Chapter 8

Tree Algorithms - Twig Query



Acknowledgements

- Nicolas Bruno, Nick Koudas, Divesh Srivastava. Holistic twig joins: optimal XML pattern matching. SIGMOD'02.
- Perter Buneman, Gao Cong, Wenfei Fan, Anastasios Kementsietsidis. Using Partial Evaluation in Distributed Query Evaluation. VLDB'06.
- Gao Cong, Wenfei Fan, Anastasios Kementsietsidis. Distributed Query Evaluation with Performance Guarantees. SIGMOD'07.
- Xin Bi, Guoren Wang, Xiangguo Zhao, Zhen Zhang, and Shuang Chen. Distributed XML Twig Query Processing Using MapReduce. APWeb'15.
- Xin Bi, Xiang-Guo Zhao, and Guo-Ren Wang. Efficient Processing of Distributed Twig Queries Based on Node Distribution. JCST'17.



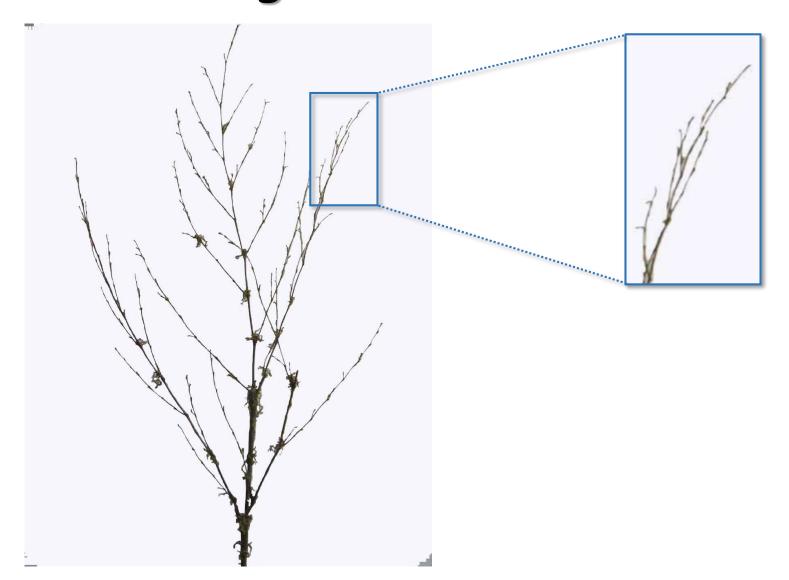
Chapter Outline

- Holistic twig query processing
- Distributed algorithms

Holistic Twig Pattern Matching



Tree & Twig





Twig Pattern Query

- Twig Pattern Query
 - Binary Structural Joins
 - The approach
 - Decompose the twig pattern into **binary** structural relationships
 - Use structural join algorithms to match the binary relationships against the XML database
 - Stitch together the basic matches
 - The problem
 - The intermediate result sizes can get large, even when the input and output sizes are more manageable

Binary Structural Join Example

XML document Query book (1, 1:150, 1)author title allauthors chapter year (1, 2:4, 2)(1, 5:60, 2)(1, 61:63, 2)(1,64:93,2)fn 1n section title XML author author author 2000 (1,6:20,3)(1,65:67,3)(1,68:78,3)(1, 3, 3)(1, 62, 3)jane doe XML. 1nhead 1n fn 1n fn fn (1, 66, 4)(1,69:71,4)(1, 7:9, 4)Origins 0 jane doe doe iane poe iohn (1, 70, 5)(1, 43, 5) (1, 46, 5)(1, 8, 5)(1, 11, 5)(1, 26, 5)**Decomposition** Number of Output Intermediate Results author – fn 1 3 author - In 3

2

2

fn – jane

In – doe



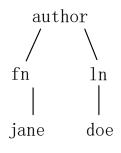
Holistic Structural Joins

- The approach
 - Uses linked stacks to compactly represent partial results to query paths
 - Merges results to query paths to obtain matches for the twig pattern
- The advantage
 - It ensures that no intermediate solutions is larger than the final answer to the query
- PathStack and TwigStack [N.Bruno, SIGMOD'02]

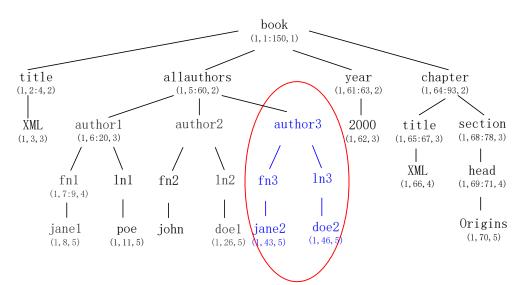


Holistic Structural Join Example

Query



XML document



Number of

1

1

Intermediate Results

Decomposition

Intermediate Results

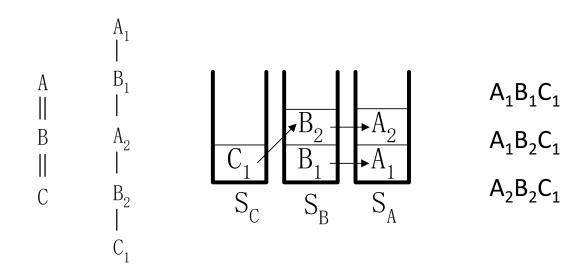
Output

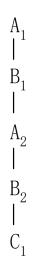
1

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PathStack

- Intuition
 - While the streams of the leaves are not empty (i.e. a solution could be found) do:
 - push the node with minimal LeftPos value into stack
 - if it is a leaf, print the solution
 - Example





 $T_A: A_1, A_2$ $T_B: B_1, B_2$

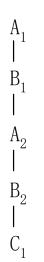
Stacks

 S_{C} S_{B} S_{A}

Comments

 $q_{min} = A$

06) moveStreamToStack(T_A, S_A, null)

