



Statistical Analysis - II Group Assignment

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Questions

Part A

A real estate agent is trying to understand the nature of housing stock and home prices in and around a medium sized town in upstate New York. She has collected data from a random sample of 1047 homes sold in the last 12 months. Data was collected on the following variables and is available in the houseprices.csv file.

- Price – the sale price of the house in \$
- Living Area – in Sq. ft.
- Bathrooms – number of bathrooms in the house (powder rooms with no tub or shower area are considered 0.5 baths)
- Bedrooms – the number of bedrooms
- Lot Size – size of the property on which the house sits (in acres).
- Age – of the house in years
- Fireplace – whether or not the house has a fireplace (Yes = 1, No = 0)

Your task in this assignment is to analyse this dataset to gain some understanding of this particular real estate market – the values of homes, their characteristics in terms of size and other features, and relationships between these. This understanding will prove immensely helpful to the real estate agent in advising her clients. Since all of the homes are from the same geographical area, location (which usually has a huge bearing on home values) is not a major concern here.

Most of the analysis will be done in response to the specific questions posed on the homework assignments. But feel free to explore and play around with the data set to enhance your own understanding of how to make sense of data.

1. a) Your friend claims that the average house price in this area is above \$150K. Do you agree? Briefly explain what the p-values in these cases mean? (1mark)

b) He also claims that the average living area is more than 1800 Sq. Ft. Do you agree with this? (Use a 5% significance level for both.). Briefly explain what the p-values in these cases mean? (1mark)
2. Are the home prices higher for houses with fireplaces as compared to those without?

a) Create side-by-side box plots of the house prices of the two groups and comment them. (2marks)

b) Formulate an appropriate hypothesis and test it in order to check the above claim. Assume that the population standard deviations of house prices in the two groups are equal. (1mark)
3. Any house aged more than 30 years is considered an "old" house. Your friend claims that old houses have larger lot sizes than new houses. Do you agree? Explain. Use a significance level of 5% for your test. Historical data suggests that old houses include some very large and some very small lot sizes but new houses are more homogeneous in their lot sizes. (2marks)
4. Based on the evidence available here, would you be willing to claim that fireplaces have become more fashionable? For simplicity, it is OK to compare only "new" houses and "old" houses. Use a significance level of 5% for your test. Use a significance level of 5% for your test. (1mark)
5. Suppose that houses with 1-2 bedrooms are considered to be "Small Houses", those with 3-4 are "Medium Houses" and 5-6 as "Big Houses". Can we conclude that the prices of Small, Medium and Big houses are not the same, at 1% level of significance? (2marks)

PART B

The data for this problem is available in Apple Advertising Data.xlsx, which provides Apple's revenues and advertising expenses.

1. Run a regression of revenues on advertising. Is advertising having a significant impact on revenues? Interpret the intercept and slope. (2 points)
2. Construct a residual plot. Do the residuals appear random? Do they satisfy the first three assumptions? (2 points)
3. Construct a Q-Q plot. Do the residuals appear to be normally distributed? (2 points)
4. If advertising expenses were to be 1500 in 2016, what would your prediction interval for revenues? (2 points)
5. Transform revenues and advertising into a log scale. Repeat the above steps 1-4. (5 points).
6. Would you recommend a linear model or log-log model? Please explain. (2 points)

Answers

PART A

Data Analysis

| | Price | Living Area | Bathrooms | Bedrooms | Lot Size | Age | Fireplace |
|-------|-----------|-------------|-----------|----------|----------|---------|-----------|
| count | 1047.00 | 1047.00 | 1047.00 | 1047.00 | 1047.00 | 1047.00 | 1047.00 |
| mean | 163862.13 | 1807.30 | 1.92 | 3.18 | 0.57 | 28.06 | 0.59 |
| std | 67651.56 | 641.46 | 0.64 | 0.75 | 0.78 | 34.90 | 0.49 |
| min | 16858.00 | 672.00 | 1.00 | 1.00 | 0.00 | 0.00 | 0.00 |
| 25% | 112014.00 | 1336.00 | 1.50 | 3.00 | 0.21 | 6.00 | 0.00 |
| 50% | 151917.00 | 1672.00 | 2.00 | 3.00 | 0.39 | 18.00 | 1.00 |
| 75% | 205235.00 | 2206.00 | 2.50 | 4.00 | 0.60 | 34.00 | 1.00 |
| max | 446436.00 | 4534.00 | 4.50 | 6.00 | 9.00 | 247.00 | 1.00 |

