {}
2315 \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {HF{B2}b} {}
2316 \prop_gput:Nnn \g_tilings_cluster_lms_rule_prop {PHAa} {}
2317 \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {PHb{B1}} {}
2318 \prop_gput:Nnn \g_tilings_cluster_lms_rule_prop {PHb{B2}} {}
2319 \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {PF{11}{11}} {}
2320 \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {PF{12}{11}} {}
2321 \prop_gput:Nnn \g_tilings_cluster_lms_rule_prop {PF{11}{12}} {}
\label{local_prop_gput:Nnn g_tilings_cluster_lms_rule_prop {PF\{12\}\{12\}\} } \{\} 
2323 \prop_gput:Nnn \g_tilings_cluster_lms_rule_prop {FHb{B1}} {}
2324 \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {FHb{B2}} {}
2325 \prop_gput:Nnn \g_tilings_cluster_lms_rule_prop {FP{11}{11}} {}
2326 \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {FP{12}{11}} {}
2327 \prop_gput:Nnn \g_tilings_cluster_lms_rule_prop {FP{11}{12}} {}
2328 \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {FP{12}{12}} {}
2329 \prop_gput:\nn \g__tilings_cluster_lms_rule_prop \{FffF\} \{\}
2330 \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {FFFf} {}
2331 \prop_gput:Nnn \g_tilings_cluster_lms_rule_prop {FF{11}{11}} {}
2332 \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {FF{12}{11}} {}
2333 \prop_gput:Nnn \g_tilings_cluster_lms_rule_prop {FF{11}{12}} {}
\label{lings_cluster_lms_rule_prop} $$ \operatorname{PF}_{12}_{12}  $$ $$
```

To help create the rules then we start with some helper macros. Each of these creates the substitution rule for a tile given certain information about where the parent tile is positioned. Most of the substitution information consists of placing the tiles next to each other, so only the first tile needs to know about a tile from a different set. This makes it relatively easy to set up some templates for the substitution rules.

```
2335 \cs_new_nopar:cpn {__tilings_T{A1}_creator:nnnnn} #1#2#3#4#5
2336
      \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {T#1{A1}#2}
2338
2339
        [{ {H#3{B1}#4} {\_tilings_tile_label:0} {\_tilings_adjoint_label:#5} }]
2340
   \cs_new_nopar:cpn {__tilings_T{A2}_creator:nnnnn} #1#2#3#4#5
2343
     \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {T#1{A2}#2}
2344
2345
        [{ \{H#3\{B2\}#4\} \{\_tilings_tile_label:0\} \{\_tilings_adjoint_label:#5\} \}]
2346
2347
2348 }
   \cs_new_nopar:cpn {__tilings_Tb_creator:nnnnn} #1#2#3#4#5
2349
2350
     \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {T#1b#2}
        [{ {H#3a#4} {\_tilings_tile_label:0} {\_tilings_adjoint_label:#5} }]
2354
2355 }
```

```
2356
2357 \cs_new_nopar:cpn {__tilings_H{B1}_creator:nnnnn} #1#2#3#4#5
2358
     \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {H#1{B1}#2}
2359
2360
        [{ {P#3A#4} {\ tilings tile label:4} {\ tilings adjoint label:#5} }]
2361
2362
        [{ {HP{B2}b} {\__tilings_tile_label:1} {\__tilings_tile_label:4} }]
2363
        [{ {TH{A1}a} {\__tilings_tile_label:0} {\__tilings_tile_label:1} }]
2364
        [{ {HTa{A2}} {\__tilings_tile_label:2} {\__tilings_tile_label:0} }]
        [{ {PHb{B2}} {\__tilings_tile_label:5} {\__tilings_tile_label:2} }]
        [{ {HT{B1}b} {\__tilings_tile_label:3} {\__tilings_tile_label:0} }]
2369
        [{ {PHAa} {\__tilings_tile_label:6} {\__tilings_tile_label:3} }]
2371
        [{ {FHb{B1}} {\_tilings_tile_label:7} {\_tilings_tile_label:1} }]
        [{ {FHb{B1}} {\_tilings_tile_label:8} {\_tilings_tile_label:2} }]
2373
        [{ {FHb{B2}} {\_tilings_tile_label:9} {\_tilings_tile_label:3} }]
2374
     }
2376 }
2377
2378 \cs_new_nopar:cpn {__tilings_H{B2}_creator:nnnnn} #1#2#3#4#5
2379
     \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {H#1{B2}#2}
2380
2381
        [{ {P#3A#4} {\_tilings_tile_label:5} {\_tilings_adjoint_label:#5} }]
2382
2383
