HM2 Serie 4 Aufgabe 1

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Datenpunkte:

- $(x_0, y_0) = (0, 1013)$
- $(x_1, y_1) = (2500, 747)$
- $(x_2, y_2) = (5000, 540)$
- $(x_3, y_3) = (10000, 226)$

Lagrange-Interpolation:

$$p(x) = 1013 \cdot l_0(3750) + 747 \cdot l_1(3750) + 540 \cdot l_2(3750) + 226 \cdot l_3(3750)$$

$$l_0(3750) = \frac{(x - x_1)(x - x_2)(x - x_3)}{(x_0 - x_1)(x_0 - x_2)(x_0 - x_3)} = \frac{(3750 - 2500)(3750 - 5000)(3750 - 10000)}{(0 - 2500)(0 - 5000)(0 - 10000)} = -\frac{5}{64}$$

$$l_1(3750) = \frac{(x - x_0)(x - x_2)(x - x_3)}{(x_1 - x_0)(x_1 - x_2)(x_1 - x_3)} = \frac{(3750 - 0)(3750 - 5000)(3750 - 10000)}{(2500 - 0)(2500 - 5000)(2500 - 10000)} = \frac{5}{8}$$

$$l_2(3750) = \frac{(x - x_0)(x - x_1)(x - x_3)}{(x_2 - x_0)(x_2 - x_1)(x_2 - x_3)} = \frac{(3750 - 0)(3750 - 2500)(3750 - 10000)}{(5000 - 0)(5000 - 2500)(5000 - 10000)} = \frac{15}{32}$$

$$l_3(3750) = \frac{(x - x_0)(x - x_1)(x - x_2)}{(x_3 - x_0)(x_3 - x_1)(x_3 - x_2)} = \frac{(3750 - 0)(3750 - 2500)(3750 - 5000)}{(10000 - 2500)(10000 - 5000)} = -\frac{1}{64}$$

$$p(x) = 1013 \cdot -\frac{5}{64} + 747 \cdot \frac{5}{8} + 540 \cdot \frac{15}{32} + 226 \cdot -\frac{1}{64} = 637.328125$$