

Example

x, y

	1	2	3	4	5
1	0	9	3	6	11
2	9	0	7	5	10
3	3	7	0	9	2
4	6	5	9	0	8
5	11	10	2	8	0

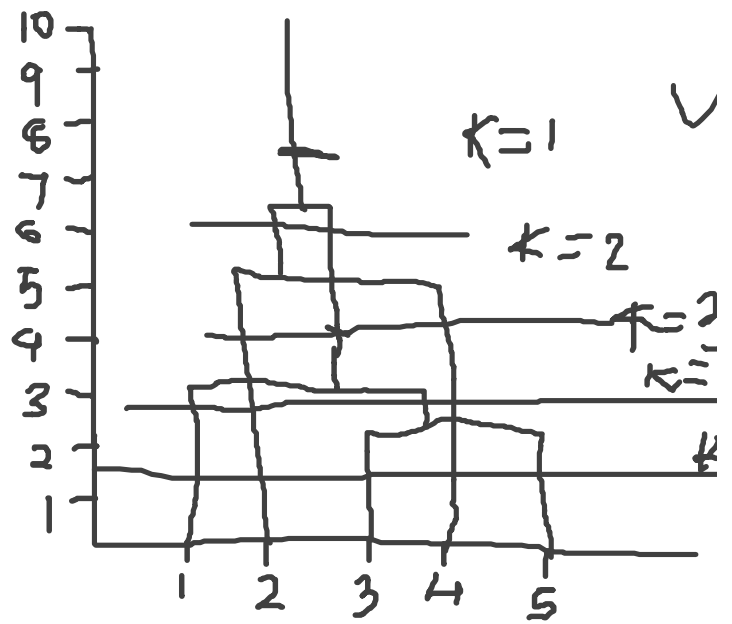
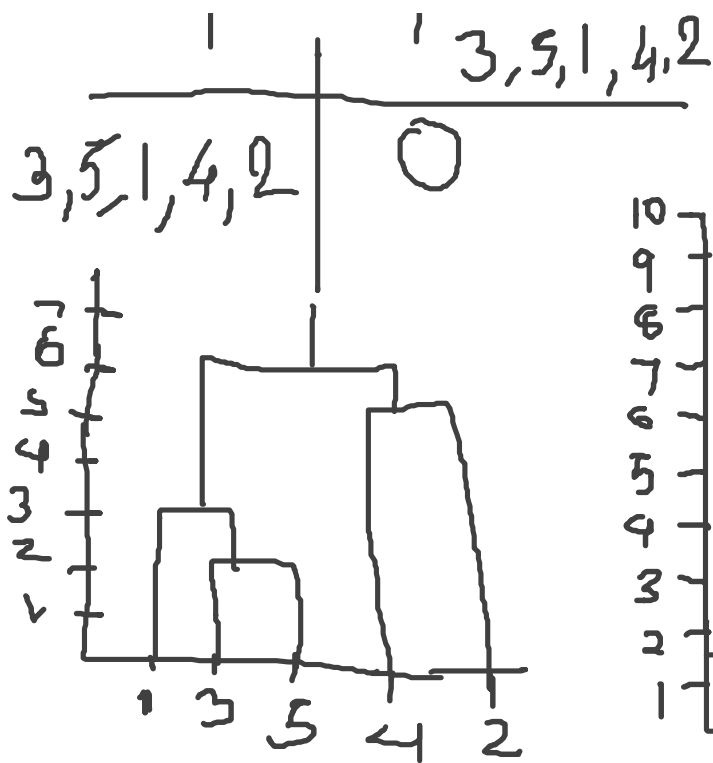
Single Linkage

d(3, 11)  
 min(7, 10)  
 min(9, 8)  
 Single

	3, 5	1	2	4
3, 5	0			
1	3	0		
2	7	9	0	
4	8	6	5	0

	3, 5, 1	2	4
3, 5, 1	0		
2	7	0	
4	6	5	0

	3, 5, 1	4, 2
3, 5, 1	0	
4, 2	6	0



## 2) Complete Linkage

	1	2	3	4	5
1	0				
2	9	0			
3	3	7	0		
4	6	5	9	0	
5	11	10	2	8	0

min  $\Rightarrow 2 \Rightarrow$  merge 3, 5  
 $\max(1, 3) / (1, 5) \quad \max(3, 11) \Rightarrow 11$