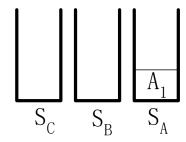


$$T_A: A_1, A_2$$

 $T_B: B_1, B_2$

 $T_C: C_1$

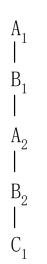
Stacks



Comments

$$q_{min} = B$$

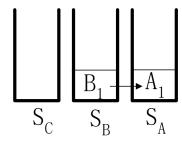
06) moveStreamToStack(T_B, S_B, A₁)



$$\begin{array}{c}
A_1 \\
B_1 \\
\underline{A_2} \\
\underline{B_2} \\
C_1
\end{array}$$

 $T_A: A_1, A_2$ $T_B: B_1, B_2$ $T_C: C_1$

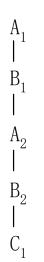
Stacks



Comments

$$q_{min} = A$$

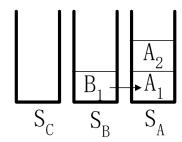
06) moveStreamToStack(T_A, S_A, null)



$$\begin{array}{c} \underline{A_1} \\ \underline{B_1} \\ \underline{A_2} \\ \underline{B_2} \\ \underline{C_1} \end{array}$$

 $T_A: A_1, A_2$ $T_B: B_1, B_2$ $T_C: C_1$

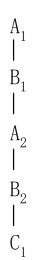
Stacks



Comments

$$q_{min} = B$$

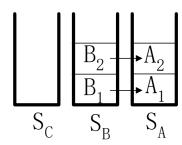
06) moveStreamToStack(T_B, S_B, A₂)



$$\begin{array}{c} \underline{A_1} \\ \underline{B_1} \\ \underline{A_2} \\ \underline{B_2} \\ \underline{C_1} \end{array}$$

 $T_A: A_1, A_2$ $T_B: B_1, B_2$ $T_C: C_1$

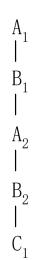
Stacks



Comments

$$q_{min} = C$$

06) moveStreamToStack(T_C , S_C , B_2)

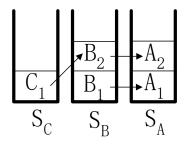


$$T_A: A_1, A_2$$

$$T_B: B_1, B_2$$

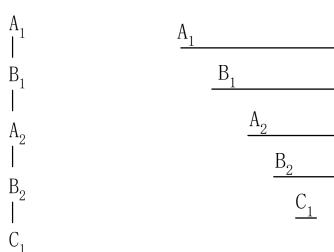
$$T_C: C_1$$

Stacks



Comments

- 07) isLeaf(C) = true
- 08) showSolutions(S_C , 1)
- 09) $pop(S_C)$



Stacks

Comments

$$T_A: A_1, A_2$$
 $T_B: B_1, B_2$
 $T_C: C_1$

$$\begin{array}{c|c} & B_2 & A_2 \\ \hline B_1 & A_1 \\ \hline S_C & S_B & S_A \end{array}$$

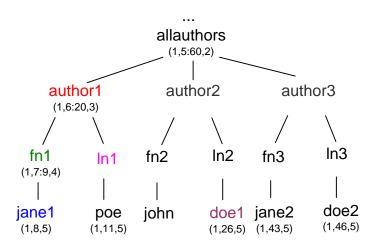
01) end(q) = true

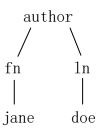
Algorithm ends.



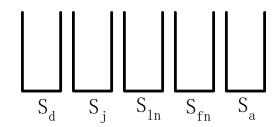
TwigStack

- Intuition
 - While the streams of the leaves are not empty (i.e. a solution could be found) do:
 - select a node that could be expanded to a solution
 - if it is a leaf, print the solution



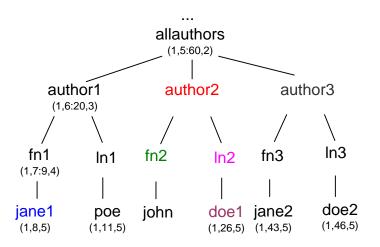


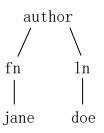
 T_a : 1, a2, a3 T_{fn} : fn1, fn2, fn3 T_{ln} : 1, ln2, ln3 T_j : 1, j2 T_d : 1, d2 **Stacks**



Comments: Phase1

01: while $(notEmpty(T_j) \mid | notEmpty(T_d))$ do:





T_a: a1, a2, a3

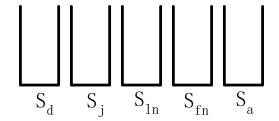
T_{fn}: fn1, fn2, fn3

T_{ln}: ln1, √n2, ln3

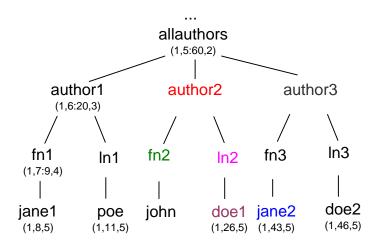
T_i: **1**, j2

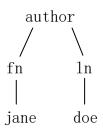
T_d: **d**1, d2

Stacks



Comments: iteration1 $q_{act} = getNext(a)$ ________fn getNext(fn) _______fn getNext(j) _______j $n_{min} = n_{max} = 8 \ (j1)$ getNext(ln) ________In getNext(d) ________d $n_{min} = n_{max} = 26 \ (d1)$ advance(ln) $n_{min} = 7(fn1)$ $n_{max} = ln2$ $advance(T_{fn})$





