



### Exercise 1 *Model + Solve*

The file portfolio31.txt has the information of 31 shares in the market (expected return per sterling pound invested and the covariance matrix). Given a capital of £1000:

1. Calculate the optimal portfolio that minimizes the total risk of the investment provided that we would like to have a minimum expected return of £5000. Save the solution to a txt file.
2. Draw a chart of the efficient frontier of the problem. Starting with a minimum return of 1000, solve every problem increasing this value by 250 until you reach an infeasible problem.

### Exercise 2 *Model + solve*

Gold-co must determine how many kilograms of gold to mine over the next two years. If Gold-co extracts  $x_1$  kilograms of gold in year one, each kilogram of gold can be sold for  $£(30 - x_1)$ . If Gold-co extracts  $x_2$  kilograms of gold in year two, each kilogram of gold can be sold for  $£(35 - x_2)$ . The cost of extracting  $x_1$  kilograms of gold in year one is  $£x_1$  and the cost of extracting  $x_2$  kilograms of gold in year two is  $£2x_2$ . A total of 20 kilograms of gold are available to mine. Write and solve a quadratic programming model that Gold-co can use to maximise their profits.

### Exercise 3 *Solve*

Solve the quadratic programming problem for the orange production firm in Florida that we discussed in class.