	3, 5	1	2	4
3, 5	0			
1	11	0		
2	10	9	0	
4	9	6	5	0

4

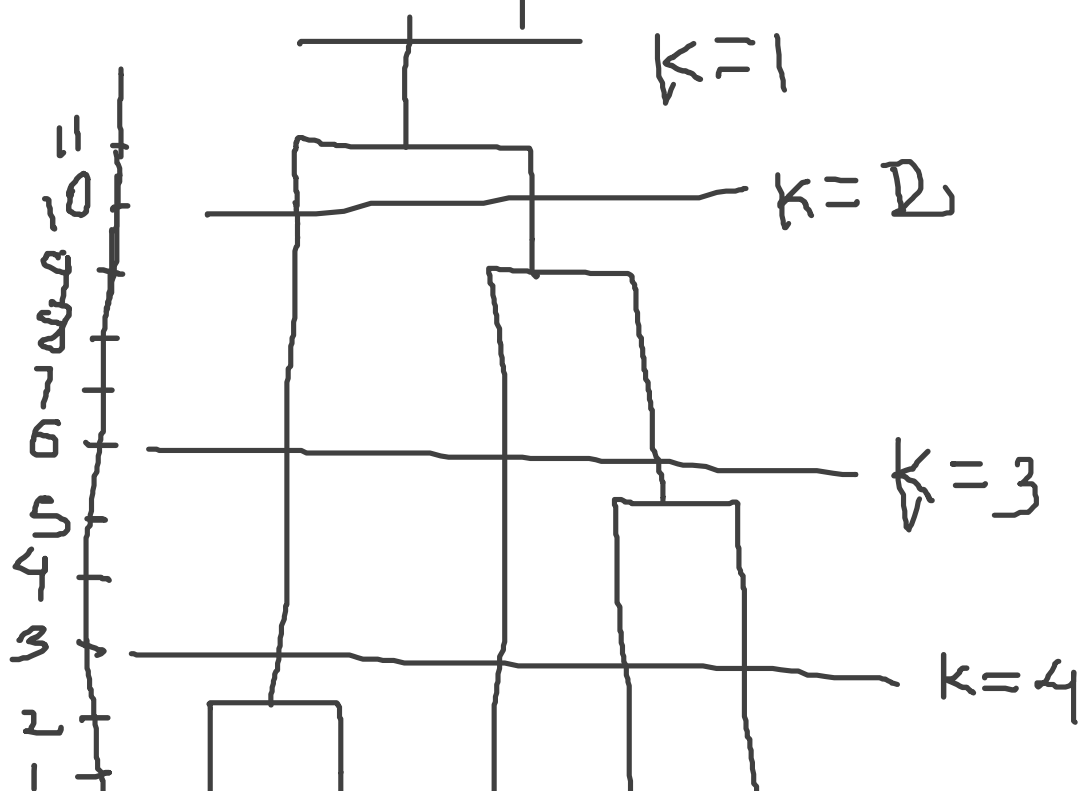
	3,5	1	2,4
3,5	0		
1	11	0	
2,4	10	9	0

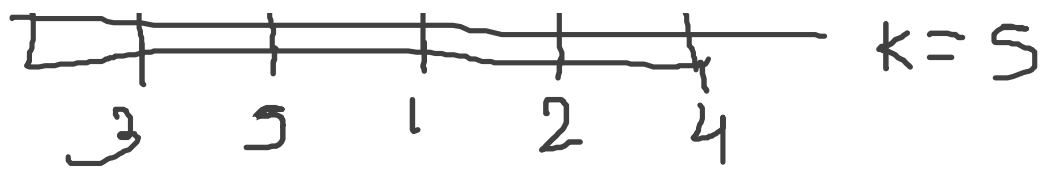
3)

	3,5	1,2,4
3,5	0	
1,2,4	11	0

4)

	3,5,1,2,4
3,5,1,2,4	0





3) Average Linkage

$$[3, 5, 1] \Rightarrow \text{Avg}([3, 5], 1) \Rightarrow \frac{3+5}{2} \Rightarrow 4$$

1)