        [{ {HP{B2}b} {\__tilings_tile_label:2} {\__tilings_tile_label:5} }]
2384
        [{ {TH{A2}a} {\__tilings_tile_label:0} {\__tilings_tile_label:2} }]
2385
        [{ {HTa{A1}} {\__tilings_tile_label:1} {\__tilings_tile_label:0} }]
        [{ {PHb{B2}} {\_tilings_tile_label:4} {\_tilings_tile_label:1} }]
        [{ {HT{B1}b} {\__tilings_tile_label:3} {\__tilings_tile_label:0} }]
2390
        [{ {PHAa} {\__tilings_tile_label:6} {\__tilings_tile_label:3} }]
2391
2392
        [{ {FHb{B1}} {\_tilings_tile_label:7} {\_tilings_tile_label:1} }]
2393
        [{ {FHb{B1}} {\__tilings_tile_label:8} {\__tilings_tile_label:2} }]
2394
        [{ {FHb{B2}} {\_tilings_tile_label:9} {\_tilings_tile_label:3} }]
     }
2396
2397 }
   \cs_new_nopar:cpn {__tilings_Ha_creator:nnnnn} #1#2#3#4#5
2400 {
      \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {H#1a#2}
2401
2402
        [{ {P#3b#4} {\__tilings_tile_label:6} {\__tilings_adjoint_label:#5} }]
2403
2404
        [{ {HPaA} {\__tilings_tile_label:3} {\__tilings_tile_label:6} }]
2405
        [{ {THb{B1}} {\__tilings_tile_label:0} {\__tilings_tile_label:3} }]
2406
        [{ {HTa{A1}} {\__tilings_tile_label:1} {\__tilings_tile_label:0} }]
        [{ {PHb{B2}} {\__tilings_tile_label:4} {\__tilings_tile_label:1} }]
        [{ {HTa{A2}} {\__tilings_tile_label:2} {\__tilings_tile_label:0} }]
2411
        [{ {PHb{B2}} {\__tilings_tile_label:5} {\__tilings_tile_label:2} }]
2412
2413
        [{ {FHb{B1}} {\__tilings_tile_label:7} {\__tilings_tile_label:1} }]
2414
        [{ {FHb{B1}} {\__tilings_tile_label:8} {\__tilings_tile_label:2} }]
2415
        [{ {FHb{B2}} {\__tilings_tile_label:9} {\__tilings_tile_label:3} }]
2416
```

```
}
2417
2418 }
2419
       \cs_new_nopar:cpn {__tilings_PA_creator:nnnnn} #1#2#3#4#5
2420
2421
            \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {P#1A#2}
2422
           {
2423
                 \begin{tabular}{ll} $$ \{H#3\{B1\}#4\} $$ (\_tilings_tile_label:1) $$ (\_tilings_adjoint_label:#5) $$ $$ (\_tilings_tile_label:1) $$ (\_tilings_adjoint_label:#5) $$ $$ (\_tilings_adjoint_
2424
                [{ {PHAa} {\__tilings_tile_label:0} {\__tilings_tile_label:1} }]
                [\{ \ \{HP\{B2\}b\} \ \{\_\_tilings\_tile\_label:2\} \ \{\\__tilings\_tile\_label:0\} \ \}]
                [{ {FHb{B2}} {\_tilings_tile_label:3} {\_tilings_tile_label:1} }]
                [{ {FHb{B1}} {\_tilings_tile_label:4} {\_tilings_tile_label:2} }]
           }
2430
2431 }
2432
2433 \cs_new_nopar:cpn {__tilings_Pb_creator:nnnnn} #1#2#3#4#5
2434
           \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {P#1b#2}
2435
                [{ {H#3a#4} {\__tilings_tile_label:2} {\__tilings_adjoint_label:#5} }]
                [{ {PHb{B2}} {\__tilings_tile_label:0}{\__tilings_tile_label:2} }]
2438
                [{ {HPaA} {\__tilings_tile_label:1} {\__tilings_tile_label:0} }]
2439
2440
                [{ {FHb{B2}} {\_tilings_tile_label:3} {\_tilings_tile_label:1} }]
2441
                [{ {FHb{B1}} {\_tilings_tile_label:4} {\_tilings_tile_label:2} }]
2442
           }
2443
2444 }
2445
2446 \cs_new_nopar:cpn {__tilings_Fb_creator:nnnnn} #1#2#3#4#5
            \prop_gput:Nnn \g__tilings_cluster_lms_rule_prop {F#1b#2}
                [{ {H#3a#4} {\__tilings_tile_label:2} {\__tilings_adjoint_label:#5} }]
                [{ {PHb{B2}} {\__tilings_tile_label:0}{\__tilings_tile_label:2} }]
2451
                [{ {HPaA} {\__tilings_tile_label:1} {\__tilings_tile_label:0} }]
2452
2453
                [{ {FHb{B2}} {\_tilings_tile_label:3} {\_tilings_tile_label:1} }]
2454
                [{ {FHb{B1}} {\__tilings_tile_label:4} {\__tilings_tile_label:2} }]
2455
                [{ {FHb{B1}} {\_tilings_tile_label:5} {\_tilings_tile_label:1} }]
2458 }
        Now that the creators are set up it is time to invoke them.
