

Panel Data Models and Diff-In-Diff Methods

Zhiyuan Chen

Empirical Methods
Renmin Business School

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Outline

- Panel Data Models

- ▶ Panel data
- ▶ Random Effects vs. Fixed Effects
- ▶ Fixed Effects vs. First Difference

- Difference-In-Differences Models

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- ▶ Common Trend Assumption & Sensitivity Tests
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Panel Data

- Now we have data for N units (people, products, firms, counties, cities, provinces, countries ...)
- For each unit we have T_i (≥ 1) observations
 - ▶ T_i typically refers to time periods
 - ▶ Could be products of a firm, students in a classroom, counties in a province

We assume that:

- ▶ N is large; consistency exists as N grows
- ▶ T_i is small; T_i stays constant as N grows

Now let's consider the regression model:

$$Y_{it} = X'_{it}\beta + u_{it}$$

- *Assumption 1*: assume independence **across individuals** but **not across time**
- *Assumption 2*: $\mathbf{E}(X_{it}u_{it}) = 0$

Consistency:

$$\hat{\beta} = \beta + \left(\frac{\sum_{i=1}^N \sum_{t=1}^{T_i} X_{it} X'_{it}}{\sum_{i=1}^N T_i} \right)^{-1} \left(\frac{\sum_{i=1}^N \sum_{t=1}^{T_i} X_{it} u_{it}}{\sum_{i=1}^N T_i} \right) \\ \rightarrow_p \beta$$

Serial Correlation

- The assumption of NO serial correlation is problematic so the asymptotic variance from before is not right
- Error terms are uncorrelated across individuals, but not within individuals
- Formally speaking, we assume that:

$$\mathbf{E}(u_{it}u_{jt}) = 0, \forall i \neq j$$

$$\mathbf{E}(u_{it}X_{it}) = 0$$

- However, the assumption of OLS is not satisfied because:

$$\mathbf{E}(u_{it}u_{is}) = 0$$

is a CRAZY assumption!

- Ignoring the serial correlation tends to **underestimate** the size of standard errors

Clustered Standard Errors

- Recall that

$$\hat{\beta} - \beta = \left(\sum_i^N \sum_t^{T_i} X_{it} X'_{it} \right)^{-1} \sum_i^N \sum_t^{T_i} X_{it} u_{it}$$

- Define $\eta_i \equiv \sum_{t=1}^{T_i} X_{it} u_{it}$, then η_i is iid
- $\text{var}(\eta_i) = V_\eta$

- Then we get

$$\sqrt{N}(\hat{\beta} - \beta) = \left(\frac{1}{N} \sum_i \sum_t X_{it} X'_{it} \right)^{-1} \left(\frac{1}{\sqrt{N}} \sum_{i=1}^N \eta_i \right)$$

- Using the Central Limit Theorem we know

$$\sqrt{N}(\hat{\beta} - \beta) \sim \mathcal{N} \left(0, \left[\mathbf{E} \left(\sum_{t=1}^{T_i} X_{it} X'_{it} \right)^{-1} \right] V_\eta \left[\mathbf{E} \left(\sum_{t=1}^{T_i} X_{it} X'_{it} \right) \right]^{-1} \right)$$

We can approximate the variance of $\hat{\beta}$ as

$$\text{Var}(\hat{\beta}) \approx \left(\sum_i \sum_t X_{it} X'_{it} \right)^{-1} \left[\sum_i \left(\sum_t X_{it} \hat{u}_{it} \right) \left(\sum_t X'_{it} \hat{u}_{it} \right) \right] \left(\sum_i \sum_t X_{it} X'_{it} \right)^{-1}$$

- This is a generalization of the heteroskedastic robust standard errors
- We are allowing $[X_{i1}u_{i1}, X_{i2}u_{i2}, \dots, X_{iT_i}u_{iT_i}]$ to have an arbitrary variance-covariance matrix

In STATA, this is done by coding `reg y x, cluster(i)`

- i is the id of the group in which the errors are serially correlated

Two-way Cluster (Cameron et al., 2011)

