

Q1A)

given data $x = [3, 4]$ and $y = 2.45$
and $w = 0.5$ we have our goal to
minimize the MSE (Loss function)

$$L = \frac{1}{n} (y_{\text{pred}} - y)^2$$

$$y_{\text{pred}} = 0.5 \times 3 = 1.5$$

$$gt = dL/dw = \frac{2}{1} * (y_{\text{pred}} - y) * x = -15$$

$$gt^2 = (-15)^2 = 225$$

$$m_t = 0.9 * 0 + (1 - 0.9) * -15 = -15$$

$$v_t = 0.999 * 0 + (1 - 0.999) * 225 = 0.225$$

$$\hat{m}_t = \frac{-15}{1 - 0.9} = -15$$

$$\hat{v}_t = \frac{0.225}{1 - 0.999} = 225$$

$$\hat{m} = -15$$

$$w_{t+1} = w_t - \left[\frac{\alpha}{\sqrt{\hat{v}_t} + \epsilon} \right] * \hat{m}_t$$

$$0.5 - 0.1 \left[\frac{-15}{\sqrt{225} + 10^{-8}} \right] = 0.6$$

$$0.5 - \left[\frac{0.1}{\sqrt{225} + 10^{-8}} \right] * 15$$

$$0.5 - (-0.1) = 0.5 + 0.1 = 0.6$$

$$w_{t+1} = 0.6$$

$$y_{\text{pred}} = 0.5 \times 4 = 2 \quad y_{\text{pred}} = 0.5 \times 4 = 2.4$$

$$gt = d_1 - d_0 = \frac{2}{4} \times (2.4 - 5) \times 4 = -20.8$$

$$gt^2 = (-20.8)^2 = 432.64$$

$$m_2 = 0.9 \times -15 + (1 - 0.9) \times (-20.8) = -11.42$$

$$\begin{aligned} V_2 &= 0.999 \times 225 + (1 - 0.999) \times (432.64) \\ &= 224.775 + (0.001 \times 432.64) \\ &= 225.20 \end{aligned}$$

$$\hat{m}_2 = \frac{11.42}{1 - 0.9} = 114.2$$

$$\hat{V}_2 = \frac{225.20}{1 - 0.999} = 225200$$

$$0.6 = \left[\frac{0.1}{\sqrt{225200} + 10^8} \right] \times 114.2$$

$$0.6 = 0.02$$

$$= 0.58$$

Q1B

(28)

$$\Delta J(w) = \frac{1}{3} [2 \times (0.5 \times [1-2]) \times 1 + 2(0.5(2-4)) \times 2 + 2(0.5(3-6)) \times 3]$$

$$= \frac{1}{3} [2 \times (-1.5) \times 1 + 2 \times (-3) \times 2 + 2 \times (-5.5) \times 3]$$

$$= \frac{1}{3} [-3 + (-12) + (-33)]$$

$$= \frac{1}{3} \times (-48) = -16$$

Initially

$G=0$ we have $G = 0 + (-16)^2 = 256$

update the w using Adagrad update rule

$$w = w - \frac{\alpha}{\sqrt{G+1}} \times \nabla J(w)$$

$$0.5 - \frac{0.1}{\sqrt{256+1}} \times (-16)$$

$$= 0.5 + 0.1 = 0.6$$

After one iteration using the Adagrad the update weight $w = 0.6$.