      \clist_map_inline:nn
2460 {
           TH{{A1}}a HP{{B1}}b06,
2461
           TH{A2}}a HP{{B2}}}b06,
2462
           THb{{B1}} HPaAO4,
2463
           THb{{B2}} HPaAO5,
2464
           PHAa HP{{{B1}}}b16,
2465
           PHb{{B1}} HPaA24,
2466
           PHb{{B2}} HPaA25,
2467
           FHb{{B1}} HPaA24,
2468
           FHb{{B2}} HPaA25,
2470 }
2471 {
2472
           \tl_clear:N \l__tilings_tmpa_tl
           \tl_put_right:Nn \l__tilings_tmpa_tl { \use:c }
2473
           \tl_put_right:Nx \l__tilings_tmpa_tl
2474
2475
                {__tilings_ \tl_item:nn {#1}{2}\tl_item:nn {#1}{4} _creator:nnnnn}
2476
```

```
{\tl_item:nn {#1}{1}}{\tl_item:nn{#1}{3}}
2477
        \tl_item:nn {#1}{5}\tl_item:nn{#1}{7}
2478
        \tl_item:nn {#1}{9}
2479
2480
     \tl_use:N \l__tilings_tmpa_tl
2481
     \tl_clear:N \l__tilings_tmpa_tl
2482
     \tl_put_right:Nn \l__tilings_tmpa_tl { \use:c }
2483
      \tl_put_right:Nx \l__tilings_tmpa_tl
2484
        {_\_tilings\_ \tl\_item:nn {#1}{1}\tl\_item:nn {#1}{3} \_creator:nnnnn}
        {\tilde{4}}_{item:nn {#1}{2}}{\tilde{4}}
        \tl_item:nn {#1}{6}\tl_item:nn{#1}{8}
2489
        \tl_item:nn {#1}{10}
     }
2490
     \tl_use:N \l__tilings_tmpa_tl
2491
2492 }
2493
2494 \prop_new:N \g__tilings_cluster_lms_action_prop
2495 \prop_gput:Nnn \g__tilings_drawables_lms_prop {cluster} {HTPF}
   \prop_gput:Nnn \g__tilings_cluster_lms_action_prop {r}
2496
2497 {
      \pgftransformrotate{\l__tilings_parameters_lms_tl}
2498
2499 }
   \prop_gput:Nnn \g__tilings_cluster_lms_action_prop {x}
2500
2501
      \pgftransformxshift{
2503
        \fp_to_dim:n
        {.5 * (\l__tilings_parameters_lms_tl) * \l__tilings_step_dim}
2504
2505
2506 }
2507
   \prop_gput:Nnn \g__tilings_cluster_lms_action_prop {y}
2508 {
      \pgftransformyshift{
2509
        \fp_to_dim:n
2510
        \{.5 * \text{sqrt}(3) * (\l_tilings_parameters_lms_tl) * \l_tilings_step_dim\}
     }
2512
2513 }
2514
2515 \prop_gput:Nnn \g__tilings_cluster_lms_action_prop {s}
2516
     \fp_set:Nn \l__tilings_tmpa_fp {
2517
        \l__tilings_step_dim
2518
2519
2520
        \c__tilings_phi_fp
2521
        \c__tilings_phi_fp
     }
2523
     \dim_set:Nn \l__tilings_step_dim {\fp_to_dim:N \l__tilings_tmpa_fp}
2524
2525 }
    The first set of actions are for when this tile is the root so doesn't have a parent
   \clist_map_inline:nn {H,T,P,F}
2526
2527 {
2528
      \prop_gput:Nnn \g__tilings_cluster_lms_action_prop {#1}
2529
2530
        \__tilings_tikz_keys_get:Nn \l__tilings_tmpa_tl {cluster~type}
2531
        \tl_set:Nx \l__tilings_tmpb_tl {\tl_item:Nn \l__tilings_parameters_lms_tl {1}}
2532
        \__tilings_place_cluster_tile_as_pic:VnVnnn
2533
        \l__tilings_tmpa_tl {#1} \l__tilings_tmpb_tl {}{}{}
```

```
}
2535
2536 }
    The second set is for when there is an adjoining edge
2537 \cs_new_protected_nopar:Npn \__tilings_place_cluster_tile_as_pic_aux:nnnn #1#2#3#4
     \__tilings_tikz_keys_get:Nn \l__tilings_tmpa_tl {cluster~type}
2539
