

# Definitely Not A Lib

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## Índice

<b>1 data_structures</b>	<b>2</b>		
1.1 Bit.hpp . . . . .	2	2.5 Pragmas.hpp . . . . .	13
1.2 CartesianTree.hpp . . . . .	3	2.6 Rng.hpp . . . . .	13
1.3 DynamicCht.hpp . . . . .	3	2.7 Stress.sh . . . . .	13
1.4 IndexedSet.hpp . . . . .	4	2.8 StressChecker.sh . . . . .	13
1.5 OffsetVector.hpp . . . . .	5	2.9 Template.cpp . . . . .	14
1.6 Pareto.hpp . . . . .	5	2.10 TemplateBig.cpp . . . . .	14
1.7 SegtreeIterative.hpp . . . . .	6	<b>3 math</b>	<b>15</b>
1.8 SegtreeLazy.hpp . . . . .	7	3.1 BasicCombi.hpp . . . . .	15
1.9 SegtreePersistent.hpp . . . . .	8	3.2 BerlekampMassey.hpp . . . . .	15
1.10 SparseTable.hpp . . . . .	10	3.3 BigInt.hpp . . . . .	16
1.11 SqrtDecomp.hpp . . . . .	10	3.4 Bigmod.hpp . . . . .	18
<b>2 utility</b>	<b>11</b>	3.5 Binpow.hpp . . . . .	18
2.1 Checker.cpp . . . . .	11	3.6 Division.hpp . . . . .	19
2.2 Gen.cpp . . . . .	12	3.7 ExtendedGcd.hpp . . . . .	19
2.3 Hash.sh . . . . .	12	3.8 FactoringAndPrimalityTest.hpp . . . . .	19
2.4 HashFile.sh . . . . .	12	3.9 Fft.hpp . . . . .	20
		3.10 Linearrecurrence.hpp . . . . .	22
		3.11 Matrix.hpp . . . . .	23
		3.12 MatrixMulMod.hpp . . . . .	25

3.13	Modint.hpp	26	6.9	Hld.hpp	43
3.14	Polynomial.hpp	27	6.10	IncrementalMst.hpp	45
3.15	Sieve.hpp	28	6.11	Isomorphism.hpp	46
<b>4</b>	<b>string</b>	<b>29</b>	6.12	Kthshortestwalk.hpp	48
4.1	AhoCorasik.hpp	29	6.13	Lca.hpp	49
4.2	HashInterval.hpp	29	6.14	Lct.hpp	50
4.3	Kmp.hpp	30	6.15	RootedTree.hpp	51
4.4	Manacher.hpp	30	6.16	Sec.hpp	52
4.5	MinRot.hpp	31	6.17	UnionFind.hpp	53
4.6	SuffixArray.hpp	31			
4.7	SuffixAutomaton.hpp	33	<b>1</b>	<b>data_structures</b>	
4.8	Trie.hpp	34	<b>1.1</b>	<b>Bit.hpp</b>	
4.9	ZFunction.hpp	34			
<b>5</b>	<b>geometry</b>	<b>35</b>			
5.1	Point.hpp	35			
<b>6</b>	<b>graph</b>	<b>35</b>			
6.1	2sat.hpp	35			
6.2	BinaryLift.hpp	36			
6.3	BipartiteMatching.hpp	37			
6.4	Dinic.hpp	38			
6.5	DsuRollback.hpp	39			
6.6	DynamicConnectivity.hpp	40			
6.7	EdgeColoring.hpp	41			
6.8	FunctionalGraph.hpp	42			

```

Hash: 321f5b
/*
from https://github.com/defnotmee/definitely-not-a-lib

Usage: BIT(n) -> creates array arr of size n where you can
make point updates and prefix queries (0-indexed!) in O(log(n))

BIT::merge(a, b) -> merges b into element a. By default a+=b.
(must be commutative and associative)

BIT::update(id, x) -> merge(arr[id],x) for every i <= id

BIT::query(id) -> initializes ret = T(), does merge(ret, arr[i])
for every i <= id, returns ret.
*/

d7 d7 #ifndef 0_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

f1 14 template<typename T = ll>
3c 71 struct BIT{
15 67     vector<T> bit;

```

```

eb 27     BIT(int n = 0){
ca 0d         bit = vector<T>(n+1);
13 cb     }

fe 4a     static void merge(T& a, T b){
b5 9f         a+=b;
37 cb     }

4e 7e     void update(int id, T x){
9e ab         id++;
21 b8         while(id < bit.size()){
0a 00             merge(bit[id],x);
24 36             id+=id&-id;
a1 cb         }
89 cb     }

98 32     T query(int id){
49 ab         id++;
b6 83         T ret = T();
32 7a         while(id){
ee df             merge(ret,bit[id]);
22 29             id-=id&-id;
1a cb         }
c9 ed         return ret;
87 cb     }
32 21 };

```

## 1.2 CartesianTree.hpp

```

Hash: 387379
/*
from https://github.com/defnotmee/definitely-not-a-lib

```

The best cartesian tree.

Given an array v, calculates the following information in O(n):

- fl[i]: biggest j < i such that v[j] <= v[i]. fl[i] = -1 by default
- fr[i]: smallest j > i such that v[j] < v[i]. fr[i] = n by default
- cl[i]: index of the element that minimizes v[j] for fl[i] < j < i. cl[i] = i by default
- cr[i]: index of the element that minimizes v[j] for i < j < fr[i]. cr[i] = i by default
- pai[i]: parent of i on the cartesian tree, that is, in the tree where i has edges to cl[i] and cr[i]. -1 by default.

In case there are repeated elements, the ones with lowest index will be closer to the root of the cartesian tree.

Can also take different comparator functions in its template \*/

```

d7 d7 #ifndef 0_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

23 bd template<typename T, typename cmp = less<T>>
4e ed struct CarTree{
ac 1a     int n;
58 51     vector<T> v;
7a 4d     vector<T> fl, fr, cl, cr, pai;
5c 88     int root;

79 7c     CarTree(vector<T>& _v) : n(_v.size()), v(_v), fl(n), fr(n),
        cl(n), cr(n), pai(n,-1){
67 60         for(int i = 0; i < n; i++){
16 0c             fl[i] = i-1;
3e 62             cl[i] = cr[i] = i;
33 23             fr[i] = n;

df 2f             int lst = -1;
51 dc             while(fl[i] != -1 && cmp()(v[i], v[fl[i]])){
c3 8e                 lst = fl[i];
18 0d                 fr[fl[i]] = i;
90 ce                 fl[i] = fl[fl[i]];
ed cb             }
f9 7c             if(lst != -1)
53 99                 cl[i] = lst, pai[lst] = i;
3c f7             if(fl[i] != -1)
63 e8                 cr[fl[i]] = i, pai[i] = fl[i];
44 cb             }

07 83             root = min_element(all(pai))-pai.begin();
92 cb         }
38 21 };

```

## 1.3 DynamicCht.hpp

```

Hash: 09bf62
/**
 * from https://github.com/defnotmee/definitely-not-a-lib
 *

```

```

* based on https://github.com/kth-competitive-programming/kactl/blob/
  main/content/data-structures/LineContainer.h
*
* Implements a data structure where you can insert functions of the
  form
*  $f(x) = ax+b$  and query the maximum/minimum value of  $f(x)$ 
*
* Usage: declare CHT<1> if you want to find maximum  $f(x)$  queries, and
* CHT<-1> if you want minimum  $f(x)$  queries.
*
*  $O(\log(n))$  amortized insertion and  $O(\log(n))$  queries
*/
d7 d7 #ifndef O_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

aa 73 using line = array<ll,2>;

// mult = 1 for maximum, mult = -1 for minimum
27 dc template<ll mult = 1>
f8 c0 class CHT{
b0 d3     struct poss{
70 54         line l;
a4 50         mutable ll maxx;

67 30         bool operator<(ll x) const {
ab 3b             return maxx < x;
6a cb         }
bd d4         bool operator<(poss o) const {
ca 3f             return l < o.l;
c3 cb         }
f2 21     };

// if x can be double, change this to -INFINITY
c0 fd     static const ll inf = LLONG_MAX;

// if x can be double, change this to a/b
2a fd     ll div_floor(ll a, ll b){
73 60         return a/b-(a%b!=0 && (a~b)<0);
cf cb     }

57 5d     multiset<poss,less<>> s;
// assuming l1 <= l2, finds smallest x such that l1(x) <= l2(
  x)
35 e4     ll intersect(line l1, line l2){
69 49         ll da = l2[0]-l1[0], db = l1[1]-l2[1];
96 bf         if(da == 0)

```

```

fd 3d         return -inf;
75 14         return div_floor(db,da);
bf cb     }

53 67     public:
// Inserts  $f(x) = ax+b$  in the structure
47 d0     void insert(ll a, ll b){
63 43         line l = {a*mult,b*mult};

53 02         auto it = next(s.insert({l}));
34 7c         while(it != s.end() && intersect(l,it->l) >= it->maxx)
bf f6             it = s.erase(it);
dd 42         prev(it)->maxx = it == s.end() ? inf : intersect(l,it->l)
;
b2 04         it--;

74 23         if(it!=s.begin()){
5f 18             auto prv = prev(it);
3a 38             ll in = intersect(prv->l, l);
ba 52             if(in > it->maxx){
29 df                 s.erase(it);
e4 50                 return;
54 cb             }
36 1f             prv->maxx = in;
a8 16             while(prv != s.begin() && prev(prv)->maxx >= prv->
  maxx){
11 3d                 s.erase(prv);
9e f4                 prv = prev(it);
49 2a                 prv->maxx = intersect(prv->l,l);
91 cb             }
8e cb         }
a8 cb     }

// Finds maximum  $f(x)$  in the structure if mult = 1 and
  minimum  $f(x)$  if mult = -1
26 4a     ll query(ll x){
5b 71         auto [a,b] = s.lower_bound(x)->l;
f2 66         return mult*(a*x+b);
0d cb     }
09 21 };

```

## 1.4 IndexedSet.hpp

Hash: 461dc5

/\*\*

\* from <https://github.com/defnotmee/definitely-not-a-lib>

```

*
* TODO: ADD usage
*/
77 77 #include <ext/pb_ds/assoc_container.hpp>
07 30 #include <ext/pb_ds/tree_policy.hpp>

f7 67 template<typename T>
06 a9 using index_set = __gnu_pbds::tree<T, __gnu_pbds::null_type, less<
    T>,
46 2c __gnu_pbds::rb_tree_tag, __gnu_pbds::
    tree_order_statistics_node_update>;

```

## 1.5 OffsetVector.hpp

```

Hash: 89f92e
/*
from https://github.com/defnotmee/definitely-not-a-lib

Create a vector that can be accessed with indexes from [-n to n-1].
*/

d7 d7 #ifndef O_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

26 67 template<typename T>
b9 40 struct offvec{

a4 51     vector<T> v;
75 b7     int offset;

b7 3d     offvec(int n = 0, T def = T()){
92 db         offset = n;
44 ea         v = vector<T>(2*n, def);
fc cb     }

bb 8d     T& operator[](int id){
a8 c8         return v[id+offset];
87 cb     }
89 21 };

```

## 1.6 Pareto.hpp

```

Hash: ac250d
/*
from https://github.com/defnotmee/definitely-not-a-lib

Maintains a partially ordered set (or pareto front), that is,
a list of pairs (x[i], y[i]) such that if for i < j:
x[i] < x[j] => y[i] < y[j].

In a practical sense, "increasing x is bad but increasing y
is good". You can edit pareto::item::fix to change that.

Can only do insertions. O(logn) per insert.
*/

d7 d7 #ifndef O_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

2d 5f struct pareto{
e7 a3     struct item{
fb 0b         ll x, y;

12 e9         bool operator<(item c) const {
3e a6             if(x == c.x)
fd 2d                 return y < c.y;
77 86             return x < c.x;
6c cb         }

25 85         inline void fix(){
                // In case increasing x is good, uncomment this:
                // x*=-1;

                // In case increasing y is bad, uncomment this:
                // y*=-1;

a2 cb         }
99 21     };

ca cd     set<item> s;

6c a1     void insert(ll x, ll y){
16 97         item cur = {x,y};
37 e5         cur.fix();
b7 b3         auto it = s.lower_bound(cur);

ee 23         if(it != s.begin()){
5b 53             auto it2 = it;

```

```

b9 af          it2--;

a3 4b          if(it2->y >= cur.y)
b2 50              return;
8d cb      }

9f 7b          while(it != s.end() && cur.y >= it->y){
45 f6              it = s.erase(it);
ef cb      }

c5 a1          s.insert(cur);
96 cb      }

// returns best item with x <= max_x,
c3 66      item bsearch(ll max_x){
a3 16          item cur = {max_x,0};
34 e5          cur.fix();
d3 87          cur.x++;
55 af          cur.y = -INFL;
fe b3          auto it = s.lower_bound(cur);
92 01          if(it == s.begin()){
                // pretends that there is a really bad item that
                // always exists
da 9b          item ret = {INFL,-INFL};
81 1e          ret.fix();
74 ed          return ret;
a0 cb      }
f1 04          it--;
9f ff          item ret = *it;
1f 1e          ret.fix();
1b ed          return ret;

ff cb      }
ac 21 };

```

## 1.7 SegtreeIterative.hpp

Hash: ca8ced  
/\*

from <https://github.com/defnotmee/definitely-not-a-lib>

Segtree that does point updates and range queries (by default, point set range sum).

The merge operation can be non-commutative.

Implementation based on <https://codeforces.com/blog/entry/18051>

Different from the implementation on that blog, the range on query is [l,r] instead of [l,r)

Commonly changed parts will be commented.  
\*/

```

d7 d7 #ifndef 0_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

```

// In case you want nodes to be a custom struct:

```

// uncomment this
// struct seg {
//     ll x = 0; // "identity value" of operation
// };

```

```

43 fc template<typename seg = ll> // comment this
39 d8 struct SegPoint{

```

```

3c e4     int sz;
9a df     vector<seg> tree;

```

```

f7 b6     SegPoint(int n = 0): sz(n), tree(2*n){};

```

```

55 fe     SegPoint(vector<seg> v){ // 0(n) builder
b1 ea         *this = SegPoint(v.size());

```

```

f9 51         for(int i = 0; i < sz; i++)
8b 71             tree[i+sz] = v[i];
f6 bc         for(int i = sz-1; i > 0; i--)
93 db             tree[i] = merge(tree[2*i], tree[2*i+1]);
00 cb     }

```

```

ab 2c     static seg merge(seg a, seg b){
58 df         return {a+b}; // here is where 2 nodes are merged
1a cb     }

```

```

ea 40     void update(int id, seg val){
c6 92         id+=sz;

```

```

50 ae         tree[id] = val; // here is where you update a point

```

```

b0 77         id>>=1;

```

```

33 7a         while(id){
89 da             tree[id] = merge(tree[2*id], tree[2*id+1]);

```

```

e0 77         id>>=1;
06 cb         }
4f cb         }

03 0d         seg query(int l, int r){
b4 ed         l += sz;
81 c0         r += sz+1;

26 86         seg retl = seg(), retri = seg(); // must be identity value
              through merge

b7 40         while(l < r){
d4 1f         if(l&1)
8a 06         retri = merge(retri, tree[l++]);
77 84         if(r&1)
96 b3         retri = merge(tree[--r], retri);

2d 45         l>>=1;
b1 e9         r>>=1;
71 cb         }

8c 5a         return merge(retri, retri);
fa cb         }

ca 21 };

```

## 1.8 SegtreeLazy.hpp

Hash: a5b495  
/\*

from <https://github.com/defnotmee/definitely-not-a-lib>

Segment tree that allows range updates and queries. By default, it supports affine transformation updates and sum queries, but commonly edited parts will be commented.

If a lazy segtree is not needed I recommend going for an `segtree_iterative.hpp` for speed.

0-indexed by default.

