Lab 1, Short Question

Contents

```
1 Political ideology (30 points)
                                                          \mathbf{2}
  3
  library(tidyverse)
library(ggplot2)
library(stargazer)
if(!"psych"%in%rownames(installed.packages())) {install.packages("psych")}
library("psych")
if(!"car"%in%rownames(installed.packages())) {install.packages("car")}
library(car)
theme_set(theme_bw()) # set the theme (theme_set is built inside ggplot2)
## To do hypothesis testing in ordinal regression model
if(!"ordinal"%in%rownames(installed.packages())) {install.packages("ordinal")}
if(!"stargazer"%in%rownames(installed.packages())) {install.packages("stargazer")}
library(stargazer)
library(ordinal)
## provides many functions useful for data analysis, high-level graphics, utility operations
library(Hmisc)
## to work with "grid" graphics
library(gridExtra)
## provides function to for Visualization techniques, summary and inference procedures such as
library(vcd)
## for multinomial log-linear models.
library(nnet)
## To use plor()
library(MASS)
## To generate regression results tables and plots
if(!"finalfit"%in%rownames(installed.packages())) {install.packages("finalfit")}
library(finalfit)
```

1 Political ideology (30 points)

These questions are based on Question 14 of Chapter 3 of the textbook "Analysis of Categorical Data with R" by Bilder and Loughin.

An example from Section 4.2.5 examines data from the 1991 U.S. General Social Survey that cross-classifies people according to

- Political ideology: Very liberal (VL), Slightly liberal (SL), Moderate (M), Slightly conservative (SC), and Very conservative (VC)
- Political party: Democrat (D) or Republican (R)
- Gender: Female (F) or Male (M).

Consider political ideology to be a response variable, and political party and gender to be explanatory variables. The data are available in the file pol_ideol_data.csv.

1.1 Recode Data (2 points)

Value

D

R

Use the factor() function with the ideology variable to ensure that R places the levels of the ideology variable in the correct order.

```
pol_ideol_data <- read.csv("~/mids_271/spring_24_central/Labs/Lab_1/data/pol_ideol_data.csv", I</pre>
head(pol_ideol_data)
##
    gender party ideol count
## 1
         F
               D
                    VL
                         44
## 2
         F
               D
                    SL
                         47
## 3
         F
               D
                    Μ
                        118
         F
## 4
               D
                   SC
                         23
## 5
         F
               D
                    VC
                         32
         F
## 6
               R
                    VL
                         18
describe(pol_ideol_data)
## pol_ideol_data
##
##
     Variables
                        Observations
##
##
  gender
##
           missing distinct
         n
##
        20
##
               F
## Value
                  M
## Frequency
              10
                  10
## Proportion 0.5 0.5
  ______
## party
##
            missing distinct
         n
##
        20
                  0
##
```

```
## Frequency
              10 10
## Proportion 0.5 0.5
## ideol
##
           missing distinct
##
         20
                  0
##
## Value
               M SC
                      SL
                         VC
                              ٧L
## Frequency
               4
                   4
                       4
                           4
## Proportion 0.2 0.2 0.2 0.2 0.2
##
  count
                                                              .05
##
         n
            missing distinct
                                 Info
                                          Mean
                                                    Gmd
                                                                      .10
##
         20
                  0
                          17
                                0.996
                                         41.75
                                                  26.57
                                                           17.70
                                                                    18.00
        .25
                                   .90
##
                 .50
                         .75
                                            .95
##
      23.00
              37.50
                       48.75
                                64.40
                                         87.60
##
## Value
               12
                     18
                         23
                                   32
                                             36
                              28
                                        34
                                                  39
                                                       44
                                                            45
                                                                      48
                                                                           51
                1
                          2
                                                        1
                                                             1
                                                                  1
                                                                       1
                                                                            1
## Frequency
                     3
                               1
                                    1
                                         1
                                              1
                                                   1
##
## Value
               53
                     62
                         86
                             118
## Frequency
                1
                      1
                           1
## Proportion 0.05 0.05 0.05 0.05
##
## For the frequency table, variable is rounded to the nearest 0
#Converting the ideology variable to factor
pol_ideol_data$ideol<- factor(pol_ideol_data$ideol)</pre>
pol_ideol_data$gender <- factor(pol_ideol_data$gender)</pre>
pol_ideol_data$party <- factor(pol_ideol_data$party)</pre>
typeof(pol_ideol_data$ideol) #This comes out as an integer. Should it come out as a factor?
## [1] "integer"
summary(pol_ideol_data$ideol)
##
   M SC SL VC VL
##
   4
      4
         4
            4
```

1.2 Test for Independence (5 points)

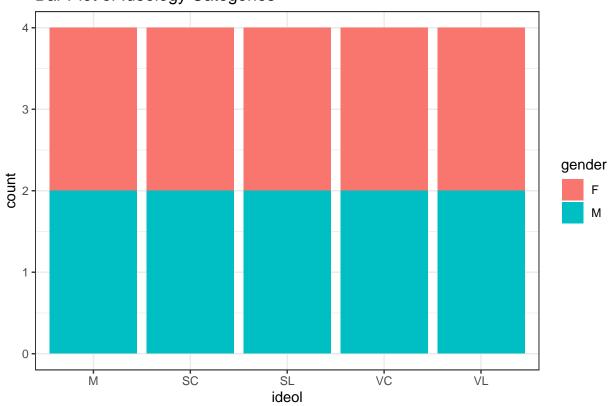
Analyze the relationships between political ideology and political party and gender using basic visualizations. Afterward, generate a contingency table and assess the independence of political ideology from political party and gender.

Comment: The null hypothesis is $H_0: \pi_{i,j} = \pi_{i+}\pi_{+j}$ for each i,j vs. $H_a: \pi_{i,j} \neq \pi_{i+}\pi_{+j}$. According

the chi-square test statistic, the null hypothesis is rejected (p<0.05) for all three relationships. There is independence among the variables.

