

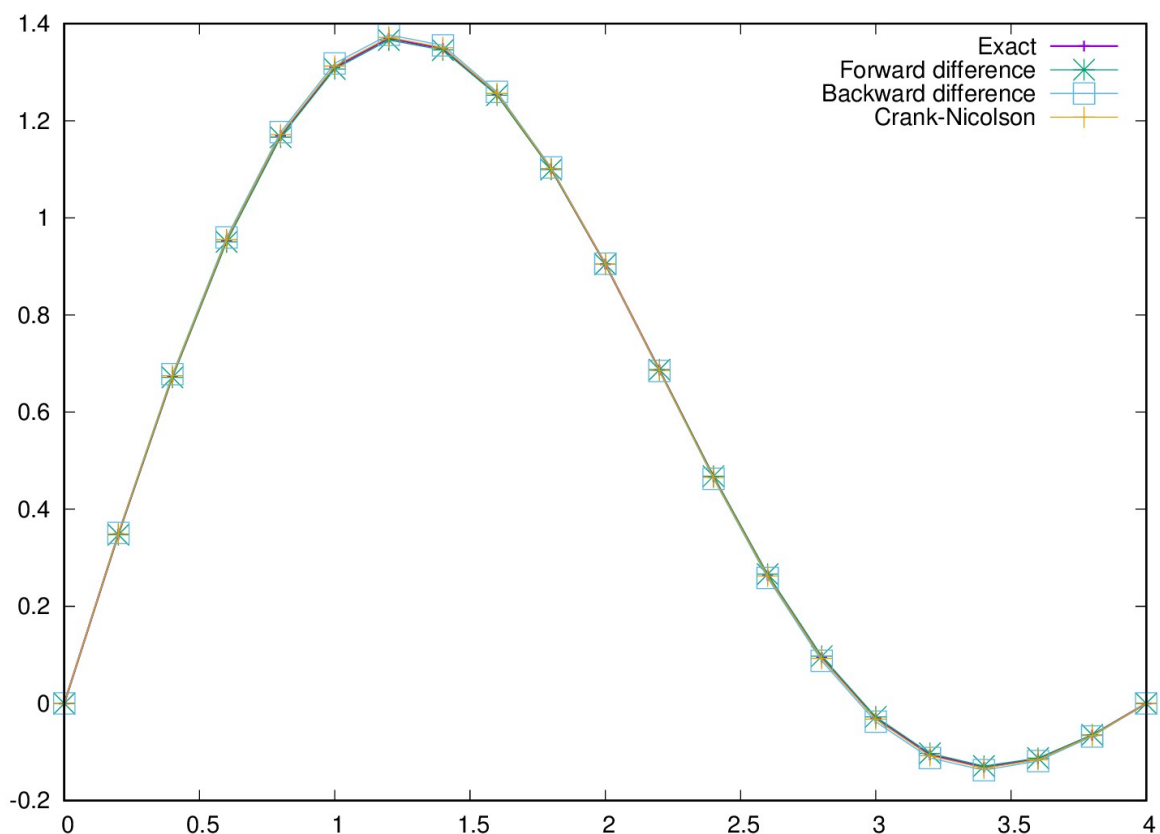
Lab Assignment – 01-11-2018

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1. Relative comparison of different methods:

| $x(t=0.4)$ | Exact | Forward | Error | Backward | Error | Crank-Nicolson | Error |
|------------|------------|------------|-----------|------------|-----------|----------------|-----------|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0.2 | 0.348688 | 0.347653 | 0.001035 | 0.351067 | 0.002379 | 0.349387 | 0.000699 |
| 0.4 | 0.673614 | 0.671643 | 0.001971 | 0.678147 | 0.004533 | 0.674945 | 0.001331 |
| 0.6 | 0.953088 | 0.950367 | 0.002721 | 0.959344 | 0.006256 | 0.954925 | 0.001837 |
| 0.8 | 1.16936 | 1.16615 | 0.00321 | 1.17675 | 0.00739 | 1.17153 | 0.00217 |
| 1 | 1.31014 | 1.30673 | 0.00341 | 1.31796 | 0.00782 | 1.31243 | 0.00229 |
| 1.2 | 1.36954 | 1.36627 | 0.00327 | 1.37707 | 0.00753 | 1.37175 | 0.00221 |
| 1.4 | 1.34852 | 1.34568 | 0.00284 | 1.35505 | 0.00653 | 1.35044 | 0.00192 |
| 1.6 | 1.25456 | 1.25241 | 0.00215 | 1.25949 | 0.00493 | 1.25601 | 0.00145 |
| 1.8 | 1.10084 | 1.09958 | 0.00126 | 1.10374 | 0.0029 | 1.10169 | 0.00085 |
| 2 | 0.904837 | 0.90457 | 0.000267 | 0.905471 | 0.000634 | 0.905023 | 0.000186 |
| 2.2 | 0.686557 | 0.687286 | 0.000729 | 0.684903 | 0.001654 | 0.686071 | 0.000486 |
| 2.4 | 0.466547 | 0.468181 | 0.001634 | 0.462813 | 0.003734 | 0.46545 | 0.001097 |
| 2.6 | 0.263916 | 0.266277 | 0.002361 | 0.258511 | 0.005405 | 0.262328 | 0.001588 |
| 2.8 | 0.0945167 | 0.0973558 | 0.0028391 | 0.0880125 | 0.0065042 | 0.0926058 | 0.0019109 |
| 3 | -0.0305034 | -0.0274796 | 0.0030238 | -0.0374332 | 0.0069298 | -0.0325391 | 0.0020357 |
| 3.2 | -0.105662 | -0.102764 | 0.002898 | -0.112306 | 0.006644 | -0.107614 | 0.001952 |
| 3.4 | -0.131513 | -0.129035 | 0.002478 | -0.137194 | 0.005681 | -0.133182 | 0.001669 |
| 3.6 | -0.114394 | -0.112588 | 0.001806 | -0.118535 | 0.004141 | -0.11561 | 0.001216 |
| 3.8 | -0.0655925 | -0.0646415 | 0.000951 | -0.0677733 | 0.0021808 | -0.0662331 | 0.0006406 |
| 4 | 0.00E+00 | 0 | 0 | 0 | 0 | 0 | 0 |

2. Graphical Comparison



3. After $\Delta t = 0.2$, the forward difference method loses its stability,