- Consider situations where each observation may belong to more than one “dimension” of groups.
 - ▶ E.g., firms belong to city group and industry group
- For errors belong to the same group, they can have an arbitrary correlation
- For two groups G and H . It turns out the variance $\hat{V}(\hat{\beta})$ can be calculated as

$$\hat{V}(\hat{\beta}) = \hat{V}^G(\hat{\beta}) + \hat{V}^H(\hat{\beta}) - \hat{V}^{G \cap H}(\hat{\beta})$$

- This can be computed by:
 - 1 Clustering on group G ;
 - 2 Clustering on group H ;
 - 3 Clustering on $G \cap H$

Random Effects vs. Fixed Effects

- Panel data enable us to take care of the idiosyncratic component in the error term
- Write the linear model as

$$Y_{it} = X'_{it}\beta + \theta_i + \varepsilon_{it}$$

- ▶ In both of the models, we assume that

$$\mathbf{E}(\varepsilon_{it}X_{it}) = 0$$

- ▶ In the Random Effects (RE) model, we assume that

$$\mathbf{E}(\theta_i X_{it}) = 0$$

- ▶ In the Fixed Effects (FE) model, we do not assume anything about the relationship between θ_i and X_i ! θ_i is an idiosyncratic constant.

Consistent Estimators for FE models

- Include individual dummies and run the regression:

$$Y_{it} = X_{it}\beta + D'_{it}\theta + \varepsilon_{it}$$

where $D_{it} = [D_{it}^{(j)}]$, $D_{it}^{(j)} = 1$ if $i = j$ and zero otherwise

- ▶ Conceptually this is a different model, but technically it delivers consistent estimates for β

- **Standard FE (Mean-Differencing) model:**

$$(Y_{it} - \bar{Y}_i) = (X_{it} - \bar{X}_i)' \beta + (\varepsilon_{it} - \bar{\varepsilon}_i)$$

where $\bar{Z}_i \equiv \frac{1}{T_i} \sum_{t=1}^{T_i} Z_{it}$

- **First-Differencing (FD) model:**

$$Y_{it} - Y_{it-1} = (X_{it} - X_{it-1})' \beta + \varepsilon_{it} - \varepsilon_{it-1}$$

- ▶ With 2 periods, this is equivalent to the standard FE model (verify it by yourself)

Fixed Effects vs. First Differencing

More generally, we consider the model

$$Y_{it} = \beta \tau_{it} + \theta_i + \varepsilon_{it}$$

Assume that $T_i = T$ for everyone, for everyone the only regressor τ_{it} is given by

$$\tau_{it} = \begin{cases} 0 & t \leq t_0 \\ 1 & t > t_0 \end{cases}$$

- τ_{it} can represent some macro-level program (trade liberalization, 5-year plan, expansion of college enrollment...) begins at $t_0 + 1$
- The FE and FD estimators are:

$$FE : \hat{\beta}_{FE} = \frac{\sum_{i=1}^N \sum_{t=t_0+1}^T Y_{it}}{N(T - t_0)} - \frac{\sum_{i=1}^N \sum_{t=1}^{t_0} Y_{it}}{Nt_0}$$

$$FD : \hat{\beta}_{FD} = \frac{\sum_{i=1}^N (Y_{it_0+1} - Y_{it_0})}{N}$$

Fixed Effects vs. Pooled Regression

The fixed effects estimator is NOT always better than pooled OLS regression

- The sample variance of the data is:

$$\begin{aligned}ss(X_{it}) &= \sum_i \sum_t (X_{it} - \bar{X})^2 \\&= \underbrace{\sum_i \sum_t (X_{it} - \bar{X}_i)^2}_{\text{within variance}} + \underbrace{\sum_i T_i (\bar{X}_i - \bar{X})^2}_{\text{between variance}}\end{aligned}$$

FE estimator only uses the within the variance of X_i :