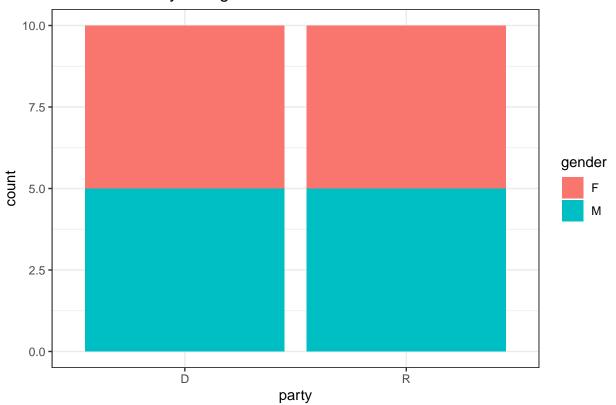
```
#Plots of party and idology with gender identified in each bar plot
p1<- pol_ideol_data %>%
    ggplot(aes(x=ideol, fill = gender)) + geom_bar() + labs(title = "Bar Plot of Ideology Category)
p1
```

Bar Plot of Ideology Categories



```
p2 <- pol_ideol_data %>%
    ggplot(aes(x=party, fill = gender)) + geom_bar() + labs(title = "Bar Plot of Party Categories)
p2
```

Bar Plot of Party Categories



```
print("Contingency table for gender and ideology")
## [1] "Contingency table for gender and ideology"
t1 <- xtabs(formula = count ~ gender + ideol, data = pol_ideol_data)</pre>
t1
##
         ideol
## gender
            M SC
                  SL
                       VC
                           VL
        F 204
##
               62
                   75
                       80
                           62
        M 115 63 52 74 48
print("Contingency table for party and ideology")
## [1] "Contingency table for party and ideology"
```

```
t2 <- xtabs(formula = count ~ party + ideol, data = pol_ideol_data) #+ labs(title = "Contingen
t2
##
        ideol
## party
           M SC
                      VC
                          VL
                  SL
##
       D 171
              41
                  81
                      55
                          80
##
       R 148
             84
                  46
                      99
                          30
print("Contingency table for party and gender")
```

[1] "Contingency table for party and gender"

```
t3 <- xtabs(formula = count ~ party + gender, data = pol_ideol_data)
        gender
##
## party F M
       D 264 164
##
       R 219 188
#Chi-Square test of independence
ind.test.1 <- chisq.test(x = t1, correct = FALSE)</pre>
ind.test.2 <- chisq.test(x = t2, correct = FALSE)</pre>
ind.test.3 <- chisq.test(x = t3, correct = FALSE)</pre>
ind.test.1
##
## Pearson's Chi-squared test
##
## data: t1
## X-squared = 10.732, df = 4, p-value = 0.02975
ind.test.2
##
## Pearson's Chi-squared test
##
## data: t2
## X-squared = 60.905, df = 4, p-value = 1.872e-12
ind.test.3
##
## Pearson's Chi-squared test
##
## data: t3
## X-squared = 5.3041, df = 1, p-value = 0.02128
\#An alternative way to calculate log-likelihood and chi-square
library(package = vcd)
lrt1 <- assocstats(x = t1)</pre>
lrt2 <- assocstats(x = t2)</pre>
lrt3 <- assocstats(x = t3)</pre>
lrt1
                       X^2 df P(> X^2)
## Likelihood Ratio 10.743 4 0.029609
## Pearson 10.732 4 0.029751
##
## Phi-Coefficient : NA
## Contingency Coeff.: 0.113
## Cramer's V : 0.113
```

```
1rt2
##
                       X^2 df
                                P(> X^2)
## Likelihood Ratio 62.333 4 9.3758e-13
## Pearson
                    60.905 4 1.8719e-12
##
## Phi-Coefficient
                     : NA
## Contingency Coeff.: 0.261
## Cramer's V
                     : 0.27
1rt3
##
                       X^2 df P(> X^2)
## Likelihood Ratio 5.3081 1 0.021227
## Pearson
                    5.3041 1 0.021275
##
## Phi-Coefficient
                     : 0.08
## Contingency Coeff.: 0.079
## Cramer's V
                     : 0.08
```

1.3 Regression analysis (5 points)

Estimate a multinomial regression model and ordinal (proportional odds) regression model that both include party, gender, and their interaction. Perform Likelihood Ratio Tests (LRTs) to test the importance of each explanatory variable.

Also, test whether the proportional odds assumption in the ordinal model is satisfied. Based on this test and other results, which model do you think is more valid?