T_a: a1, a2, a3

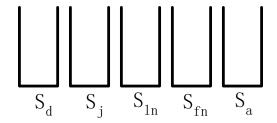
T_{fn}: fn1, fn2, fn3

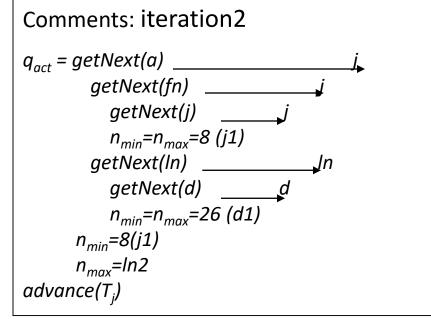
T_{In}: ln1, n2, ln3

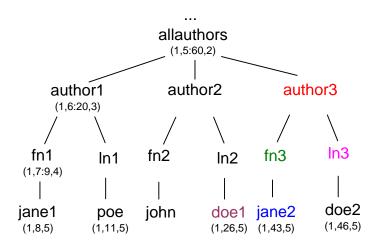
T_i: j1, 🔽

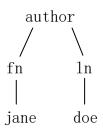
T_d: **₫1**, d2

Stacks









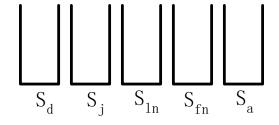
T_a: a1, a2, 3

 T_{fn} : fn1, fn2, fn3

T_j: j1, 🔽

T_d: **₫1**, d2

Stacks



```
q_{act} = getNext(a) _______fn

getNext(fn) _______fn

getNext(j) ______j

n_{min} = n_{max} = 43 \ (j2)

advance(fn)

getNext(ln) _______ln

getNext(d) _______d

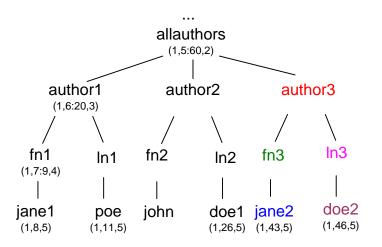
n_{min} = n_{max} = 26 \ (d1)

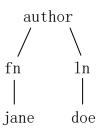
n_{min} = ln2

n_{max} = fn3

advance(T_a)
```

Comments: iteration3





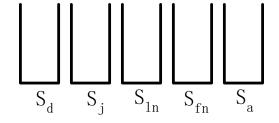
 T_a : a1, a2, $\frac{1}{8}$ 3

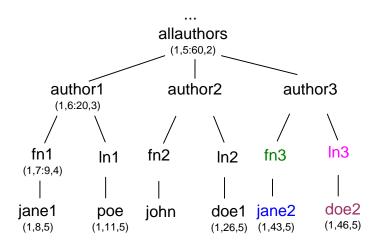
 T_{fn} : fn1, fn2, fn3

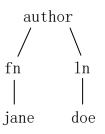
T_j: j1, 🔽

T_d: d1, d2

Stacks







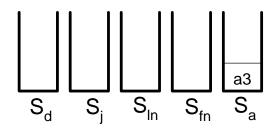
T_a: a1, a2, a3 ⋅

 T_{fn} : fn1, fn2, fn3

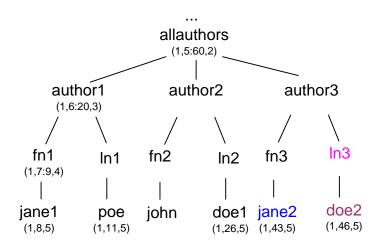
T_i: j1, 🔽

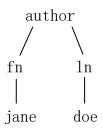
T_d: d1, d2

Stacks



Comments: iteration5 $q_{act} = getNext(a) \underline{\qquad \qquad } q$ $getNext(fn) \underline{\qquad \qquad } fn$ $getNext(j) \underline{\qquad \qquad } j$ $n_{min} = n_{max} = 43 \ (j2)$ $getNext(ln) \underline{\qquad \qquad } Jn$ $getNext(d) \underline{\qquad \qquad } d$ $n_{min} = n_{max} = 46 \ (d2)$ $n_{min} = fn3$ $n_{max} = ln3$ $moveStreamToStack(T_a)$ $advance(T_a)$





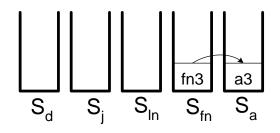
T_a: a1, a2, a3

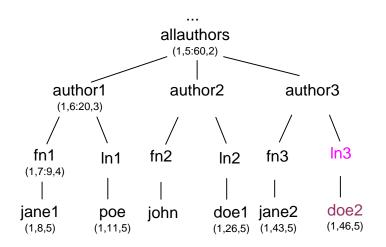
 T_{fn} : fn1, fn2, fn3

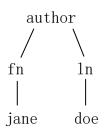
T_i: j1, 🛂

T_d: d1, d2

Stacks





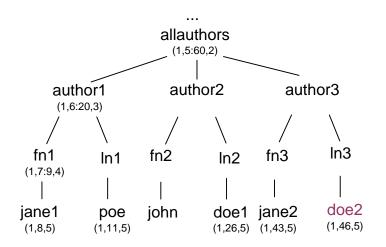


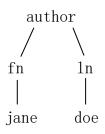
Streams T_a : a1, a2, a3 \downarrow T_{fn} : fn1, fn2, fn3 \downarrow T_{ln} : ln1, ln2, \downarrow n3 T_{j} : j1, j2 \downarrow S_d S_j S_{ln} S_{fn} S_a T_d : d1, \downarrow 2

path: (j2, fn3, a3)

"Merge-joinable" root-to-leaf

Comments: iteration7 $q_{act} = getNext(a)$ getNext(fn) getNext(j) $n_{min} = n_{max} = 43 (j2)$ getNext(In) getNext(d) $n_{min} = n_{max} = 46 (d2)$ n_{min} =43(j2) $n_{max}=In3$ moveStreamToStack(T;) $advance(T_i)$ $pop(S_i)$ showSolutionsWithBlocking(j)

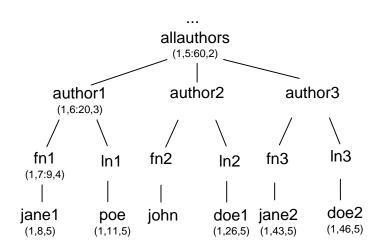


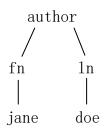


Streams Stacks T_a : a1, a2, a3 T_{fn} : fn1, fn2, fn3 T_{ln} : ln1, ln2, ln3 T_{j} : j1, j2 S_d S_j S_{ln} S_n S_a

 T_d : d1, d2

"Merge-joinable" root-to-leaf path: (j2, fn3, a3)