	3, 5	1	2	4
3, 5	0			
1	7	0		
2	8.5	9	0	
4	8.5	6	<u>5</u>	0

As  $\min \Rightarrow 5$  merge (2, 4)

2)

	3, 5	1	2, 4
3, 5	0		
1	<u>7</u>	0	
2, 4	8.5	7.5	0

$\min \Rightarrow 7$  merge 3, 5, 1

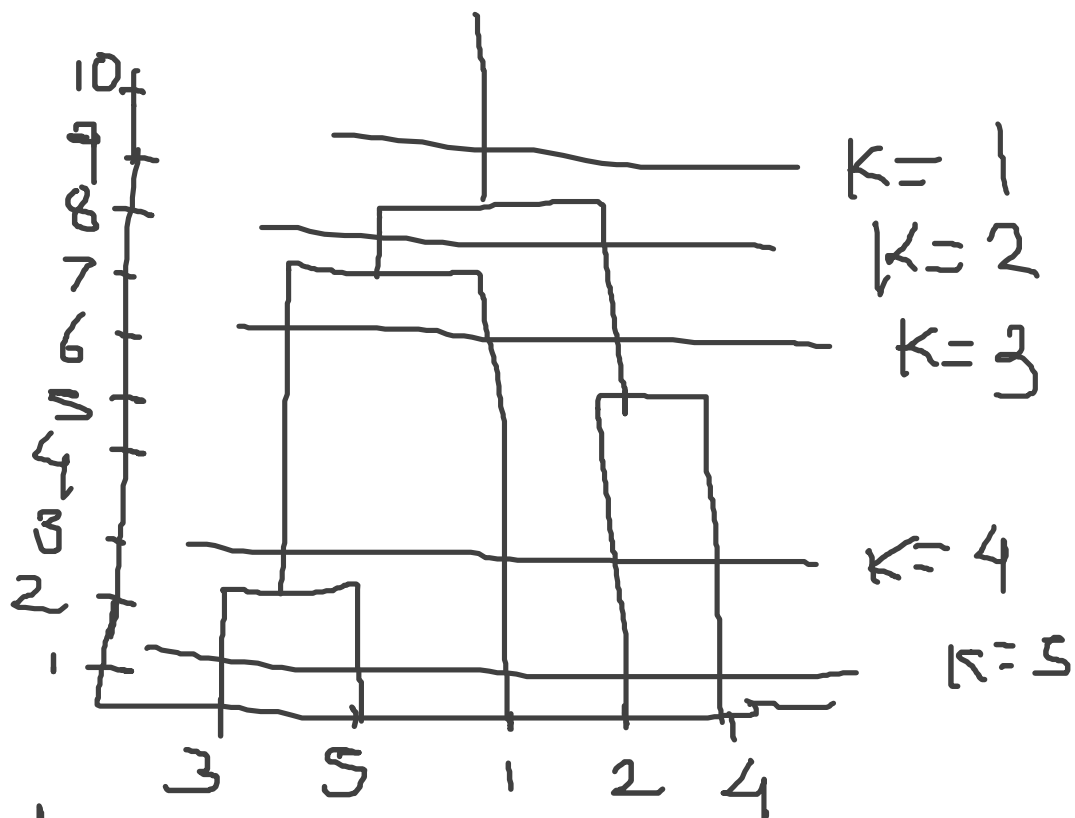
3)

	3, 5, 1	2, 4
3, 5, 1	0	
2, 4	<u>8</u>	0

4) 

1, 3, 5, 2, 4
1, 3, 5, 2, 4

 0



4) singl, complete & Average

	1	2	3	4	5
1	0				
2	2	0			
3	6	3	0		
4	10	9	7	0	
5	9	8	5	4	0

9

	A	B	C	D	E	F
X	1	1.5	5	3	4	2

$x_2$	1	1.5	5	4	4	3.5
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A) Using Euclidean distance first  
 ✓ Create distance Matrix