Comment: The multinomial regression model is weighted by the count of people in each category. The categorization (in no particular order) of political ideology is regressed against party affiliation, gender, and the interaction of gender and party.

```
#Multinomial regression
library(package = nnet)
mlmodel <- multinom(formula = ideol ~ gender + party + party:gender, weights = count, data = p
## # weights: 25 (16 variable)
## initial value 1343.880657
## iter 10 value 1230.618951
## iter 20 value 1229.545101
## final value 1229.543342
## converged
summary(mlmodel)
## Call:
## multinom(formula = ideol ~ gender + party + party:gender, data = pol_ideol_data,
##
       weights = count)
##
## Coefficients:
```

```
(Intercept)
                              partyR genderM:partyR
##
                  genderM
## SC -1.6351796 0.5552530 0.8443896
                                       -0.08493261
## SL -0.9205509 0.4766365 -0.2015820
                                       -0.59127885
## VC -1.3049495 0.4701437 0.7218048
                                       -0.08231277
## VL -0.9864951 0.5997181 -0.5774785
                                       -0.67796167
##
## Std. Errors:
     (Intercept)
                  genderM
                             partyR genderM:partyR
      0.2279304 0.3554943 0.2986994
## SC
                                        0.4494401
## SL 0.1724860 0.2793397 0.2776568
                                        0.4439118
## VC 0.1993102 0.3194857 0.2686741
                                       0.4126370
                                      0.4944618
## VL 0.1766403 0.2790119 0.3136642
##
## Residual Deviance: 2459.087
## AIC: 2491.087
#Ordinal Regression
levels(pol_ideol_data$ideol) #Checking order of dependent variable levels
## [1] "M" "SC" "SL" "VC" "VL"
pol_ideol_data$ideol.order <- factor(pol_ideol_data$ideol, levels = c("VL", "SL", "M", "SC", "
levels(pol_ideol_data$ideol.order)
## [1] "VL" "SL" "M" "SC" "VC"
library(package = MASS)
ord.model <- polr( formula = ideol.order ~ gender + party:gender, data = pol_ideol_data
summary(ord.model)
##
## Re-fitting to get Hessian
## Call:
## polr(formula = ideol.order ~ gender + party + party:gender, data = pol_ideol_data,
      weights = count, method = "logistic")
##
##
## Coefficients:
                  Value Std. Error t value
##
## genderM
                 -0.1431
                            0.1820 -0.7861
## partyR
                 0.7562
                            0.1659 4.5593
## genderM:partyR 0.5091
                            0.2550 1.9965
##
## Intercepts:
        Value
                Std. Error t value
## VL|SL -1.5521 0.1332 -11.6560
## SL|M -0.5550 0.1157
                            -4.7965
## M|SC
          1.1647
                  0.1226
                             9.5009
```

```
## SCIVC 2.0012 0.1364
                              14.6666
##
## Residual Deviance: 2470.15
## AIC: 2484.15
print("The likelihood ratio tests for the multinomial parameters")
## [1] "The likelihood ratio tests for the multinomial parameters"
Anova (mlmodel)
## Analysis of Deviance Table (Type II tests)
##
## Response: ideol
##
                LR Chisq Df Pr(>Chisq)
                  8.965 4
## gender
                              0.06198 .
                  60.555 4 2.218e-12 ***
## party
                               0.51763
## gender:party
                  3.245 4
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
print("The likelihood ratio tests for the ordinal parameters")
## [1] "The likelihood ratio tests for the ordinal parameters"
Anova(ord.model)
## Analysis of Deviance Table (Type II tests)
## Response: ideol.order
##
               LR Chisq Df Pr(>Chisq)
## gender
                  0.843 1
                               0.35864
                  56.847 1 4.711e-14 ***
## party
                  3.992 1
## gender:party
                               0.04571 *
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
#nominal_test(ord.model)
#Is the proportional odds assumption satisfied?
#Can use nominal test
mod.ord2 <- clm(ideol.order ~ gender + party + party:gender, data = pol_ideol_data)</pre>
nominal_test(mod.ord2)
## Tests of nominal effects
## formula: ideol.order ~ gender + party + party:gender
                              AIC LRT Pr(>Chi)
                Df logLik
                  -32.189 78.378
## <none>
```

```
## gender 3 -32.189 84.378 0 1
## party 3 -32.189 84.378 0 1
## gender:party 9 -32.189 96.378 0 1
```

1.4 Estimated probabilities (5 points)

Compute the estimated probabilities for each ideology level given all possible combinations of the party and gender levels.

```
#Odds of each ideology given the possible combinations of party and gender levels....
v.table <- xtabs(formula = count ~ ideol.order + gender + party, data = pol_ideol_data)
v.table
## , , party = D</pre>
```

```
##
##
               gender
## ideol.order
                   F
                  44
                      36
##
             VL
             SL
                 47
                      34
##
                 118
                      53
##
             Μ
             SC
                  23
##
                      18
##
             VC
                  32
                      23
##
##
   , , party = R
##
##
               gender
## ideol.order
                   F
                       М
##
             VL
                  18
                      12
##
             SL
                  28
                      18
##
                      62
             Μ
                  86
             SC
##
                  39
                      45
##
             VC
                  48
                      51
ideol.prob <- v.table/rowSums(v.table)</pre>
ideol.prob
```

```
## , , party = D
##
##
              gender
## ideol.order
                        F
                                  М
##
            VL 0.4000000 0.3272727
##
            SL 0.3700787 0.2677165
##
            M 0.3699060 0.1661442
            SC 0.1840000 0.1440000
##
            VC 0.2077922 0.1493506
##
##
##
  , , party = R
##
##
              gender
```

```
## ideol.order F M
## VL 0.1636364 0.1090909
## SL 0.2204724 0.1417323
## M 0.2695925 0.1943574
## SC 0.3120000 0.3600000
## VC 0.3116883 0.3311688
```

1.5 Contingency table of estimated counts (5 points)

Construct a contingency table with estimated counts from the model. These estimated counts are found by taking the estimated probability for each ideology level multiplied by their corresponding number of observations for a party and gender combination.

For example, there are 264 observations for gender = "F" and party = "D". Because the multinomial regression model results in $\hat{\pi}_{VL} = 0.1667$, this model's estimated count is $0.1667 \times 264 = 44$.

• Are the estimated counts the same as the observed? Conduct a goodness of fit test for this and explain the results.

```
#Convert contingency table to data frame
v.flat <- ftable(v.table, row.vars = c("gender", "party"), col.vars = c("ideol.order"))</pre>
DF <- as.data.frame(v.flat )</pre>
pi.hat <- predict(object = mlmodel, newdata = DF, type = "probs")</pre>
pi.hat
##
              Μ
                       SC
                                 SL
                                            VC
## 1
     0.4469704 0.0871223 0.1780281 0.1212122 0.16666692
     0.3231705 0.1097553 0.2073204 0.1402427 0.21951113
     0.3926937 0.1780812 0.1278550 0.2191782 0.08219185
     0.3297877 0.2393626 0.0957436 0.2712756 0.06383054
     0.4469704 0.0871223 0.1780281 0.1212122 0.16666692
     0.3231705 0.1097553 0.2073204 0.1402427 0.21951113
     0.3926937 0.1780812 0.1278550 0.2191782 0.08219185
     0.3297877 0.2393626 0.0957436 0.2712756 0.06383054
     0.4469704 0.0871223 0.1780281 0.1212122 0.16666692
  10 0.3231705 0.1097553 0.2073204 0.1402427 0.21951113
## 11 0.3926937 0.1780812 0.1278550 0.2191782 0.08219185
## 12 0.3297877 0.2393626 0.0957436 0.2712756 0.06383054
  13 0.4469704 0.0871223 0.1780281 0.1212122 0.16666692
  14 0.3231705 0.1097553 0.2073204 0.1402427 0.21951113
## 15 0.3926937 0.1780812 0.1278550 0.2191782 0.08219185
## 16 0.3297877 0.2393626 0.0957436 0.2712756 0.06383054
## 17 0.4469704 0.0871223 0.1780281 0.1212122 0.16666692
## 18 0.3231705 0.1097553 0.2073204 0.1402427 0.21951113
## 19 0.3926937 0.1780812 0.1278550 0.2191782 0.08219185
## 20 0.3297877 0.2393626 0.0957436 0.2712756 0.06383054
estprob <- data.frame(gender = DF[1:4,], party = DF[1:4, 2], round(pi.hat, 4))
```