- 1 It is inefficient. Standard errors are very large when X_{it} does not change
- 2 It can even lead to a worse bias:

$$\begin{aligned}\hat{\beta}_{POLS} &= \beta + \frac{\text{cov}(X_{it}, \theta_i + \varepsilon_{it})}{\text{var}(X_{it})} \\ \hat{\beta}_{FE} &= \beta + \frac{\text{cov}(X_{it} - \bar{X}_i, \varepsilon_{it} - \bar{\varepsilon}_i)}{\text{var}(X_{it} - \bar{X}_i)}\end{aligned}$$

Attenuation Bias of FE Estimates

- The year-to-year changes in explanatory variables may be mostly noise, especially when X_{it} varies a little over time, causing attenuation bias from measurement error
- More measurement error in the differenced regressors than in leveled variables
- **Attenuation Bias:** Measurement errors bias the estimates towards zero

True model: $y_i = \beta x_i + \varepsilon_i$, $\mathbf{E}(x_i \varepsilon_i) = 0$

Measurement error: $\tilde{x}_i = x_i + u_i$

Orthogonality condition: $\mathbf{E}(u_i) = 0$; $\mathbf{E}(x_i u_i) = 0$; $\mathbf{E}(u_i \varepsilon_i) = 0$

$$\Rightarrow \hat{\beta}^{bias} = \frac{cov(\tilde{x}_i, y_i)}{var(\tilde{x}_i)} = \frac{cov(x_i + u_i, \beta x_i + \varepsilon_i)}{var(x_i + u_i)} = \frac{var(x_i)}{var(x_i) + var(u_i)} \beta$$

- ▶ The estimate of β moves towards zero when $var(u_i)$ is relatively larger than $var(x_i)$.

Example: Almond, Chay, and Lee (QJE, 2005)

- Their goal is to estimate the effects of birth weight on health:

$$h_{ij} = \alpha + \beta bw_{ij} + X_i' \gamma + a_i + \varepsilon_{ij}$$

where

- ▶ h_{ij} : health of newborn j of mother i
- ▶ bw_{ij} : birth weight
- ▶ a_i : mother specific effect

- The pooled OLS regression of h_{ij} on bw_{ij} gives us

$$\hat{\beta}_{POLS} = \beta + \frac{\text{cov}(bw_{ij}, X_i' \gamma)}{\text{var}(bw_{ij})} + \frac{\text{cov}(bw_{ij}, a_i)}{\text{var}(bw_{ij})}$$

- Their clever solution is to **use twins**:
 - ▶ Twins share the same mother, so a_i effectively controls for **race, age, education, family background**...
 - ▶ Estimate the model as

$$\Delta h_{ij} = \beta \Delta bw_{ij} + \Delta \varepsilon_{ij}$$

where they assume that $\text{cov}(\Delta bw_{ij}, \Delta \varepsilon_{ij}) = 0$

- Attenuation bias caused by measurement errors?

Difference-In-Differences

Simple Before-After Policy Evaluation: Two-by-One Case

- Data on individuals right before and after the policy intervention: *Pre* and *Post*
- Two years dated 0 and 1 and that the policy is enacted in between
- We can simply identify the effect as:

$$\hat{\alpha} = \bar{Y}_1 - \bar{Y}_0$$

We could justify this using a FE model:

$$Y_{it} = \alpha_0 + \alpha\tau_{it} + \theta_i + \varepsilon_{it}$$

where

$$\tau_{it} = \begin{cases} 0 & t = 0 \\ 1 & t = 1 \end{cases}$$

We assume that $\mathbf{E}(\tau_{it}\varepsilon_{it}) = 0$ but no particularly assumption on θ_i

In the two-period case, FE model is equivalent to FD model, which is

$$Y_{i1} - Y_{i0} = \alpha + u_{i1} - u_{i0}$$

The estimator for the policy effect is

$$\hat{\alpha} = \bar{Y}_{i1} - \bar{Y}_{i0}$$

- We assume no other changes in time between and attribute whatever that is to the program
- Add time dummies into the model the treatment effect is not separated from the policy's impact

After adding time dummy variables, the model becomes

$$Y_{it} = \alpha_0 + \alpha \tau_{it} + \delta t + \theta_i + \varepsilon_{it}$$

