

**Module-3- Fourier Series- (Radian Form)**

**Fourier Series (University Que. Paper Weightage 20 Marks)**

1. Find Fourier series for the function  $f(x) = \begin{cases} 1 + \frac{2x}{\pi} & -\pi \leq x \leq 0 \\ 1 - \frac{2x}{\pi} & 0 \leq x \leq \pi \end{cases}$  And

hence prove that  $\frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \frac{1}{7^2} + \dots = \frac{\pi^2}{8}$  (Dec-11,12,15,18-May -10)

2. Find Fourier series for the function  $f(x) = \begin{cases} x + \frac{\pi}{2} & -\pi < x < 0 \\ \frac{\pi}{2} - x & 0 < x < \pi \end{cases}$  and

hence prove that  $\frac{1}{1^4} + \frac{1}{3^4} + \frac{1}{5^4} + \dots = \frac{\pi^4}{96}$  (Dec-08,09,15,16,18-May -12)

3. Find Fourier series for the function  $f(x) = \sqrt{1 - \cos x}$  in  $(0, 2\pi)$

Hence deduce that  $\frac{1}{2} = \sum_{n=1}^{\infty} \frac{1}{4n^2 - 1}$  (Dec-13,15,16-May -13)

4. Find Fourier series for the function  $f(x) = x^2 + x$  in  $[0, 2\pi]$  with

$f(x + 2\pi) = f(x)$  (Dec-08,11-May -10)

5. Obtain Fourier series for  $f(x) = e^x$  in  $(0, 2\pi)$  (May -10, 13)

6. Obtain Fourier series for  $f(x) = x \sin x$ , in  $(-\pi, \pi)$  (May-13)