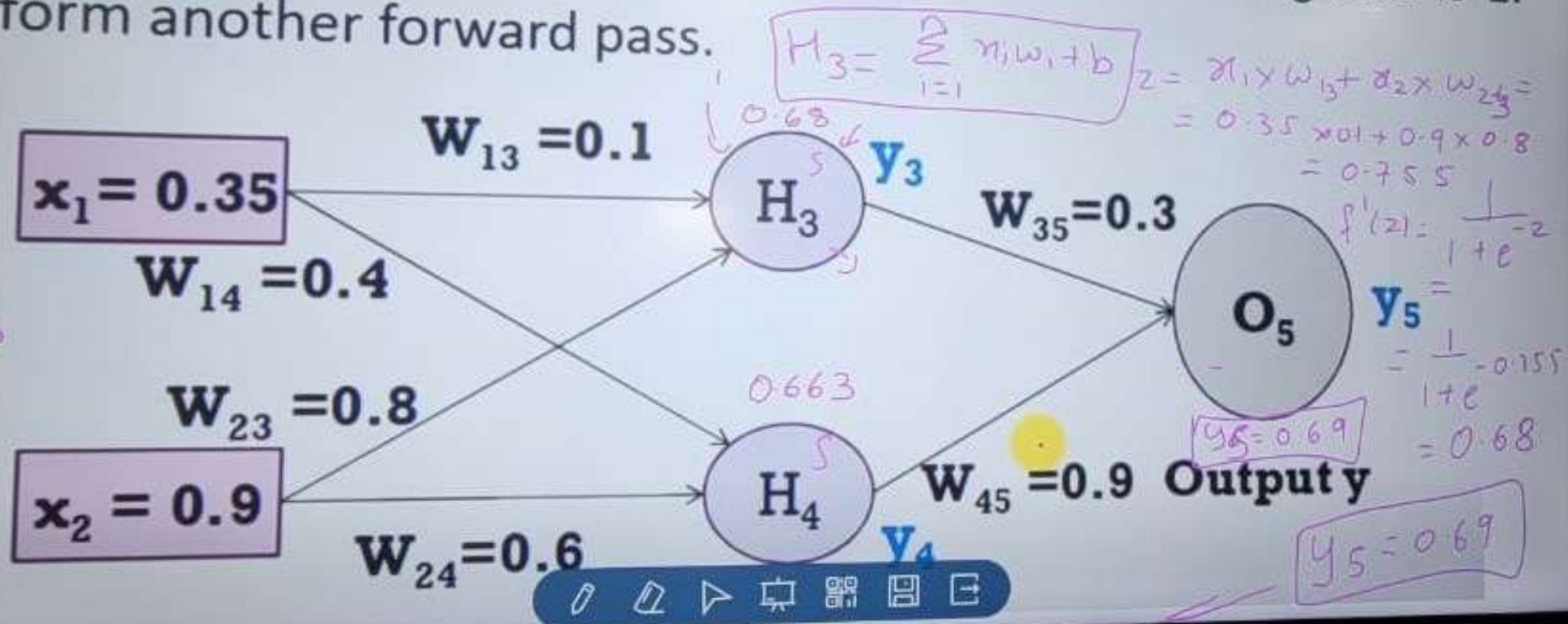
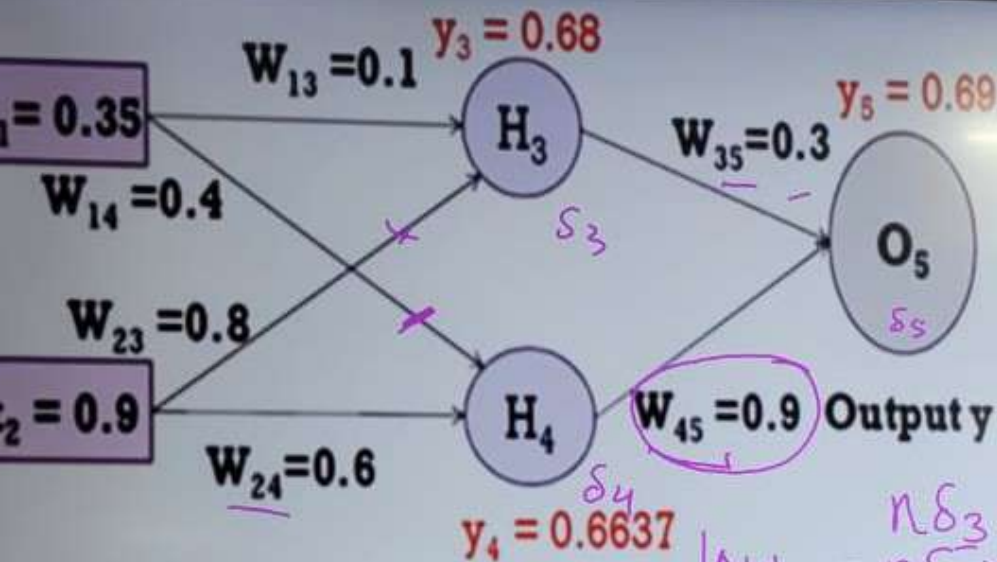


Backpropagation

Assume that the neurons have a sigmoid activation function. Perform a forward pass and a backward pass on the network. Assume that the actual output of y is 0.5 and learning rate is 1. Perform another forward pass.