Then the difference estimator delivers

$$\begin{aligned} \mathbf{E}(Y_{i1} - Y_{i0}) &= \mathbf{E}[(\alpha_0 + \alpha + \delta + \theta_i + \varepsilon_{i1}) - (\alpha_0 + \theta_i + \varepsilon_{i0})] \\ &= \alpha + \delta \neq \alpha \end{aligned}$$

Using the first-order difference, we generally cannot separate the time trend (δ) from the treatment effects (α)

- The Diff-in-Diff estimator is designed to solve this problem

Difference-In-Differences: The Two-by-Two Case

Now we have Two periods for Two groups:

- 1 People who are affected by the policy changes (*treated*): Y_{it}^1
- 2 People who are not affected by the policy changes (*controls*): Y_{it}^0

We can think:

- 1 Using the treated to pick up the time changes and policy effects:

$$\hat{\alpha} + \hat{\delta} = \bar{Y}_{i1}^1 - \bar{Y}_{i0}^1$$

- 2 Under the **Common Trend Assumption** controls pick up the time changes:

$$\hat{\delta} = \bar{Y}_{i1}^0 - \bar{Y}_{i0}^0$$

We can then estimate the policy effect as a difference in difference

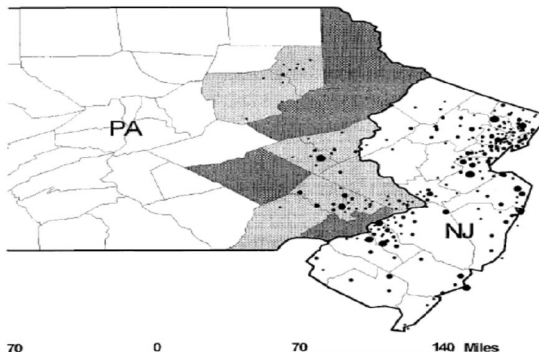
$$\hat{\alpha} = (\bar{Y}_1^1 - \bar{Y}_0^1) - (\bar{Y}_1^0 - \bar{Y}_0^0)$$

Example of Two-by-Two DID

Card and Krueger (1994)

- In 1992, New Jersey increased its minimum wage substantially while Pennsylvania kept its minimum wage constant.
- Card and Krueger compared fast-food restaurants in New Jersey ("treated group") with similar restaurants in nearby parts of Pennsylvania ("control group").

Location of Restaurants (Card and Krueger 2000)



Estimation using STATA

- data source: <http://dss.princeton.edu/training/Panel101.dta>
- Generate variables indicating treatment and time:
`gen time=(year>=1994)&!missing(year)`
`gen treated=(country>4)&!missing(country)`
`gen did=time*treated`
- Regression: `reg y time treated did, r`

- An alternative is to use the hashtag command:

```
reg y time##treated, r
```

- Or use the diff program in STATA:

```
ssc install diff
```

```
diff y, t(treated) p(time)
```

More General Formulation of DID Estimator

Formally, we can write the DGP (data generating process) for the DID estimator as

$$Y_{it} = \alpha_0 + \alpha \tau_{it}^{g_i} + \delta t + \theta_i + \varepsilon_{it}$$

where

$$\tau_{it}^{g_i} = \begin{cases} 1 & t = 1, g_i = 1 \\ 0 & \text{otherwise} \end{cases}$$

$\tau_{it}^{g_i}$ is usually written as $g_i \times t$

- Now we run a fixed effect regression and get a consistent estimate of the treatment effects α

Recall that the FE estimator for two-period data is equivalent to the FD estimator:

$$\begin{aligned}\hat{\alpha} &= \frac{\sum_{i=1}^N \left[(\tau_{i1}^{g_i} - \tau_{i0}^{g_i}) - \overline{(\tau_{i1}^{g_i} - \tau_{i0}^{g_i})} \right] (Y_{i1} - Y_{i0})}{\sum_{i=1}^N \left[(\tau_{i1}^{g_i} - \tau_{i0}^{g_i}) - \overline{(\tau_{i1}^{g_i} - \tau_{i0}^{g_i})} \right]^2} \\ &= (\bar{Y}_1^1 - \bar{Y}_0^1) - (\bar{Y}_1^0 - \bar{Y}_0^0)\end{aligned}$$

