**Problem 1:**

Answer: When the length n = 4, according to the "greedy" strategy, it is cut into steel bars of length 1 and 3 separately. So, p = 1 + 8 = 9. And the optimal solution is when it is cut into 2 steel bars of length 2. The optimal value is: p = 5 + 5 = 10> 9.

**Problem 2:**

Answer: Create a new array m [0 ... n] to record the number of cutting segments of the optimal solution for each length of steel bar. When the optimal solution for the steel bar of length i is completed, update m [i +1] = m [j] + 1, where the steel bar of length (i + 1) is cut into two large sections of length (i + 1-j) and j. And the steel bar of length j continues to be cut.

**Algorithm is following:**

Let r[0...n] and m[0...n] be new arrays

r[0] = 0, m[0] = 0

for i = 1 to n

q = -∞

for j = 1 to i

if q < p[j] + r[i-j] - m[i-j]\*c

q = p[j] + r[i-j] - m[i-j]\*c

m[i] = m[i-j] + 1

r[i] = q

return r[n]

**Problem 3:**

Answer:

**Dynamic programming method pseudocode**:

// Values (stored in array v)

// Weights (stored in array w)

// Number of distinct items (n)

// Knapsack capacity (W)

Function Knapsack\_dp(W , wt , val , n)

{//return the maximum value that could be put into knapsack

for j = 0 to W do:

if w[i] < j then: m[n, j] := 0

else: m[n, j] := v[n]

//build table k[][] from the bottom to the top

for i = n - 1 downto 1 do:

for j from 0 to W do:

if w[i] <= j then:

m[i, j] := max(m[i + 1, j], m[i + 1, j - w[i]] + v[i])

else:

m[i, j] := m[i + 1, j]

}

**Recursive method pseudocode:**

Function knapsackRecursive(W , wt , val , n){

//Base Case

  if n == 0 or W == 0 :

        return 0

   // If weight of the nth item is more than the Knapsack of capacity W,

   // this item should be ignored

    if (wt[n-1] > W):

        return knapSack(W , wt , val , n-1)

    // return the maximum of two cases: nth item included, not included

    else:

        return max(val[n-1] + knapSack(W-wt[n-1] , wt , val , n-1),

                   knapSack(W , wt , val , n-1))

}

1. In teach
2. the data curve and the expressions are following.

A screenshot of a cell phone

Description automatically generated

Recursive method: A close up of a map

Description automatically generated

Dp method: A screenshot of a cell phone

Description automatically generated

1. My implementation of the program is C++. The val is generated randomly, the range is [1,100], and the weight is random generated from [1,30]. I found the time complexity of dynamic programming method executes linear, which is O(Kn). The time complexity of recursive method executes exponentially, which is O(). I collected it with desmos. Additionally, with the W growing, the execute time of recursive will be exponential. The dp time is nearly linear. The test value is following:

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Description automatically generated

**Problem 4:**

Answer:

1. The question could convert into 01- knapsack problem, which is optimal values. Total price is the limit W, weight is w, each item’s price is val, n is the max weight each person can carry. It means that we could create a same logic dynamic programming algorithm to maximum the total price.

**Pseudocode**:

Function Knapsack\_dp(W , w , val , n)

{//return the maximum value that could be put into knapsack

for j = 0 to W do:

if w[i] < j then: m[n, j] := 0

else: m[n, j] := v[n]

//build table k[][] from the bottom to the top

for i = n - 1 downto 1 do:

for j from 0 to W do:

if w[i] <= j then:

m[i, j] := max(m[i + 1, j], m[i + 1, j - w[i]] + v[i])

else:

m[i, j] := m[i + 1, j]

}

b) In theoretical running time is O(N\*)where N is the given item. The M will reach maximum when each person got their personal max value Mi, which means the capacity of bag is M1+M2+…+Mf, 1iF.

c) in teach