=====

```

Declaration: SegTree<type>(size), where type is the datatype that
represents a node of the segtree
Update: update(l, r, {mult, add}), for l <= i <= r, v[i] = v[i]*mult+
add
Query: query(l,r), returns seg object equivalent to the sum of all
values on range [l,r]

*/

d7 d7 #ifndef 0_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

0a 38 struct SegTree{
              // Uncomment if you need a custom struct
              // struct seg{
              //     int x = 0; // identity value of the merge operation
              // }
6b 5f using seg = ll; // <--- comment this if you need a custom
              struct

4b 07 struct lazy{
f7 7d     ll mult = 1, add = 0; // "identity value" of lazy tag

              // Here is where you edit how to propagate the lazy tag
              // for the children
              // of a segtree node
35 ef void operator+=(const lazy& a){
a1 76     add*=a.mult;
32 d4     mult*=a.mult;
a2 29     add+=a.add;
cd cb     }
7d 21     };
3b 5a static inline seg null = seg(); // identity element through
              the merge operation

              // Here is where you change how to merge nodes
52 2c static seg merge(seg a, seg b){
8a 53     return a+b;
61 cb     }

26 df vector<seg> tree;
f5 2c vector<lazy> lz;

4e 40 int sz, ql, qr;
1f a5 lazy val;

```

```

0f 23 SegTree(int n = 0){
76 43     sz = n;
72 93     tree = vector<seg>(4*n,null);
3d 73     lz = vector<lazy>(4*n);
8b cb }

d7 30 void build(int id, int l, int r, vector<seg> & v){
49 89     if(l == r){
63 62         tree[id] = v[l];
51 50         return;
71 cb     }

37 08     const int e = id*2+1, d = id*2+2, m = (l+r)>>1;

01 f7     build(e,l,m,v);
c6 30     build(d,m+1,r,v);
bd 72     tree[id] = merge(tree[e],tree[d]);

8f cb }

95 2b SegTree(vector<seg> v){ // O(n) builder
c9 46     *this = SegTree(v.size());
56 49     build(0,0,sz-1,v);
58 cb }

8d 8d void refresh(int id, int l, int r){
cd 57     if(l != r){
15 08         const int e = id*2+1, d = id*2+2, m = (l+r)>>1;

49 c0         lz[e]+=lz[id];
6f b6         lz[d]+=lz[id];
4a cb     }

    // Here is where you update the value of the current node
    based on the lazy tag
f8 d2     tree[id] = tree[id]*lz[id].mult+lz[id].add*(r-l+1);
e7 b0     lz[id] = lazy();
28 cb }

ab 51 void update(int l, int r, lazy x){
e0 40     ql = l, qr = r, val = x;
54 8b     upd(0,0,sz-1);
d1 cb }

93 0d seg query(int l, int r){
ae e2     ql = l, qr = r;

```

```

b1 b0         return qry(0,0,sz-1);
6a cb     }

e2 bf     private:

12 bf     void upd(int id, int l, int r){
ce a7         refresh(id,l,r);

76 ce         if(ql <= l && r <= qr){
08 3f             lz[id] += val;
b2 a7             refresh(id,l,r);
c7 50             return;
f3 cb         }
fb 87         if(ql > r || l > qr)
e1 50             return;

3a 08         const int e = id*2+1, d = id*2+2, m = (l+r)>>1;

89 b7         upd(e,l,m);
e5 ad         upd(d,m+1,r);

33 72         tree[id] = merge(tree[e], tree[d]);
76 cb     }

4c 31     seg qry(int id, int l, int r){
f6 a7         refresh(id,l,r);

d1 43         if(ql <= l && r <= qr)
d6 c9             return tree[id];

5e 87         if(ql > r || l > qr)
fc 54             return null;

d1 08         const int e = id*2+1, d = id*2+2, m = (l+r)>>1;
5d c3         return merge(qry(e,l,m), qry(d,m+1,r));
0b cb     }
a5 21 };

```

## 1.9 SegtreePersistent.hpp

Hash: 126ce7

/\*

from <https://github.com/defnotmee/definitely-not-a-lib>

Persistent Segment Tree with point updates. By default, does point set and range sum



```

To create a segtree use PSegTree<type>(min_coord, max_coord).
You can effectively copy a segtree in O(1) by just copying a PSegTree
instance.
*/

d7 d7 #ifndef O_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

// Bump allocator for extra performance:

// static char buf[450 << 20]; // by default can store 4.7e8 bytes
// void* operator new(size_t s) {
//     static size_t i = sizeof buf;
//     assert(s < i);
//     return (void*)&buf[i -= s];
// }
// void operator delete(void*) {}

// implementation above from https://github.com/kth-competitive-
// programming/kactl/blob/main/content/various/BumpAllocator.h

// Uncomment if you need a custom struct.
// struct seg{

// };

43 fc template<typename seg = ll>
80 bf struct Node{
92 c5     Node(seg x = null) : x(x){}

        // identity value of element through merge operation
46 5a     static inline seg null = seg();

1b c7     seg x = null;
78 f4     Node* e = nullptr, *d = nullptr;

1a 2c     static seg merge(seg a, seg b){
8a 53         return a+b;
52 cb     }

1e fb     void refresh(){
ce ae         if(!e)
cf 9a         e = new Node(), d = new Node();

```

```

5a cb     }

37 2e     void update(ll l, ll r, ll q, seg val){
36 89         if(l == r){
91 d1             x = val;
0a 50             return;
9d cb         }

dd 13         refresh();

d8 0f         ll m = (l+r)>>1;

a1 27         if(q <= m)
80 37             (e = new Node(*e))->update(l,m,q,val);
1b a9         else (d = new Node(*d))->update(m+1,r,q,val);

81 6a         x = merge(e->x, d->x);
25 cb     }

06 04     seg query(ll l, ll r, ll ql, ll qr){

40 ce         if(ql <= l && r <= qr){
81 ea             return x;
58 cb         }
ba 87         if(ql > r || l > qr)
db 54             return null;

ac 13         refresh();

d3 0f         ll m = (l+r)>>1;
ca cc         return merge(e->query(l,m,ql,qr), d->query(m+1,r,ql,qr));
ca cb     }

21 21 };

e5 fc template<typename seg = ll>
92 e0 struct PSegTree{

34 f8     ll l, r;
ed c1     Node<seg>* head;

91 cd     PSegTree(ll l = 0, ll r = 0) : l(l), r(r), head(new Node<seg>
>()){}

be 00     seg query(ll ql, ll qr){
61 57         return head->query(l,r,ql,qr);

```

```

a1 cb      }

ad 65      void update(ll q, seg val){
8b 6c          (head = new Node<seg>(*head))->update(l,r,q,val);
ba cb      }
12 21 };

```

## 1.10 SparseTable.hpp

Hash: dec367

```

/*
from https://github.com/defnotmee/definitely-not-a-lib

```

With  $O(n \log(n))$  pre-processing, creates a data structure that answers minimum range queries (RMQ) in  $O(1)$ . Can be modified to work with any idempotent function.

```

*/

```

```

d7 d7 #ifndef O_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

95 93 template<typename T = int>
a1 76 struct RMQ{
a8 1a     int n;
79 21     vector<vector<T>> sp;

e4 96     RMQ(vector<T> v) : n(v.size()), sp(int(log2(n))+1, vector<T>(
    n)){
fc f7         sp[0] = v;

96 a7         for(int i = 1; i < sp.size(); i++)
ee 06             for(int j = 0; j + (1<<i) <= n; j++)
c5 7d                 sp[i][j] = merge(sp[i-1][j], sp[i-1][j+(1<<i-1)])
    ;

1d cb     }

6e b6     static T merge(T a, T b){
1a 23         return min(a,b);
86 cb     }

76 b7     T query(int l, int r){ // must be called with l <= r
fd 1e         int logg = log2(r-l+1);

```

```

b8 e9         return merge(sp[logg][l], sp[logg][r-(1<<logg)+1]);
de cb     }
de 21 };

```

## 1.11 SqrtDecomp.hpp

Hash: 3d0d8b

```

/*
from https://github.com/defnotmee/definitely-not-a-lib

```

Divides an array into blocks of sqrt. In this case, its doing range addition update and range maximum query.

```

TODO: clean code, make it more general
*/

```

```

d7 d7 #ifndef O_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

76 51 const int LEN = 400;

7c 14 template<typename T = ll>
41 ff struct decomp{
11 3d     vector<T> elem;
de af     vector<T> block, lz;

69 99     decomp(int n = 0){
fc 56         elem = vector<T>(n);
a1 af         block = vector<T>((n+LEN-1)/LEN);
9e 4e         lz = vector<T>((n+LEN-1)/LEN);
e1 cb     }

d1 57     void reconstruct(int bid){
82 e0         block[bid] = 0;
c4 a0         for(int i = bid*LEN; i < min(int(elem.size()), (bid+1)*
    LEN); i++){
72 6d             block[bid] = max(block[bid], elem[i]);
32 cb         }
a3 e6         block[bid]+=lz[bid];
06 cb     }

88 41     void update(int l, int r, T x){
32 9a         int bl = l/LEN+1, br = r/LEN;

18 16         if(bl >= br){

```

```

42 24         for(int i = l; i <= r; i++)
89 0f             elem[i]+=x;

13 76         reconstruct(br);
45 5c         if(bl-1 != br)
63 06             reconstruct(bl-1);
08 9d     } else {
7b 50         for(int i = l; i < bl*LEN; i++)
ac 0f             elem[i]+=x;
cc 37         for(int i = bl; i < br; i++)
3c bb             lz[i]+=x, block[i]+=x;
d4 69         for(int i = br*LEN; i <= r; i++)
e7 0f             elem[i]+=x;

21 06         reconstruct(bl-1);
62 76         reconstruct(br);
ee cb     }
d7 cb }

45 b7     T query(int l, int r){
87 9a         int bl = l/LEN+1, br = r/LEN;
84 83         T ret = T();

35 16         if(bl >= br){
f8 24             for(int i = l; i <= r; i++)
06 13                 ret = max(ret,elem[i]+lz[i/LEN]);
d5 9d     } else {
f3 50         for(int i = l; i < bl*LEN; i++)
b8 1f             ret = max(ret,elem[i]+lz[bl-1]);
fa 37         for(int i = bl; i < br; i++)
cc cb             ret = max(ret,block[i]);
70 69         for(int i = br*LEN; i <= r; i++)
56 66             ret = max(ret,elem[i]+lz[br]);
62 cb     }
11 ed     return ret;
57 cb }
3d 21 };

```

## 2 utility

### 2.1 Checker.cpp

```

Hash: 8101f6
/*

```

```

from https://github.com/defnotmee/definitely-not-a-lib

Example checker for stress_checker.sh
*/

2b 2b #include<bits/stdc++.h>
64 01 #define all(x) begin(x), end(x)
0d df #define ff first
d9 a9 #define ss second
80 92 #define O_0
6d ca using namespace std;
af 67 template <typename T>
a3 7f using bstring = basic_string<T>;
ba 67 template <typename T>
d9 f2 using matrix = vector<vector<T>>>;
df 34 typedef unsigned int uint;
78 f4 typedef unsigned long long ull;
2e ad typedef long long ll;
96 ff typedef pair<int,int> pii;
0f 0d typedef pair<ll,ll> pll;
91 6d typedef double dbl;
fd 68 typedef long double dbll;
ec 5a const ll INFL = 4e18+25;
e0 dc const int INF = 1e9+42;
3f 2a const double EPS = 1e-7;
22 f2 const int MOD = (1<<23)*17*7 + 1; // 998244353
93 d1 const int RANDOM = chrono::high_resolution_clock::now().
    time_since_epoch().count();
cb fc const int MAXN = 1e6+1;

77 e8 int main(){

2c 8b     ios_base::sync_with_stdio(false);
4c 00     cin.tie(nullptr);

b7 2b     ifstream ccin("input");

6a ba     int a, b;
1b 0a     cin >> a >> b;

34 c7     assert(a < b);

20 0a     int c;
ed d1     ccin >> c;

91 6f     if(a*b != c){

```

```

43 2d      cout << "a*b is not c\n";
c6 6a      return 1;
4d cb      }

1f f3      cout << "ok\n";

35 bb      return 0;

81 cb }

```

## 2.2 Gen.cpp

```

Hash: 59c40c
/*
from https://github.com/defnotmee/definitely-not-a-lib

```

```

Example of a generator for stress.sh
*/

```

```

2b 2b #include<bits/stdc++.h>
64 01 #define all(x) begin(x), end(x)
0d df #define ff first
d9 a9 #define ss second
80 92 #define O_0

6d ca using namespace std;
af 67 template <typename T>
a3 7f using bstring = basic_string<T>;
ba 67 template <typename T>
d9 f2 using matrix = vector<vector<T>>;
df 34 typedef unsigned int uint;
78 f4 typedef unsigned long long ull;
2e ad typedef long long ll;
96 ff typedef pair<int,int> pii;
0f 0d typedef pair<ll,ll> pll;
91 6d typedef double dbl;
fd 68 typedef long double dbll;
ec 5a const ll INFL = 4e18+25;
e0 dc const int INF = 1e9+42;
3f 2a const double EPS = 1e-7;
22 f2 const int MOD = (1<<23)*17*7 + 1; // 998244353
93 d1 const int RANDOM = chrono::high_resolution_clock::now().
    time_since_epoch().count();
cb fc const int MAXN = 1e6+1;

dc 01 mt19937 rng;

```

```

54 6b int range(int l, int r){
df 0d     return uniform_int_distribution<>(l,r)(rng);
d4 cb }

4b 6f int main(int argc, char ** argv){

e8 8b     ios_base::sync_with_stdio(false);
aa 00     cin.tie(nullptr);

9e 83     rng.seed(atoi(argv[1]));
42 d8     int n = range(1,5), m = range(1,5), k = range(0,n*m);

d7 18     cout << n << ' ' << m << ' ' << k << endl;

6c bb     return 0;

59 cb }

```

## 2.3 Hash.sh

```

Hash: d78ff6
d4 d4 # From https://github.com/tdas0/lib/blob/master/library/contest/
    hash.sh

d4 d4 # Usage: bash hash.sh arquivo.cpp l1 l2
d4 d4 # Finds hash of file from line l1 to line l2

d7 d7 sed -n $2', '$3' p' $1 | sed '/^#/d' | cpp -dD -P -fpreprocessed
    | tr -d '[:space:]' | md5sum | cut -c-6

```

## 2.4 HashFile.sh

```

Hash: c85258

d4 d4 # From https://github.com/tdas0/lib/blob/master/library/contest/
    gethash.sh

d4 d4 # Gets hash of file to compare to the pdf of the library
d4 d4 # Usage: bash gethash.sh arquivo.cpp

f5 f5 echo "" > pref.txt
5e 95 while IFS= read -r l; do
ca e8     echo "$l" >> pref.txt
db 65     echo "$l" > line.txt

```

```

22 d4 hp=$(echo $(bash hash.sh pref.txt 1 1000) | cut -c-2)
b5 fd hl=$(echo $(bash hash.sh line.txt 1 1000) | cut -c-2)
d9 ae echo -e "$hp $hl $l"
c8 65 done < "$1"

```

## 2.5 Pragas.hpp

```

Hash: 5e11de
/*
from https://github.com/defnotmee/definitely-not-a-lib

Useful pragmas from nor's blog: https://codeforces.com/blog/entry/96344
*/

88 88 #pragma GCC optimize("O3,unroll-loops")
5a 82 #pragma GCC target("avx2,bmi,bmi2,lzcnt,popcnt")

// Pragma for randomized solutions by magnus.hegdahl

5e a0 #pragma VOD00 magic("Please work this time")

```

## 2.6 Rng.hpp

```

Hash: 263a2f
/**
 * from https://github.com/defnotmee/definitely-not-a-lib
 *
 * Basic RNG functionality. High quality.
 */
d7 d7 #ifndef O_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

a5 d5 const int SEED = chrono::high_resolution_clock::now().
    time_since_epoch().count();
74 57 mt19937 rng(SEED);

// Returns random integer from l to r.
d4 6b int range(int l, int r){
25 d2     return uniform_int_distribution<int>(l,r)(rng);
26 cb }

```

## 2.7 Stress.sh

```

Hash: 687d34
d4 d4 #!/usr/bin/env bash

d4 d4 # Based on tyrowhiz's template.
d4 d4 # Usage: bash stress.sh wrong_sol bruteforce generator
    test_case_count

d4 d4 # wrong_sol, bruteforce and generator must be WITHOUT extensions

07 07 make $1
ab d3 make $2
ee 49 make $3

42 07 for ((testNum=0;testNum<$4;testNum++))
45 d4 do
08 2c     ./3 $testNum > input
a0 7e     ./2 < input > outSlow
17 a2     ./1 < input > outWrong
d0 ac     if !(diff -b "outWrong" "outSlow")
fd 0e     then
7e 75         echo "Error found!"
3a 62         echo "Input:"
7b c5         cat input
49 98         echo "Wrong Output:"
60 a2         cat outWrong
59 97         echo "Slow Output:"
94 a8         cat outSlow
cf f2         exit
16 75     fi
1c d6         echo Passed Test:$testNum
7e 6b done
68 1b echo Passed $4 tests

```

## 2.8 StressChecker.sh

```

Hash: 55d9cc
d4 d4 #!/usr/bin/env bash

d4 d4 # Based on tyrowhiz's template.
d4 d4 # Usage: bash stress.sh wrong_sol checker generator
    test_case_count

d4 d4 # - checker should return 0 if the solution is correct and
    anything else otherwise

```

```

d4 d4 # - if the checker needs the original input, it will be on a file
      named input and
d4 d4 # you could use something like "ifstream ccin("input"); ccin >>
      something" to read it

d4 d4 # wrong_sol, checker and generator must be WITHOUT extensions

07 07 make $1
ab d3 make $2
ee 49 make $3

42 07 for ((testNum=0;testNum<$4;testNum++))
45 d4 do
08 2c     ./$3 $testNum > input
d3 fd     ./$1 < input > out

5b 5e     if !(./$2 < out > veredict)
f7 0e     then
1d 75         echo "Error found!"
cb 62         echo "Input:"
7d c5         cat input
63 37         echo "Output:"
94 6b         cat out
bc 0b         echo "Checker Veredict:"
af 56         cat veredict
4a f2         exit
ee 75         fi
87 d6         echo Passed Test:$testNum
82 6b done
55 1b echo Passed $4 tests

```

## 2.9 Template.cpp

```

Hash: 617e5f
/*
by Leonardo Valente Nascimento
*/

2b 2b #include<bits/stdc++.h>
64 01 #define all(x) begin(x), end(x)
0d df #define ff first
d9 a9 #define ss second
80 92 #define O_0
6d ca using namespace std;
a1 90 using ll = long long;
56 67 template<typename T>

```

```

e0 f2 using matrix = vector<vector<T>>;
37 a0 using pii = pair<int,int>;
e2 f3 using ull = unsigned long long;
1a 4e const int MOD = 998244353;
5e dc const int INF = 1e9+42;
47 e3 const ll INFL = 2e18;
4a 9c const int MAXN = 1e6+10;

81 e8 int main(){

94 21     cin.tie(0)->sync_with_stdio(0);

ec bb     return 0;

61 cb }

```

## 2.10 TemplateBig.cpp

```

Hash: 55ce33
/*
by Leonardo Valente Nascimento

Big version of template.cpp (used for when copyasting is allowed)
*/

2b 2b #include<bits/stdc++.h>
64 01 #define all(x) begin(x), end(x)
0d df #define ff first
d9 a9 #define ss second
80 92 #define O_0
6d ca using namespace std;
af 67 template <typename T>
a3 7f using bstring = basic_string<T>;
ba 67 template <typename T>
d9 f2 using matrix = vector<vector<T>>;
2f 90 using ll = long long;
f9 ae using uint = unsigned int;
e4 f3 using ull = unsigned long long;
5c e5 using dbl = double;
ed 93 using dbl1 = long double;
c9 79 using ci = complex<int>;
18 db using cl = complex<ll>;
94 a0 using pii = pair<int,int>;
e8 bb using pll = pair<ll,ll>;
25 5a const ll INFL = 4e18+25;

```

```

a2 dc const int INF = 1e9+42;
2c 2a const double EPS = 1e-7;
80 f2 const int MOD = (1<<23)*17*7 + 1; // 998244353
d1 d5 const int SEED = chrono::high_resolution_clock::now().
    time_since_epoch().count();
d4 fc const int MAXN = 1e6+1;
df 57 mt19937 rng(SEED);

fc e8 int main(){

5c 8b ios_base::sync_with_stdio(false);
cc 00 cin.tie(nullptr);

ed bb return 0;

55 cb }

```

## 3 math

### 3.1 BasicCombi.hpp

```

Hash: 6fe4d8
/*
from https://github.com/defnotmee/definitely-not-a-lib

Calculates factorials and binomials modulo p for all
numbers from 0 to n-1. By default creates the struct
for n = MAXN and names it combi.

Idea for  $O(n)$  inverse of each number from this blog:
https://codeforces.com/blog/entry/83075
*/

d7 d7 #ifndef O_0
99 6d #include "../utility/template.cpp"
91 53 #include "modint.hpp"
25 f2 #endif

22 86 template<ull M>
b6 d8 struct Combi{