     \tl_set:Nx \l__tilings_tmpb_tl {\__tilings_tile_label:}
2540
     \tl_set:Nx \l__tilings_tmpc_tl {\__tilings_adjoint_label:}
2541
     \__tilings_place_cluster_tile_as_pic:VnVVnn
2542
     \l__tilings_tmpa_tl {#1} \l__tilings_tmpb_tl \l__tilings_tmpc_tl {#4}{#3}
2543
2544 }
2545
2546 \clist_map_inline:nn {
     TH{A1}a,
     TH{A2}a,
     THb\{B1\},
     THb{B2},
     HTa{A1},
2551
     HTa{A2},
2552
     HT{B1}b,
2553
     HT{B2}b,
2554
     HPaA,
2555
     HP\{B1\}b,
2556
     HP\{B2\}b,
2557
     HF{B1}b,
     HF\{B2\}b,
     PHAa,
     PHb{B1},
2561
     PHb{B2},
2562
     PF{11}{11},
2563
     PF{12}{11},
2564
     PF{11}{12},
2565
     PF{12}{12},
2566
     FHb{B1},
2567
     FHb{B2},
     FP{11}{11},
     FP{12}{11},
     FP{11}{12},
2571
     FP{12}{12},
2572
     FFfF,
2573
     FFFf,
2574
     FF{11}{11},
2575
     FF{12}{11},
2576
     FF{11}{12},
2577
     FF{12}{12}
2578
2579 }
2580 {
     \prop_gput:Nnn \g__tilings_cluster_lms_action_prop {#1}
2581
2582
        \__tilings_place_cluster_tile_as_pic_aux:nnnn #1
2583
     }
2584
2585 }
2586
2587 \ExplSyntaxOff
2588 \ProvidesFile {tikzlibrarypenrose.code.tex}
    [2023/06/01 v2.0 TikZ pics for Penrose tiles]
2590 \usetikzlibrary{tilings.penrose}
    Backwards compatibility mode:
```

• \SetPenrosePath is \SetTilingPath

- \BakePenroseTile and \MakePenroseTile are \BakeTile
- \UsePenroseTile is \UseTile
- \PenroseDecomposition is \TilingDecomposition

```
2591 \ExplSyntaxOn
2592 \NewDocumentCommand \SetPenrosePath { m }
2593 {
      \__tilings_set_tiling_path:n {#1}
2594
2596 \NewDocumentCommand \BakePenroseTile {m}
2597 {
      \_tilings_bake_tile:n {#1}
2599 }
{\tt 2600} \ {\tt NewDocumentCommand} \ {\tt MakePenroseTile} \ \{{\tt m}\}
2601
      \__tilings_bake_tile:n {#1}
2602
2603 }
2604 \NewDocumentCommand \UsePenroseTile {O{} m}
2605 {
      \_tilings_use_tile:nn {#1}{#2}
2607 }
2608 \NewDocumentCommand \PenroseDecomposition { O{} m m m }
2610
      __tilings_tiling_decomposition:nnnn {#1}{#2}{#3}{#4}
2611 }
2612 \ExplSyntaxOff
2613 \tikzset{
     save Penrose path/.forward to=/tikz/save tiling path,
2614
     clone Penrose side path/.forward to=/tikz/clone tiling side path,
     spath/prefix/Penrose side/.forward to=/tikz/spath/prefix/tiling side,
     spath/suffix/Penrose side/.forward to=/tikz/spath/suffix/tiling side,
     clone Penrose tile path/.forward to=/tikz/clone tiling tile path,
     spath/prefix/Penrose tile/.forward to=/tikz/spath/prefix/tiling tile,
2619
     spath/suffix/Penrose tile/.forward to=/tikz/spath/suffix/tiling tile,
     Penrose step/.forward to=/tikz/tiling step,
2621
     every tile/.append style={
2622
        every Penrose tile/.try
2623
     },
     every tile clip/.append style={
        every Penrose tile clip/.try
2627
     },
     every tile pic/.append style={
2628
        every Penrose pic/.try
2629
     },
2630
     tile/.append style={
2631
        Penrose tile #1/.try,
2632
        Penrose tile/.try=#1
2633
2634
2635 }
```