T_a: a1, a2, a3

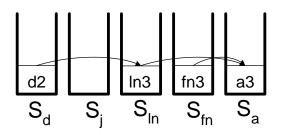
 $T_{\rm fn}$: fn1, fn2, fn3

T_{In}: ln1, ln2, ln3 ↓

T_j: j1, j2 ↓

 T_d : d1, d2

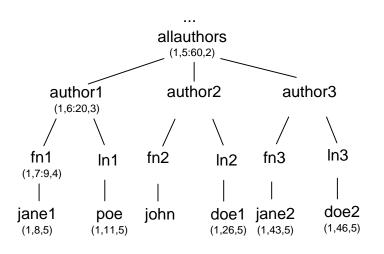
Stacks

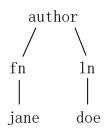


"Merge-joinable" root-to-leaf paths: (j2, fn3, a3)

(d2, ln3, a3)

Comments: iteration9





Stacks

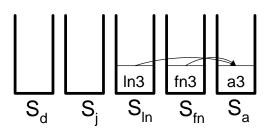
T_a: a1, a2, a3 ⋅

 T_{fn} : fn1, fn2, fn3

T_{In}: ln1, ln2, ln3 ↓

T_j: j1, j2 ↓

T_d: d1, d2



TwigStack solution:

(j2, fn3, d2, ln3, a3)

Comments: Phase2

12: MergeAllPathSolutions()

Distributed Twig Query Processing



Distributed Algorithms

- Distributed TwigStack
- DisT3/DisT2
- ParBoX
- PaX3/PaX2

Distributed TwigStack



Arbitrary XML partition

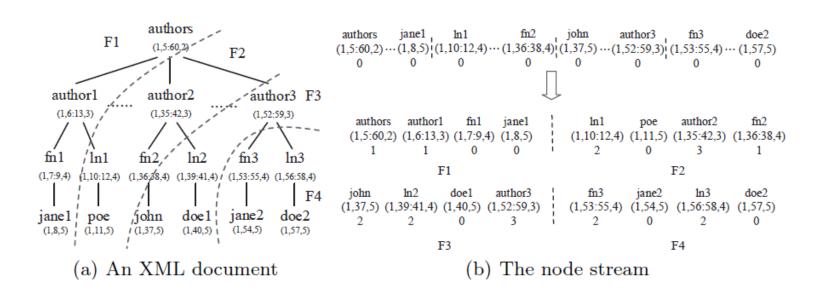
Arbitrariness

- Stored on distributed file system before query processing
- Impractical to repartition and restore according to each query
- <label,rcode,type> as an XML node
 - no-cut (type 0): neither the parent edge nor a child edge is cut;
 - child-edge-cut (type 1): at least a child edges is cut, but not the parent edge;
 - parent-edge-cut (type 2): the parent edge is cut, but not the child edges;
 - all-cut (type 3): both the parent edge and at least one child edge are cut.



Arbitrary XML partition

An example





Distributed query processing

- Naïve solution (2-round MapReduce)
 - Round 1
 - Map: find all the matches to the query nodes on the local machine, emit key-value pairs using the match node as value and its highest ancestor which is also a match of root of the query as key;
 - Reduce: collect the key-value pairs for the next round. Each final result can be derived from a sub-tree rooted by a key;
 - Round 2
 - Map: run a twig algorithm to generate final results;
 - Reduce: collect all the final results.
- Drawbacks
 - Unnecessary intermediate results in the first round
 - MapReduce job start-up is time-consuming



Distributed TwigStack

- Intuition
 - Relaxed matching rules to retain results across partitions
 - Coordinator to guarantee the distribution of intermediate results

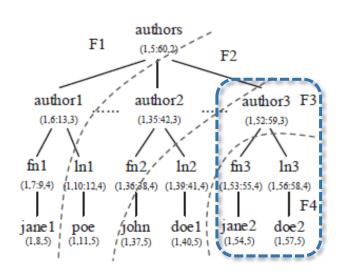
DTS

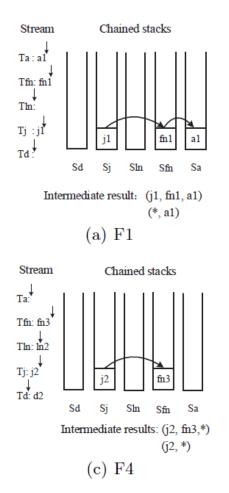
- Relaxed Local TwigStack (RL-TwigStack)
 - Relaxed Local GetNext (RL-GetNext)
 - Relaxed Local ShowSolutions (RL-ShowSolutions)
 - Emit <key, solution>
- Coordinator
 - Refined key-value pairs <refinedKey, solution>

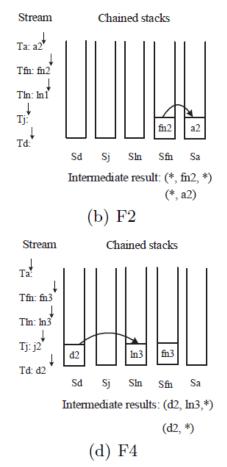


Distributed TwigStack

//author[fn/text()="jane"^ln/text()="doe"]







DisT3/DisT2



Motivation

- repartitioning and restoring large-scale XML data for different applications are impractical.
- 2. the intrusion into the existing distributed framework, such as Hadoop, should be minimized.
- 3. any partition strategy should be supported, including the default partition strategy of Hadoop.



Aim at processing large-scale tree data efficiently no matter how the data are partitioned and stored on the distributed file system



Major Concerns

- **Data Storage**. The algorithm should support arbitrary partitions without the prior knowledge of query patterns, especially in the cloud environment.
- Local Computation. The local computation should achieve high efficiency and pruning ability to reduce computation cost.
- **Network Traffic**. The parallelism should be improved so that the algorithm consumes minimal communication cost among machines in the cluster.



DisT3: Principles

- Since the region code can be used to determine the relationship between different nodes, we use it as the key for tuple identification.
- To be specific, we use rc of the match nodes of the root node in query Q as the key, so that all the match nodes of Q will have the same key value.
- All the keys from each partition have to be gathered by a coordinator, so that all the keys can be reset to their highest ancestors.