Table 1. Five-point summary of Dataset

Conclusion we draw from Five-point summary of each data point

- The data set contains 1047 records.
- None of records have null value for any data point.
- Average house price as per sample is ~\$164K
- Average Living area is 1807sq.ft in the sample
- All houses in sample have bathroom and bedroom, on an average there are roughly 2 bathrooms and 3 bedrooms
- Interesting point to note that sample standard deviation is more than average for lot size

| | Price | Living Area | Bathrooms | Bedrooms | Lot Size | Age | Fireplace |
|-------------|-------|-------------|-----------|----------|----------|-------|-----------|
| Price | 1.00 | 0.78 | 0.67 | 0.47 | 0.16 | -0.36 | 0.46 |
| Living Area | 0.78 | 1.00 | 0.72 | 0.66 | 0.20 | -0.26 | 0.48 |
| Bathrooms | 0.67 | 0.72 | 1.00 | 0.49 | 0.10 | -0.44 | 0.44 |
| Bedrooms | 0.47 | 0.66 | 0.49 | 1.00 | 0.14 | -0.06 | 0.30 |
| Lot Size | 0.16 | 0.20 | 0.10 | 0.14 | 1.00 | 0.02 | 0.05 |
| Age | -0.36 | -0.26 | -0.44 | -0.06 | 0.02 | 1.00 | -0.25 |
| Fireplace | 0.46 | 0.48 | 0.44 | 0.30 | 0.05 | -0.25 | 1.00 |

Table 2. Correlation matrix of Dataset

Correlation Analysis

As expected:

- Living area and price are strongly positively correlated followed by bathrooms, bedrooms and fireplace. Lot size has the weakest correlation with the price among all variables.
- Age has negative correlation. The prices decrease as the houses age more.
- Larger the living area, more the no. of bathrooms and bedrooms.

Counter Intuitive:

- Age has no relation with Lot size, no. of Bedrooms.
- Fireplace is negatively correlated with age. As age becomes more, lesser the houses with fireplace which could indicate that fireplace may be a fashion trend in newer houses. to understand this more, this data needs further analysis.

Solution to PART A

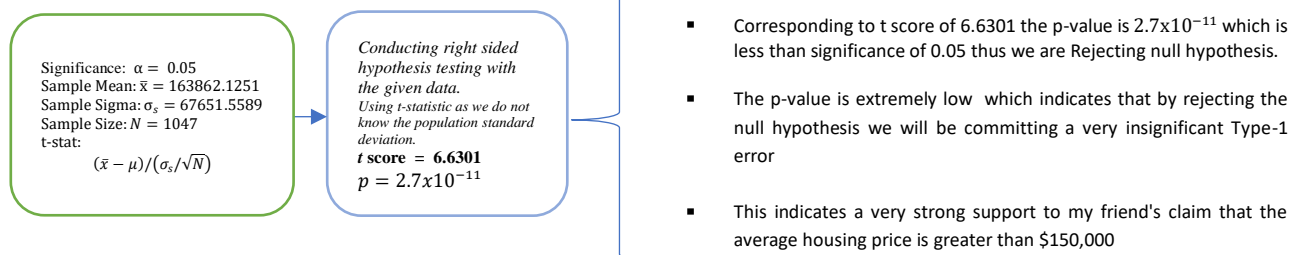
1.a

Based on "friend's claim" and observed sample, we build our hypothesis as:

Null Hypothesis: Average housing price is less than or equal to \$150K, and Alternate Hypothesis: Average housing price is more than \$150K

$$\therefore \begin{aligned} H_0 : \mu &\leq \$150,000 \\ H_1 : \mu &> \$150,000 \end{aligned}$$

We formulate:



1.b

Based on "friend's claim" and observed sample, we build our hypothesis as:

Null Hypothesis: Average living area is less than or equal to 1800sq.ft, and Alternate Hypothesis: Average living area is more than 1800sq.ft

$$\therefore \begin{aligned} H_0 : \mu &\leq 1800\text{sq.ft} \\ H_1 : \mu &> 1800\text{sq.ft} \end{aligned}$$

We formulate:

Significance: $\alpha = 0.05$
Sample Mean: $\bar{x} = 1807.30$
Sample Sigma: $\sigma_s = 641.4609$
Sample Size: $N = 1047$
t-stat:

$$(\bar{x} - \mu) / \sigma_s / \sqrt{N}$$

Conducting right sided hypothesis testing with the given data.
Using t-statistic as we do not know the population standard deviation.
t score = 0.3684
p = 0.3563

- Corresponding to t score of 0.3684 the p-value is 0.3563 which is more than significance of 0.05 thus we fail to reject the null hypothesis.
- The p-value that we received from the sample indicates that if we reject the null hypothesis the probability of committing a Type-I error will be 35.63% which is very significant and beyond accepted significance level of 5%
- This indicates that there is not enough evidence to the friend's claim that the average living area is greater than 1800sq.ft.

2.a

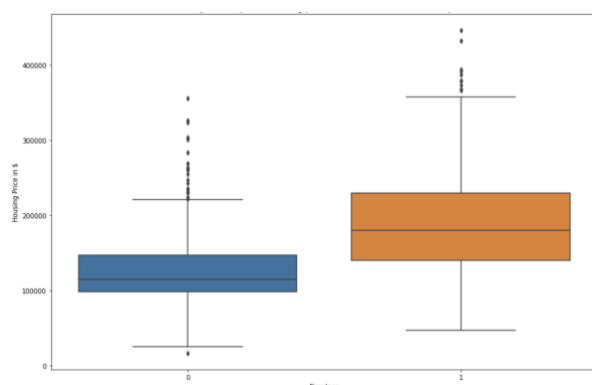


Figure 1. Side by Side boxplots of house prices for houses with and without Fireplaces

As per Figure 1, we conclude:

- From the boxplots, we can clearly observe that the data for both the cases is right skewed and there is presence of outliers in both cases
- Additionally, the median price value of the houses with fireplace is higher than that of houses without fireplace
- Almost 60-70 percentile of the price values for houses without fireplace fall within the 25th percentile of the values with fireplace

2.b

We build our hypothesis (Two sample independent test), It is stated to assume that population standard deviations of house prices in the two groups are equal.

Let:

- μ_1 represent the mean housing price of houses with fireplace
- μ_2 represent the mean housing price of houses without fireplace
- μ_{D0} represent the claimed mean housing price difference between houses with & without fireplace. This is 0 in this case.
- $\alpha = 0.05$ Assuming the significance level of 0.05

Hypothesis

$$\therefore \begin{aligned} H_0 : \mu_1 - \mu_2 &\leq 0 \\ H_1 : \mu_1 - \mu_2 &> 0 \end{aligned}$$

The test statistic for the paired-observation t test is

$$df = N_1 + N_2 - 2 = 1045$$

$$S_p^2 = \frac{(n_1 - 1)S_1^2 + (n_2 - 1)S_2^2}{n_1 + n_2 - 2} \quad t = \frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)_0}{\sqrt{S_p^2(1/n_1 + 1/n_2)}} \\ \underline{t = 16.7581}$$

$$p \text{ value of } t \text{ score} = \underline{0.00}$$

- Corresponding to t score of 16.7581 the p-value is 0.00 which is very less than the significance of 0.05 thus we are Rejecting null hypothesis. Claimed mean pricing difference is greater than zero.
- The p-value is so significantly low that it indicates by rejecting the null hypothesis, we will be committing a very insignificant Type-1 error

This indicates a very strong support to the claim that the home prices are higher for houses with fireplaces as compared to those without

3

We formulate our hypothesis for Two sample independent test with varied population standard deviations, It is stated that the lot sizes differ a lot in old houses and homogeneous in new houses.