```

```

// note that inv[0] = 1 in this impl
bb a8 vector<ll> fac, inv, invfac;

f2 bc Combi(int n = MAXN){
bf 6b fac = inv = invfac = vector<ll>(n,1);

4b 9f for(int i = 2; i < n; i++){
58 e0 fac[i] = fac[i-1]*i%M;
77 ea inv[i] = inv[M%i]*(M-M/i)%M;
bc 3b invfac[i] = invfac[i-1]*inv[i]%M;
5f cb }
ac cb }

17 ab ll choose(int n, int k){
de 37 if(n < k)
28 bb return 0;
00 76 return fac[n]*invfac[k]%M*invfac[n-k]%M;
f5 cb }
02 21 };

6f b7 Combi<MOD> c;

```

### 3.2 BerlekampMassey.hpp

```

Hash: 616591
/*
from https://github.com/defnotmee/definitely-not-a-lib

Based on https://mzhang2021.github.io/cp-blog/berlekamp-massey/

Finds coefficients of the shortest linear recurrence that
describes a given sequence in  $O(n^2)$ . If the original linear recurrence
is of order k,  $2k$  terms will be necessary to pinpoint it exactly.

Returns a sequence  $c_0c_1c_2\dots c_k$  where if the sequence is  $s_0s_1s_2\dots s_n$ 
it will hold that  $s_i = \sum(c(j)*s(i-j-1))$  for  $i > k$ .
*/

d7 d7 #ifndef O_0
cb c8 #include "../utility/template.cpp"
91 f2 #endif

42 67 template<typename T>
55 f7 vector<T> berlekamp_massey(vector<T> s){
de 59 vector<T> c, oc;
d4 e8 T ldelta = 0;

```

```

4d d2     int f = 0;
ec 1c     for(int i = 0; i < s.size(); i++){
62 fa         T delta = s[i];

52 22         for(int j = 0; j < c.size(); j++){
4f d7             delta-=c[j]*s[i-j-1];
80 cb         }

fb 84         if(delta == 0)
cc 5e             continue;
28 22         if(ldelta == 0){
4b b3             c = vector<T>(i+1);
34 ab             f = i;
7c a4             ldelta = delta;
96 5e             continue;
cf cb         }

4f 4e         vector<T> maybe = c;
85 fd         vector<T> d = oc;

10 82         for(auto& i : d)
d1 37             i*=-1;

35 af         d.insert(d.begin(),T(1));

70 7b         c.resize(max(c.size(), d.size()+i-f-1));

00 71         T mult = delta/ldelta;
f3 1b         for(int j = 0; j < d.size(); j++)
62 d1             c[j+i-f-1]+=d[j]*mult;

3d c3         if(i+oc.size() > f+maybe.size()){
a5 60             oc = maybe;
62 ab             f = i;
ab a4             ldelta = delta;
17 cb         }
46 cb     }

14 80     return c;

61 cb }

```

### 3.3 BigInt.hpp

```

Hash: 5afbdf
/**

```

```

* from https://github.com/defnotmee/definitely-not-a-lib
*
* Implements arithmetic operations with arbitrary precision integers.
*
*/
d7 d7 #ifndef 0_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

78 45 template<ll B = 10>
51 97 struct Big{
d3 e9     static_assert(B >= 1);

fa 6b     vector<ll> v;
c3 75     bool minus = 0;

cb f3     Big(ll x = 0) {
6d 30         if(x < 0)
2b 4a             minus = 1, x*=-1;
96 f4         while(x){
24 c0             v.push_back(x%B);
6a 57             x/=B;
88 cb         }
20 95         if(v.empty())
73 20             v.push_back(0);
67 cb     }

7b a0     void trim(){
81 0c         while(v.size() > 1 && v.back() == 0)
57 de             v.pop_back();
aa cb     }

a2 3d     Big(string s){
4b 00         static_assert(B <= 10);
65 73         reverse(all(s));
8f 33         if(s.back() == '-')
5d cb             minus = 1, s.pop_back();
8b 72         for(int i = 0; i < s.size(); i++)
d9 cb             v.push_back(s[i]-'0');
11 0e         trim();
c4 cb     }

/**
* Converts an Big Integer from base A to base B
*
* ASSUMES THAT A IS A POWER OF B OR VICE VERSA
*

```



```

    * Useful for speeding up operations (for example,
    * doing multiplication in base 10^9 is 81x faster than
    * base 10)
    */
46 66 template<ll A>
8a d9 Big(Big<A> x){
8b db     minus = x.minus;
bc be     if(A == B){
30 44         v = x.v;
fc 50         return;
78 cb     }
01 7f     if(A < B){
c5 20         v.push_back(0);
f7 01         ll cur = 1;
15 26         for(ll i = 0; i < x.v.size(); i++){
47 85             v.back()+=cur*x.v[i];
7b 72             cur*=A;
1f d3             if(cur == B)
79 33                 cur = 1, v.push_back(0);
5e cb         }
51 0e         trim();
6e 9d     } else {
e8 31         for(int i = 0; i < x.v.size(); i++){
22 01             ll cur = 1;
4c fc             while(cur != A){
95 3d                 v.push_back(x.v[i]%B);
6e 35                 x.v[i]/=B;
23 63                 cur*=B;
89 cb             }
13 cb         }
8c 0e         trim();
cc cb     }
00 cb }

7c cd void extend(int sz){
74 82     if(v.size() < sz)
e7 ea         v.resize(sz);
8d cb }

32 4b Big& operator+=(Big& o){
4b 8f     if(minus == o.minus){
79 c9         extend(o.v.size());
72 73         o.extend(v.size());
c4 20         v.push_back(0);
d2 ae         for(int i = 0; i < o.v.size(); i++){
c0 f2             v[i]+=o.v[i];
0c 82             v[i+1]+=v[i]/B;

```

```

a2 f0             v[i]%B;
8d cb         }
f2 0e         trim();
e1 cb     }
cd 35         return *this;
3c 21     };

c1 7b Big& operator--(Big o){
51 c4     o.minus ^= 1;
ac 64     return *this += o;
c3 cb }

4a bc Big operator+(Big o){
59 59     Big x;
1d 9e     return x+=o;
a8 cb }

95 64 Big operator-(Big o){
b6 59     Big x;
52 45     return x-=o;
0e cb }

9b de Big operator*(Big o) const {
40 6a     Big ret;
42 e1     ret.extend(v.size()+o.v.size());
ad f1     for(int i = 0; i < v.size(); i++){
e4 1e         for(int j = 0; j < o.v.size(); j++){
2a b0             ret.v[i+j]+=v[i]*o.v[j];
b7 84             ret.v[i+j+1]+=ret.v[i+j]/B;
15 02             ret.v[i+j]%B;
5f cb         }
44 cb     }
32 9b     ret.trim();
b4 ed     return ret;
4f cb }

56 fe friend istream& operator>>(istream& in, Big& x){
2e ac     string s;
c5 bd     in >> s;
85 53     x = Big(s);
fa 09     return in;
43 cb }

a2 ce friend ostream& operator<< (ostream& out, Big& x){
ff 03     x.trim();
f6 0d     if(x.minus)
ef 82         out << '-';

```

```

2b 13      for(int i = int(x.v.size())-1; i >= 0; i--){
65 90          out << x.v[i];
01 cb      }
b1 fe      return out;
09 cb      }
5a 21 };

```

### 3.4 Bigmod.hpp

```

Hash: 5902df
/*
from https://github.com/defnotmee/definitely-not-a-lib

Implements modulo operations for big MOD. Important for
number theory stuff.
*/

d7 d7 #ifndef 0_0
cb c8 #include "../utility/template.cpp"
91 f2 #endif

bf 55 inline ull modadd(ull a, ull b, ull m){
2b 47     return min(a+b,a+b-m);
26 cb }

34 8f inline ull modsub(ull a, ull b, ull m){
9f ec     return min(a-b,a-b+m);
94 cb }

// stolen from https://github.com/kth-competitive-programming/kactl/
// blob/main/content/number-theory/ModMulLL.h
// works for a,b,m < 7.2e18
e7 f8 inline ull modmul(ull a, ull b, ull m){
2d 8d     ull ret = a*b - m*ull((long double)(a)*b/m);
af 9d     return min({ret,ret+m,ret-m});
e4 cb }

1f b3 ull inverse(ull a, ull m){
4c 5c     ull x = a, y = m;
85 be     complex<ull> cx = {1,0}, cy = {0,1};

63 f4     while(x){
bf 0e         ull curdiv = y/x;
97 61         y-=curdiv*x;
bc eb         cy-=curdiv*cx;
c0 0e         swap(cx, cy);

```

```

de 9d         swap(x, y);
71 cb     }

2c 50     return min(cy.real()+m, cy.real());
ad cb }

0b 0d ull divmul(ull a, ull b, ull m){
1e a5     return modmul(a,inverse(b,m),m);
d6 cb }

e6 5b ull power(ull in, ull exp, ull m){
34 cc     ull ret = 1;
89 fb     while(exp){
03 87         if(exp&1)
27 a0             ret = modmul(ret,in,m);
17 3d         in = modmul(in,in,m);
30 ef         exp>>=1;
60 cb     }
53 ed     return ret;
59 cb }

```

### 3.5 Binpow.hpp

```

Hash: 984c7c
/*
from https://github.com/defnotmee/definitely-not-a-lib

Does binary exponentation. By default can handle exponents
< 2^63, for more you just edit the constants in the function.
*/

d7 d7 #ifndef 0_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

26 67 template<typename T>
38 0d T power(T cur, ll exp){
aa 7b     T ret = T(1); // works for modint.cpp by default

8d fb     while(exp){
07 87         if(exp&1)
2b 27             ret*=cur;
d7 73         cur*=cur;
c8 ef         exp>>=1;
6f cb     }
fa ed     return ret;

```

```
98 cb }
```

### 3.6 Division.hpp

Hash: 82cbc8

```
/**
 * from https://github.com/defnotmee/definitely-not-a-lib
 *
 * Integer division with ceil and floor that works for
 * potentially negative numbers
 */
```

```
d7 d7 #ifndef O_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif
```

```
3e fd ll div_floor(ll a, ll b){
fd 60     return a/b-(a%b!=0 && (a^b)<0);
2a cb }
27 ab ll div_ceil(ll a, ll b){
a0 61     return a/b+(a%b!=0 && (a^b)>0);
82 cb }
```

### 3.7 ExtendedGcd.hpp

Hash: d571a8

```
/*
from https://github.com/defnotmee/definitely-not-a-lib

based on https://cp-algorithms.com/algebra/extended-euclid-algorithm.
html

Given 2 numbers x, y, returns {gcd(x,y), alpha, beta} such that alpha*x
+ beta*y = gcd(x,y)
*/
```

```
d7 d7 #ifndef O_0
cb c8 #include "../utility/template.cpp"
91 f2 #endif

e4 99 auto gcd_ex(ll x, ll y){
c6 ca     complex<ll> cx = {1,0}, cy = {0,1};

49 f4     while(x){
```

```
73 41         ll curdiv = y/x;
```

```
58 61         y-=curdiv*x;
8d 4e         cy-=cx*curdiv;
```

```
b5 0e         swap(cx, cy);
d2 9d         swap(x,y);
70 cb     }
```

```
88 bf         struct res{ll gcd, alpha, beta};;
5d ed         return res{y,cy.real(),cy.imag()};
d5 cb }
```

### 3.8 FactoringAndPrimalityTest.hpp

Hash: faecfd

```
/*
from https://github.com/defnotmee/definitely-not-a-lib
Implements primality check with miller-rabin in  $O(7\log n)$  and
prime factorization in  $O(n^{1/4})$  with pollard-rho.
Primality checking is [supposedly] deterministic but factoring
is a monte carlo algorithm.
Pollard-rho impl is heavily based on:
https://github.com/kth-competitive-programming/kactl/blob/main/content/
number-theory/Factor.h
*/
```

```
d7 d7 #ifndef O_0
cb c8 #include "../utility/template.cpp"
4f a7 #include "bigmod.hpp"
b1 f2 #endif
```

```
73 87 bool is_prime(ull n){
45 c9     if(n <= 1)
96 d1         return false;
```

```
f2 74     ull ctz = __builtin_ctz(n-1);
e4 70     ull d = n>>ctz;
```

```
ae 0e         auto primes = {2, 3, 5, 13, 19, 73, 193, 407521, 299210837};
// all primes up to 37 is a reasonable option too
0b a7         auto bases = {2, 325, 9375, 28178, 450775, 9780504,
1795265022};
```

```
a7 ce         for(ull p : primes)
98 e7             if(n == p)
```

```

17 6a          return 1;

aa e4  for(ull base : bases){
c2 0c      ull cur = power(base,d,n);
8d 66      if(cur == 1)
4c 5e          continue;
79 2b      for(int i = 0; i < ctz; i++){
03 56          if(cur == n-1)
da 20              goto NEXT;
72 1f          cur = modmul(cur,cur,n);
59 cb      }
02 d1      return false;
fb 8f      NEXT::;
4b cb      }

05 8a      return true;

b5 cb }

02 67 template<typename T>
04 cc void pollard(T n, vector<T>& v){
97 e7     if(n == 1)
bc 50         return;
5e a7     if(is_prime(n)){
de 3b         v.push_back(n);
ba 50         return;
1f cb     }

04 dd     static mt19937_64 rng(RANDOM);
bf dc     uniform_int_distribution<T> rg(0,n-1);
bd fb     T c = rg(rng);
ae 64     T x, y;
f5 e8     x = y = rg(rng);

ea ce     auto next = [&](T x){
9d fd         return modadd(modmul(x,x,n),c,n);
a8 21     };

1e a4     T prod = 2;
41 aa     T g = 1;
e3 8f     while((g = gcd(prod,n)) == 1){
43 ac         for(int i = 0; i < 50; i++){
1d 2a             if(x == y)
da 1f                 x = y = rg(rng), c = rg(rng);
b3 53             x = next(x);
b1 1d             y = next(next(y));
41 80             ll cur = modmul(abs(x-y),prod,n);

```

```

71 69          if(cur)
ac 27              prod = cur;
ec cb          }
41 cb      }

57 36      pollard(g,v);
71 6c      pollard(n/g,v);
91 cb }

d7 67 template<typename T>
b2 4f vector<T> factorize(T n, bool sorted = 0){
c9 5a     vector<T> ret;

80 0e      pollard(n,ret);

db 64      if(sorted)
6c 2f          sort(all(ret));

3b ed      return ret;
fa cb }

```

### 3.9 Fft.hpp

Hash: 40a300

```

/**
 * from https://github.com/defnotmee/definitely-not-a-lib
 *
 * Thanks -is-this-fft- for your blog https://codeforces.com/blog/entry/111371
 *
 * References for implementation:
 *
 * https://cp-algorithms.com/algebra/fft.html
 * http://neerc.ifmo.ru/trains/toulouse/2017/fft2.pdf
 * https://github.com/kth-competitive-programming/kactl/blob/main/content/numerical/FastFourierTransform.h
 */
d7 d7 #ifndef O_0
cb c8 #include"../utility/template.cpp"
91 f2 #endif

74 06 using cdl = complex<long double>;
4f 23 using cd = complex<double>; // if WA, change this to long double
and pray

```

```

17 ec void fft(vector<cd>& v, bool inverse = 0){
8d 3d     int n = v.size();
81 77     int lg = log2(n);

24 8a     static vector<cd> loots;
42 dc     static vector<cd> roots;

1b 27     if(loots.size() < n){
dc cb         loots.resize(n,1);
55 7b         roots.resize(n,1);
03 cb     }

a0 89     for(static int len = 2; len < n; len<=1){
41 d8         cd z = polar(1.01, acos(-1.01)/len);
fc d8         for(int i = len; i < 2*len; i++){
96 00             roots[i] = loots[i] = loots[i/2] * ((i&1) ? z : 1);
61 cb         }
0d cb     }

4c 80     vector<int> rev(n);

1e 6f     for(int i = 1; i < n; i++){
31 56         rev[i] = (rev[i>>1]>>1)+((i&1)<<lg-1);
28 fc         if(rev[i] > i)
ba 60             swap(v[i],v[rev[i]]);
13 cb     }

07 9b     for(int len = 1; len < n; len<=1){
1a 27         for(int block = 0; block < n; block+=2*len){
b4 5d             for(int l = block; l < block+len; l++){
23 c4                 cd cur = roots[l-block+len]*v[l+len];
2b d8                 tie(v[l], v[l+len]) =
63 f6                     make_pair(v[l]+cur, v[l]-cur);
e4 cb             }
82 cb         }
e8 cb     }

8d 1f     if(inverse){
9f 83         reverse(1+all(v));
f3 2d         for(auto& i : v)
9b c4             i/=n;
44 cb     }
b6 cb }

dd f1 vector<ll> convolution(vector<ll>& a, vector<ll>& b){

```

```

90 43     int n = 1;
35 0c     while(n+1 < a.size()+b.size())
af c1         n<<=1;

39 b0     vector<cd> in(n);

c1 43     for(int i = 0; i < a.size(); i++){
a4 0a         in[i].real(a[i]);
a9 c0     for(int i = 0; i < b.size(); i++){
ae f4         in[i].imag(b[i]);

b0 21     fft(in);

f0 4d     vector<cd> newin(n);

cf 60     for(int i = 0; i < n; i++){
86 d6         int opos = (n-i)&(n-1);
b5 2c         newin[i] = (in[opos]+conj(in[i]))
d7 24             *(in[opos]-conj(in[i]))*cd(0, -0.25/n);
de cb     }

a5 1e     fft(newin);

01 8a     vector<ll> ret(a.size()+b.size()-1);
55 2a     for(int i = 0; i < a.size()+b.size()-1; i++){
74 f6         ret[i] = round(newin[i].real());
8f cb     }

9f ed     return ret;

62 cb }

a2 5e vector<cd> convolution(vector<cd> a, vector<cd> b){
42 f7     int rets = a.size()+b.size()-1;
ac 43     int n = 1;
9c 0c     while(n+1 < a.size()+b.size())
bd c1         n<<=1;

81 ca     a.resize(n), b.resize(n);

c1 0f     fft(a), fft(b);

c0 60     for(int i = 0; i < n; i++){
3e db         a[i]*=b[i];
40 cb     }

2e c3     fft(a,1);