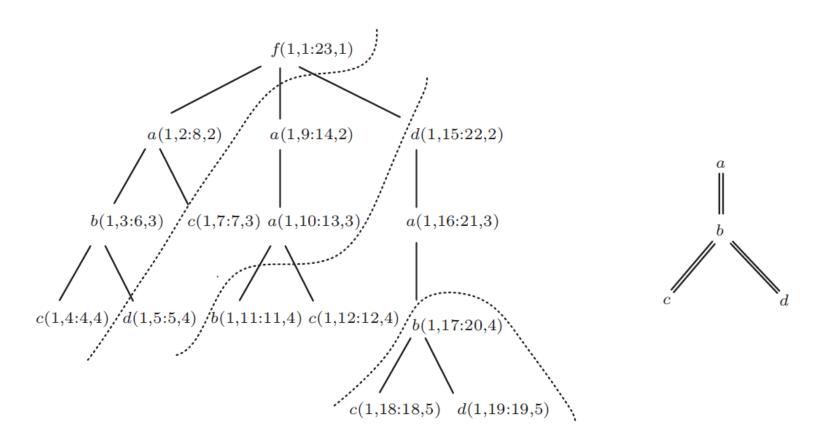
DisT3: Phases

- 1. Each machine scans each partition and sends *rc* of each match node to the coordinator.
- 2. The coordinator resets the key to the *rc* of its highest ancestors, and sends them back to all the partitions.
- 3. Each partition emits the nodes with their refined keys. All the nodes with the same keys are gathered in the same machines and processed by local twig join operations.



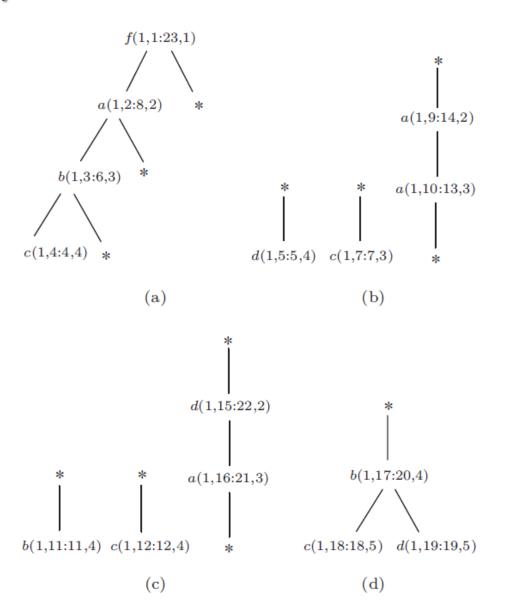
Example: Raw Data

• Each node is represented as a 2-tuple <1, rc>, where I is the label and rc is the region code



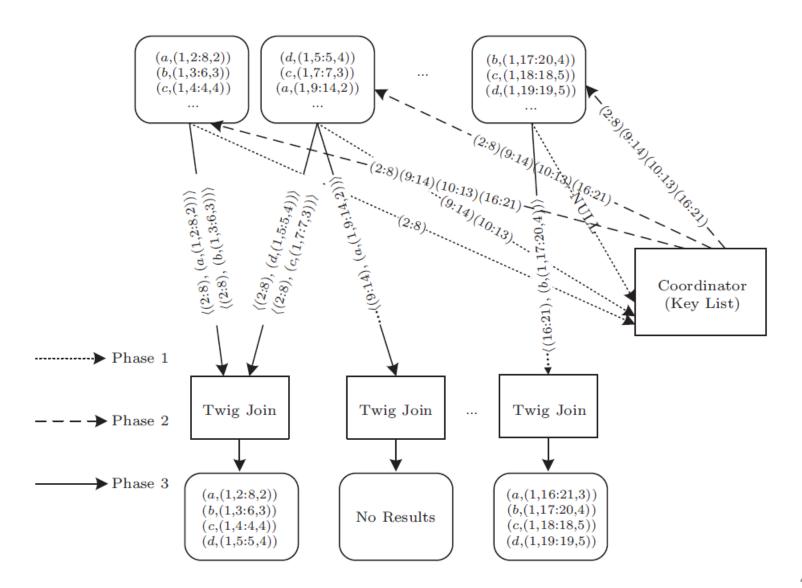


Example: Partitions





Example: Flowchart





DisT2ReP

Definitions

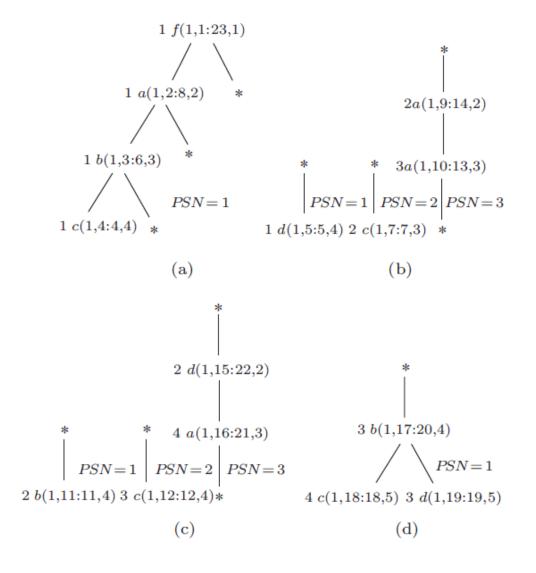
Definition 2 (Virtual Ancestor Label). Given an XML document D and its partitions (F1, F2, ..., Fn), for Fi, if a node v on the other partitions has descendent nodes in Fi, then v is a virtual ancestor of Fi, and the label of v is a virtual ancestor label, denoted as VAL.

Definition 4 (Partition Subtree Number). Given a partition Fi and all the subtrees $(t_1^i, t_2^i, ..., t_m^i)$ on Fi, all the nodes in each subtree t_j have the same partition subtree number j, denoted as PSN.