This clearly indicates that the population standard deviations for lot size for the old & new houses are not same.

Let:

μ_{new} represent the mean lot size of new houses

μ_{old} represent the mean lot size of old houses

μ_{D0} represent the claimed mean lot size difference between old & new houses. This is 0 in this case.

$\alpha = 0.05$ Assuming the significance level of 0.05

Hypothesis

$$\therefore H_0: \mu_{\text{new}} - \mu_{\text{old}} \leq 0$$

$$H_1: \mu_{\text{new}} - \mu_{\text{old}} > 0$$

The test statistic for the paired-observation t test is given by

$$df = \left\lfloor \frac{(S_1^2/n_1 + S_2^2/n_2)^2}{(S_1^2/n_1)^2/(n_1 - 1) + (S_2^2/n_2)^2/(n_2 - 1)} \right\rfloor$$

$$t = \frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)_0}{\sqrt{S_1^2/n_1 + S_2^2/n_2}}$$

Substituting values we get:

$$t = 0.6080$$

$$p \text{ value for the } t \text{ score} = \mathbf{0.2717}$$

- Corresponding to t score of 0.6080 the p-value is 0.2717 which is considerably greater than the significance of 0.05, thus we Fail to reject null hypothesis. Claimed mean lot size difference may not be greater than zero.
- The p-value is so high which indicates that by rejecting the null hypothesis, we will be committing a very high Type-1 error

This indicates that the average lot size of old houses may not be larger than the new houses

4

We formulate our hypothesis for (Two sample independent test for testing difference between two population proportions): the test needs to be done to check if there are higher proportion of fireplaces in New houses than old houses.

That is difference of fireplace proportions of houses between Old & New > 0 or not.

Let:

p_{new} represent the sample proportion of fireplaces in new houses

p_{old} represent the sample proportion of fireplaces in old houses

p_{D0} represent the claimed mean lot size difference between old & new houses. This is 0 in this case.

$\alpha = 0.05$ Assuming the significance level of 0.05

Hypothesis

$$\therefore H_0: p_{\text{new}} - p_{\text{old}} \leq 0$$

$$H_1: p_{\text{new}} - p_{\text{old}} > 0$$

The test statistic for the difference between two population proportions where the null hypothesis difference is zero is:

$$z = \frac{\hat{p}_1 - \hat{p}_2 - 0}{\sqrt{\hat{p}(1 - \hat{p})(1/n_1 + 1/n_2)}}$$

$$\hat{p} = \frac{x_1 + x_2}{n_1 + n_2}$$

Substituting values we get:

$$z = 5.6317$$

$$p \text{ value of } z \text{ score} = \mathbf{8.922 \times 10^{-9}}$$

- Corresponding to t score of 5.6317 the p-value is 8.922×10^{-9} which is considerably lower than the significance of 0.05, thus Rejecting null hypothesis. Claimed mean lot size difference is greater than zero.
- The p-value is so significantly low which indicates that by rejecting the null hypothesis, we will be committing a very insignificant Type-1 error

This indicates a very strong support to the claim that the fireplaces have become more fashionable as the proportion of New houses with fireplaces are more than in Old houses.

5

For this analysis we set the hypothesis based on Analysis of variance test or ANOVA Test: We need to check whether

The average housing prices across Small, Medium and Big houses are same or not.

Let:

μ_{small} : represent the average housing price for Small houses.