```

```

55 68      a.resize(rets);

5f 3f      return a;
36 cb }

bd e3 template<ull M = MOD>
46 b9 vector<ll> convolutionmod(vector<ll>& a, vector<ll>& b){
ab 57      const int len = sqrt(M);
41 43      int n = 1;
3e 0c      while(n+1 < a.size()+b.size())
85 c1          n<<=1;

09 53      vector<cd> ca(n), cb(n);

64 43      for(int i = 0; i < a.size(); i++)
d3 67          ca[i] = cd(a[i]%len, a[i]/len);

57 c0      for(int i = 0; i < b.size(); i++)
4f 61          cb[i] = cd(b[i]%len, b[i]/len);

f0 ec      fft(ca), fft(cb);

25 52      vector<cd> p1(n), p2(n);

5e 60      for(int i = 0; i < n; i++){
39 d6          int opos = (n-i)&(n-1);

                // also inverting for fft inverse
ea b7          p1[i] = (ca[opos]+conj(ca[i]))*cb[opos]*cd(0.5/n);
16 79          p2[i] = (ca[opos]-conj(ca[i]))*cb[opos]*cd(0,-0.5/n);
28 cb      }

3f bb      fft(p1), fft(p2);

88 8a      vector<ll> ret(a.size()+b.size()-1);

29 9c      for(int i = 0; i < ret.size(); i++){
cf df          ll r1 = round(p1[i].real()), i1 = round(p1[i].imag());
0b aa          ll r2 = round(p2[i].real()), i2 = round(p2[i].imag());

4b 0a          ll small = r1%MOD, mid = (i1+r2)%MOD, big = i2%MOD;
01 fd          (ret[i] = small + mid*len + big*len%MOD*len)%=MOD;
38 cb      }

7f ed      return ret;
40 cb }

```

### 3.10 Linearrecurrence.hpp

```

Hash: d73748
/*
from https://github.com/defnotmee/definitely-not-a-lib
*/

d7 d7 #ifndef O_0
99 6d #include "../utility/template.cpp"
a3 97 #include "polynomial.hpp"
6d f2 #endif

1d 67 template<typename T>
c6 08 T get_kth_term(vector<T> s, vector<T> c, ll k){

56 85      Poly<T> charac(c.size()+1);
6a 97      for(int i = 0; i < c.size(); i++)
b2 cc          charac[i] = c[c.size()-i-1]*-1;
5e 5f      charac.p.back() = 1;

7a 95      Poly<T> retp(c.size());
3f f1      retp[0] = 1;
6d 75      Poly<T> mul(c.size());
9c f3      if(c.size() == 1)
a0 17          mul[0] = c[0];
92 7f      else mul[1] = 1;

27 95      while(k){
59 33          if(k&1){
26 13              retp*=mul;
0d ab              retp%=charac;
57 cb          }

5d 64          mul*=mul;
44 d3          mul%=charac;

4c b4          k>>=1;
85 cb      }

c8 ce      T ret = 0;

bd 01      for(int i = 0; i < c.size(); i++){
9b 88          ret+=s[i]*retp[i];
55 cb      }

f6 ed      return ret;
d7 cb }

```

### 3.11 Matrix.hpp

Hash: 48af65

```
/*  
from https://github.com/defnotmee/definitely-not-a-lib
```

```
Implements matrices and linear algebra stuff for them.
```

```
Includes multiplication, addition, solving system of equation,  
finding ranks, etc  
*/
```

```
d7 d7 #ifndef O_0  
cb c8 #include "../utility/template.cpp"  
91 f2 #endif  
  
42 67 template<typename T>  
65 bf struct Matrix{  
  
9f 14     int n, m;  
f9 e2     valarray<valarray<T>> v;  
  
0a 73     Matrix(int _n, int _m, int id = 0) : n(_n), m(_m), v(valarray  
      <T>(m),n) {  
7b 9e         if(id){  
15 af             for(int i = 0; i < min(n,m); i++)  
b9 62                 v[i][i] = 1;  
12 cb         }  
09 cb     }  
  
37 97     valarray<T>& operator[] (int x){  
56 7b         return v[x];  
cc cb     }  
  
35 4e     Matrix transpose(){  
5b bc         Matrix newv(m,n);  
  
cb 83         for(int i = 0; i < n; i++)  
4f a7             for(int j = 0; j < m; j++)  
49 06                 newv[j][i] = (*this)[i][j];  
  
b9 b0         return newv;  
3d cb     }  
  
f6 58     Matrix operator+(Matrix& b){  
a3 50         Matrix ret(*this);
```

```
df 2c         return ret.v+=b.v;  
3a cb     }  
  
db c6     Matrix& operator+=(Matrix& b){  
11 8c         return v += b.v;  
7e cb     }  
  
69 7b     Matrix operator*(Matrix b){  
35 5b         Matrix ret(n, b.m);  
  
64 83         for(int i = 0; i < n; i++)  
b4 a7             for(int j = 0; j < m; j++)  
fa bc                 for(int k = 0; k < b.m; k++)  
0a 66                     ret[i][k] += v[i][j]*b.v[j][k];  
  
4e ed         return ret;  
7a cb     }  
  
b4 80     Matrix& operator*=(Matrix b){  
d7 0a         return *this = *this*b;  
81 cb     }  
  
ec d6     Matrix power(ll exp){  
d2 7b         Matrix in = *this;  
2a 01         Matrix ret(n, n, 1);  
  
e2 fb         while(exp){  
88 87             if(exp&1)  
c3 6c                 ret*=in;  
25 f5                 in*=in;  
23 ef                 exp>>=1;  
98 cb             }  
b4 ed         return ret;  
06 cb     }  
  
/*  
Alters current matrix.  
  
Does gaussian elimination and puts matrix in  
upper echelon form (possibly reduced).  
  
Returns the determinant of the square matrix with side equal  
to the number  
of rows of the original matrix.  
*/  
  
a1 50     T gaussjordanize(int reduced = 0){
```

```

08 f0      T det = T(1);

ae bd      int line = 0;
b1 6f      for(int col = 0; col < m; col++){

57 e7          int pivot = line;
8f 94          while(pivot < n && v[pivot][col] == T(0))
db 05              pivot++;

40 ae          if(pivot >= n)
a3 5e              continue;

15 84          swap(v[line], v[pivot]);

94 b4          if(line != pivot)
43 0f              det *= T(-1);

d7 01          det*=v[line][line];

d6 a6          v[line]/=T(v[line][col]);

20 0e          if(reduced)
fd 6d              for(int i = 0; i < line; i++){
2a 7f                  v[i] -= T(v[i][col])*v[line];
89 cb              }

ee bd          for(int i = line+1; i < n; i++){
e7 7f              v[i] -= T(v[i][col])*v[line];
ab cb          }

de 64          line++;
20 cb      }

c0 41      return det * (line == n);
7a cb  }

/*
When called on any matrix, puts it in reduced row echelon
form and solves the system of equations
it represents. In particular, if called on matrix A, finds a
vector x such that Ax = y

Returns {possible x, number of solutions (2 if there are
infinite solutions)}

In case theres no solution, returns {{},0}
*/

```

```

21 ab      pair<vector<T>,int> solve_system(vector<T> y){

0a 10          Matrix aug(n, m+1);

95 60          for(int i = 0; i < n; i++){
a6 a7              for(int j = 0; j < m; j++){
05 78                  aug[i][j] = v[i][j];
4d 77                  aug[i][m] = y[i];
b1 cb              }

b8 b0          aug.gaussjordanize(1);

b1 18          int solcount = n < m ? 2 : 1;

cb 72          vector<T> x(m);

2a 45          for(int i = n-1; i >= 0; i--){
c7 1e              if(i < m && aug[i][i] == T(0))
10 e5                  solcount = 2;

13 e8              int pivot = 0;
95 ca              while(pivot < m && aug[i][pivot] == T(0))
c8 05                  pivot++;

19 41              if(pivot == m){
b4 ff                  if(aug[i][m] != T(0)){
c6 14                      return {{},0};
08 cb                  }
c0 5e                  continue;
0f cb              }

a3 98          x[pivot] = aug[i][m];

a8 c6          for(int j = pivot+1; j < m; j++){
a6 39              x[pivot]-=x[j]*aug[i][j];
99 cb          }
d6 cb      }

d2 60          for(int i = 0; i < n; i++){
70 a7              for(int j = 0; j < m; j++){
a2 ab                  v[i][j] = aug[i][j];
9c cb              }

5f d8          return {x, solcount};

42 cb      }

```



```

/*
Finds a possible solution for the system of linear equations,
as well as a
basis for the solution. The set of solutions will be a linear
combination of
the basis, added to the initial answer provided.

First return value is the initial solution, and the second is
the basis of the solution.
If there is no solution, both return values will be empty
vectors.
*/
d8 cb pair<vector<T>, vector<vector<T>>> basis_solution(vector<T> y
){
54 af     auto [x0, solcount] = solve_system(y);

09 57     if(solcount == 0){
b0 21         return {};
d3 cb     }

94 e3     vector<int> pivot(n);
73 35     vector<int> pivoted(m);
26 60     for(int i = 0; i < n; i++){
38 10         while(pivot[i] < m && v[i][pivot[i]] == T(0))
3d 8f             pivot[i]++;
b3 9a         if(pivot[i] < m)
5e ed             pivoted[pivot[i]] = 1;
06 cb     }

ba be     vector<vector<T>> basis;
79 dd     for(int i = 0; i < m; i++){
3e e8         if(pivoted[i])
2c 5e             continue;
b8 04         vector<T> cbasis(m);
af e0         cbasis[i] = 1;
37 57         for(int j = 0; j < n; j++){
d9 35             if(pivot[j] != m)
88 8e                 cbasis[pivot[j]] += T(-1)*v[j][i];
61 cb         }
51 90         basis.push_back(cbasis);
a2 cb     }
7b 71     assert(bool(solcount > 1) == bool(basis.size()));

27 8d     return {x0,basis};
6a cb }

/*

```

```

Does not alter current matrix.
Returns {inverse matrix, is current matrix invertable}
*/
pair<Matrix<T>, bool> find_inverse(){
45 3d     int n = v.size();
fc 02     Matrix<T> aug(n, 2*n);

a2 83     for(int i = 0; i < n; i++)
94 f9         for(int j = 0; j < n; j++){
c7 78             aug[i][j] = v[i][j];

34 83     for(int i = 0; i < n; i++)
0c 4c         aug[i][n+i] = 1;

28 90     T det = aug.gaussjordanize(1);

a3 18     Matrix<T> ret(n,n);
78 60     for(int i = 0; i < n; i++){
30 16         ret[i] = valarray<T>(aug[i][slice(n,n,1)]);
a2 cb     }

04 59     return {ret, det != T(0)};
68 cb }

// Returns rank of matrix. Does not alter it.
66 2c int get_rank() const {
a0 09     if(m == 0)
bf bb         return 0;

fe 34     Matrix<T> aux(*this);

25 c9     aux.gaussjordanize();

44 3b     int resp = 0;

b0 83     for(int i = 0; i < n; i++)
b0 9a         resp += (aux[i] != valarray<mint>(m)).sum();

56 68     return resp;
75 cb }

48 21 };

```

### 3.12 MatrixMulMod.hpp

Hash: 378c2d

```

/*
from https://github.com/defnotmee/definitely-not-a-lib

Fast matrix multiplication with modulo. Useful for matrix
exponentiation problems and such.
*/

d7 d7 #ifndef O_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

6b e3 template<ull M = MOD>
a2 cb void mat_mul(matrix<ll> a, matrix<ll> b){
55 50     matrix<ll> ret(a.size(), vector<ll>(b[0].size()));

d1 bb     for(int i = 0; i < a.size(); i++){
be 12         for(int j = 0; j < b[0].size(); j++){
74 9b             int ct = LONG_LONG_MAX/(M*M);
91 58             for(int k = 0; k < b.size(); k++, ct--){
91 34                 ret[i][j] += a[i][k]*b[k][j];
03 1a                 if(ct)
fc 73                     ret[i][j]%=M;
1d cb             }
b7 73             ret[i][j]%=M;
f5 cb         }
c8 cb     }

ab ed     return ret;
37 cb }

```

### 3.13 Modint.hpp

```

Hash: b90b52
/*
from https://github.com/defnotmee/definitely-not-a-lib

Implements integers in Z_MOD.
At all points it is assumed that 0 <= x < MOD and that MOD*MOD + MOD
fits unsigned long long

If you want non-const MOD, use beegmod.cpp

*** If you only want to one value of MOD, check the "mint" alias at the
bottom of the code. ***
*/

```

```

d7 d7 #ifndef O_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

ac 86 template<ull M>
b1 1b struct modint{
34 0e     ull x;

        // It is assumed -M <= v.
ba e7     constexpr modint(ll v = 0) : x(v >= M ? (v+M)%M : v){};

2d c3     bool operator==(const modint& o){
56 d2         return x == o.x;
47 cb     }

        // Example on how to implement operators if youre lazy:
        // modint operator+(modint b){
        //     return x+b.x;
        // }

4a 1c     modint operator+(modint b) const{
16 dc         return min(x+b.x, x+b.x-M);
2b cb     }

00 d7     modint operator-(modint b) const{
de 6b         return min(x-b.x, x-b.x+M);
84 cb     }

c0 ac     modint operator*(modint b) const {
b1 dc         return x*b.x%M;
c0 21     };

a8 2f     modint inverse(){
7d 26         ll x = this->x, y = M;

68 ca         complex<ll> cx = {1,0}, cy = {0,1};

8c f4         while(x){
bd 41             ll curdiv = y/x;
a9 61             y-=curdiv*x;
34 eb             cy-=curdiv*cx;
31 0e             swap(cx, cy);
7b 9d             swap(x, y);
4e cb         }

a3 77         return cy.real();
83 cb     }

```

```

f5 e3      modint operator/(modint b) const {
12 78          return *this*b.inverse();
10 cb      }

d5 34      void operator+=(modint b){
6c 4f          x = min(x+b.x, x+b.x-M);
62 cb      }

41 cc      void operator-=(modint b){
b2 60          x = min(x-b.x, x-b.x+M);
3f cb      }

66 41      void operator*=(modint b){
72 76          (x*=b.x)%=M;
85 cb      }

7c 92      void operator/=(modint b){
74 7d          *this = *this/b;
5d cb      }

bf 66      friend istream& operator>> (istream& in, modint& v){
48 4a          ll x;
6b 14          in >> x;
69 6c          v = modint(x);
a8 09          return in;
bc cb      }

cf e8      friend ostream& operator<< (ostream& out, modint v){
3d d5          return out << v.x;
4f cb      }
4f 21 };

b9 9a using mint = modint<MOD>;

```

### 3.14 Polynomial.hpp

```

Hash: 00f872
/*
from https://github.com/defnotmee/definitely-not-a-lib
*/

d7 d7 #ifndef O_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

```

```

26 67 template<typename T>
c7 21 struct Poly{
59 1a      int n;
0e b8      vector<T> p;

d7 03      Poly(int n) : n(n), p(n){}
a4 0c      Poly(const vector<T>& v) : n(v.size()), p(v){}

bd 8d      T& operator[](int id) {
ab 77          return p[id];
bf cb      }

44 c8      Poly operator+(Poly b) const {
29 f7          Poly ret(max(n, b.n));

0a a8          for(int i = 0; i < ret.n; i++)
f0 10              ret[i] = p[i]+b[i];
e0 ed          return ret;
6c cb      }

75 bd      Poly operator-(Poly b) const {
30 f7          Poly ret(max(n, b.n));

51 a8          for(int i = 0; i < ret.n; i++)
ef 09              ret[i] = p[i]-b[i];
e6 ed          return ret;
c6 cb      }

6e 88      Poly operator*(Poly b) const {
13 3e          Poly ret(n+b.n-1);

9c 83          for(int i = 0; i < n; i++)
ce 11              for(int j = 0; j < b.n; j++)
8f 75                  ret[i+j] += p[i]*b[j];

18 ed          return ret;
c4 cb      }

71 aa      Poly operator*(T b) const {
df 69          Poly ret = *this;
eb 83          for(int i = 0; i < n; i++)
a8 09              ret[i]*=b;
21 ed          return ret;
05 cb      }

0a ca      Poly operator%(Poly b) const {
d1 7a          Poly ret(*this);

```

```

24 36      b*=T(1)/b.p.back();

7b 66      for(int i = n-b.n; i >= 0; i--){
d3 ef          T scale = ret[i+b.n-1];
35 11          for(int j = 0; j < b.n; j++)
19 c9              ret[i+j]-=b[j]*scale;
eb cb      }

8e 66      ret.p.resize(b.n-1);
d3 04      ret.n = b.n-1;

98 ed      return ret;
85 cb      }

d0 e2      void operator%=(Poly b) {
93 7b          (*this) = (*this) % b;
e4 cb      }

f4 21      void operator+=(Poly b){
cd 17          (*this) = (*this) + b;
9e cb      }

a4 11      void operator-=(Poly b){
ff 46          (*this) = (*this) - b;
62 cb      }

62 5b      void operator*=(Poly b){
e2 b3          (*this) = (*this) * b;
fa cb      }

b3 e2      void operator*=(T b){
3e b3          (*this) = (*this) * b;
7e cb      }
00 21 };

```

### 3.15 Sieve.hpp

```

Hash: bfe02d
/*
from https://github.com/defnotmee/definitely-not-a-lib

```

Calculates smallest prime that divides each number for all  $x < n$  and also maintains a list of all primes up to that in  $O(n)$

By default creates a sieve named sieve of size MAXN.

```

*/

d7 d7 #ifndef 0_0
cb c8 #include "../utility/template.cpp"
91 f2 #endif

78 3a struct Sieve{
66 fd      vector<int> primes;
38 89      vector<int> next;

20 8b      Sieve(int n){
84 8c          next = vector<int>(n);

0f 9f          for(int i = 2; i < n; i++){
d3 72              if(!next[i])
22 20                  next[i] = i, primes.push_back(i);

17 7c              for(ll j : primes){
0d a1                  if(j*i >= n)
2b c2                      break;
b8 da                      next[j*i] = j;
e0 4f                      if(j == next[i])
0d c2                          break;
e1 cb                      }
96 cb                  }
a5 cb              }

be 2a      inline bool is_prime(int n){
22 74          return next[n] == n;
55 cb      }

// returns pairs in form {prime, exponent}
// will always return them in ascending order
e0 bb      vector<pii> factorize(int n){
3a a5          vector<pii> ret;

a7 02          while(n != 1){
24 f6              int p = next[n];
ad d9              int ct = 0;
73 bf              while(n%p == 0)
42 31                  ct++, n/=p;
e6 fd              ret.push_back({p,ct});
88 cb          }
65 ed          return ret;
11 cb      }
bf 93 } sieve(1e6+10);

