

Introduction

Area of a Circle

Area of a circle is πr^2 , where $\pi = 22/7$ or ≈ 3.14 (can be used interchangeably for problem-solving purposes) and r is the radius of the circle.

π is the ratio of the circumference of a circle to its diameter.

Circumference of a circle

The perimeter of a circle is the distance covered by going around its boundary once. The perimeter of a circle has a special name: Circumference, which is π times the diameter which is given by the formula $2\pi r$

The segment of a circle

A circular segment is a region of a circle which is “cut off” from the rest of the circle by a secant or a chord

A sector of a circle

A circle sector/ sector of a circle is defined as the region of a circle enclosed by an arc and two radii. The smaller area is called the minor sector and the larger area is called the major sector.

The angle of a Sector

The angle of a sector is that angle which is enclosed between the two radii of the sector.

Length of an arc of a sector

The length of the arc of a sector can be found by using the expression for the circumference of a circle and the angle of the sector, using the following formula:

$$L = (\theta/360^\circ) \times 2\pi r$$

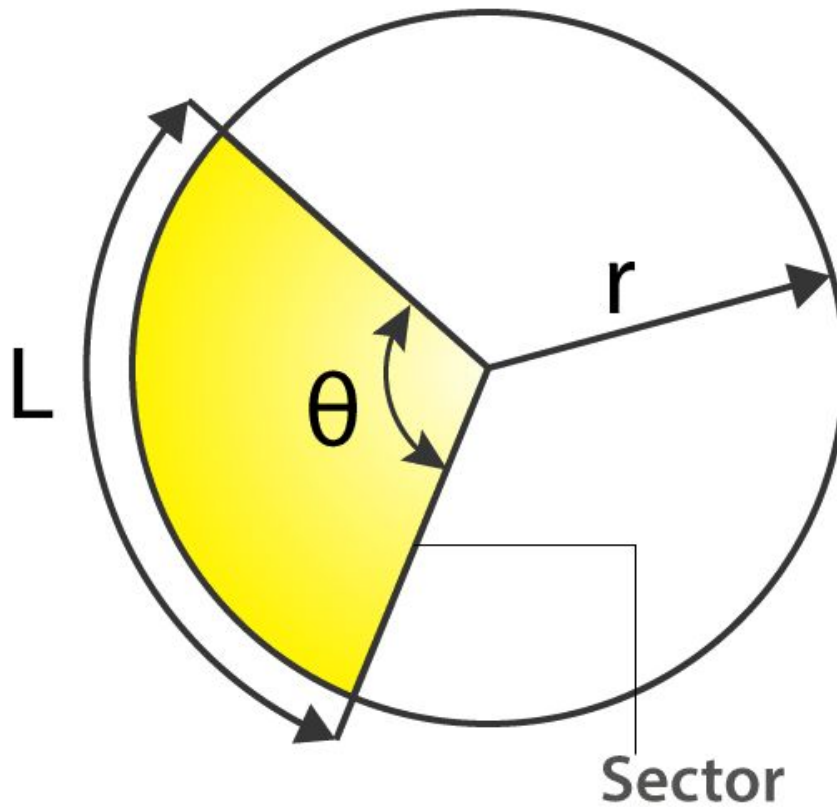
where θ is the angle of sector and r is the radius of the circle.

Area of a Sector of a Circle

Area of a sector is given by

$$(\theta/360^\circ) \times \pi r^2$$

where $\angle \theta$ is the angle of this sector (minor sector in the following case) and r is its radius