μ_{medium} : represent the average housing price for Medium houses.

μ_{big} : represent the average housing price for Big houses.

$\alpha = 0.01$ Assuming the significance level of 0.01 (99%)

Hypothesis

$$\therefore H_0: \mu_{\text{small}} = \mu_{\text{medium}} = \mu_{\text{big}}$$

$$H_1: \text{Not all three } \mu_i \text{ are equal}$$

The test statistic for analysis of Variance is

$$F_{(r-1, n-r)} = \frac{MSTR}{MSE}, \quad MSE = \frac{SSE}{n-r}, \text{ and} \quad SST = SSTR + SSE \Rightarrow$$

$$MSTR = \frac{SSTR}{r-1} \quad \sum_{i=1}^r \sum_{j=1}^{n_i} (x_{ij} - \bar{x})^2 = \sum_{i=1}^r n_i (\bar{x}_i - \bar{x})^2 + \sum_{i=1}^r \sum_{j=1}^{n_i} (x_{ij} - \bar{x}_i)^2$$

Substituting values we get:

$$F = 58.7103$$

$$p \text{ value of } F \text{ score} = \mathbf{0.00}$$

- Corresponding to F score of 58.7103 the p-value is 0.00, thus Rejecting null hypothesis. Average housing prices across small, medium and big houses are not same.
- The p-value is so significantly low which indicates that by rejecting the null hypothesis, we will be committing a very insignificant Type-1 error

This indicates a very strong support that the average housing prices across small, medium and big houses are not same.

PART B

Data analysis

1. There are total 24 records – and 2 numerical data point viz. Revenue, and Adv. Exp
2. From 1992 to 2015 – we have total revenue vs advertising expense
3. We see the trend that as time progresses, advertising costs increase and same trend is followed by revenue.
4. Revenue and Ad expenses both indicate increase in respective values YoY

Table 4 on right suggests that there is strong positive relation between revenue and advertising expenses – as the revenue increases, Ad expenses also increase, this is discussed in more detail in answer to questions

Table 3. Five point summary of data points

Revenue - Total Advertising Expense

| | | |
|-------|-----------|---------|
| count | 24.00 | 24.00 |
| mean | 47829.80 | 470.39 |
| std | 68404.60 | 433.82 |
| min | 5363.00 | 134.13 |
| 25% | 7085.16 | 190.50 |
| 50% | 10447.50 | 271.00 |
| 75% | 48485.00 | 548.50 |
| max | 233715.00 | 1800.00 |

Table 4. Correlation matrix

Revenue - Total Advertising Expense

| | | |
|---------------------|------|------|
| Revenue - Total | 1.00 | 0.98 |
| Advertising Expense | 0.98 | 1.00 |

Solution to Part B

1

- On right we generated plot of regression of revenues on advertising.

Impact of Advertising on Revenues: Interpreting the intercept and slope:

- We observe a clear increasing trend from the graph. As advertising spend increases, revenues do too.
- Slope of the equation tells us that for each additional dollar spent on advertising fetches a revenue of \$154.39.
- The intercept is negative which mathematically means when advertising spend is 0, the revenue will be -24793.51. However data suggests that all revenues are positive and also practically revenues cannot be a function of advertising alone and fall negative in absence of advertising.
- Hence, practically negative intercept doesn't make sense so we choose to ignore this.

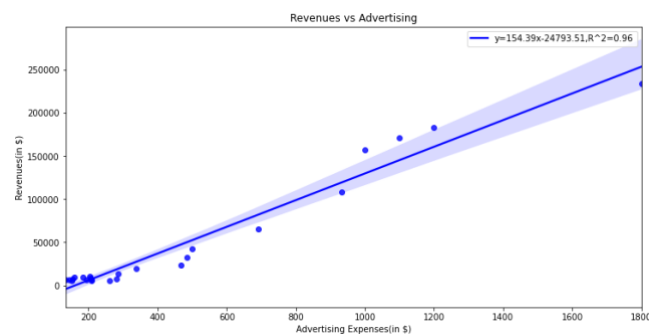


Figure 2. Regression plot - Advertising expense vs Revenue

- Slope Equation $\Rightarrow y = 154.39x - 24793.51$
- $R^2 = 0.96$

The Revenues vs Advertising graph indicates that the advertising have a significant impact on revenues.