```

## 4 string

### 4.1 AhoCorasik.hpp

```
Hash: 207c79
/*
from https://github.com/defnotmee/definitely-not-a-lib
*/

d7 d7 #ifndef 0_0
ac 30 #include "trie.hpp"
8d 6d #include "../utility/template.cpp"
c4 f2 #endif

2b e8 template<int ALPHA = 26, int INI = 'a'>
2f 83 struct SuperTrie : Trie<ALPHA, INI>{
59 02     vector<int> in_suffix, slink, pai, paic, match;
a1 53     using Trie<ALPHA, INI>::trie;
2e 09     vector<bstring<int>> rslink;

92 1f     SuperTrie(int expected = MAXN) : Trie<ALPHA, INI>(MAXN){}

7b a4     int next(int id, int c){
78 fe         while(id && trie[id].ptr[c] == -1)
b7 3a             id = slink[id];
8c 11             if(trie[id].ptr[c] != -1)
ed 90                 id = trie[id].ptr[c];
a3 64             return id;
63 cb     }

34 a2     void calc_link(){
fb 5a         in_suffix = slink = pai = paic = match = vector<int>(trie
.size());
87 c4         rslink = vector<bstring<int>>(trie.size());
96 26         queue<int> q;

bb 53         q.push(0);

93 14         while(!q.empty()){
03 69             int cur = q.front();
7a 83             q.pop();
12 6b             for(int c = 0; c < ALPHA; c++){
ca f8                 int viz = trie[cur].ptr[c];
92 60                 if(viz == -1)
f6 5e                     continue;
ed aa                 pai[viz] = cur;
```

```
58 71                 paic[viz] = c;
7a 84                 q.push(viz);
e8 cb             }
d0 b3             if(!cur)
97 5e                 continue;

2b bb                 slink[cur] = next(slink[pai[cur]], paic[cur]);
9e 59                 slink[cur] = (slink[cur] != cur)*slink[cur];
ba bd                 rslink[slink[cur]].push_back(cur);

46 c5                 in_suffix[cur] = in_suffix[slink[cur]]+trie[cur].term
;
e2 cb             }
8c cb     }

73 84     void add_str(string& s, int ct = 1){
c5 04         int id = 0;
9b 0a         int sid = 0;

48 d5         while(sid < s.size()){
73 ba             int c = s[sid] - INI;
91 f0             id = next(id, c);
7e b7             match[id] += ct;
d5 be             sid++;
a3 cb         }
d2 cb     }

a6 fb     void calc_match(int id = 0){
e3 67         for(int i : rslink[id]){
4e a7             calc_match(i);
8f b8             match[id] += match[i];
22 cb         }
44 cb     }
20 21 };
```

### 4.2 HashInterval.hpp

```
Hash: 3b59e4
/*
from https://github.com/defnotmee/definitely-not-a-lib
*/

d7 d7 #ifndef 0_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif
```

```

6b e3 template<ull M = MOD>
e8 a2 struct Hasher{
d0 ce     vector<ull> psum, power;

4a 0d     Hasher(string& s, ull c = 123){
7e 77         psum = vector<ull>(s.size()+1);
e0 f5         power = vector<ull>(s.size()+1,1);
ea 63         for(int i = 1; i < power.size(); i++)
26 7c             power[i] = power[i-1]*c%M;
ad 01         for(int i = 1; i < psum.size(); i++)
27 a5             (psum[i] = psum[i-1]*c+s[i-1])%=M;
a6 cb     }

f6 47     ull sub_hash(int l, int r){
66 79         return (psum[r+1]-psum[l]*power[r-l+1]%M+M)%M;
e6 cb     }
84 bf     ull hash(){
3d 08         return psum.back();
0a cb     }
3b 21 };

```

### 4.3 Kmp.hpp

```

Hash: f1429a
/**
 * from https://github.com/defnotmee/definitely-not-a-lib
 *
 * Let pi(s) := size of the biggest proper prefix of s that is
 * also a suffix of s.
 *
 * kmp(s) calculates pi(s[0..i]) for all i from 0 to n-1 in O(n)
 *
 * Useful for multiple applications, for example string matching.
 *
 * Also has a function that finds the automaton corresponding
 * to how the prefix function will change. Formally:
 *
 * kmp_automaton<ALPHA,INI>(s)[p][c-INI] := pi(s+"#"+t+"c") given that
 * pi(s+"#"+t) = p, the alphabet size is ALPHA and the smallest
 * character
 * is INI.
 */
d7 d7 #ifndef 0_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

```

```

26 67 template<typename T>
18 33 vector<int> kmp(const T s){
a5 27     vector<int> pi(s.size());
6b 88     for(int i = 1; i < s.size(); i++){
7c 8d         pi[i] = pi[i-1];
0f e3         while(pi[i] != 0 && s[pi[i]] != s[i]){
10 77             pi[i] = pi[pi[i]-1];
2d cb         }
5f 18         pi[i]+=s[i]==s[pi[i]];
b5 cb     }
a5 81     return pi;
9e cb }

26 e8 template<int ALPHA = 26, int INI = 'a'>
4d 08 vector<array<int,ALPHA>> kmp_automaton(const string s){
0b 6b     vector<int> pi = kmp(s);
ce 5b     vector<array<int,ALPHA>> ret(s.size()+1);

52 ff     ret[0][s[0]-INI] = 1;
a9 88     for(int i = 1; i < s.size(); i++){
24 12         ret[i] = ret[pi[i-1]];
26 b1         ret[i][s[i]-INI] = i+1;
b3 cb     }
05 69     ret.back() = ret[pi.back()];

3e ed     return ret;
f1 cb }

```

### 4.4 Manacher.hpp

```

Hash: 9f4181
/**
 * from https://github.com/defnotmee/definitely-not-a-lib
 */
d7 d7 #ifndef 0_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

1c fc vector<int> manacher(string in){
92 9b     string s = "#";

d3 31     for(char i : in)
2d 94         s+=i + string("#");

fd 16     int n = s.size();

```

```

12 82      vector<int> ret(n);

e4 39      int mid = 0, r = 0;

de a4      for(int i = 1; i < n-1; i++){
da 88          if(i < r)
fc e9              ret[i] = min(r-i, ret[mid*2-i]);

bb 3d          while(ret[i] <= i && i+ret[i] < n && s[i-ret[i]] == s[i+
ret[i]])
55 84              ret[i]++;

06 c6          if(i+ret[i] > r)
cd 59              mid = i, r = i+ret[i];
58 cb      }

c4 6c      return vector<int>(1+all(ret)-1);
9f cb  }

```

## 4.5 MinRot.hpp

```

Hash: 2aac66
/**
 * from https://github.com/defnotmee/definitely-not-a-lib
 *
 * Given a string/vector s, finds all the lexicographically minimum
 * rotations of s in O(nlogn)
 */

d7 d7 #ifndef 0_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

26 67 template<typename T>
fd 14 vector<int> min_rot(T v){
2c 3d     int n = v.size();
09 a9     vector<int> cand;
ce b2     auto mn = *min_element(all(v));
8a 87     for(auto i : v)
87 4c         if(i == mn)
c0 5b         cand.push_back(i);

a2 f9     vector<int> is_cand(n);
78 ea     for(int i : cand)
41 7f         is_cand[i] = 1;

```

```

5a bf     int k = 1;
84 66     while(true){
0b 7a         auto mn = v[(cand[0]+k)%n];

e2 98         for(int i : cand){
17 b6             is_cand[(i+k)%n] = 0;
6b 1b             if(v[(i+k)%n] != mn)
ee 28                 is_cand[i] = 0;
89 cb         }
91 00         vector<int> newcand;

92 ea         for(int i : cand)
66 d4             if(is_cand[i])
05 53                 newcand.push_back(i);

55 75         if(newcand.empty())
31 9c             return cand;

91 06         swap(cand, newcand);

3f ac         k++;
f1 cb     }
2a cb  }

```

## 4.6 SuffixArray.hpp

```

Hash: bcbfc1
/**
 * from https://github.com/defnotmee/definitely-not-a-lib
 */

d7 d7 #ifndef 0_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

13 3f struct SuffixArray{
a6 1a     int n;
8b ac     string s;
d9 74     vector<int> sa, rnk;

03 19     SuffixArray(string& s) : s(s), n(s.size()), sa(n), rnk(n
+1, -1){
95 83         for(int i = 0; i < n; i++)
4e 16             rnk[i] = s[i];

```

```

17 b9      iota(all(sa),0);

24 c3      for(int k = -1; k == -1 || (1<<k) <= n; k++){
be ea          int off = k == -1 ? 0 : (1<<k);

8c 1e          vector<pii> lookup(n);
71 54          vector<int> ct(max(256, n));
17 ee          vector<int> nsa(n);

19 60          for(int i = 0; i < n; i++){
60 30              ct[rnk[i]]++;
d6 6a              lookup[i] = {rnk[i], rnk[min(n,i+off)]};
e0 cb          }

d8 ee          vector<int> ps = ct;

9c ee          for(int i = 1; i < ps.size(); i++)
a9 36              ps[i]+=ps[i-1];

91 ea          auto aux=[&](int id){
45 1e              nsa[ps[rnk[id]] - (ct[rnk[id]]--)] = id;
56 21          };

e9 7c          for(int i = n-off; i < n; i++)
1f 63              aux(i);

ca 83          for(int i = 0; i < n; i++)
3a 52              if(sa[i] >= off)
87 3b                  aux(sa[i]-off);

a9 43          swap(sa,nsa);

6b f3          rnk[sa[0]] = 0;

4d aa          for(int i = 1; i < n; i++)
9d b8              rnk[sa[i]] = rnk[sa[i-1]]+(lookup[sa[i]] !=
lookup[sa[i-1]]);

ec cb          }

61 75          rnk.pop_back();

66 cb      }
69 21 };

bd 6a struct LCP : SuffixArray{

```

```

28 a5      vector<int> lcp;

bf 77      matrix<int> sparse;

8b c0      LCP(string& s) : SuffixArray(s), lcp(n), sparse(int(log2(n)
+1), vector<int>(n)) {

d9 60          for(int i = 0; i < n; i++){
96 27              int& clcp = lcp[rnk[i]];
39 15              if(rnk[i]+1 == n){
33 11                  clcp = 0;
e4 5e                  continue;
fc cb              }
46 a7              int nxt = sa[rnk[i]+1];

68 59              while(i+clcp < n && nxt+clcp < n && s[i+clcp] == s[
nxt+clcp]){
f4 9c                  clcp++;
bc cb              }

f2 9a              if(i+1 < n)
6d 2a                  lcp[rnk[i+1]] = max(0,clcp-1);
7d cb              }

c0 2d          sparse[0] = lcp;

88 61          for(int i = 1; i < sparse.size(); i++){
df 8b              for(int j = 0; j + (1<<i) <= n; j++){
92 61                  sparse[i][j] = min(sparse[i-1][j], sparse[i-1][j
+(1<<i-1)]);
81 cb              }
49 cb          }
9a cb      }

// returns the lcp between s[sa[l]..n] and s[sa[r]..n]
5c 9e      int get_lcp_sa(int l, int r){
3b c2          if(l > r)
eb e4              swap(l,r);
46 61          r--;
06 1e          int logg = log2(r-l+1);
42 d3          return min(sparse[logg][l], sparse[logg][r-(1<<logg)+1]);
6e cb      }

// returns lcp between s[l..n] and s[r..n]
ed f9      int get_lcp(int l, int r){
42 29          return get_lcp_sa(rnk[l], rnk[r]);
ff cb      }

```



```

c6 e6      void debug(){
4e 1c      for(int i = 0; i < s.size(); i++){
cb 68          cerr << i << ": " << "sa[i] = " << sa[i] << ", suffix
    = " << s.substr(sa[i]) << ", lcp = " << lcp[i] << '\n';
75 cb      }
af cb      }
bc 21 };

```

## 4.7 SuffixAutomaton.hpp

```

Hash: c79348
/**
 * from https://github.com/defnotmee/definitely-not-a-lib
 */
d7 d7 #ifndef O_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

92 e8 template<int ALPHA = 26, int INI = 'a'>
e6 92 struct SuffixAutomaton {
02 2d     struct state{
b4 01         int len, firstpos, link = -1, is_clone = 0;
4c be         array<int, ALPHA> ptr;

8b fc         state(int len = 0, int firstpos = -1)
1d ae             : len(len), firstpos(firstpos){
36 b0                 fill(all(ptr), -1);
2d cb             }
47 21     };

fa 76     vector<state> sa;
10 5c     int last = 0;
3b d9     int ct = 0;
c3 a1     SuffixAutomaton(){
4f 97         sa = {{}};
29 cb     }

fb 62     void extend(int c){
5c a6         c-=INI;
25 d9         int nxt = sa.size();
89 c0         sa.push_back({sa[last].len+1, ct++});

cf 94         int pivot = last;

11 3b         while(pivot != -1 && sa[pivot].ptr[c] == -1)

```

```

14 78             sa[pivot].ptr[c] = nxt, pivot = sa[pivot].link;

4c b9         if(pivot == -1){
7d da             sa[nxt].link = 0;
bd 9d         } else {
49 52             int tmp = sa[nxt].link = sa[pivot].ptr[c];
e4 7f             if(sa[tmp].len != sa[pivot].len+1){
ab f7                 int nlink = sa[nxt].link = sa.size();
ad 0b                 sa.push_back(sa[tmp]);
1d d9                 sa.back().len = sa[pivot].len+1;
3b a3                 sa.back().is_clone = 1;
0c 82                 int tmp = sa[pivot].ptr[c];
c8 58                 sa[tmp].link = nlink;

a5 9d                 while(pivot != -1 && sa[pivot].ptr[c] == tmp){
83 2d                     sa[pivot].ptr[c] = nlink;
25 33                     pivot = sa[pivot].link;
34 cb                 }
42 cb             }
32 cb         }
f0 a7         last = nxt;
fa cb     }

be 84     SuffixAutomaton(string s){
d7 97         sa = {{}};
f2 3b         sa.reserve(2*s.size());
0a 29         for(char i : s)
6f 89             extend(i);

30 cb     }

7c a4     bool accept(string s){
53 04         int id = 0;

33 54         for(char i : s){
30 b8             id = sa[id].ptr[i-INI];
06 a5             if(id == -1)
4a bb                 return 0;
38 cb         }
3a 6a         return 1;
37 cb     }

b7 30     vector<int> get_ct(){
52 8f         vector<int> ct(sa.size());
55 88         vector<bstring<int>> rslink(sa.size());

3e b5         for(int i = 1; i < sa.size(); i++){

```

```

90 50      rslink[sa[i].link].push_back(i);
4c cb      }

d7 82      auto dfs = [&](int id, auto && dfs) -> void {
db 50          ct[id] = !sa[id].is_clone;

82 4d          for(int i : rslink[id])
29 49              dfs(i,dfs), ct[id]+=ct[i];
81 21      };

04 c2      dfs(0,dfs);

55 b6      return ct;
98 cb      }

c1 81      state& operator[](int id){
ea 39          return sa[id];
a7 cb      }

9f 28      int size(){
a1 bd          return sa.size();
ad cb      }
c7 21 };

```

## 4.8 Trie.hpp

```

Hash: 136607
/*
from https://github.com/defnotmee/definitely-not-a-lib
*/

d7 d7 #ifndef 0_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

92 e8 template<int ALPHA = 26, int INI = 'a'>
19 71 struct Trie {
1a 67     public:
b6 3c     struct node{
39 be         array<int,ALPHA> ptr;
50 f7         int term; // number of strings that terminate on the node
9b bf         int sub;  // number of strings in the subtree of the node

62 a7         constexpr node() : term(0), sub(0){
44 b5             for(int i = 0; i < ALPHA; i++){
f8 99                 ptr[i] = -1;

```

```

a5 cb      }
74 21      };
6d 95      vector<node> trie;

b5 99      Trie(int expected = MAXN) : trie(1) {
41 48          trie.reserve(expected);
cb cb      }

38 cd      void insert(const string& s, int ct = 1){
e2 04          int id = 0;
30 be          int pos = 0;
ff 51          while(pos < s.size()){
3d 72              char cur = s[pos]-INI;
53 42              if(trie[id].ptr[cur] == -1)
09 a3                  trie[id].ptr[cur] = trie.size(), trie.push_back
                    ({});
6e c2                  trie[id].sub+=ct;
97 8a                  id = trie[id].ptr[cur];
31 65                  pos++;
f6 cb          }
1c c2          trie[id].sub += ct;
18 9a          trie[id].term += ct;
2f cb      }

99 e4      int find(const string& s){
09 43          int id = 0, pos = 0;
d5 51          while(pos < s.size()){
60 72              char cur = s[pos]-INI;
3a 42              if(trie[id].ptr[cur] == -1)
c0 da                  return -1;
b1 8a                  id = trie[id].ptr[cur];
e4 65                  pos++;
1d cb          }
7a 64          return id;
6d cb      }
13 21 };

```

## 4.9 ZFunction.hpp

```

Hash: d2a27d
/**
 * from https://github.com/defnotmee/definitely-not-a-lib
 */
d7 d7 #ifndef 0_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

```

```

3a ba vector<int> z_function(auto s){
00 16     int n = s.size();
69 fa     int l = 0, r = 0;
fd 2e     vector<int> z(n);
a3 6f     for(int i = 1; i < n; i++){
76 88         if(i < r)
88 14             z[i] = min(r-i, z[i-l]);
a2 81         while(i + z[i] < n && s[i+z[i]] == s[z[i]])
5a 9f             z[i]++;
4b fe         if(i+z[i] > r)
d0 a1             l = i, r = i+z[i];
fd cb     }
58 07     return z;
d2 cb }

```

## 5 geometry

### 5.1 Point.hpp

```

Hash: df8967
/*
from https://github.com/defnotmee/definitely-not-a-lib
*/

```

```

d7 d7 #ifndef 0_0
77 12 #include "template.cpp"
9d f2 #endif

```

```

3a 14 template<typename T = ll>
c9 be struct point{
96 64     T x, y;

```

```

20 ab     inline point operator+(point b){
75 4f         return {x+b.x, y+b.y};
34 cb     }

```

```

c1 5d     inline point operator-(point b){
cb 53         return {x-b.x, y-b.y};
d9 cb     }

```

```

e9 92     inline point operator*(T scale){
02 1a         return {x*scale, y*scale};
81 cb     }

```

```

57 92     inline T cross(point b){
44 a9         return x*b.y-b.x*y;
67 cb     }

```

```

47 27     inline T dot(point b){
f3 e0         return x*b.x + y*b.y;
75 cb     }

```

```

a8 fd     inline T dist2(){
cd 2b         return x*x+y*y;
e0 cb     }

```

```

2b fe     inline double dist(){
0a d4         return sqrt(dist2());
cc cb     }
df 21 };

```

## 6 graph

### 6.1 2sat.hpp

```

Hash: 0f603e
/*
from https://github.com/defnotmee/definitely-not-a-lib
*/

```

```

d7 d7 #ifndef 0_0
99 6d #include "../utility/template.cpp"
df 3e #include "scc.hpp"
2f f2 #endif

```

```

19 d9 struct TwoSat{
29 1a     int n;
f6 3c     SCC scc;

```

```

61 e2     TwoSat(int n = 0) : n(n), scc(2*n){}

```

```

7f b1     static constexpr int no(int x){
7a 61         return 2*x;
d4 cb     }

```

```

68 50     static constexpr int yes(int x){
0d 46         return 2*x+1;
e0 cb     }

```

```

c9 b5 void add_or(int a, int b){
dd 56     scc.add_edge(a^1, b);
6f 18     scc.add_edge(b^1, a);
7b cb }

f3 d9 void add_xor(int a, int b){
3a 23     add_or(a,b);
56 77     add_or(a^1,b^1);
3c cb }

// If impossible, returns an empty vector
// If possible, returns a possible construction where
// ret[i] = 1 <=> i is true
2a 6e vector<int> get_sat(){
0b 41     scc.kosaraju();
08 82     vector<int> ret(n);

12 60     for(int i = 0; i < n; i++){
95 32         if(scc.scc[no(i)] == scc.scc[yes(i)])
53 21             return {};
16 60         ret[i] = scc.scc[no(i)] < scc.scc[yes(i)];
22 cb     }

1d ed     return ret;
d1 cb }

0f 21 };

```

## 6.2 BinaryLift.hpp

Hash: 017f86  
 /\*  
 from <https://github.com/defnotmee/definitely-not-a-lib>

Given an array of ancestors (par), is able to get information about starting on a certain node and going to the ancestor of the current node k steps in a row in  $O(\log(k))$  per query. Is able to work with any functional graph, but the lca function just works for trees.