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Backward Pass: Compute δ_3 , δ_4 and δ_5 .

For output unit:

$$\delta_5 = y(1-y)(y_{\text{target}} - y) = 0.69 * (1 - 0.69) * (0.5 - 0.69) = -0.0406$$

For hidden unit:

$$\delta_3 = y_3(1-y_3)w_{35} * \delta_5 = 0.68 * (1 - 0.68) * (0.3 * -0.0406) = -0.00265$$

Compute new weights

$$\Delta w_{ji} = \eta \delta_j o_i$$

$$\Delta w_{45} = \eta \delta_5 y_4 = 1 * -0.0406 * 0.6637 = -0.0269$$

$$w_{45}(\text{new}) = \Delta w_{45} + w_{45}(\text{old}) = -0.0269 + (0.9) = 0.8731$$

$$\Delta w_{14} = \eta \delta_4 x_1 = 1 * -0.0082 * 0.35 = -0.00287$$

$$w_{14}(\text{new}) = \Delta w_{14} + w_{14}(\text{old}) = -0.00287$$

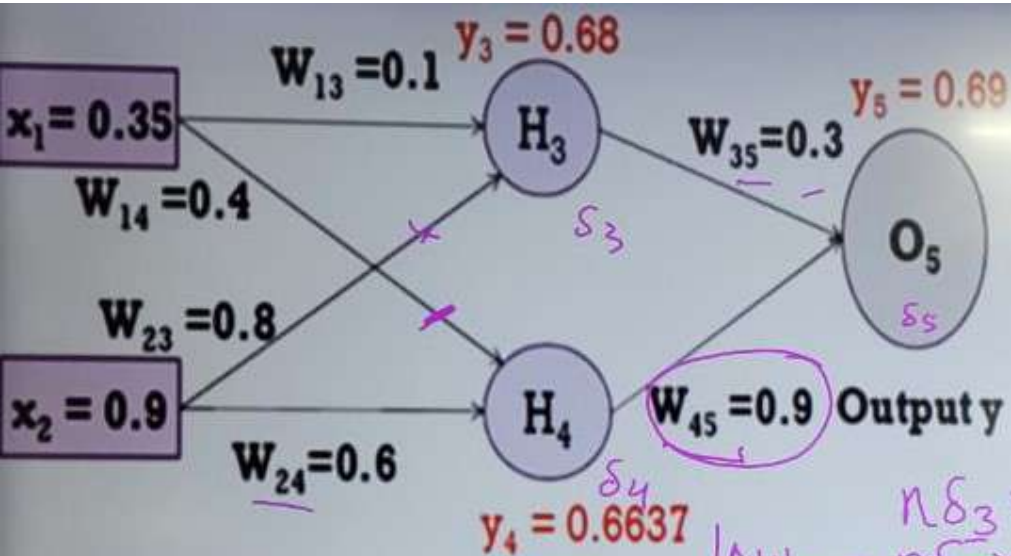
$$\Delta w_{23} = \eta \delta_3 x_2 = 1 * -0.0026 * 0.9 = -0.002385$$

$$w_{23}(\text{new}) = 0.8 - 0.002385 = 0.7976$$

$$\delta_4 = y_4(1-y_4)w_{45} * \delta_5 = 0.6637 * (1 - 0.6637) * (0.9 * -0.0406) = -0.0082$$

$$\Delta w_{35} = \eta \delta_5 y_3 = 1 * -0.0406 * 0.68 = -0.0276$$

$$w_{35}(\text{new}) = 0.3 - 0.0276 = 0.2724$$



Backward Pass: Compute δ_3 , δ_4 and δ_5 .

For output unit:

$$\delta_5 = y(1-y) (y_{\text{target}} - y)$$

$$= 0.69 * (1 - 0.69) * (0.5 - 0.69) = -0.0406$$

$\delta_5 \rightarrow O/P$

For hidden unit:

$$\delta_3 = y_3(1-y_3) w_{35} * \delta_5$$

$$= 0.68 * (1 - 0.68) * (0.3 * -0.0406) = -0.00265$$

Compute new weights

$$\Delta w_{ji} = \eta \delta_j o_i$$

$$\Delta w_{45} = \eta \delta_5 y_4 = 1 * -0.0406 * 0.6637 = -0.0269$$

$$w_{45}(\text{new}) = \Delta w_{45} + w_{45}(\text{old}) = -0.0269 + (0.9) = 0.8731$$

$$\delta_4 = y_4(1-y_4) w_{45} * \delta_5$$

$$= 0.6637 * (1 - 0.6637) * (0.9 * -0.0406) = -0.0082$$

$$w_{14} = \eta \delta_4 x_1 = 1 * -0.0082 * 0.35 = -0.00287$$

$$\Delta w_{35} = \eta \delta_5 y_3 = (1 * -0.0406) * 0.68 = -0.0276$$

Handwritten notes:

$$\Delta w_{23} = \eta \delta_3 x_2$$

$$= 1 * -0.0026 * 0.9 = -0.002385$$

$$\text{new } w_{23} = 0.7976$$