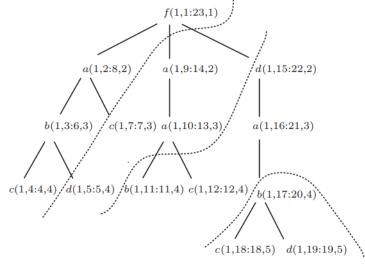
Definition 3 (Global Label Number). Given an XML document D and its streams S of each label, for a node v with label a and its label stream $S_a \in S$, the sequence number of node v in S_a is the global label number of v, denoted as GLN.

Definition 5 (Partition Subtree Region). Given a prtition Fi, all the subtrees $(t_1^i, t_2^i, ..., t_m^i)$ on Fi and a virtual ancestor u, if node u is an ancestor of subtrees $(t_j^i, ..., t_k^i)$, then the partition subtree region of node u is denoted as $PSR = (GLN_u, PSN_i^i:PSN_k^i)$, where GLN_u is the GLN of node u, and PSN_j^i and PSN_k^i are the PSN of subtrees t_j^i and t_k^i on partition Fi respectively.

DisT2ReP: PaSS and ReP Index



DisT2ReP



Partition

ReP Index

Partition

ReP Index

⟨label, regionCode, reCount, sid⟩ ⟨ancLabel, (reCount, sidRegion)⟩

f	(1,1:23,1)	1	1
\boldsymbol{a}	(1,2:8,2)	1	1
\boldsymbol{b}	(1,3:6,3)	1	1
c	(1,4:4,4)	1	1

Null Null

d	(1,5:5,4)	1	1
c	(1,7:7,3)	2	2
a	(1,9:14,2)	2	3
a	(1,10:13,3)	3	3

(1,1:3)(1,1:2)a(1,1:1)

(b)

(c)

Partition

ReP Index

Partition

ReP Index

 $\langle label, regionCode, reCount, sid \rangle$

 $\langle ancLabel, (reCount, sidRegion) \rangle$

 $\langle label, regionCode, reCount, sid \rangle$ $\langle ancLabel, (reCount, sidRegion) \rangle$

\boldsymbol{b}	(1,11:11,4)	2	1
c	(1,12:12,4)	3	2
d	(1,15:22,2)	2	3
\boldsymbol{a}	(1,16:21,3)	4	3

f	(1,1:3)
a	(2,1:2)(3,1:2)

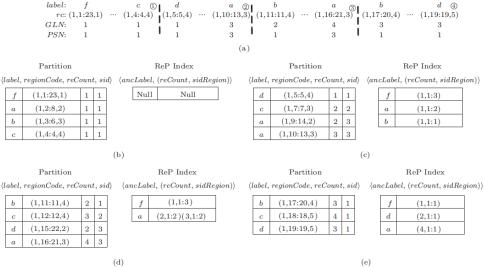
b	(1,17:20,4)	3	1
c	(1,18:18,5)	4	1
d	(1,19:19,5)	3	1

f	(1,1:1)
d	(2,1:1)
a	(4,1:1)

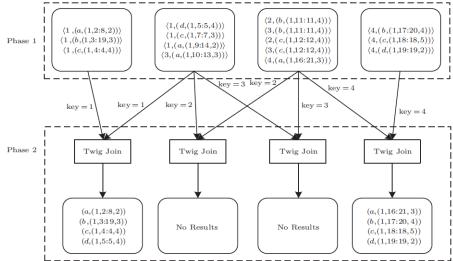
48

(label, regionCode, reCount, sid) (ancLabel, (reCount, sidRegion))

Example



Example 4 (Algorithm DisT2ReP). Based on the ReP index in example 3, as to partition F1, the first node (f, (1, 1:23, 1), 1, 1) is not a match node of query root node a, and the ancestor array is empty, thereby we do not set the emit key of the node f. The next node (a, (1, 2:8, 2), 1, 1) is a match of query root node, thus we directly set its key, generate $\langle 1, (a, (1, 2:8, 2)) \rangle$, and save the 2-tuple of its region code and GLN (2:8, 1) into the ancestor array. The next node (b, (1, 3:6, 3), 1, 1) is not a match of query root node a, and we



check the ancestor array and find its descendant (2:8, 1), thus we set its GLN as the key of this node b and (b, (1, 3:6, 3)) as its value to form (1, (b, (1, 3:6, 3))). Then we check the ReP index on F1, which is empty, thus we do nothing. Similarly, node (c, (1, 4:4, 4), 1,1) generates tuple $\langle 1, (c, (1, 4:4, 4)) \rangle$. In the same way, on partition F_{2} , each of nodes (d, (1, 5:5, 4), 1, 1), (c, 4)(1, 7:7, 3), (2, 2), (a, (1, 9:14, 2), 2, 3) and (a, (1, 10:13, 4))3), 3, 3) generates a tuple separately. On partition F3, each of nodes (b, (1, 11:11, 4), 2, 1) and (c, (1, 12:12, 4), 4)4), 3, 2) generates two tuples separately, and node (a, (1, 16:21, 3), 4, 3) generates a tuple. On partition F4, each of all the nodes generates a tuple. With the tuples generated in phase 1, the tuples with the same keys are distributed to the same node, where holistic twig algorithm is executed to generate final results



Performance Guarantees

- *Visit Times*. Each machine traverses its own partitions only once.
- *Parallelism*. All the local computations are executed in parallel on the machines with corresponding partitions.
- Computation Cost. The local computation cost on each partition F_i is $O(|S^i_Q||ReP_i|)$, where $|S^i_Q|$ is the number of match nodes on F_i and $|ReP_i|$ is the size of ReP index on F_i .
- **Communication Cost**. The total communication cost is the size of match nodes having contributions to the final results, which is O(|results|) in the best case, and $O(|S_Q|)$ in the worst case. |results| is the size of final results and $|S_Q|$ is the size of streams with labels in the query pattern, i.e., the number of match nodes.



Implementation

- DisT2ReP can be implemented in any distributed computing framework, including MapReduce of Hadoop, due to the following advantages:
 - 1. Supporting any distributed storage mechanism, regardless of how the XML data are partitioned;
 - 2. Enabling to process twig queries without priori knowledge of the query patterns, so that it does not need to repartition and restore the large-scale data each time when a new query comes;
 - 3. Requiring no communication among computing nodes in each of the two phases.