Usage:

- BinLift(par): constructs the structure. par is assumed to be 0-indexed

```

- lift: an auxiliary class that stores information about the path (for
  example
  what is the maximum edge on the path). By default only stores the
  vertex you will end
  up in after going up a certain number of times.
- k_up(id,k): returns a lift structure of starting on id and going to
  the ancestor
  k times in a row.
- lca(a,b,h): assuming the functional graph given is a tree, if h is a
  vector representing
  the height of the nodes in a tree, returns the lift structure of the
  path between a and b.
The .to member of the return value will be the lca between a and b. If
you are storing more
information about the path, it needs to be commutative (for example,
you can store max).
*/

d7 d7 #ifndef 0_0
cb c8 #include "../utility/template.cpp"
91 f2 #endif

5f 6b struct lift{
18 70     int to = 0;
44 aa     int mn = 1e9; // Example of path aggregate, must be identity
  value through merge
bd 21 };

e1 71 struct BinLift{

5c 8b     int n, lg;

// what happens when you go through a, and then go through b?
6f 4e     static lift merge(lift a, lift b){
bb 97         return {b.to, min(a.mn, b.mn)};
f6 cb     }

b0 50     matrix<lift> jmp;

c9 be     BinLift(vector<lift> par) : n(par.size()), lg(log2(n)+1){
7f 38         jmp = matrix<lift>(lg,par);

60 82         for(int i = 1; i < lg; i++){
a1 27             for(int j = 0; j < par.size(); j++){
55 52                 jmp[i][j] = merge(jmp[i-1][j], jmp[i-1][jmp[i-1][
j].to]);
d6 cb             }

```

```

d0 cb      }
7c cb      }

80 fe      lift k_up(int id, int k){
9d 51      lift ret{id}; // needs to be an identity element through
merge
ca 95      while(k){
1c 3e      ret = merge(ret, jmp[__builtin_ctz(k)][ret.to]);
f6 ab      k-=k&-k;
73 cb      }
9a ed      return ret;
98 cb      }

58 b2      lift lca(int a, int b, vector<int>& h){
03 be      if(h[a] < h[b])
c8 25      swap(a,b);

28 fe      int d = h[a]-h[b];
4a 91      lift la = k_up(a,d), lb = {b}; // needs to be an identity
element through merge

b0 97      if(la.to == lb.to)
60 c9      return la;

77 35      for(int i = lg-1; i >= 0; i--){
12 7e      if(jmp[i][la.to].to != jmp[i][lb.to].to)
82 4c      la = merge(la, jmp[i][la.to]), lb = merge(lb, jmp[i
][lb.to]);
03 cb      }

c1 d4      la = merge(la, jmp[0][la.to]);
af 04      lb = merge(lb, jmp[0][lb.to]);

fd 91      return merge(la,lb);
a8 cb      }

01 21 };

```

### 6.3 BipartiteMatching.hpp

```

Hash: 915763
/*
from https://github.com/defnotmee/definitely-not-a-lib

```

Uses hopcroft-karp's algorithm to find the maximum matching on a

```

bipartite graph. Runs in time  $O(E \cdot \sqrt{V})$  on worst case, and time
 $O(E \cdot \log(V))$  on random graphs.

Depending on the application, the dinic.hpp interface may be more
convenient.
*/

d7 d7 #ifndef O_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

86 53 struct BiGraph{ // bipartite graph of sizes n and m

83 14      int n, m;
fc 3b      vector<basic_string<int>> g;
0f d3      vector<int> matched, match;

4e b3      BiGraph(int _n, int _m) : n(_n), m(_m), g(n), matched(n),
match(m, -1){

42 01      void add_edge(int a, int b){
02 02          g[a].push_back(b);
10 cb      }

00 0b      vector<pii> max_matching(){

17 4b          while(augment());

03 14          vector<pii> resp;
af 94          for(int i = 0; i < m; i++){
13 e3              if(match[i] != -1)
ca 76                  resp.push_back({match[i], i});

56 68          return resp;
52 cb      }

ac bf      private:
2a cb      bool augment(){
b5 ee          vector<int> dist(n, -1);

9c 26          queue<int> q;
d6 60          for(int i = 0; i < n; i++){
b8 89              if(!matched[i])
14 4b                  q.push(i), dist[i] = 0;
2b cb          }

19 28          bool fail = 1;

```

```

44 9d         while(!q.empty() && fail){
2a 69             int cur = q.front();
c1 83             q.pop();
85 95             for(int i : g[cur]){
4c 56                 if(match[i] == -1){
72 1e                     fail = 0;
83 c2                     break;
78 cb                 }
7f 56                 if(dist[match[i]] == -1){
5c 65                     dist[match[i]] = dist[cur]+1;
25 c5                     q.push(match[i]);
57 cb                 }
d1 cb             }
71 cb         }

88 59         if(fail)
5d d1             return false;

78 f9         vector<int> check(n);

9f 44         auto dfs = [&](int id, auto && dfs) -> bool {
5e e8             check[id] = 1;
4b a6             for(int i : g[id]){
8d 97                 int& mi = match[i];
15 98                 if(mi == -1 ||
8b bf                 (!check[mi] && dist[mi] == dist[id]+1 && dfs(mi,
dfs))){
47 90                     mi = id;
fa c5                     matched[id] = 1;
4a 8a                     return true;
8b cb                 }
81 cb             }
76 d1             return false;
45 21         };

8a 60         for(int i = 0; i < n; i++){
ed 3a             if(!check[i] && !matched[i])
c3 e6                 dfs(i,dfs);
a1 cb         }

d0 8a         return true;
c5 cb     }

91 21 };

```

## 6.4 Dinic.hpp

Hash: e411bf

```

/**
 * from https://github.com/defnotmee/definitely-not-a-lib
 * Based on https://github.com/kth-competitive-programming/kactl/blob/
 * main/content/graph/Dinic.h
 *
 * Uses Dinic's algorithm to find maximum flow between two vertices.
 *
 *  $O(VE \log(U))$ , where  $U$  is max capacity. Faster in practice. On unit
 * networks
 * (graphs where capacities not connected to source or sink are 1),
 * complexity
 * improves to  $O(\sqrt{V}E)$ .
 *
 * After calling max_flow, the corresponding flow on edges is
 * recoverable
 * with Edge::flow() and left_of_mincut becomes well defined.
 */
d7 d7 #ifndef O_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

27 14 struct Dinic{
d6 e9     struct Edge{
8c e4         ll to, cap, ocap, rev;
93 c2         ll flow(){
eb f2             return max(ocap-cap, 0ll);
bf cb         }
c6 21     };

af ed     vector<vector<Edge>> g;

31 80     void add_edge(int u, int v, ll cap){
1d 60         g[u].push_back({v, cap, cap, (ll)g[v].size()});
f2 ee         g[v].push_back({u, 0, 0, (ll)g[u].size()-1});
4f cb     }

    // Returns if v is in the same side of the min_cut as s
88 4b     bool left_of_mincut(int v){
59 96         return dist[v] != -1;
da cb     }

8c ff     ll max_flow(int s, int t){
91 7a         ll flow = 0;

```

```

e4 98         for(int k = 30; k >= 0; k--)
12 ed             while(bfs(s,t,k)) while (ll it = dfs(s,t,LLONG_MAX))
            flow += it;
d5 99         return flow;
dd cb     }

89 2a     Dinic(int n) : g(n), ptr(n), dist(n){

16 bf     private:
3c c7     vector<int> ptr, dist;

eb 03     ll dfs(int id, int t, ll x){
75 f1         if(id == t || !x)
f0 ea             return x;

28 75         for(int & i = ptr[id]; i < g[id].size(); i++){
c5 28             Edge& e = g[id][i];
f4 6c             if(dist[e.to] != dist[id]+1)
a0 5e                 continue;
54 b4             if(!filled = dfs(e.to, t, min(x, e.cap))){
38 06                 e.cap-=filled;
be 8c                 g[e.to][e.rev].cap+=filled;
91 2e                 return filled;
63 cb             }
78 cb         }

13 bb         return 0;
95 cb     }

65 c1     bool bfs(int s, int t, int k){
2f 4c         fill(all(ptr),0), fill(all(dist),-1);
33 ef         vector<int> q({s});
c8 66         q.reserve(g.size());
a4 a9         dist[s] = 0;
47 2a         for(int i = 0; i < q.size(); i++){
80 5a             int id = q[i];
95 37             for(auto i : g[id]){
33 5f                 if(dist[i.to] == -1 && (i.cap>>k)){
78 11                     dist[i.to] = dist[id]+1;
37 e0                     q.push_back(i.to);
a6 cb                 }
db cb             }
de cb         }
56 69         return dist[t]+1;
64 cb     }
e4 21 };

```

## 6.5 DsuRollback.hpp

```

Hash: 084442
/*
from https://github.com/defnotmee/definitely-not-a-lib
*/

d7 d7 #ifndef 0_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

47 d8 struct DSU_Rollback{
a8 61     struct log{
59 4b         int node1, node2;
9e a3         int prev1, prev2;
5b 21     };
97 bf     private:
f8 99     vector<int> v; // Either parent (if v[i] >= 0) or size (if v[
i] < 0 and i is a root) of the component
17 2f     vector<log> history;
f7 67     public:
b3 2a     int comp_ct;

0f 37     DSU_Rollback(int n = 0) : v(n,-1), comp_ct(n){}

a1 a6     constexpr int size(int id){ // returns size of the component
id belongs to
76 93         return -v[find(id)];
24 cb     }

f6 96     constexpr int pai(int id){ // Returns parent of id
ff 0c         return v[id] < 0 ? id : v[id];
9f cb     }

67 13     int find(int id){ // removing path compression
fa a4         return v[id] < 0 ? id : find(v[id]);
c9 cb     }

fb c8     bool union(int a, int b){
04 bc         a = find(a);
8e b8         b = find(b);

1d ae         if(a == b)
c8 bb             return 0;

22 ad         if(size(a) > size(b)) // union by size

```

```

a0 25          swap(a,b);

1f 4c          comp_ct--;
69 69          history.push_back({a,b,v[a],v[b]});
93 72          v[b] += v[a];
e9 4c          v[a] = b;
42 6a          return 1;
14 cb      }

05 5c      void rollback(){
78 d5          auto [a,b,va,vb] = history.back();
67 8b          v[a] = va;
fd 99          v[b] = vb;
d2 2c          comp_ct++;
e5 7d          history.pop_back();
58 cb      }

60 3d      bool same(int a, int b){
5e c0          return find(a) == find(b);
5e cb      }

95 cd      constexpr int snapshot(){
0a 53          return history.size();
9e cb      }

08 21 };

```

## 6.6 DynamicConnectivity.hpp

```

Hash: d1c2a4
/*
from https://github.com/defnotmee/definitely-not-a-lib

Offline Dynamic Connectivity in  $O(n \log^2(n))$ . Allows for duplicate
edges.
If an edge that doesn't exist is deleted, it is just ignored.

By default answers how many connected components were in the graph at
a given point.
*/

d7 d7 #ifndef O_0
99 6d #include "../utility/template.cpp"
ea 4c #include "dsu_rollback.hpp"
09 f2 #endif

```

```

a4 fd struct Dynamic_Connectivity{
04 1a      int n;
d7 13      DSU_Rollback uf;
c8 e1      vector<pii> edges;
e2 1d      vector<int> ponta;
2c ce      map<pii, basic_string<int>> st;

4f 3d      Dynamic_Connectivity(int n = 0, int expected = 0) : n(n), uf(
n){
64 c7          ponta.reserve(expected);
7f 81          edges.reserve(expected);
b8 cb      }

86 01      void add_edge(int a, int b){
4e f7          if(a > b)
b6 25              swap(a,b);
06 1e          st[{a,b}].push_back(edges.size());
f2 9b          edges.push_back({a,b});
18 e8          ponta.push_back(-2);
02 cb      }

ac 05      void rem_edge(int a, int b){
7e f7          if(a > b)
f0 25              swap(a,b);
3c 1f          if(st[{a,b}].empty()) // removing edge that is not there
e8 50              return;
00 62          int removed = st[{a,b}].back();
99 7d          st[{a,b}].pop_back();

33 87          ponta[removed] = edges.size();
aa b0          ponta.push_back(removed);
7a 9b          edges.push_back({a,b});
3d cb      }

0e e3      void add_query(){
d7 40          edges.push_back({-1,-1});
22 a4          ponta.push_back(-1);
65 cb      }

0a 9c      vector<int> solve(){
20 1e          for(int& i : ponta)
c8 28              if(i == -2) i = ponta.size();

16 07          vector<int> resp;

44 54          solve(0, int(ponta.size())-1,resp);

```



```

8e 68     return resp;
10 cb     }

51 bf     private:

a8 cb     void solve(int l, int r, vector<int>& resp){

05 89         if(l == r){
a4 93             if(ponta[l] == -1){
21 10                 resp.push_back(uf.comp_ct);
b3 cb             }
c3 50             return;
e7 cb         }

3d 77         int version = uf.snapshot();

0f 27         int m = (l+r)>>1;

e0 11         for(int i = m+1; i <= r; i++){
01 27             if(ponta[i] < l){
32 78                 uf.onion(edges[i].ff, edges[i].ss);
ef cb             }
20 cb         }

38 de         solve(l,m,resp);

b8 ea         while(uf.snapshot() != version)
95 c1             uf.rollback();

b7 e9         for(int i = l; i <= m; i++){
87 3d             if(ponta[i] > r){
23 78                 uf.onion(edges[i].ff, edges[i].ss);
e5 cb             }
25 cb         }

a1 12         solve(m+1,r,resp);

d1 ea         while(uf.snapshot() != version)
aa c1             uf.rollback();
a4 cb     }
d1 21 };

```

## 6.7 EdgeColoring.hpp

Hash: 603344

```

/**
 * from https://github.com/defnotmee/definitely-not-a-lib
 *
 * Copied from https://github.com/koosaga/olympiad/blob/master/Library/
 * codes/graph/edgecolor_bipartite.cpp
 *
 * I have no idea how to use this, but why not put it here.
 *
 * O(nm)
 */
d7 d7 #ifndef O_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

47 69 const int MAXM = 1000;

4f 53 struct edge_color{ // must use 1-based
03 fb     int deg[2][MAXN];
15 ae     pii has[2][MAXN][MAXN];
7b de     int color[MAXN];
ae 95     int c[2];
8c c4     void clear(int n){
a9 2e         for(int t=0; t<2; t++){
3d cc             for(int i=0; i<=n; i++){
ac c0                 deg[t][i] = 0;
34 fe                 for(int j=0; j<=n; j++){
c5 55                     has[t][i][j] = pii(0, 0);
d0 cb                 }
3e cb             }
d3 cb         }
ea cb     }

d6 82     void dfs(int x, int p) {
5d e7         auto i = has[p][x][c[!p]];
46 6f         if (has[!p][i.first][c[p]].second) dfs(i.first,!p);
d6 8d         else has[!p][i.first][c[!p]] = pii(0,0);
4d 8f         has[p][x][c[p]] = i;
9b 22         has[!p][i.first][c[p]] = pii(x,i.second);
1a bd         color[i.second] = c[p];
3e cb     }

87 85     int solve(vector<pii> v, vector<int> &cv){
4e ef         int m = v.size();
5d 1a         int ans = 0;
bc c2         for (int i=1;i<=m;i++) {
fe 99             int x[2];
65 72             x[0] = v[i-1].first;
36 05             x[1] = v[i-1].second;
1e ec             for (int d=0;d<2;d++) {

```

```

e3 cf          deg[d][x[d]]+=1;
cb 08          ans = max(ans,deg[d][x[d]]);
c2 4b          for (c[d]=1;has[d][x[d]][c[d]].second;c[d]++);
a3 cb          }
c7 d9          if (c[0]!=c[1]) dfs(x[1],1);
47 f7          for (int d=0;d<2;d++) has[d][x[d]][c[0]] = pii(x[!d],i)
;
3e 16          color[i] = c[0];
d2 cb          }
ef f5          cv.resize(m);
e8 c2          for(int i=1; i<=m; i++){
4d a0          cv[i-1] = color[i];
c6 bb          color[i] = 0;
7a cb          }
3f ba          return ans;
49 cb      }
60 b8 }EC;

```

## 6.8 FunctionalGraph.hpp

Hash: ab49e6

```

/*
from https://github.com/defnotmee/definitely-not-a-lib

```

Constructs a functional graph. Is able to answer distance directed distance queries in  $O(1)$ .