Warning in data.frame(gender = DF[1:4,], party = DF[1:4, 2], round(pi.hat, :

row names were found from a short variable and have been discarded estprob

```
##
      gender.gender gender.party gender.ideol.order gender.Freq party
                                                                                Μ
## 1
                   F
                                 D
                                                    VL
                                                                        D 0.4470
## 2
                   Μ
                                 D
                                                    ٧L
                                                                 36
                                                                        D 0.3232
                   F
## 3
                                 R
                                                    VL
                                                                 18
                                                                        R 0.3927
## 4
                   М
                                 R
                                                    VL
                                                                 12
                                                                        R 0.3298
## 5
                   F
                                 D
                                                    VL
                                                                 44
                                                                        D 0.4470
## 6
                   М
                                                    VL
                                                                        D 0.3232
                                 D
                                                                 36
## 7
                   F
                                 R
                                                    VL
                                                                 18
                                                                        R 0.3927
## 8
                                                    VL
                                                                 12
                                                                        R 0.3298
                   Μ
                                 R
                   F
## 9
                                                                        D 0.4470
                                 D
                                                    VL
                                                                 44
## 10
                   М
                                 D
                                                    VL
                                                                 36
                                                                        D 0.3232
                   F
                                                                        R 0.3927
## 11
                                 R
                                                    VL
                                                                 18
## 12
                   М
                                 R
                                                    VL
                                                                 12
                                                                        R 0.3298
## 13
                   F
                                                    VL
                                                                 44
                                                                        D 0.4470
                                 D
## 14
                   М
                                 D
                                                    VL
                                                                 36
                                                                        D 0.3232
                                                    VL
## 15
                   F
                                 R
                                                                 18
                                                                        R 0.3927
## 16
                   Μ
                                 R
                                                    VL
                                                                 12
                                                                        R 0.3298
                   F
                                                                        D 0.4470
## 17
                                 D
                                                    VL
                                                                 44
## 18
                   Μ
                                 D
                                                    VL
                                                                 36
                                                                        D 0.3232
                   F
## 19
                                 R
                                                    VL
                                                                 18
                                                                        R 0.3927
## 20
                   Μ
                                 R
                                                    VL
                                                                 12
                                                                        R 0.3298
##
          SC
                  SL
                         VC
                                 VL
## 1
     0.0871 0.1780 0.1212 0.1667
     0.1098 0.2073 0.1402 0.2195
     0.1781 0.1279 0.2192 0.0822
     0.2394 0.0957 0.2713 0.0638
     0.0871 0.1780 0.1212 0.1667
## 5
     0.1098 0.2073 0.1402 0.2195
      0.1781 0.1279 0.2192 0.0822
     0.2394 0.0957 0.2713 0.0638
## 9 0.0871 0.1780 0.1212 0.1667
## 10 0.1098 0.2073 0.1402 0.2195
## 11 0.1781 0.1279 0.2192 0.0822
## 12 0.2394 0.0957 0.2713 0.0638
## 13 0.0871 0.1780 0.1212 0.1667
## 14 0.1098 0.2073 0.1402 0.2195
## 15 0.1781 0.1279 0.2192 0.0822
## 16 0.2394 0.0957 0.2713 0.0638
## 17 0.0871 0.1780 0.1212 0.1667
## 18 0.1098 0.2073 0.1402 0.2195
## 19 0.1781 0.1279 0.2192 0.0822
## 20 0.2394 0.0957 0.2713 0.0638
#estimate counts
```

est.count <- round(estprob[,6:10]*v.flat[,0:5], 1)</pre>

```
est.count
##
         Μ
             SC
                   SL
                        VC
                             VL
## 1
      19.7
            3.8
                 7.8
                       5.3
                            7.3
  2
            2.0
                 3.7
                       2.5
##
       5.8
                            4.0
##
      14.1
            6.4
                 4.6
                       7.9
                            3.0
## 4
       4.0
            2.9
                  1.1
                       3.3
                            0.8
                 8.4
## 5
      21.0
            4.1
                       5.7
                            7.8
  6
       9.0
            3.1
                  5.8
                       3.9
                            6.1
##
  7
      13.4
            6.1
                 4.3
                       7.5
                            2.8
## 8
       5.9
            4.3
                 1.7
                       4.9
                            1.1
## 9
      52.7 10.3 21.0 14.3 19.7
## 10 27.8
           9.4 17.8 12.1 18.9
## 11 20.8 9.4
                 6.8 11.6
## 12 20.4 14.8
                 5.9 16.8
           2.0
## 13 10.3
                 4.1
                       2.8
## 14 12.6
            4.3
                 8.1
                       5.5
## 15
       7.1
            3.2
                 2.3
                       3.9
                            1.5
## 16 14.8 10.8
                 4.3 12.2
                            2.9
## 17 14.3
            2.8
                 5.7
                       3.9
                            5.3
## 18 15.5
            5.3 10.0
                       6.7 10.5
## 19
      9.0 4.1
                 2.9
                       5.0
                            1.9
## 20 16.8 12.2 4.9 13.8
                            3.3
chisq.test(x = est.count, correct = FALSE)
## Warning in chisq.test(x = est.count, correct = FALSE): Chi-squared
## approximation may be incorrect
##
##
    Pearson's Chi-squared test
##
## data:
          est.count
## X-squared = 76.543, df = 76, p-value = 0.461
```

1.6 Odds ratios and confidence intervals (8 points)

To better understand relationships between the explanatory variables and the response, compute odds ratios and their confidence intervals from the estimated models and interpret them.