Using Partial Evaluation in Distributed Query Evaluation

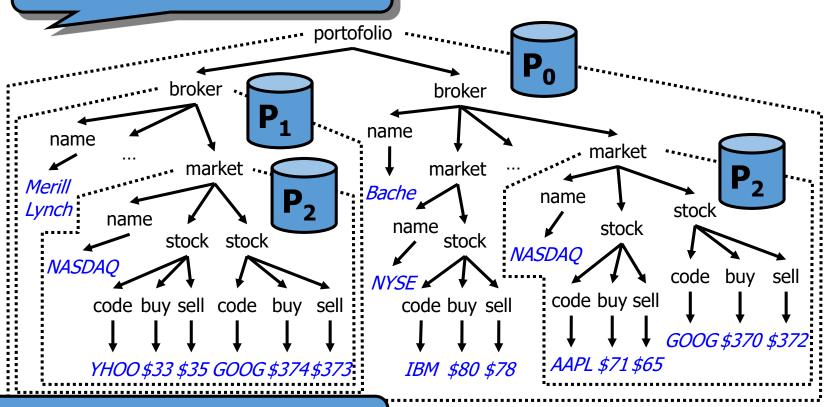
Peter Buneman, Gao Cong, Wenfei Fan, Anastasios (Tasos) Kementsietsidis

VLDB'06



Cutting Down Trees...

Tell me when GOOG stock sells for 376: [//stock[code = "GOOG" ∧ sell = 376]



Let's do a Depth-first traversal. We visit:

$$P_0 \rightarrow P_1 \rightarrow P_2 \rightarrow P_1 \rightarrow P_0 \rightarrow P_2 \rightarrow P_0$$



Status report...

- We have XML Trees arbitrarily fragmented and distributed
- We want to execute **Boolean Xpath** queries Q = [q] over the fragmented trees.

q := p | p/text()=str | label() = A |
$$\neg$$
q | q \wedge q | q \vee q p := ε | A | * | p//p | p/p | p[q]

Lessons learned:

- We want to visit each peer only **once**, irrespectively of the number of (tree) fragments it stores.
- We want to minimize communication costs. Ideally, no fragment data should be send while evaluating a query.
 Our motto: Send processing to data NOT data to processing



Partial Evaluation

Consider a function f(s, d) and part of its input, say s.

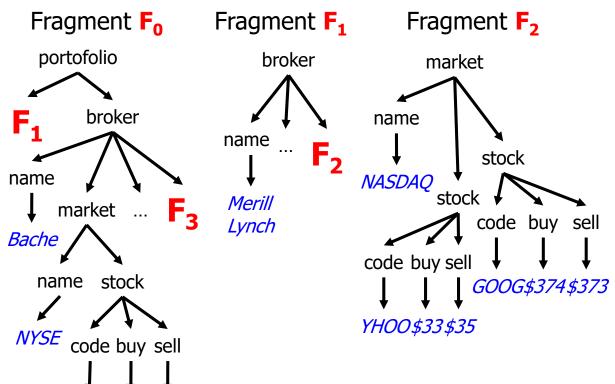
Then, **partial evaluation** is to specialize f(s, d), i.e., to perform the part of f's computation that depends only on s.

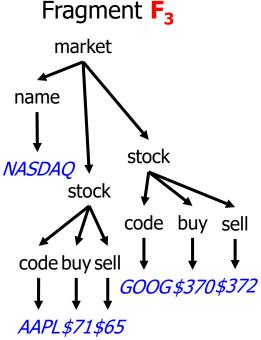
This generates a **residual** function g(d) that depends only on d.

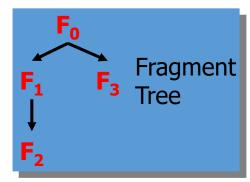


Tree Fragments

IBM \$80 \$78









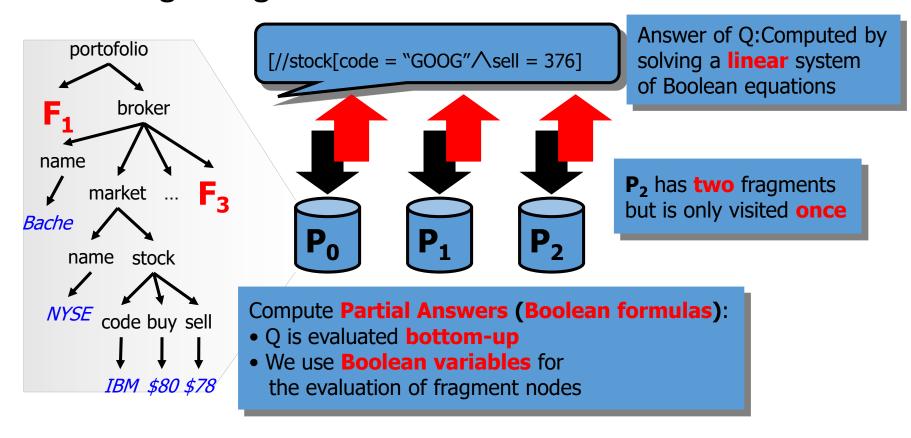
Tree Fragments

- Fragmentation
 - No constraints on the fragmentation
 - No constraints on how the fragmentation are distributed
- Storage
 - Root fragment and sub-fragment
 - Virtual node
 - Source tree



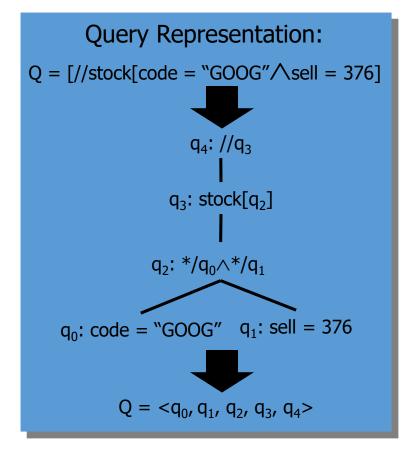
Distributed Partial Evaluation

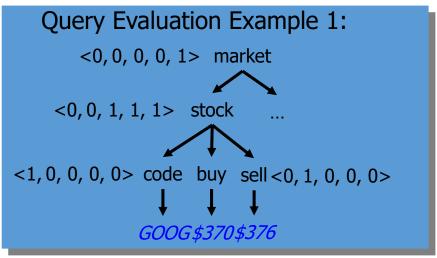
 Main idea: Given a query Q, send Q to every peer holding a fragment