For each vertex stores the following information

- pai[v]: parent of a vertex
- height[v]: ammount of steps necessary to reach a vertex on a cycle
- cycleid[v]: which cycle v ends up in. If cycleid[v] != cycleid[u], they are on different components
- cyclepos[v]: index of the first vertex from the cycle that v touches on clist[cycleid[v]]
- tin[v]: preorder of v on its corresponding tree (rooted on clist[cycleid[v]][cyclepos[v]])
- tout[v]: preorder of v on its corresponding tree (rooted on clist[cycleid[v]][cyclepos[v]])

In addition, for each cycle, stores a list of the vertices in the cycle on clist[v]

All of this is  $O(n)$  preprocessing.

```

*/

```

```

d7 d7 #ifndef 0_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

a1 7c struct FuncGraph{
73 1a     int n;
8b f8     vector<int> pai, height, cycleid, cyclepos, is_cycle, tin,
tout;
b6 0f     vector<basic_string<int>> rev, clist;

dc f6     FuncGraph(vector<int> v) : n(v.size()), pai(v), height(n),
f3 5a     rev(n), cycleid(n,-1), cyclepos(n), clist(n), is_cycle(n),
tin(n), tout(n){
be 83         for(int i = 0; i < n; i++)
d2 3a             rev[pai[i]].push_back(i);

8e 60         for(int i = 0; i < n; i++){
70 f4             if(cycleid[i] == -1)
34 bc                 get_cycle(i);
ef cb             }
88 cb         }

c4 d0     void get_cycle(int id){
b0 5b         int a = id, b = id;

ad 01         do{
b6 5a             a = pai[a];
9f 57             b = pai[pai[b]];
d6 54         } while(a != b);

06 5f         process_cycle(a);
01 cb     }

30 97     void process_cycle(int id){
f5 e9         int cid = cycleid[id] = id;

ad 02         int v = id;
8a 01         do{
f2 b5             cyclepos[v] = clist[cid].size();
62 89             clist[cid].push_back(v);
2b 15             is_cycle[v] = 1;
a2 90             v = pai[v];
20 5a             cycleid[v] = cid;
d9 81         } while(v != id);

```

```

85 01         do{
24 6b             dfs(v);
13 90             v = pai[v];
2b 81         } while(v != id);

d0 cb     }

93 26     void dfs(int id){
30 36         tout[id] = tin[id];
89 c6         for(int i : rev[id]){
13 75             if(cycleid[i] == -1){
dd 24                 cycleid[i] = cycleid[id];
74 68                 cyclepos[i] = cyclepos[id];
cc db                 height[i] = height[id]+1;
21 7b                 tin[i] = ++tout[id];
2b 1e                 dfs(i);
d2 e6                 tout[id] = tout[i];
99 cb             }
b1 cb         }
18 cb     }

// returns directed distance from a to b, or INF if its not
// possible to go from a to b
78 b5     int dist(int a, int b){
cd f4         if(cycleid[a] != cycleid[b])
16 cd             return INF;
2b 5f         if(is_cycle[a] && !is_cycle[b])
8f cd             return INF;
bf e7         if(!is_cycle[a] && !is_cycle[b]){
45 e4             if(height[a] < height[b] || cyclepos[a] != cyclepos[b]
])
f4 cd                 return INF;
aa 17             if(tin[b] <= tin[a] && tin[a] <= tout[b]){
96 91                 return height[a]-height[b];
60 cb             }
c9 cd             return INF;
fd cb         }

8f 53         return height[a]+dist_in_cycle(cyclepos[a], cyclepos[b],
clist[cycleid[a]].size());
6b cb     }

0e bf     private:

da 9b     int dist_in_cycle(int a, int b, int csize){
d9 7e         if(b >= a)
09 49             return b-a;

```

```

7f 03         return csize+b-a;
59 cb     }

ab 21 };

```

## 6.9 Hld.hpp

Hash: 02a01c

/\*

from <https://github.com/defnotmee/definitely-not-a-lib>

Heavy-Light Decomposition. Does path queries in  $O(\log^2(n))$ .

Requires a SegTree.

\*/

```

d7 d7 #ifndef 0_0
cb c8 #include "../utility/template.cpp"
f8 1f #include "../data_structures/segtree_lazy.hpp"
a3 f2 #endif

13 40 struct HLD {
3f bf     private:
11 bd         int n, root;
df ae         vector<int> tin, tout, sub, pai, height;
0e 3b         vector<basic_string<int>> g;
3b cb         int m = 0;
7f e0         SegTree st;
5f 31         vector<int> head;
75 82         using lazy = SegTree::lazy;
01 e9         using seg = SegTree::seg;

c8 67     public:
b5 d3         HLD(int n, int root = 0) : n(n), root(root), g(n),
af bb             tin(n), tout(n), sub(n,1), pai(n), height(n),
12 f7             st(n), head(n) {}

89 01     void add_edge(int a, int b){
91 02         g[a].push_back(b);
fb 3e         g[b].push_back(a);
bc 7b         m++;
a7 cb     }

58 11     void calc_tree(){
0e 9b         assert(m == n-1);
a9 00         prec(root);
8d 7d         hld(root,root);

```

```

9c cb    }

fc 76    void calc_tree(vector<seg>& v){
de 6e        calc_tree();
41 26        vector<seg> v2(n);
8f 83        for(int i = 0; i < n; i++)
94 16            v2[tin[i]] = v[i];
b4 c9        st = SegTree(v2);
ce cb    }

c6 7b    int lca(int a, int b){
5f 2d        while(head[a] != head[b]){
e3 06            if(tin[a] < tin[b])
6d 25                swap(a,b);
e5 1f            a = pai[head[a]];
de cb        }
b8 9b        return min(a,b,[&](int a, int b){
23 db            return tin[a] < tin[b];
6d c0        });
c1 cb    }

7b b5    int dist(int a, int b){
36 c5        return height[a] + height[b] - 2*height[lca(a,b)];
9f cb    }

76 f5    void update_point(int id, SegTree::lazy upd){
7a 9c        st.update(tin[id], tin[id], upd);
5a cb    }

// if no_root = 1, the root won't be included in the update;
4e d4    void update_subtree(int id, SegTree::lazy upd, int no_root =
0){
d9 58        st.update(tin[id]+no_root, tout[id], upd);
d6 cb    }

// if no_root = 1, the root won't be included in the update;
72 6c    void update_path(int a, int b, SegTree::lazy upd, int no_root
= 0){
b0 2d        while(head[a] != head[b]){
61 06            if(tin[a] < tin[b])
ec 25                swap(a,b);
05 eb            st.update(tin[head[a]], tin[a], upd);
f4 1f            a = pai[head[a]];
a5 cb        }
fe a0        if(tin[a] > tin[b])
02 25            swap(a,b);
ae b2        st.update(tin[a]+no_root, tin[b], upd);

```

```

40 cb    }

a3 e6    seg query_point(int id){
f2 6f        return st.query(tin[id],tin[id]);
8a cb    }

// if no_root = 1, the root won't be included in the query;
6f 30    seg query_subtree(int id, int no_root = 0){
85 82        return st.query(tin[id]+no_root,tout[id]);
56 cb    }

// if no_root = 1, the root won't be included in the query;
// this query will work even if the query is non commutative
ee 33    seg query_path(int a, int b, int no_root = 0){
ce 86        seg retl = seg(), retr = seg();

e4 2d        while(head[a] != head[b]){
62 4c            seg& ret = tin[a] > tin[b] ? retl : retr;
3a 33            int& v = tin[a] > tin[b] ? a : b;
90 6b            ret = st.merge(ret,st.query(tin[head[v]], tin[v]));
0c 58            v = pai[head[v]];
c6 cb        }

bd a0        if(tin[a] > tin[b])
1e 25            swap(a,b);

45 37        return st.merge(st.merge(retl,st.query(tin[a]+no_root,tin
[b])), retr);

86 cb    }

02 bf    private:

9c c7    void prec(int id){
d6 5a        if(g[id].size() && g[id][0] == pai[id])
10 a8            swap(g[id][0], g[id].back());
76 20        for(int& v : g[id]){
e0 85            if(v == pai[id])
ab 5e                continue;
eb 21            pai[v] = id;
4a 09            height[v] = height[id]+1;
33 f9            prec(v);
48 b0            sub[id]+=sub[v];
af df            if(sub[v] > sub[g[id][0]])
57 00                swap(v,g[id][0]);
ec cb        }
62 cb    }

```

```

e8 a2 void hld(int id, int hd){
69 36     tout[id] = tin[id];
18 a6     head[id] = hd;
ad 5c     if(g[id].size() && g[id][0] != pai[id]){
e7 38         tin[g[id][0]] = tout[id]+1;
10 e2         hld(g[id][0],hd);
36 8a         tout[id] = tout[g[id][0]];
0d cb     }
69 8f     for(int i = 1; i < g[id].size(); i++){
3a 85         int v = g[id][i];
a0 85         if(v == pai[id])
29 5e             continue;
1d bd         tin[v] = tout[id]+1;
e0 97         hld(v, v);
83 b1         tout[id] = tout[v];
7b cb     }
4b cb }
02 21 };

```

## 6.10 IncrementalMst.hpp

```

Hash: be6a3a
/**
 * from https://github.com/defnotmee/definitely-not-a-lib
 */
d7 d7 #ifndef 0_0
99 6d #include "../utility/template.cpp"
9e ed #include "../utility/rng.hpp"
a8 f2 #endif

78 a6 struct IncrementalMST{
73 bc     vector<int> par, sz, prio;
80 3d     vector<pii> parw;

b2 0c     IncrementalMST(int n) : par(n), sz(n,1), prio(n), parw(n,{INF
,INF}){
54 6a         iota(all(prio),0);
28 bd         par = prio;
41 1e         shuffle(all(prio),rng);
37 cb     }
bf bf     private:

da 98     int find(int v, pii w = {INF-1,INF}){
a4 f9         while(parw[v] <= w){

```

```

3f e9         while(parw[v] > parw[par[v]]){
32 07             sz[par[v]] -= sz[v];
54 43             par[v] = par[par[v]];
24 cb         }
b9 c3         v = par[v];
33 cb     }
6f 6d     return v;
c3 cb }

54 17 void disconnect(int v){
7e 71     if(par[v] == v)
ba 50         return;
36 0e     disconnect(par[v]);
45 07     sz[par[v]] -= sz[v];
04 cb }

c1 cc int connect(int v, pii w = {INF-1, INF}){
fe f9     while(parw[v] <= w){
da 3e         sz[par[v]] += sz[v];
b1 c3         v = par[v];
80 cb     }
9d 6d     return v;
76 cb }

64 0f void consider_edge(int a, int b, pii w){
97 0a     disconnect(a), disconnect(b);

a2 98     while(a != b){
59 c8         a = connect(a,w);
08 eb         b = connect(b,w);
97 46         if(prio[a] > prio[b])
59 25             swap(a,b);
8a de         swap(par[a],b);
a2 40         swap(parw[a],w);
70 cb     }

df 69     connect(a);
be cb }

31 67 public:

/**
 * Finds maximum edge in the path from a to b
 * @return weight of maximum edge from a to b (or {INF,-1} if
 * they are disconnected)
 */
29 4f pii max_edge(int a, int b){

```

```

74 82     int ra = find(a), rb = find(b);
0d 7b     if(ra != rb)
9a 56         return {INF,-1};

43 6e     if(parw[a] > parw[b])
83 25         swap(a,b);
fb 02     while(par[a] != b){
9d 3a         a = par[a];
ff 6e         if(parw[a] > parw[b])
93 25             swap(a,b);
85 cb     }
9a d6     return parw[a];
68 cb }

/**
 * Deletes maximum edge of the path from a to b
 * from the MST
 * @return weight of the edge removed from the MST (or {INF
 *     ,-1} if
 * they are disconnected)
 */
27 16 pii delete_maximum(int a, int b){
60 82     int ra = find(a), rb = find(b);
10 7b     if(ra != rb)
35 56         return {INF,-1};

43 6e     if(parw[a] > parw[b])
78 25         swap(a,b);
34 02     while(par[a] != b){
eb 3a         a = par[a];
86 6e         if(parw[a] > parw[b])
d8 25             swap(a,b);
5b cb     }

02 d9     b = a;
6e ad     while(par[b] != b){
7d ac         sz[par[b]]-=sz[a];
89 08         b = par[b];
ca cb     }
b1 21     par[a] = a;
46 25     pii ret = {INF,INF};
01 fa     swap(parw[a],ret);
47 ed     return ret;
55 cb }

/**
 * Adds edge between a and b with weight w to the graph.

```

```

 * @return weight of the edge removed from the MST (or {INF
 *     ,-1} if
 * there was none)
 */
e4 27 pii add_edge(int a, int b, pii w){
b4 ae     if(a == b)
9c 56         return {INF,-1};

7b 67     pii ret = delete_maximum(a,b);
33 b6     if(ret <= w)
e7 1c         swap(w,ret);

ae cf     consider_edge(a,b,w);

6b ed     return ret;
01 cb     }
be 21 };

```

## 6.11 Isomorphism.hpp

Hash: 71fe5b

/\*

from <https://github.com/defnotmee/definitely-not-a-lib>

Gives a way to hash a tree, either considering it rooted or not.  
(choose the corresponding struct depending on the case)

Usage:

Rooted\_Isomorphism(n, root) initializes the structure for a  
tree of size n (0 indexed) rooted at root.

add\_edge(a,b) is self explanatory

After adding all edges, call calc\_tree() to get the hash of the tree.

After calling calc\_tree(), hashsub[i] will contain the hash of subtree  
i.

For Unrooted\_Isomorphism, the biggest difference is that the hashub  
array will  
be meaningless.  
\*/

d7 d7 #ifndef 0\_0

cb c8 #include "../utility/template.cpp"

```

91 f2 #endif

2b d5 const int SEED = chrono::high_resolution_clock::now().
    time_since_epoch().count();

05 84 struct Rooted_Isomorphism{

fa bd     int n, root;
65 ae     vector<int> tin, tout, sub, pai, height;
d6 3b     vector<basic_string<int>> g;
75 cb     int m = 0;
88 99     ull seed;
93 81     vector<ll> hashsub;

95 79     ull hasher(ull x){
        // http://xorshift.di.unimi.it/splitmix64.c
2a 6e     x+=0x9e3779b97f4a7c15;
c2 3e     x = (x^(x>>30)) * 0xbf58476d1ce4e5b9;
74 31     x = (x^(x>>27)) * 0x94d049bb133111eb;
19 10     return x^(x>>31)^seed;
05 cb     }

71 b1     Rooted_Isomorphism(int n = 0, int root = 0, ull seed = SEED)
        : n(n), root(root),
db 8d     tin(n), tout(n), sub(n,1), pai(n,root), height(n), g(n),
19 1f     seed(seed), hashsub(n) {}

        // use this if you want the same graph for a different root,
        // otherwise important info wont be reset
f8 1e     Rooted_Isomorphism(Rooted_Isomorphism& r, int root) :
        Rooted_Isomorphism(r.n, root){
9f c9         m = r.m;
33 69         g = r.g;
3c cb     }

6a 01     void add_edge(int a, int b){
24 02         g[a].push_back(b);
28 3e         g[b].push_back(a);
27 7b         m++;
fc cb     }

        // returns hash of the whole tree
8c d9     ull calc_tree(){
97 9b         assert(m == n-1);
e2 00         prec(root);
fb 0d         return hashsub[root];
b3 cb     }

```

```

1c bf     private:

9a c7     void prec(int id){
fb 36         tout[id] = tin[id];
b7 81         for(int v : g[id]){
7f 85             if(v == pai[id])
04 5e                 continue;
38 21             pai[v] = id;
ff 09             height[v] = height[id]+1;
2f bd             tin[v] = tout[id]+1;
fb f9             prec(v);
d3 b1             tout[id] = tout[v];
37 b0             sub[id]+=sub[v];
e9 ff             hashsub[id]+=hashsub[v];
4d cb         }
50 06         hashsub[id] = hasher(hashsub[id]);
35 cb     }

9f 21 };

d7 50 struct Unrooted_Isomorphism{
15 40     Rooted_Isomorphism tree;

31 b6     Unrooted_Isomorphism(int n) : tree(n){}

59 01     void add_edge(int a, int b){
6d 3b         tree.add_edge(a,b);
59 cb     }

57 37     pii find_centroids(){
cc 96         int id = tree.root;

75 66         while(true){
2c a0             for(int v : tree.g[id]){
95 a3                 if(tree.pai[id] != v && tree.sub[v]*2 >= tree.n){
69 c4                     id = v;
44 20                     goto NEXT;
64 cb                 }
6a cb             }
cd c2             break;
36 8f             NEXT;;
0e cb         }
68 02         if(tree.sub[id]*2 == tree.n)
b0 83             return {tree.pai[id], id};
4a 70         return {id,id};
1e cb     }

```

```

a8 d9      ull calc_tree(){
df e2      tree.calc_tree();
37 9d      auto [c1, c2] = find_centroids();

28 99      tree = Rooted_Isomorphism(tree,c1);
dc 0f      ull tmp = tree.calc_tree();

38 f9      tree = Rooted_Isomorphism(tree,c2);

15 b6      return min(tmp, tree.calc_tree());
76 cb      }
71 21 };

```

## 6.12 Kthshortestwalk.hpp

```

Hash: b77c3c
/**
 * from https://github.com/defnotmee/definitely-not-a-lib
 *
 * Copied from https://judge.yosupo.jp/submission/246093
 * Thanks nor!!
 */
d7 d7 #ifndef 0_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

78 4f template <class T>
6d b2 using min_heap = priority_queue<T, vector<T>, greater<T>>;

d5 65 template <class Distance, class Graph>
f3 7b auto dijkstra(const Graph& g, int s) {
db ee      vector<Distance> d(g.size(), numeric_limits<Distance>::max())
;
69 d5      vector<Distance> prv(g.size(), -1);
09 3e      min_heap<pair<Distance, int>> heap;
70 1c      heap.emplace(d[s] = 0, s);
61 74      while (!heap.empty()) {
50 41          auto [dv, v] = heap.top();
08 77          heap.pop();
24 05          if (dv != d[v]) continue;
5b e1          for (auto&& [to, w] : g[v]) {
e5 a3              if (d[to] > dv + w) {
51 bc                  d[to] = dv + w;
5b 12                  heap.emplace(d[to], to);
e8 ac                  prv[to] = v;