Comment: The odds ratios for a given variable, depend on the category of comparison (e.g., VL, SL, N, SC, or VL). In the multinomial logit model, the left-out gender category was female and the left-out party category was democrat. The comparison level for ideology was 'Neutral.' We compare the odds of the different coefficients for the coefficients from each VL, SL, SC, and VL level. Assuming the model specification $\log(\pi_j/\pi_1) = \beta_{j0} + \beta_{jGender}x_{Gender} + \beta_{jParty} + \beta_{jGender*Party}$ where j = SC, SL, VC, VL.

The Odds Ratio for male versus female for the each jth level is equal to $\frac{exp(\beta_{j0}+\beta_{j1}*(gender+c)+\beta_{j3}*party*(gender+c))}{exp(\beta_{j0}+\beta_{j1}*gender+\beta_{j3}*party*gender)} = \frac{exp(\beta_{j0}+\beta_{j1}*(gender+c)+\beta_{j3}*party*(gender+c))}{exp(\beta_{j0}+\beta_{j1}*gender+\beta_{j3}*party*gender)} = \frac{exp(\beta_{j0}+\beta_{j1}*(gender+c)+\beta_{j3}*party*(gender+c))}{exp(\beta_{j0}+\beta_{j1}*gender+\beta_{j3}*party*gender)} = \frac{exp(\beta_{j0}+\beta_{j1}*(gender+c)+\beta_{j3}*party*(gender+c))}{exp(\beta_{j0}+\beta_{j1}*gender+\beta_{j3}*party*gender)} = \frac{exp(\beta_{j0}+\beta_{j1}*gender+\beta_{j3}*party*gender+\beta_{j3}*party*gender)}{exp(\beta_{j0}+\beta_{j1}*gender+\beta_{j3}*party*gender+\beta_{j3}*gender+\beta_{j3}*gender+\beta_{j3$

 $exp(\beta_{j1}*c+\beta_{j3}*party*c)$ where c = 1 for a categorical variable. Further, gender will be equal to one as it is also a categorical variable.

```
The Odds Ratio for republican versus democrat for each jth level is equal to \frac{exp(\beta_{j0}+\beta_{j2}*(party+c)+\beta_{j3}*gender*(party+c))}{exp(\beta_{j0}+\beta_{j2}*(party+c)+\beta_{j3}*gender*(party+c))}
exp(\beta_{j2}*c+\beta_{j3}*gender*c) where c=1.
## [1] "M" "SC" "SL" "VC" "VL"
## [1] "model summary"
## Call:
   multinom(formula = ideol ~ gender + party + party:gender, data = pol_ideol_data,
##
        weights = count)
##
## Coefficients:
##
       (Intercept)
                       genderM
                                     partyR genderM:partyR
##
        -1.6351796 0.5552530
                                 0.8443896
                                                 -0.08493261
       -0.9205509 0.4766365 -0.2015820
                                                 -0.59127885
        -1.3049495 0.4701437 0.7218048
                                                 -0.08231277
##
        -0.9864951 0.5997181 -0.5774785
                                                 -0.67796167
##
## Std. Errors:
       (Intercept)
                                    partyR genderM:partyR
##
                       genderM
## SC
         0.2279304 0.3554943 0.2986994
                                                  0.4494401
## SL
         0.1724860 0.2793397 0.2776568
                                                  0.4439118
## VC
         0.1993102 0.3194857 0.2686741
                                                  0.4126370
## VL
         0.1766403 0.2790119 0.3136642
                                                  0.4944618
##
## Residual Deviance: 2459.087
## AIC: 2491.087
## [1] "beta_hats"
##
       (Intercept)
                       genderM
                                     partyR genderM:partyR
## SC
        -1.6351796 0.5552530
                                 0.8443896
                                                 -0.08493261
   SL
       -0.9205509 0.4766365 -0.2015820
                                                 -0.59127885
       -1.3049495 0.4701437 0.7218048
## VC
                                                 -0.08231277
       -0.9864951 0.5997181 -0.5774785
                                                 -0.67796167
```

Table Odds Ratios for Gender

Generally, there are higher odds men will be rated as either slightly or very conservative rather than neutral compared to women. Men are more likely to fall in the conservative categories instead of the neutral category if they are republicans, rather than democrats. Men were much more likely than women to be in the liberal categories instead of the neutral category conditional if they were classified as democrat. Generally, republican women than democratic women to be in the the conservative categories rather than neutral. Democrats are

```
ideology_labels <- c('SC', 'SC', 'SC', 'SL', 'SL', 'SL', 'VC', 'VC', 'VC', 'VL', 'VL', 'VL')</pre>
gender_labels <- c('Male', 'Male', 'Female', 'Male', 'Male', 'Female', 'Male', 'Female', 'Female', 'Female', 'Female', 'Male', 'Female', 'Male', 'Female', 'Male', 'Male', 'Female', 'Male', 'Mal
party_labels <- c('Rep', 'Dem', 'Rep', 'Rep', 'Dem', 'Rep', 'Dem', 'Rep', 'Rep', 'Rep', 'Rep', 'Pem', 'Rep', 
odds_ratio_gender <- c(sc.beta.male.rep, sc.beta.male.dem ,sc.beta.fem.rep, sl.beta.male.rep, s
gender_odds <- data.frame(Ideology = ideology_labels, Gender = gender_labels, Party = party_la</pre>
gender_odds
##
                                      Ideology Gender Party OR.hat
## 1
                                                                             SC
                                                                                                             Male
                                                                                                                                                           Rep 1.6005
## 2
                                                                             SC
                                                                                                             Male
                                                                                                                                                           Dem 1.7424
## 3
                                                                             SC Female
                                                                                                                                                          Rep 0.9186
## 4
                                                                             SL
                                                                                                             Male
                                                                                                                                                          Rep 0.8917
## 5
                                                                             SL
                                                                                                             Male
                                                                                                                                                          Dem 1.6106
## 6
                                                                            SL Female
                                                                                                                                                          Rep 0.5536
## 7
                                                                             VC
                                                                                                            Male
                                                                                                                                                          Rep 1.4738
## 8
                                                                             VC
                                                                                                            Male
                                                                                                                                                          Dem 1.6002
## 9
                                                                             VC Female
                                                                                                                                                          Rep 0.9210
```