~~Q1~~ Q2 A Le Net Architecture

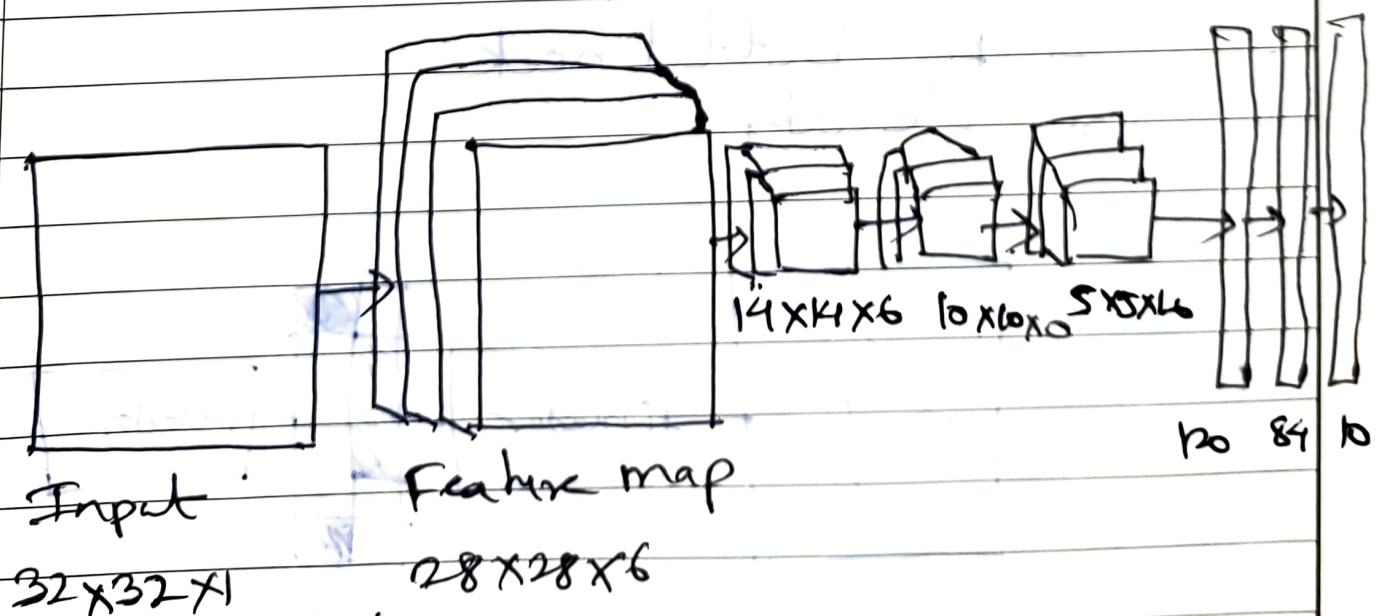
LeNet is the first CNN architecture. It was developed in 1998 by Yann Lecun, Corinna Cortes for handwritten digit recognition problem. LeNet was one of the first successful CNN's. It is one of the earliest and most widely-used CNN architecture and has been successfully applied to tasks as such as handwritten digit recognition. At high level, LeNet consists of two parts:

- (i) a convolutional encoder consisting of two convolutional layers and
- (ii) a dense block consisting of three fully connected layers. The architecture is summarized in Fig.

The basic units in each convolutional block are a convolutional layer, a sigmoid activation function and a subsequent average pooling operation. Each convolutional layer uses a 5×5 kernel and a sigmoid activation function.

These layers map spatially arranged inputs to a number of two-dimensional feature maps. typically increasing the number of channels. The first convolutional layer has 6 output channels while the second has 16. Each 2×2 pooling operation (stride 2) reduces dimensionality by a factor of 4 via spatial down sampling.

Finally, we flatten the output of second convolution layer to 120 features of size 1×1 followed by fully connected layer of 84 units and last layers uses softmax to produce 10 outputs corresponding to 10 digits. (0-9)



Q2

Q2 L

Q2(B)

1 2 3 4 5

6 7 8 9 10

11 12 13 14 15

16 17 18 19 20

21 22 23 24 25

Input

Kernel

0.2	0.2	0.2
0.2	0.2	0.2
0.2	0.2	0.2

After performing conv operation
the final o/p is

14.4	16.5	18.6
24.9	27.0	29.1
35.4	37.5	39.6

~~Q2(b)~~ Autoencoder are map high dimensional data to lower dimensional data to compress data or image.