$$D(A, B) = \sqrt{(1.5-1)^2 + (1.5-1)^2}$$

$$= \sqrt{(0.5)^2 + (0.5)^2}$$

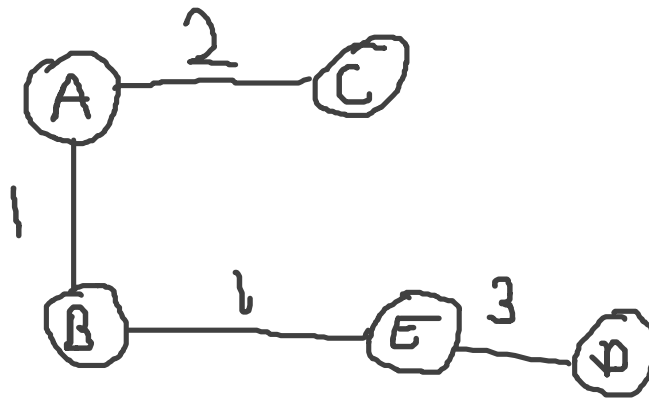
$$= 0.71$$

	A	B	C	D	E	F
A	0					
B	0.7	0				
C	5.65	4.95	0			
D	3.6	2.92	2.42	0		
E	4.24	3.54	1.41	1	0	
F	3.2	2.5	2.5	0.5	1.2	0

Divisive Algorithm

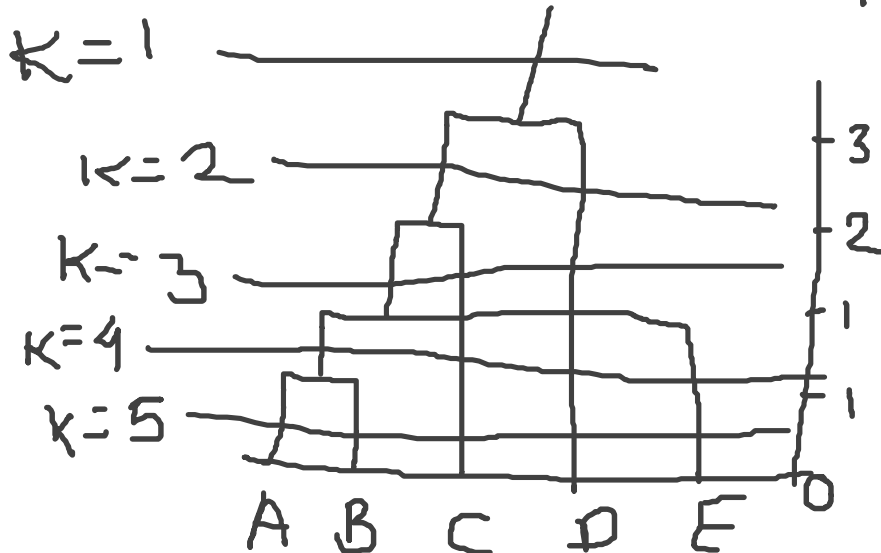
	A	B	C	D	E
A	0				
B	1	0			
C	2	3	0		

D	5	4	6	0	
E	4	1	2	3	0



A	✓
B	✓
C	✓
D	✓
E	✓
F	✓

$$\text{cost} = 2 + 1 + 1 + 3 = 7$$



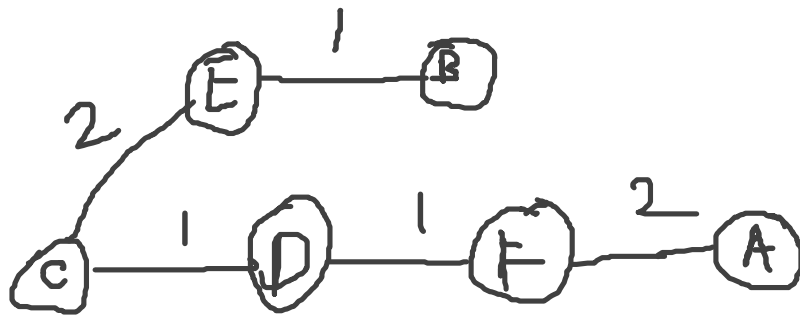
Q. 10 M

Apply Divisive Based approach to from the clusters

a)

	A	B	C	D	E	F
A	0					
B	3	0				
C	4	2	0			
D	7	3	1	0		
E	5	1	2	3	0	

F | 2 | 6 | 7 | 1 | 4 | 0 |



~~A~~  
~~B~~  
C  
D  
F  
A