Table of Odds Ratio for Party

VL

VL

Male

Male

VL Female

10

11

12

Adults were more likely to be in conservative categories compared to the neutral category if they were republican. If someone is republican and male, the likelihood of being slightly conservative rather than neutral is 2.13. A woman who is republican is even more likely to be slightly conservative than neutral conditional on republican party membership or her odds ratio is 2.33. Conditional on male gender, democrats are less likely to be in any category compared to Neutral.

Rep 0.9247

Dem 1.8216

Rep 0.5077

```
odds_ratio_party <- c(sc.beta.rep.male, sc.beta.rep.fem,sc.beta.dem.male, sl.beta.rep.male, sl
party_table_party_labels <- c('Republican', 'Republican', 'Democrat', 'Republican', 'Republican'
party_table_gender_labels <- c('Male', 'Female', 'Male', 'Male', 'Female', 'Male', 'Male', 'Female', 'Male', 'Male', 'Female', 'Male', 'Female', 'Male', 'Female', 'Male', 'Male',
```

```
##
      Ideology
                   Gender
                          Party OR.hat
## 1
            SC Republican
                             Male 2.1371
## 2
            SC Republican Female 2.3266
## 3
            SC
                 Democrat
                             Male 0.9186
## 4
            SL Republican
                             Male 0.4525
## 5
            SL Republican Female 0.8174
## 6
            SL
                 Democrat
                             Male 0.5536
## 7
            VC Republican
                             Male 1.8955
```

```
## 8
            VC Republican Female 2.0581
## 9
            VC
                 Democrat
                            Male 0.9210
## 10
            VL Republican
                            Male 0.2850
## 11
            VL Republican Female 0.5613
## 12
                 Democrat
            VL
                             Male 0.5077
##Confidence Intervals for Odds Ratios
conf.beta <- confint(object = mlmodel, level = 0.95)</pre>
conf.beta #Results are in 3-D array
## , , SC
##
                                  97.5 %
##
                        2.5 %
## (Intercept)
                  -2.0819150 -1.1884441
## genderM
                  -0.1415030 1.2520090
## partyR
                   0.2589495
                               1.4298298
## genderM:partyR -0.9658190 0.7959538
## , , SL
##
##
                         2.5 %
                                   97.5 %
## (Intercept)
                  -1.25861721 -0.5824845
## genderM
                  -0.07085921
                                1.0241321
## partyR
                  -0.74577933 0.3426154
## genderM:partyR -1.46133007 0.2787724
##
## , , VC
##
##
                       2.5 %
                                  97.5 %
## (Intercept)
                  -1.6955903 -0.9143088
## genderM
                  -0.1560368 1.0963242
## partyR
                   0.1952132
                               1.2483964
## genderM:partyR -0.8910664 0.7264409
##
##
  , , VL
##
##
                         2.5 %
                                    97.5 %
## (Intercept)
                  -1.33270378 -0.64028647
## genderM
                   0.05286477
                                1.14657140
## partyR
                  -1.19224905
                               0.03729199
## genderM:partyR -1.64708891
                               0.29116558
#Outcomes for Gender
varcov <- vcov(mlmodel)</pre>
varcov
##
                     SC: (Intercept)
                                       SC:genderM
                                                      SC:partyR SC:genderM:partyR
## SC:(Intercept)
                         0.051952281 -0.051952281 -0.051952281
                                                                      0.051952281
                        -0.051952281 0.126376177 0.051952281
## SC:genderM
                                                                     -0.126376177
```

```
0.089221361
                                                                      -0.089221361
## SC:partyR
                        -0.051952281
                                      0.051952281
  SC:genderM:partyR
                         0.051952281 -0.126376177 -0.089221361
                                                                       0.201996408
## SL:(Intercept)
                         0.008474562 -0.008474562 -0.008474562
                                                                       0.008474562
## SL:genderM
                        -0.008474562
                                      0.027342502
                                                   0.008474562
                                                                      -0.027342502
                                      0.008474562
  SL:partyR
                        -0.008474562
                                                   0.020102481
                                                                      -0.020102481
   SL:genderM:partyR
                         0.008474562 -0.027342502 -0.020102481
                                                                       0.055099430
  VC:(Intercept)
                         0.008474562 -0.008474562 -0.008474562
                                                                       0.008474562
                                                                      -0.027342502
## VC:genderM
                        -0.008474562
                                      0.027342502
                                                    0.008474562
## VC:partyR
                        -0.008474562
                                      0.008474562
                                                   0.020102481
                                                                      -0.020102481
## VC:genderM:partyR
                         0.008474562 -0.027342502 -0.020102481
                                                                       0.055099430
## VL:(Intercept)
                         0.008474562 -0.008474562 -0.008474562
                                                                       0.008474562
  VL:genderM
                        -0.008474562
                                      0.027342502
                                                    0.008474562
                                                                      -0.027342502
## VL:partyR
                        -0.008474562
                                      0.008474562
                                                    0.020102481
                                                                      -0.020102481
## VL:genderM:partyR
                         0.008474562 -0.027342502 -0.020102481
                                                                       0.055099430
##
                      SL: (Intercept)
                                       SL:genderM
                                                      SL:partyR SL:genderM:partyR
                         0.008474562 -0.008474562 -0.008474562
## SC:(Intercept)
                                                                       0.008474562
## SC:genderM
                        -0.008474562
                                      0.027342502