2

Analysis of Residuals plot:

The residuals are not random and independent; they show curvature.

The situation can be corrected by adding the variable X2 to the model. This also entails the techniques of multiple regression analysis

Assumption 1: Linearity

Though $R^2 = 0.96$, which is very high, but from the above Revenues vs Advertising plot, it seems that the relationship of the independent variable with Revenues is NOT linear

Assumption 2: Homoscedasticity

Homoscedasticity means that the residuals have equal or almost equal variance across the regression line.

The scatter plot between residuals and ad expenses confirms heteroscedasticity is present. (ref Figure 3), The residuals may show a pattern as predictor variable x is advertising spend each year and hence on x-axis time is increasing. The errors may be correlated as this data is collected over time.

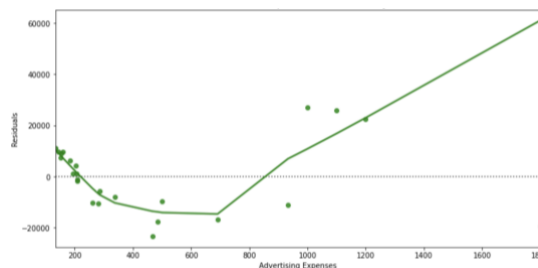
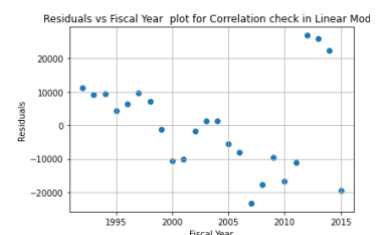


Figure 3. Advertising expense vs Residuals plot for Homoscedasticity check

Assumption 3: Correlation

$\text{Corr}[\epsilon_i, \epsilon_j] = 0$ for all $i \neq j$

Since the residuals show a trend w.r.t advertising expenses there could be a possibility that this is caused by time series data, hence we plot residuals vs fiscal year to confirm this possibility. As we observe in the graph on right, The d value from Durbin-Watson Test is **0.888** which is very less than $d_{\text{lower_critical}}$ of 1.257 hence we reject the null hypothesis. This means that There is correlation between subsequent errors.



3

When sample and theoretical quantiles of residuals are plotted against each other, the resulting plot is called Q-Q plot of residuals. This plot provides a summary of whether the distributions of two variables are similar or not with respect to the locations.

Analysis of Q-Q Plot:

- The theoretical and actual quantiles of residuals form the Q-Q plot
- In the Q-Q plot, we observe that the dots are found spiralling around the 45° line, and are not in parallel to it, thus we conclude:

The residuals distribution is NEARLY normal.

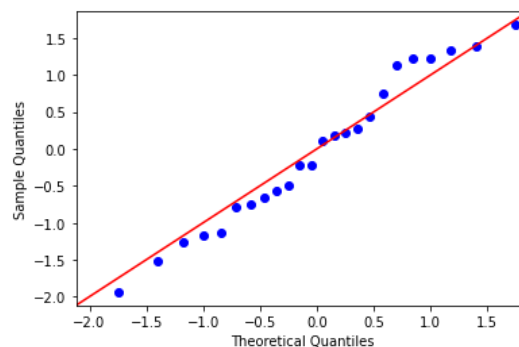


Figure 4. Q-Q Plot – Theoretical vs Sample quantities

4

\bar{x} : mean of AdvertisingExpense = 470.3910

x : data point for Advertising Expense

\bar{y} : mean of Revenue Total

y : data point for Revenue Total

n : Total records in sample = 24

As we know:

$$SSE = \sum (y - \bar{y})^2$$

$$MSE = \frac{SSE}{(n - 2)}$$

$$u_{\text{interval}} = \hat{y}_0 + t_{\frac{\alpha}{2}} \times s \times \sqrt{\left(1 + \frac{1}{n}\right) + \frac{(x_1 - \bar{x})^2}{SS_x}}$$

$$\Rightarrow u_{\text{interval}} = \$173355.8422$$

$$s = \sqrt{MSE} \Rightarrow s = 14212.4661$$

$$t_{\frac{\alpha}{2}} = 2.074$$

$$\text{slope} = 154.39$$

$$\text{intercept} = -24793.51$$

$$\hat{y} = \text{slope} \times x + \text{intercept} = 206790.34$$

$$SS_x = 4328635.2090$$

$$\alpha = 0.025$$

$$x_1 = 1500$$

$$\beta_0 = \text{intercept}, \quad \beta_1 = \text{slope}$$

$$\hat{y}_0 = \beta_0 + \beta_1 \times x_1 \Rightarrow 206790.34$$

$$i_{\text{interval}} = \hat{y}_0 - t_{\frac{\alpha}{2}} \times s \times \sqrt{\left(1 + \frac{1}{n}\right) + \frac{(x_1 - \bar{x})^2}{SS_x}}$$

$$\Rightarrow i_{\text{interval}} = \$240224.8378$$

For advertising expenses equal to 1500 in 2016, the prediction interval with 95% CI for revenues: (\$173355.84, \$240224.84)

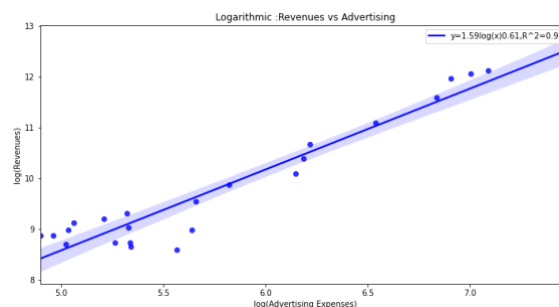
5

Part 1

After transformation to Log-Log scale, we obtain $R^2: 0.93$, Slope eqn: $\Rightarrow \log_e(y) = 1.59\log_e(x) + 0.61$

Further we observe and conclude that

- P value associated with intercept 0.61 is 0.28 which is higher than significance level of 0.05 – thus it is not Mathematically significant
- Elasticity Interpretation for slope: For 1% increase in advertising expense, revenue increase will be by 1.59%



5. Part 2

As per the plot on right, we find that the residuals are not random and independent, they show curvature.

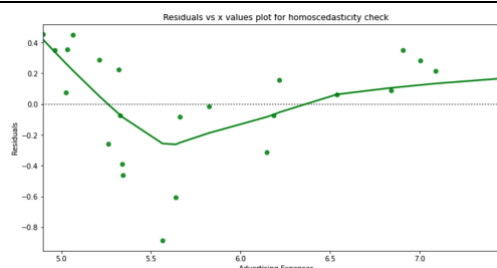
Assumption 1: Linearity

Although the $R^2 = 0.93$, which is very high, but from the above Revenues vs Advertising log-log plot, it seems that the relationship of the independent variable with Revenues is NOT linear.

Assumption 2: Homoscedasticity

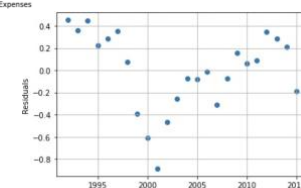
Check for Homoscedasticity. Homoscedasticity means that the residuals have equal or almost equal variance across the regression line.

This above quadratic shaped scatter plot obtained from the scatter plot confirms heteroscedasticity is present.



Assumption 3: Correlation

The d value from Durbin-Watson Test is 0.4243 which is very less than $d_{\text{lower_critical}}$ of 1.257 hence we reject the null hypothesis. This means that there is correlation between subsequent errors.



