

HM2 Serie 1 Aufgabe 2

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a1)

$$w(x, t) = \sin(x + ct)$$

$$\frac{\partial w}{\partial t} = \cos(x + ct) \cdot c$$

$$\frac{\partial}{\partial t} \left(\frac{\partial w}{\partial t} \right) = -\sin(x + ct) \cdot c^2$$

$$\frac{\partial v}{\partial x} = \cos(x + ct)$$

$$\frac{\partial}{\partial x} \left(\frac{\partial v}{\partial x} \right) = -\sin(x + ct)$$

Wellengleichung ist erfüllt, da:

$$-\sin(x + ct) \cdot c^2 = c^2 \cdot (-\sin(x + ct))$$

a2)

$$v(x, t) = \sin(x + ct) + \cos(2x + 2ct)$$

$$\frac{\partial w}{\partial t} = \cos(x + ct) \cdot c - \sin(2x + 2ct) \cdot 2c$$

$$\frac{\partial}{\partial t} \left(\frac{\partial w}{\partial t} \right) = -\sin(x + ct) \cdot c^2 - \cos(2x + 2ct) \cdot 4c^2$$

$$\frac{\partial v}{\partial x} = \cos(x + ct) - \sin(2x + 2ct) \cdot 2$$

$$\frac{\partial}{\partial x} \left(\frac{\partial v}{\partial x} \right) = -\sin(x + ct) - \cos(2x + 2ct) \cdot 4$$

Wellengleichung ist erfüllt, da:

$$-\sin(x + ct) \cdot c^2 - \cos(2x + 2ct) \cdot 4c^2 = c^2 \cdot (-\sin(x + ct) - \cos(2x + 2ct) \cdot 4))$$