                                                    0.008474562
                                                                      -0.027342502
                                      0.008474562
                                                                      -0.020102481
## SC:partyR
                        -0.008474562
                                                    0.020102481
  SC:genderM:partyR
                         0.008474562 -0.027342502 -0.020102481
                                                                       0.055099430
  SL: (Intercept)
                                                                       0.029751418
                         0.029751418 -0.029751418 -0.029751418
## SL:genderM
                        -0.029751418
                                      0.078030645
                                                    0.029751418
                                                                      -0.078030645
## SL:partyR
                        -0.029751418
                                      0.029751418
                                                    0.077093303
                                                                      -0.077093303
  SL:genderM:partyR
                         0.029751418 -0.078030645 -0.077093303
                                                                       0.197057722
## VC:(Intercept)
                         0.008474562 -0.008474562 -0.008474562
                                                                       0.008474562
## VC:genderM
                        -0.008474562
                                      0.027342502
                                                                      -0.027342502
                                                   0.008474562
                        -0.008474562
## VC:partyR
                                      0.008474562
                                                   0.020102481
                                                                      -0.020102481
  VC:genderM:partyR
                         0.008474562 -0.027342502 -0.020102481
                                                                       0.055099430
## VL:(Intercept)
                         0.008474562 -0.008474562 -0.008474562
                                                                       0.008474562
## VL:genderM
                        -0.008474562
                                      0.027342502
                                                    0.008474562
                                                                      -0.027342502
                        -0.008474562
                                      0.008474562
                                                    0.020102481
                                                                      -0.020102481
  VL:partyR
##
   VL:genderM:partyR
                         0.008474562 -0.027342502 -0.020102481
                                                                       0.055099430
##
                                       VC:genderM
                     VC: (Intercept)
                                                      VC:partyR VC:genderM:partyR
## SC:(Intercept)
                         0.008474562 -0.008474562 -0.008474562
                                                                       0.008474562
                                      0.027342502
                                                                      -0.027342502
  SC:genderM
                        -0.008474562
                                                    0.008474562
## SC:partyR
                        -0.008474562
                                      0.008474562
                                                    0.020102481
                                                                      -0.020102481
  SC:genderM:partyR
                         0.008474562 -0.027342502 -0.020102481
                                                                       0.055099430
  SL: (Intercept)
                         0.008474562 -0.008474562 -0.008474562
                                                                       0.008474562
  SL:genderM
                                                                      -0.027342502
##
                        -0.008474562
                                      0.027342502
                                                   0.008474562
## SL:partyR
                        -0.008474562
                                      0.008474562
                                                   0.020102481
                                                                      -0.020102481
## SL:genderM:partyR
                         0.008474562 -0.027342502 -0.020102481
                                                                       0.055099430
## VC:(Intercept)
                         0.039724536 -0.039724536 -0.039724536
                                                                       0.039724536
## VC:genderM
                        -0.039724536
                                      0.102071124
                                                    0.039724536
                                                                      -0.102071124
## VC:partyR
                        -0.039724536
                                      0.039724536
                                                    0.072185777
                                                                      -0.072185777
## VC:genderM:partyR
                         0.039724536 -0.102071124 -0.072185777
                                                                       0.170269291
## VL:(Intercept)
                         0.008474562 -0.008474562 -0.008474562
                                                                       0.008474562
## VL:genderM
                        -0.008474562
                                      0.027342502
                                                   0.008474562
                                                                      -0.027342502
## VL:partyR
                        -0.008474562
                                      0.008474562
                                                   0.020102481
                                                                      -0.020102481
## VL:genderM:partyR
                         0.008474562 -0.027342502 -0.020102481
                                                                       0.055099430
```

```
##
                     VL: (Intercept)
                                       VL:genderM
                                                     VL:partyR VL:genderM:partyR
## SC:(Intercept)
                        0.008474562 -0.008474562 -0.008474562
                                                                      0.008474562
## SC:genderM
                       -0.008474562 0.027342502 0.008474562
                                                                     -0.027342502
## SC:partyR
                       -0.008474562 0.008474562 0.020102481
                                                                     -0.020102481