- Notice that

$$\begin{aligned}\overline{(\tau_{i1}^{g_i} - \tau_{i0}^{g_i})} &= \frac{1}{N_1 + N_0} \sum_i (\tau_{i1}^{g_i} - \tau_{i0}^{g_i}) \\ &= \frac{1}{N_1 + N_0} \left[\sum_{\{i: g_i=1\}} (\tau_{i1}^1 - \tau_{i0}^1) + \sum_{\{i: g_i=0\}} (\tau_{i1}^0 - \tau_{i0}^0) \right] \\ &= \frac{N_1}{N_1 + N_0}\end{aligned}$$

“In principle, you don't need panel data to implement DID regression; repeated cross-section data are fine!”

- In general, we can write the DID regression as

$$Y_{t_i} = \alpha_0 + \alpha \tau_{t_i}(g_i) + \delta t_i + \gamma g_i + \varepsilon_i$$

- ▶ where g_i is the group indicator of person i and t_i is the time period in which i exists in the data
- ▶ $\tau_{t_i}(g_i) = g_i \times t_i$
- We have 4 categories of people: (before, treated), (before, controls), (after, treated), (after, controls)
- We end up with having 4 groups of *moment conditions*:

$$\mathbf{E}(\varepsilon_i) = 0$$

$$\mathbf{E}(\tau_{t_i}(g_i)\varepsilon_i) = 0$$

$$\mathbf{E}(t_i\varepsilon_i) = 0$$

$$\mathbf{E}(g_i\varepsilon_i) = 0$$

Using

$$Y_i = \hat{\alpha}_0 + \hat{\alpha}\tau_{t_i}(g_i) + \hat{\delta}t_i + \hat{\gamma}g_i + \hat{\varepsilon}_i$$

We can rewrite the *sample analog* of the moment conditions as

$$\bar{Y}_0^1 = \hat{\alpha}_0 + \hat{\gamma}$$

$$\bar{Y}_1^1 = \hat{\alpha}_0 + \hat{\alpha} + \hat{\delta} + \hat{\gamma}$$

$$\bar{Y}_0^0 = \hat{\alpha}_0$$

$$Y_1^0 = \hat{\alpha}_0 + \hat{\delta}$$

We can solve for the parameters as

$$\hat{\alpha}_0 = \bar{Y}_0^0$$

$$\hat{\gamma} = \bar{Y}_0^1 - \bar{Y}_0^0$$

$$\hat{\delta} = \bar{Y}_0^1 - \bar{Y}_0^0$$

$$\hat{\alpha} = (Y_1^1 - \bar{Y}_0^1) - (\bar{Y}_1^0 - \bar{Y}_0^0)$$

More generally, we can add more control variables and specify the DID model as

$$Y_i = \alpha \tau_{t_i}(g_i) + \mathbf{X}'_{it} \beta + \delta_{t_i} + \theta_{g_i} + \varepsilon_i$$

Question: What is \mathbf{X}_{it} actually picking up?

This setting is simple yet powerful! There are many papers that do this basic stuff.

- Eissa and Liebman (QJE, 1996): Estimate the effect of the earned income tax credit on the labor supply of women
- Dohahue and Levitt (QJE, 2001): Impact of legalized abortion on crime

Multiple Periods: Event Studies

- The treatment effects could be dynamic, with short-run effects differing from long-run effects
- We can easily extend the baseline model to allow for this:

$$Y_i = \beta_0 + \sum_{j=0}^J \alpha_j \tau_{t_i-j}(g_i) + \delta_{g_i} + \gamma_{t_i} + \varepsilon_i$$

where

$$\tau_t(g_i) = \begin{cases} 1 & g_i = 1 \text{ and policy started in year } t \\ 0 & \text{otherwise} \end{cases}$$