Area of a sector

Area of a Triangle

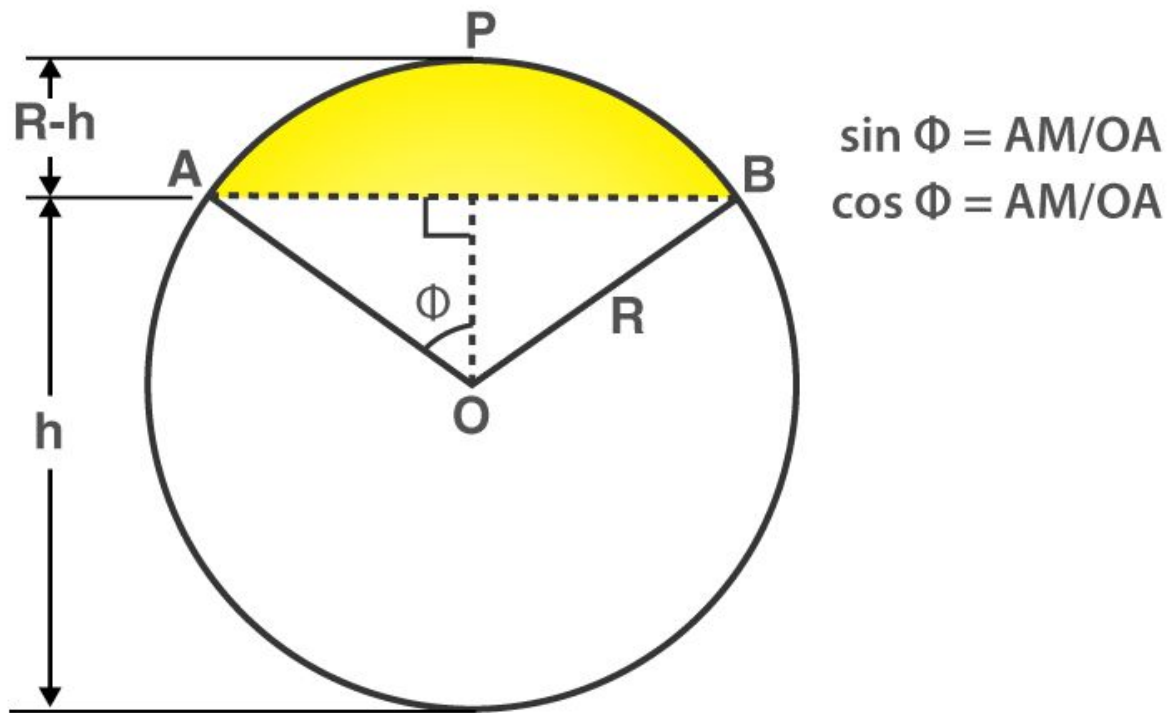
Area of a triangle is,

$$\text{Area} = (1/2) \times \text{base} \times \text{height}$$

If the triangle is an equilateral then

$$\text{Area} = \frac{\sqrt{3}}{4} \times a^2 \quad \text{where } a \text{ is the side of the triangle.}$$

Area of a Segment of a Circle



Area of the segment

Area of segment APB (highlighted in yellow)

= (Area of sector OAPB) – (Area of triangle AOB)

$$= \left[\left(\frac{\theta}{360^\circ} \right) \times \pi r^2 \right] - \left[\left(\frac{1}{2} \right) \times AB \times OM \right]$$

[To find the area of triangle AOB, use trigonometric ratios to find OM (height) and AB (base)]

Also, Area of segment APB can be calculated directly if the angle of the sector is known using the following formula.

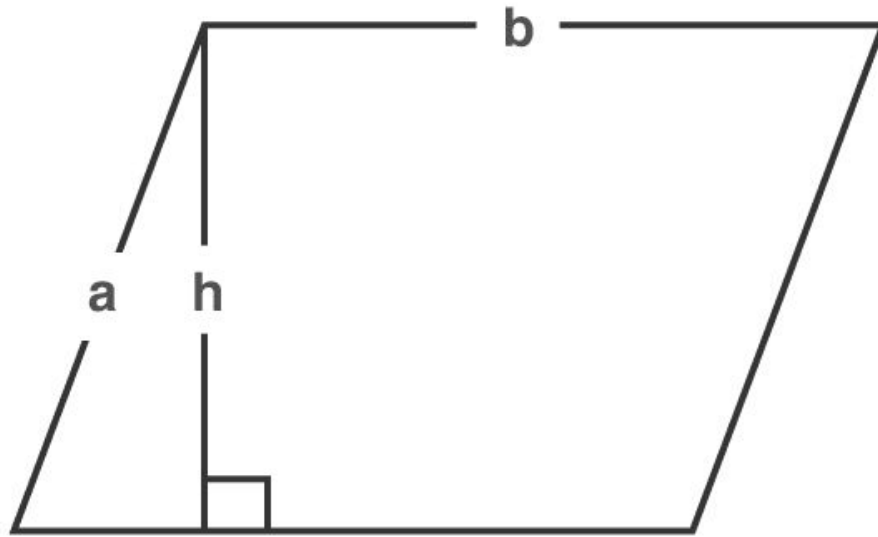
$$= \left[\left(\frac{\theta}{360^\circ} \right) \times \pi r^2 \right] - \left[r^2 \times \sin \frac{\theta}{2} \times \cos \frac{\theta}{2} \right]$$

where θ is the angle of the sector and r is the radius of the circle

Visualisations

Areas of different plane figures

- Area of a square (side l) $=l^2$
- Area of a rectangle $=l \times b$, where l and b are the length and breadth of the rectangle
- Area of a parallelogram $=b \times h$, where b is the base and h is perpendicular height.



parallelogram

Area of a trapezium $=\frac{(a+b) \times h}{2}$,

where

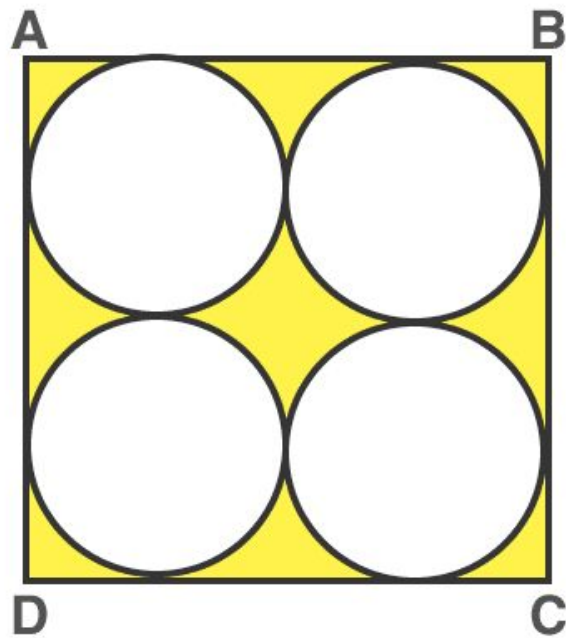
a & b are the parallel sides length

h is the trapezium height

Area of a rhombus $=\frac{pq}{2}$, where p & q are the diagonals

Areas of Combination of Plane figures

For example: Find the area of the shaded part in the following figure: Given the ABCD is a square of side 28cm and has four equal circles enclosed within.



Area of the shaded region

Looking at the figure we can visualise that the required shaded area = $A(\text{square ABCD}) - 4 \times A(\text{Circle})$.

Also, the diameter of each circle is 14 cm.

$$= (l^2) - 4 \times (\pi r^2)$$

$$= (28^2) - [4 \times (\pi \times 49)]$$

$$= 784 - [4 \times 227 \times 49]$$

$$= 784 - 616$$

$$= 168 \text{ cm}^2$$