## SC:genderM:partyR
                        0.008474562 -0.027342502 -0.020102481
                                                                      0.055099430
## SL:(Intercept)
                        0.008474562 -0.008474562 -0.008474562
                                                                      0.008474562
## SL:genderM
                       -0.008474562 0.027342502 0.008474562
                                                                     -0.027342502
## SL:partyR
                       -0.008474562 0.008474562 0.020102481
                                                                     -0.020102481
## SL:genderM:partyR
                        0.008474562 -0.027342502 -0.020102481
                                                                      0.055099430
## VC:(Intercept)
                        0.008474562 -0.008474562 -0.008474562
                                                                      0.008474562
## VC:genderM
                       -0.008474562 0.027342502 0.008474562
                                                                     -0.027342502
## VC:partyR
                       -0.008474562 0.008474562 0.020102481
                                                                     -0.020102481
## VC:genderM:partyR
                        0.008474562 -0.027342502 -0.020102481
                                                                      0.055099430
## VL:(Intercept)
                        0.031201801 -0.031201801 -0.031201801
                                                                      0.031201801
## VL:genderM
                       -0.031201801 0.077847652 0.031201801
                                                                     -0.077847652
## VL:partyR
                       -0.031201801 0.031201801 0.098385225
                                                                     -0.098385225
## VL:genderM:partyR 0.031201801 -0.077847652 -0.098385225
                                                                      0.244492432
genderlevels1 \leftarrow c(1,1,0,1,1,0,1,1,0,1,1,0)
partylevels1 \leftarrow c(1,0,1,1,0,1,1,0,1,1,0,1)
interactlevels1 \leftarrow c(1,0,0,1,0,0,1,0,0,1,0,0)
sc.beta.male.rep.ci <- sc.beta.male.rep + qnorm(p= c(0.025, 0.975))*sqrt((varcov[1,1]+varcov[3
sc.beta.male.rep.ci
## [1] 0.6302194 2.5707944
sc.beta.male.dem.ci \leftarrow sc.beta.male.dem + qnorm(p= c(0.025, 0.975))*sqrt((varcov[1,1]))
sc.beta.male.dem.ci
## [1] 1.295646 2.189117
sc.beta.fem.rep.ci \leftarrow sc.beta.fem.rep + qnorm(p= c(0.025, 0.975))*sqrt((varcov[3,3]))
sc.beta.fem.rep.ci
## [1] 0.333134 1.504014
sl.beta.male.rep.ci <- sl.beta.male.rep + qnorm(p= c(0.025, 0.975))*sqrt((varcov[5,5]+varcov[7
sl.beta.male.rep.ci
## [1] 0.0922994 1.6910705
sl.beta.male.dem.ci \leftarrow sl.beta.male.dem + qnorm(p= c(0.025, 0.975))*sqrt((varcov[5,5]))
sl.beta.male.dem.ci
## [1] 1.272581 1.948714
sl.beta.fem.rep.ci \leftarrow sl.beta.fem.rep + qnorm(p= c(0.025, 0.975))*sqrt((varcov[7,7]))
sl.beta.fem.rep.ci
## [1] 0.009421494 1.097816181
```

```
vc.beta.male.rep.ci <- vc.beta.male.rep + qnorm(p= c(0.025, 0.975))*sqrt((varcov[9,9]+varcov[1
vc.beta.male.rep.ci
## [1] 0.6164013 2.3311599
vc.beta.male.dem.ci \leftarrow vc.beta.male.dem + qnorm(p= c(0.025, 0.975))*sqrt((varcov[9,9]))
vc.beta.male.dem.ci
## [1] 1.209583 1.990865
vc.beta.fem.rep.ci \leftarrow vc.beta.fem.rep + qnorm(p= c(0.025, 0.975))*sqrt((varcov[11,11]))
vc.beta.fem.rep.ci
## [1] 0.3943923 1.4475754
vl.beta.male.rep.ci <- vl.beta.male.rep + qnorm(p= c(0.025, 0.975))*sqrt((varcov[13,13]+varcov
vl.beta.male.rep.ci
## [1] 0.06594692 1.78353138
vl.beta.male.dem.ci \leftarrow vl.beta.male.dem + qnorm(p= c(0.025, 0.975))*sqrt((varcov[13,13]))
vl.beta.male.dem.ci
## [1] 1.475397 2.167814
vl.beta.fem.rep.ci \leftarrow vl.beta.fem.rep + qnorm(p= c(0.025, 0.975))*sqrt((varcov[15,15]))
vl.beta.fem.rep.ci
## [1] -0.1071198 1.1224212
gender_odds_cis <- data.frame(Ideology = ideology_labels, Gender = gender_labels, Party = part</pre>
gender_odds_cis
##
      Ideology Gender Party
                                 Wald.CI
## 1
            SC
                 Male
                        Rep 0.630219365
## 2
            SC
                 Male
                        Dem 2.570794363
## 3
            SC Female
                        Rep 1.295646289
## 4
            SL
                 Male
                        Rep 2.189117158
                 Male
## 5
            SL
                        Dem 0.333134017
## 6
            SL Female
                        Rep 1.504014344
## 7
            VC
                 Male
                        Rep 0.092299396
## 8
            VC
                 Male
                        Dem 1.691070535
## 9
            VC Female
                        Rep 1.272581471
## 10
                 Male
            VL
                        Rep 1.948714139
## 11
            VL
                 Male
                        Dem 0.009421494
## 12
            VL Female
                        Rep 1.097816181
## 13
            SC
                 Male
                        Rep 0.616401324
## 14
                 Male
            SC
                        Dem 2.331159850
## 15
            SC Female
                        Rep 1.209583409
## 16
            SL
                 Male
                        Rep 1.990864845
            SL
                 Male
                        Dem 0.394392279
## 17
```

```
## 18
            SL Female
                         Rep 1.447575434
## 19
            VC
                 Male
                         Rep 0.065946924
## 20
            VC
                 Male
                         Dem 1.783531380
## 21
            VC Female
                         Rep 1.475396538
## 22
            VL
                 Male
                         Rep 2.167813847
## 23
                 Male
                         Dem -0.107119819
## 24
            VL Female
                         Rep 1.122421221
#Outcomes for Party
sc.beta.rep.male.ci <- sc.beta.rep.male + qnorm(p= c(0.025, 0.975))*sqrt((varcov[2,2]+varcov[3
sc.beta.rep.fem.ci \leftarrow sc.beta.rep.fem + qnorm(p= c(0.025, 0.975))*sqrt((varcov[3,3]))
sc.beta.dem.male.ci \leftarrow sc.beta.dem.male + qnorm(p= c(0.025, 0.975))*sqrt((varcov[2,2]))
sl.beta.rep.male.ci \leftarrow sl.beta.rep.male + qnorm(p= c(0.025, 0.975))*sqrt((varcov[6,6]+varcov[7
sl.beta.rep.fem.ci \leftarrow sl.beta.rep.fem + qnorm(p= c(0.025, 0.975))*sqrt((varcov[6,6]))
sl.beta.dem.male.ci \leftarrow sl.beta.dem.male + qnorm(p= c(0.025, 0.975))*sqrt((varcov[7,7]))
vc.beta.rep.male.ci <- vc.beta.rep.male + qnorm(p= c(0.025, 0.975))*sqrt((varcov[10,10]+varcov
vc.beta.rep.fem.ci \leftarrow vc.beta.rep.fem + qnorm(p= c(0.025, 0.975))*sqrt((varcov[10,10]))
vc.beta.dem.male.ci <- vc.beta.rep.fem + qnorm(p= c(0.025, 0.975))*sqrt((varcov[11,11]))
vl.beta.rep.male.ci <- vl.beta.rep.male + qnorm(p= c(0.025, 0.975))*sqrt((varcov[14,14]+varcov
vl.beta.rep.fem.ci <- vl.beta.rep.fem + qnorm(p= c(0.025, 0.975))*sqrt((varcov[14,14]))
vl.beta.dem.male.ci <- vl.beta.dem.male + qnorm(p= c(0.025, 0.975))*sqrt((varcov[15,15]))
```