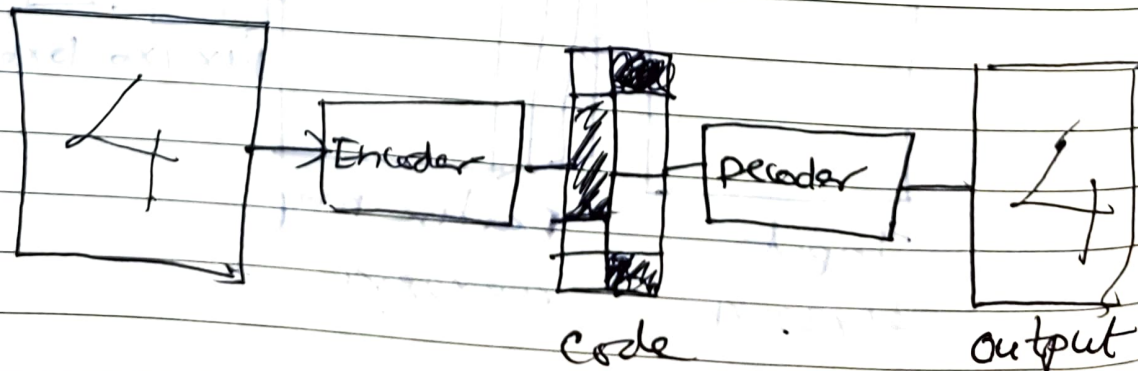
Application of Autoencoder are

- (1) Image Compression
- (2) Image Denoising
- (3) Dimensionality reduction
- (4) Recommendation System
- (5) Anomaly detection
- (6) Image Production
- (7) Image Colorization

Architecture of Autoencoder

An autoencoder consists of three parts

- (1) An encoder
- (2) A bottleneck
- (3) decoder



Encoder:- A module that compresses the input data into an encoded representation that is typically several orders of magnitude smaller than the input data.

(2) Bottleneck:- A module that contains the compressed knowledge representation and is therefore the most important part of the network.

(3) Decoder:- A module that helps the network decompress the knowledge representations and reconstructs the data back from its encoded form. The output is then compared with ground truth.

The encoder compresses the input and the decoder attempts to recreate the input from the compressed version, provided by the encoder.

Auto encoder ~~compresses~~ compresses the input into a lower-dimensional code and then reconstructs the output from this representation. The ~~code~~ code is a compact "Summary" or "Compression" of the input also called the latent space representation.

Q2

Q1 L

Q2(B)

1 2 3 4 5

6 7 8 9 10

11 12 13 14 15

16 17 18 19 20

21 22 23 24 25

Input

Kernel

0.2	0.2	0.2
0.2	0.2	0.2
0.2	0.2	0.2

After performing CNN operation
the final o/p is

14.4	16.5	18.6
24.9	27.0	29.1
35.4	37.5	39.6

Q3A1

$$x = 1$$

$$w_1 = 0.5 \quad w_2 = 0.8$$

$$b_1 = 0 \quad b_2 = 0$$

$$n = 0.1$$

AF = Sigmoid

$$y = 1$$

$$z = 0.5 \times 1 + 0 = 0.5$$

$$AF = a_1 = \sigma(0.5) = \frac{1}{1 + e^{-0.5}}$$

$$a_1 = 0.6225$$

$$y_{pred} = 0.622$$

$$\begin{aligned} \text{Loss} &= \frac{1}{2m} (y - \hat{y})^2 \\ &= \frac{1}{2 \times 1} (1 - 0.622)^2 \\ &= \frac{(1 - 0.622)^2}{2} \\ &= \frac{0.14576}{2} \\ &= 0.0718 \end{aligned}$$

Back propagation

$$-(1 - 0.622) = -0.378$$

$$\begin{aligned} z_2 &= -(0.378) \times 0.235 \\ &= -0.089 \end{aligned}$$

$$\begin{aligned} w_2 &= (-0.089) \times 0.622 \\ &= -0.055 \end{aligned}$$

updated weight $w_1 = 0.501$
 $w_2 = 0.8055$