Common Trend Assumption

- Recall that the model we specified for DID is:

$$Y_i = \beta_0 + \alpha \tau_{t_i}(g_i) + \delta t_i + \gamma g_i + \varepsilon_i$$

The DID estimator is

$$\hat{\alpha}_{DID} = \alpha + (\bar{\varepsilon}_1^1 - \bar{\varepsilon}_0^1) - (\bar{\varepsilon}_1^0 - \bar{\varepsilon}_0^0)$$

To obtain a consistent estimator, we require that

$$\mathbf{E} [(\bar{\varepsilon}_1^1 - \bar{\varepsilon}_0^1) - (\bar{\varepsilon}_1^0 - \bar{\varepsilon}_0^0)] = 0$$

- The treated units can have different *levels* of the error term, but the *change* in the error term must be random
- Two approaches to validate the common trend assumption: **placebo policies** and **add group-specific time trends**

Placebo Policies

- *A popular strategy for robustness check*: if a policy was enacted in say 2010 you could pretend it was enacted in 2005 in the same place and then only use data through 2009
- The easiest (and most common) is in the Event framework: include leads as well as lags in the model (Bertrand, Duflo, Mullainathan, 2004, QJE)
- To implement it you can run a regression like:

$$Y_i = \beta_0 + \sum_{j=-\tilde{J}, j \neq -1}^J \alpha_j \tau_{t_i-j}(g_i) + \delta_{g_i} + \rho_{t_i} + \varepsilon_i$$

where $t_i = -\tilde{J}, \dots, J$ and the period of enactment to be zero

- ▶ $\tau_{t_i-j}^1 = 1$ whenever $t_i - j = 0$
- ▶ Note $\sum_{j=-\tilde{J}}^J \tau_{t_i-j}(g_i) = \delta_{g_i}$, so we drop one period to avoid perfect co-linearity

If we normalize $\alpha_{-1} = 0$, α_{-2} is estimated as

$$\hat{\alpha}_{-2} = (\bar{Y}_{-2}^1 - \bar{Y}_{-1}^1) - (\bar{Y}_{-2}^0 - \bar{Y}_{-1}^0)$$

where

$$\bar{Y}_{-2}^1 = \hat{\beta}_0 + \hat{\alpha}_{-2} + \hat{\delta} + \hat{\rho}_{-2}$$

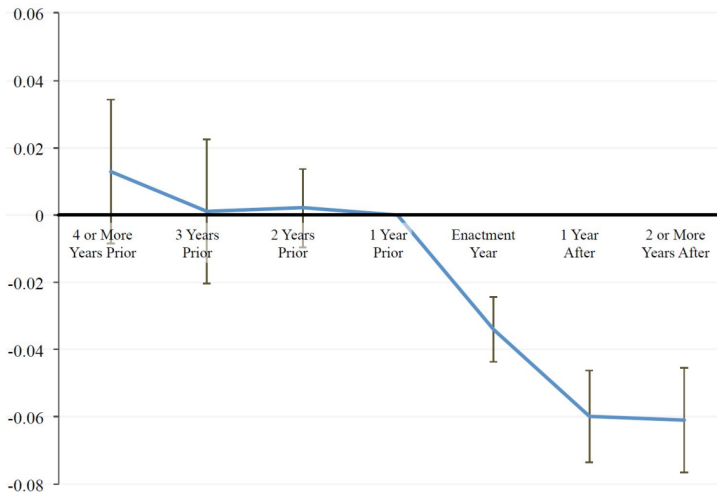
$$\bar{Y}_{-1}^1 = \hat{\beta}_0 + \hat{\delta} + \hat{\rho}_{-1}$$

$$\bar{Y}_{-2}^0 = \hat{\beta}_0 + \hat{\rho}_{-2}$$

$$\bar{Y}_{-1}^0 = \hat{\beta}_0 + \hat{\rho}_{-1}$$

- $\hat{\alpha}_{-2}$ should be zero under the common trend assumption
- $\hat{\alpha}_{-j} (j \geq 2)$ should also be zero under the common trend assumption