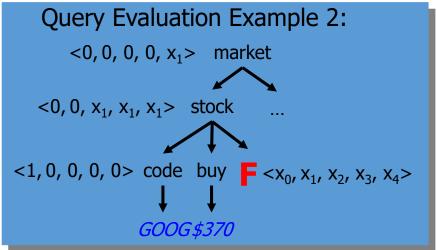




Query Evaluation





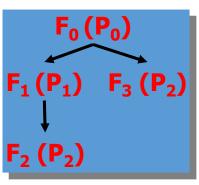




The ParBoX Algorithm

Three stages

- Stage 1: Querying peer P_Q sends query Q to all peers having a fragment (use the fragment tree to identify all such peers)
- Stage 2: Evaluate Q, in parallel, over each fragment
 F_i in peer P_i
- Stage 3: Collect partial answers in P_Q and compute the answer to Q.



Key considerations/concerns:

- (Total/Parallel) Computation costs.
- Communication costs.
- Level of fragmentation.

ParBoX comes in flavors:

- HybridParBoX
- FullDistParBoX
- LazyParBoX



Analysis of Algorithms

Communication costs are **LOW** and independent of T (the data)

Algorithm	Visits/Peer		Computation	Communication
NaiveCentralized	1		O(Q T)	O(T)
NaiveDistributed	card(S _i)	O(Q T)		O(Q card(T))
DarPoV	1	Tot	O(Q (T + card(T)))	$O(O \operatorname{card}(T))$
ParBoX	1	Par	$O(Q (\max_{P_j} F_{P_j} + card(T)))$	O(Q card(T))
Hybrid Dar BoV	1	Tot	O(Q T)	O(ITI)
HybridParBoX	1	Par	$O(Q (\max_{P_j} F_{P_j} + card(T)))$	O(T)
FullDistParBoX	cond(C)	Tot	O(Q (T + card(T)))	0(Q <i>card(T)</i>)
FUIIDISTRATION	card(S _i)	Par	$O(Q (\max_{P_j} F_{P_j} + card(T)))$	O(Q Caru(1))
LazyDarPoV	DawDaV and(C)	Tot	O(Q (T + card(T)))	$O(O \operatorname{card}(T))$
LazyParBoX	card(S _i)	Par	$O(Q card(T) max_T F_i)$	O(Q card(T))

 $card(S_i) = \#$ of fragments in peer P_i card(T) = # of fragments of tree T. Note that $card(T) \le |T|$ $|F_{Sj}| = \text{sum of fragments (sizes) in peer } P_j$

Distributed Query Evaluation with Performance Guarantees

Gao Cong, Wenfei Fan, Anastasios Kementsietsidis

SIGMOD'07



ParBoX

- Algorithm based on partial evaluation, which evaluates
 Boolean xml queries over a fragmented tree that is distributed over a number of different sites
- Partially evaluates the whole query Q, in parallel, over each fragment of the tree.
- Partial answers are all collected to a single coordinator site and are composed resulting in the final answer to Q.





Parallel XPath (PaX3)

- Evaluation algorithm, based on partial evaluation for generic dataselecting XPath queries. Guarantees:
- 1. Max 3 visits per site
- 2. Parallel query processing
- 3. Total computation comparable to the best-known centralized algorithm
- 4. Total network traffic determined by the size of:
 - the query
 - query answer
 - not the xml tree





Example

- Q = client [country/text() = "us"] /broker [market/name/text() = "nasdaq"]/name
- normalize(Q) = client/ ε [country/ ε [text()="us"]] /broker/ ε[market/name/ ε [text() = "nasdag"]]/name
- SVect(Q) = [q1, q2, q3] where
 - q1 = client, q2 = q1/broker, q3 = q2/name
- QVect(Q) = [q1, q2, q3, q4, q5, q6, q7, q8, q9], where
 - q1 = country, q2 = [text()="us"], $q3 = q1/\epsilon [q2]$, $q4 = * / \epsilon [q3], q5 = name, q6 = [text()="nasdaq"],$ $q7 = q5/\epsilon [q6], q8 = market/q7, q9 = * / \epsilon [q8]$



Three stages of PaX3

- Each stage → single visit of a site holding tree fragments
- Partially evaluate the qualifiers of query Q.

At the end for each node we know:

- the actual value of each qualifier or
- a Boolean formula whose value is yet to be determined
- 2. Partially **evaluate the selection part** of query Q.

At the end for each node we know:

- whether or not the node is part of the answer of query Q
- that the node is a candidate to be part of the answer
- 3. Determine which candidate answer nodes are true answer nodes → all nodes belonging to the answer of Q are transmitted to site S



Analysis

- Communication cost : O((|Q| |F_T|) + |ans|) (optimal)
 - cost of transmitting our query over the various sites +
 - cost of retrieving the actual answers to our query
- Total computation cost : O(|Q| |T|)
 - at each node v of F_i at most O(|Q|) operations are performed
 - total computation for each fragment is O(|Q| |F_i |)
- Parallel computation cost: O(|Q| max_{si} |F_{si} |)
 - |F_{Si}|: total size of the fragments in site Si
- Correctness: correct answer Q(T) on any xml tree T no matter how T is fragmented and distributed



PaX2

- Two stages and max two visits of each site
- Combine the first two stages of PaX3 into a single stage
 - evaluation of qualifiers + evaluation of selection paths

- 1. Querying site S_Q makes a remote procedure call to all the sites holding fragments
- 2. At each such site, combines the partial evaluation of selection paths with that of qualifiers, over a fragment Fj.
- 3. The procedure performs a top-down traversal of fragment Fj.
- 4. At each node v of Fj, two types of computation are performed: a preorder computation and a post-order computation.

End of Chapter 9