Residuals vs Fiscal yr scatter plot for correlation check in Log-Log model

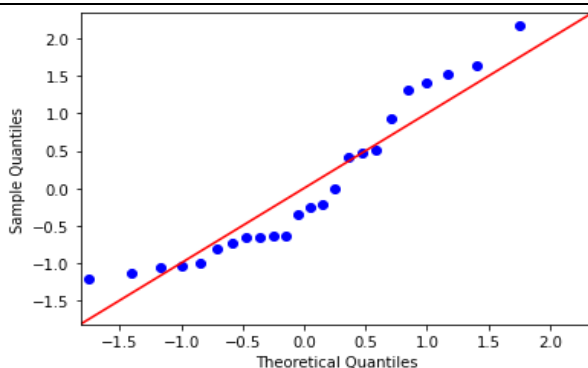
5. Part 3

When sample and theoretical quantiles of residuals are plotted against each other, the resulting plot is called Q-Q plot of residuals.

This plot provides a summary of whether the distributions of two variables are similar or not with respect to the locations.

Even with logarithmic transformation, we observe that the dots are found spiralling around the 45° line, therefore:

The residuals distribution is NEARLY normal



5. Part 4

x_{log} : Log of advertising expense data

\bar{x}_{log} : Mean of $x_{log} = 5.8288$

y_{log} : Log of Revenue Total data

\bar{y}_{log} : Mean of $y_{log} = 9.8940$

n : Total records in sample = 24

As we know:

$$SSE = \sum (y_{log} - \bar{y}_{log})^2$$

$$MSE = \frac{SSE}{(n-2)}$$

$$u_{interval} = \hat{y}_0 + t_{\frac{\alpha}{2}} \times s \times \sqrt{\left(1 + \frac{1}{n}\right) + \frac{(x_1 - \bar{x})^2}{SS_x}}$$

$$\Rightarrow \mathbf{11.4476}$$

$$\Rightarrow \exp(u_{interval}) = \$93676.25$$

$$s = \sqrt{MSE} \Rightarrow s = 0.3579209$$

$$t_{\frac{\alpha}{2}} = 2.074$$

$$\hat{y} = \text{slope} \times x_{log} + \text{intercept}$$

$$SS_x = 14.1198$$

$$\alpha = 0.025$$

$$x_1 = \log(1500)$$

$$\beta_0 = \text{intercept} = 0.61332576$$

$$\beta_1 = \text{slope} = 1.592219$$

$$\hat{y}_0 = \beta_0 + \beta_1 \times x_1 \Rightarrow 12.26$$

$$i_{interval} = \hat{y}_0 - t_{\frac{\alpha}{2}} \times s \times \sqrt{\left(1 + \frac{1}{n}\right) + \frac{(x_1 - \bar{x})^2}{SS_x}}$$

$$\Rightarrow \mathbf{13.0724}$$

$$\Rightarrow \exp(i_{interval}) = \$475632.13$$

For advertising expenses equal to 1500 in 2016, the prediction interval with 95% CI for revenues: (\$93676.25 , \$475632.13)

6

Compared to linear model (refer table) log-log model has

- Lower R^2 value
- Data points are more scattered around regression line
- The prediction interval is much wider
- However, we find slight improvement in randomization of residuals

Based upon above observations we conclude that linear model better explains the relationship of Apple financial year revenue with advertising expenses per year.

References

1. [Python Jupyter notebook](#) with derivations and calculations
2. Text Book : Complete Business Statistics, 7th edition (The McGraw-Hill Irwin Series)
3. <https://www.real-statistics.com/multiple-regression/autocorrelation/detecting-autocorrelation-graphically/>
4. <https://www.real-statistics.com/multiple-regression/autocorrelation/durbin-watson-test/>
5. <https://www.real-statistics.com/statistics-tables/durbin-watson-table/>
6. <https://online.stat.psu.edu/stat501/lesson/9/9.3>