Figure 1: Typical event studies for the placebo policies



Group-Specific Time Trends

- One might be worried that units that are trending up or trending down are more likely to change policy
- One can include group \times time dummy variables in the model to fix this problem
- Now let's consider the three-period case where the policy happens between period 1 and 2, the model becomes

$$Y_i = \beta_0 + \alpha \tau_{t_i}(g_i) + \delta_0 t_i \times (1 - g_i) + \delta_1 t_i \times g_i + \delta_2 \mathbb{I}(t_i = 2) + \gamma g_i + \varepsilon_i$$

- We can write the estimator of α as a Triple Difference (DDD):

$$\begin{aligned}\hat{\alpha}_{DDD} &= (\bar{Y}_2^1 - \bar{Y}_1^1) - (\bar{Y}_2^0 - \bar{Y}_1^0) - [(\bar{Y}_1^1 - \bar{Y}_0^1) - (\bar{Y}_1^0 - \bar{Y}_0^0)] \\ &\approx (\alpha + \delta_1 + \delta_2) - (\delta_0 + \delta_2) - (\delta_1 - \delta_0) \\ &= \alpha\end{aligned}$$

If we do not add the group-specific time trends, the error term is a composite:

$$\tilde{\varepsilon}_i = \varepsilon_i + \delta_0 t_i \times (1 - g_i) + \delta_1 t_i \times g_i - \delta t_i$$

We go back to the common trend assumption and get

$$\begin{aligned} \mathbf{E}((\bar{\tilde{\varepsilon}}_1^1 - \bar{\tilde{\varepsilon}}_1^0) - (\bar{\tilde{\varepsilon}}_1^0 - \bar{\tilde{\varepsilon}}_0^0)) &= \mathbf{E}((\bar{\varepsilon}_1^1 - \bar{\varepsilon}_1^0) - (\bar{\varepsilon}_1^0 - \bar{\varepsilon}_0^0)) \\ &\quad + (\delta_1 - \delta) - (\delta_0 - \delta) \\ &= \mathbf{E}((\bar{\varepsilon}_1^1 - \bar{\varepsilon}_1^0) - (\bar{\varepsilon}_1^0 - \bar{\varepsilon}_0^0)) + \delta_1 - \delta_0 \\ &\approx \delta_1 - \delta_0 \neq 0 \end{aligned}$$

Thus the common trend assumption is likely to fail!

Inference: Get the Right Standard Errors

- In applications, we often have individual data (people, firms...) and the policy is enacted at more aggregated level (cities, provinces)
- It seems that we have more data than we need

Consider the individual-level model

$$Y_i = \alpha \tau_{t_i}(g_i) + Z_i' \delta + X_{g_i t_i}' \beta + \theta_{g_i} + \gamma_{t_i} + u_i$$

One could aggregate the data by group and year:

$$\bar{Y}_{gt} = \alpha \bar{\tau}_{gt} + Z_{gt}' \delta + X_{gt}' \beta + \theta_g + \gamma_t + \bar{u}_{gt}$$

The second regression also gives consistent estimates for the treatment effects

- **HOWEVER, two regressions yield different standard errors: which one should we use?**

- The error term for the individual level model is

$$u_i = \eta_{g_i t_i} + \varepsilon_i$$

- ▶ The i.i.d assumption for error term u_i is violated if $\eta_{g_i t_i}$ exists
- ▶ Standard solution: *Cluster the standard error by group*×year to allow for arbitrary correlation within a group
- Bertrand, Duflo, and Mullainathan (QJE, 2004):
 - ▶ If there is serial correlation in η_{gt} , cluster by group×year is problematic
- *Solutions:*
 - ▶ **# of groups is large:** block bootstrap by state works well
 - ▶ **Moderate # of states:** asymptotic approximation of the variance-covariance matrix
 - ▶ **Small # of states:** collapse the data into a “pre”- and “post”-period and account for the effective sample size
- A practitioner's guide is offered by Cameron and Miller (2015, JHR)