

- ① The dimension of input $[X]$ is 6
The dimension of kernel $[K]$ is 3

There are total of 9 parameters in kernel.

- ② Assuming stride=1

$$X = \begin{bmatrix} 7 & 5 & 0 & 0 & 3 & 2 \\ 6 & 4 & 5 & 1 & 4 & 8 \\ 9 & 0 & 2 & 2 & 5 & 4 \\ 6 & 3 & 4 & 7 & 9 & 8 \\ 5 & 7 & 5 & 6 & 9 & 0 \\ 7 & 9 & 0 & 8 & 2 & 5 \end{bmatrix} \quad K = \begin{bmatrix} 1 & 0 & -1 \\ 2 & 0 & -2 \\ 1 & 0 & -1 \end{bmatrix}$$

In the first step consider

$$\begin{bmatrix} 7 & 5 & 0 \\ 6 & 4 & 5 \\ 9 & 0 & 2 \end{bmatrix} \begin{bmatrix} 1 & 0 & -1 \\ 2 & 0 & -2 \\ 1 & 0 & -1 \end{bmatrix}$$

$$\begin{aligned} &= 7 \times 1 + 5 \times 0 + 0 \times (-1) + 6 \times 2 + 4 \times 0 + 5 \times (-2) + \\ &= 7 + 12 - 10 + 9 - 2 \quad 9 \times 1 + 0 \times 0 + 2 \times (-1) \\ &= 16. \end{aligned}$$

Similarly with stride=1

$$\begin{bmatrix} 5 & 0 & 0 \\ 4 & 5 & 1 \\ 0 & 2 & 2 \end{bmatrix} \begin{bmatrix} 1 & 0 & -1 \\ 2 & 0 & -2 \\ 1 & 0 & -1 \end{bmatrix}$$

$$\begin{aligned} &= 5 \times 1 + 0 \times 0 + 0 \times (-1) + 4 \times 2 + 5 \times 0 + 1 \times (-2) + \\ &= 5 + 8 - 2 - 2 = 9 \quad 0 \times 1 + 2 \times 0 + 2 \times (-1) \end{aligned}$$

Similarly the results for all

$$O = \begin{bmatrix} 16 & 9 & -4 & -18 \\ 17 & -5 & -10 & -12 \\ 11 & -9 & -17 & 2 \\ 9 & -1 & -15 & 16 \end{bmatrix}$$

③ After applying maxpooling on

$$O = \begin{bmatrix} 16 & 9 & -4 & -18 \\ 17 & -5 & -10 & -12 \\ 11 & -9 & -17 & 2 \\ 9 & -1 & -15 & 16 \end{bmatrix}$$

Max pooling with 3×3 kernel with stride 1

$$\begin{bmatrix} 17 & 9 \\ 17 & 16 \end{bmatrix}$$