```

```

96 cb      }
7f cb      }
a6 cb      }
47 97      return make_pair(d, prv);
91 cb }

0f 6b template <typename Key, typename Value>
11 a6 struct LeftistHeap {
2e 2a      using self_t = LeftistHeap<Key, Value>;
ba 59      int rank;
18 e5      Key key;
cb 1a      Value value;
f0 88      self_t *left, *right;
e5 52      constexpr LeftistHeap(int rank_, Key key_, Value value_,
self_t* left_,
0c 40      self_t* right_)
1e d0      : rank{rank_}, key{key_}, value{value_}, left{left_},
right{right_} {}
67 3a      inline static deque<LeftistHeap> alloc;
52 23      static self_t* insert(self_t* const a, const Key k, const
Value v) {
08 ca          if (not a or k <= a->key) {
9b 55              alloc.emplace_back(1, k, v, a, nullptr);
d1 14              return &alloc.back();
28 cb          }
0f a0          auto l = a->left, r = insert(a->right, k, v);
7a 46          if (not l or r->rank > l->rank) swap(l, r);
46 2e          alloc.emplace_back(r ? r->rank + 1 : 0, a->key, a->value,
l, r);
fb 14          return &alloc.back();
65 cb      }
ea 21 };

1a 52 template <typename Distance, typename Graph>
9e 2d auto kth_shortest_paths(int n, const Graph& g, int source, int
sink, int k) {
56 6f      Graph g_rev(n);
d1 5b      for (int u = 0; u < n; ++u)
9a d2          for (auto [v, w] : g[u]) g_rev[v].push_back({u, w});
fb 77      auto [d, prv] = dijkstra<Distance>(g_rev, sink);
97 60      if (d[source] == numeric_limits<Distance>::max())
42 0c          return vector<Distance>{};
1b ca      vector<basic_string<int>> tree(n);
b9 5b      for (int u = 0; u < n; ++u)
24 6e          if (prv[u] != -1) tree[prv[u]].push_back(u);
ff 83      using heap_t = LeftistHeap<Distance, int>;
5b d4      vector<heap_t*> h(n, nullptr);

```



```

71 f9      {
f7 94      queue<int> q({sink});
00 99      while (not q.empty()) {
3c c0          const int u = q.front();
ba 83          q.pop();
66 c1          bool seen_p = false;
80 1d          for (const auto [v, w] : g[u]) {
ee fa              if (d[v] == numeric_limits<Distance>::max())
                    continue;
30 dd              const auto c = w + d[v] - d[u];
df 24              if (not seen_p and v == prv[u] and c == 0) {
ab 63                  seen_p = true;
6a 5e                  continue;
c4 cb              }
14 fa              h[u] = heap_t::insert(h[u], c, v);
95 cb          }
08 8f          for (auto v : tree[u]) h[v] = h[u], q.push(v);
69 cb      }
d2 cb  }
93 61      vector<Distance> ans{d[source]};
2a 05      ans.reserve(k);
8f 5b      if (not h[source]) return ans;
03 f9      {
38 2f          min_heap<pair<Distance, heap_t*>> q;
1b 29          q.push({d[source] + h[source]->key, h[source]});
2a 33          while (not q.empty() and (int) ans.size() < k) {
58 35              auto [cd, ch] = q.top();
32 83              q.pop();
a2 d8              ans.push_back(cd);
7a 30              if (h[ch->value]) q.push({cd + h[ch->value]->key, h[
                    ch->value]});
c8 95              if (ch->left) q.push({cd + ch->left->key - ch->key,
                    ch->left});
87 52              if (ch->right) q.push({cd + ch->right->key - ch->key,
                    ch->right});
8c cb          }
94 cb      }
f3 ba      return ans;
b7 cb  }

```

## 6.13 Lca.hpp

```

Hash: f5e683
/*
from https://github.com/defnotmee/definitely-not-a-lib

```

Extension of tree\_rooted.hpp that calculates lca in  $O(n \log n)$  precomputation and  $O(1)$  per query.

Isnt able to calculate things on the path to the LCA.  
(see binlift.hpp for that)  
\*/

```

d7 d7 #ifndef O_0
cb c8 #include "../utility/template.cpp"
4f f4 #include "rooted_tree.hpp"
6d f2 #endif

f8 ae struct LCATree : Tree {
5d cf     vector<int> euler, eid;
88 77     matrix<int> sparse;

4e 9b     LCATree(int n = 0, int root = 0) : Tree(n, root), eid(n) {
7f ed         euler.reserve(2*n);
93 cb     }

a2 08     int get_lower(int a, int b){
98 d0         return height[a] < height[b] ? a : b;
79 cb     }

b7 11     void calc_tree(){
ad 9b         assert(m == n-1);
bb 00         prec(root);

                // not on rooted_tree.hpp
16 d4         int lg = log2(euler.size())+1;
44 18         sparse = matrix<int>(lg, euler);
c3 82         for(int i = 1; i < lg; i++){
a3 84             for(int j = 0; j + (1<<i) <= euler.size(); j++){
a3 ed                 sparse[i][j] = get_lower(sparse[i-1][j], sparse[i
                    -1][j+(1<<i-1)]);
e6 cb             }
6d cb         }

56 7b     int lca(int a, int b){
e7 a0         a = eid[a], b = eid[b];
12 f7         if(a > b)
a7 25             swap(a,b);
b3 33         int logg = log2(b-a+1);
af 1e         return get_lower(sparse[logg][a], sparse[logg][b-(1<<logg
                    )+1]);
9f cb     }

```

```

1b b5     int dist(int a, int b){
f7 c5         return height[a]+height[b]-2*height[lca(a,b)];
d4 cb     }

ef bf     private:

42 c7     void prec(int id){
8d 36         tout[id] = tin[id];
b8 43         eid[id] = euler.size(); // not on rooted_tree.hpp
e9 09         euler.push_back(id); // not on rooted_tree.hpp
1e 81         for(int v : g[id]){
c5 85             if(v == pai[id])
71 5e                 continue;
cb 21             pai[v] = id;
6c 09             height[v] = height[id]+1;
97 bd             tin[v] = tout[id]+1;
ef f9             prec(v);
97 b1             tout[id] = tout[v];
69 b0             sub[id]+=sub[v];
79 09             euler.push_back(id); // not on rooted_tree.hpp
ec cb         }
43 cb     }
f5 21 };

```

## 6.14 Lct.hpp

```

Hash: cf66bb
/**
 * from https://github.com/defnotmee/definitely-not-a-lib
 *
 * Implementation from https://codeforces.com/blog/entry/75885
 * Will implement it myself eventually but will just put it here
 * until I do.
 *
 * Different from other algos on this library, it is 1-INDEXED!!!
 */

d7 d7 #ifndef O_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

44 b8 struct SplayTree {
7c bf     struct Node {
0e e0         int ch[2] = {0, 0}, p = 0;
64 bf         ll self = 0, path = 0;           // Path aggregates
5e 6d         ll sub = 0, vir = 0;             // Subtree aggregates

```

```

ab d2         bool flip = 0;                  // Lazy tags
36 21     };
26 3e     vector<Node> T;

6a 98     SplayTree(int n) : T(n + 1) {}

7e 6c     void push(int x) {
76 e9         if (!x || !T[x].flip) return;
80 57         int l = T[x].ch[0], r = T[x].ch[1];

1c cd         T[l].flip ^= 1, T[r].flip ^= 1;
0d a1         swap(T[x].ch[0], T[x].ch[1]);
bf 4d         T[x].flip = 0;
76 cb     }

f0 42     void pull(int x) {
59 5b         int l = T[x].ch[0], r = T[x].ch[1]; push(l); push(r);

81 63         T[x].path = T[l].path + T[x].self + T[r].path;
50 0d         T[x].sub = T[x].vir + T[l].sub + T[r].sub + T[x].self;
de cb     }

0d 21     void set(int x, int d, int y) {
72 1a         T[x].ch[d] = y; T[y].p = x; pull(x);
6f cb     }

3d 07     void splay(int x) {
40 d0         auto dir = [&](int x) {
3c 06             int p = T[x].p; if (!p) return -1;
df 8d             return T[p].ch[0] == x ? 0 : T[p].ch[1] == x ? 1 : -1;
2a 21         };
43 0a         auto rotate = [&](int x) {
f9 07             int y = T[x].p, z = T[y].p, dx = dir(x), dy = dir(y);
28 47             set(y, dx, T[x].ch[!dx]);
28 52             set(x, !dx, y);
8e 75             if (~dy) set(z, dy, x);
f8 3f             T[x].p = z;
74 21         };
bb 22         for (push(x); ~dir(x); ) {
fa 02             int y = T[x].p, z = T[y].p;
71 5d             push(z); push(y); push(x);
55 8c             int dx = dir(x), dy = dir(y);
48 30             if (~dy) rotate(dx != dy ? x : y);
eb 64             rotate(x);
0e cb         }
88 cb     }
e2 21 };

```

```

37 6f struct LinkCut : SplayTree {
ee e5     LinkCut(int n) : SplayTree(n) {}

b7 ac     int access(int x) {
16 16         int u = x, v = 0;
10 3a         for (; u; v = u, u = T[u].p) {
89 6d             splay(u);
eb 11             int& ov = T[u].ch[1];
4a 8d             T[u].vir += T[ov].sub;
33 4f             T[u].vir -= T[v].sub;
db e1             ov = v; pull(u);
72 cb         }
d2 97     return splay(x), v;
8f cb     }

5a d9 void reroot(int x) {
be ef     access(x); T[x].flip ^= 1; push(x);
2d cb     }

f7 c0 void Link(int u, int v) {
22 a2     reroot(u); access(v);
9d a8     T[v].vir += T[u].sub;
77 fb     T[u].p = v; pull(v);
b0 cb     }

38 ad void Cut(int u, int v) {
0a a2     reroot(u); access(v);
59 5c     T[v].ch[0] = T[u].p = 0; pull(v);
52 cb     }

// Rooted tree LCA. Returns 0 if u and v arent connected.
32 4c int LCA(int u, int v) {
55 60     if (u == v) return u;
cd 84     access(u); int ret = access(v);
11 d0     return T[u].p ? ret : 0;
62 cb     }

// Query subtree of u where v is outside the subtree.
6c a0 ll Subtree(int u, int v) {
e5 89     reroot(v); access(u); return T[u].vir + T[u].self;
83 cb     }

// Query path [u..v]
cc 5e ll Path(int u, int v) {
0b b0     reroot(u); access(v); return T[v].path;
1f cb     }

```

```

// Update vertex u with value v
b8 41 void Update(int u, ll v) {
52 ec     access(u); T[u].self += v; pull(u);
a7 cb     }
cf 21 };

```

## 6.15 RootedTree.hpp

Hash: 221a00

/\*

from <https://github.com/defnotmee/definitely-not-a-lib>

Stores a rooted tree with relevant information like height, dfs order (tin and tout), height, the parent (pai) the size of the subtrees (sub).

Intended to be inherited or composed for other algos.

Usage:

Tree(n,root): prepares tree of size n with vertices from 0 to n-1

add\_edge(a,b): adds edge between a and b

After adding all edges, call calc\_tree().

\*/

```
d7 d7 #ifndef O_0
```

```
cb c8 #include"../utility/template.cpp"
```

```
91 f2 #endif
```

```
46 5a struct Tree{
```

```
97 bd     int n, root;
```

```
49 ae     vector<int> tin, tout, sub, pai, height;
```

```
95 3b     vector<basic_string<int>> g;
```

```
35 cb     int m = 0;
```

```
a4 3d     Tree(int n = 0, int root = 0) : n(n), root(root),
```

```
35 1d     tin(n), tout(n), sub(n,1), pai(n,root), height(n), g(n){}
```

```
ce 01     void add_edge(int a, int b){
```

```
6e 02         g[a].push_back(b);
```

```
94 3e         g[b].push_back(a);
```

```
34 7b         m++;
```

```
35 cb     }
```

```

2b 11 void calc_tree(){
07 9b     assert(m == n-1);
d6 00     prec(root);
21 cb }

// call only after calc_tree
3b 37 pii find_centroids(){
45 8e     int id = root;

47 66     while(true){
bc 81         for(int v : g[id]){
52 e2             if(pai[id] != v && sub[v]*2 >= n){
67 c4                 id = v;
d9 20                 goto NEXT;
ef cb             }
7c cb         }
50 c2         break;
0c 8f         NEXT::;
5e cb     }
d7 f3     if(sub[id]*2 == n)
5f b4         return {pai[id], id};
4e 70     return {id,id};
bf cb }

f9 d9 protected:
0c c7 void prec(int id){
44 36     tout[id] = tin[id];
0d 81     for(int v : g[id]){
44 85         if(v == pai[id])
47 5e             continue;
b9 21         pai[v] = id;
de 09         height[v] = height[id]+1;
33 bd         tin[v] = tout[id]+1;
19 f9         prec(v);
21 b1         tout[id] = tout[v];
03 b0         sub[id]+=sub[v];
14 cb     }
b9 cb }
22 21 };

```

## 6.16 Scc.hpp

```

Hash: 6fd52b
/*
from https://github.com/defnotmee/definitely-not-a-lib

```

Implements kosaraju's algorithm for finding strongly connected components.

Usage:

SCC(n) : prepares graph of size n with vertices from 0 to n-1  
add\_edge(a,b) : adds directed edge from a to b

After adding all the edges, call kosaraju().

This call will make SCC::scc have information on the strongly connected components:

(I)  $0 \leq \text{scc}[i] < \text{scc\_count}$   
(II)  $\text{scc}[i] = \text{scc}[j] \iff$  there is a path from i to j and from j to i.  
(III)  $\text{scc}[i] < \text{scc}[j] \implies$  there is no path from j to i. [bonus from kosaraju!]

get\_condensation() will return a graph of the scc's (condensation graph).

It will be a DAG!

fun fact: if you want to dp in the condensation graph you don't need to dfs,

you can just process the sccs in **\*\*descending\*\*** order because of property (III)!

\*/

```

d7 d7 #ifndef 0_0
99 6d #include "../utility/template.cpp"
e9 f2 #endif

28 bf struct SCC{

e1 1a     int n;
70 47     vector<basic_string<int>> g, r;

af 1b     vector<int> scc;
ef 0b     int scc_count = 0;

ce 20     SCC(int n = 0) : n(n), g(n), r(n), scc(n,-1){

76 01     void add_edge(int a, int b){
51 02         g[a].push_back(b);
d8 7c         r[b].push_back(a);
83 cb     }

```

```

8d db    void kosaraju(){
15 f9        vector<int> check(n);

3f 51        vector<int> euler;
3b 06        euler.reserve(n);

a1 83        for(int i = 0; i < n; i++)
4d 9f            if(!check[i]) dfs(i,check,euler);

d0 6b        reverse(all(euler));

4f f1        for(int i : euler)
c2 0e            if(check[i] == 1) rdfs(i,check), scc_count++;
d5 cb    }

6c 36    struct Condensation{
ed 1a        int n; // number of nodes
ad 43        int sn; // number of sccs
21 3b        vector<basic_string<int>> g; // Edges going out of the
scc
ea 18        vector<basic_string<int>> in_scc; // List of vertices in
scc[i]

08 e4        Condensation(int n, int sn) : n(n), sn(sn), g(sn), in_scc
(sn){};
75 21    };

8e c5    Condensation get_condensation(){
a8 1a        if(scc.back() == -1)
cc 75            kosaraju();

d3 10        Condensation ret(n,scc_count);

ec 60        for(int i = 0; i < n; i++){
82 a1            ret.in_scc[scc[i]].push_back(i);
2d 48            for(int j : g[i]){
39 95                if(scc[j] != scc[i])
59 f0                    ret.g[scc[i]].push_back(scc[j]);
cc cb            }
52 cb        }

// comment if you dont care about repeated edges
11 a6        for(int i = 0; i < scc_count; i++){
d9 31            sort(all(ret.g[i]));
b8 26            ret.g[i].erase(unique(all(ret.g[i])),ret.g[i].end());
4f cb        }
e7 ed        return ret;

```

```

83 cb    }

89 bf    private:

0d 4f    void dfs(int id, vector<int>& check, vector<int>& euler){
85 e8        check[id] = 1;
bb 54        for(int i : g[id])
4c 34            if(!check[i])
64 c3                dfs(i,check,euler);
1c 09        euler.push_back(id);
7f cb    }

82 ed    void rdfs(int id, vector<int>& check){
3a d1        scc[id] = scc_count;
9b a1        check[id] = 2;
0d d0        for(int i : r[id])
32 9a            if(check[i] == 1)
de 17                rdfs(i,check);
8c cb    }

6f 21 };

```

## 6.17 UnionFind.hpp

Hash: 5c4f1c

/\*

from <https://github.com/defnotmee/definitely-not-a-lib>

Disjoint Set Union with union by size and path compression. Complexity is  $O(n \cdot \text{inverse\_ackermann}(n))$ , where  $n$  is the number of updates.

Use the "size" and "pai" functions to get the size of the group and the parent of the current vertex.

\*/

```
d7 d7 #ifndef 0_0
```

```
99 6d #include "../utility/template.cpp"
```

```
e9 f2 #endif
```

```
de 60 class UnionFind{
```

```
4d 99     vector<int> v; // Either parent (if v[i] >= 0) or size (if v[
i] < 0 and i is a root) of the component
```

```
d5 67     public:
```

```
4a 92     UnionFind(int n = 0) : v(n,-1){}
```

```

0a 13      int find(int id){
fd e1      return v[id] < 0 ? id : v[id] = find(v[id]);
db cb      }

73 34      int size(int id){ // Returns size of the component id belongs
to         to
bc 93      return -v[find(id)];
c4 cb      }

04 f1      int pai(int id){ // Returns parent of id
01 0c      return v[id] < 0 ? id : v[id];
59 cb      }

// Returns 1 if a and b were in different groups.
// Useful for Kruskal.
e4 c8      bool union(int a, int b){
6e bc      a = find(a);
4a b8      b = find(b);

59 ae      if(a == b)
eb bb      return 0;

83 ad      if(size(a) > size(b)) // union by size
e8 25      swap(a,b);

// b will now be the parent of a

cb 72      v[b] += v[a];
58 4c      v[a] = b;
6e 6a      return 1;
01 cb      }

b7 3d      bool same(int a, int b){
68 c0      return find(a) == find(b);
00 cb      }
5c 21 };

```