Homography Estimation: RANSAC

When you take a panaramic image with your camera, you end up with a sequence of images of the same scene taken from different perspectives. Each image has a slightly difference appearance but in many cases it is possible to transform them so they can be combined into a single image or panarama. In this Lab you will program automatic homography estimation between two images. Although this lab is not dependent on labs from previous weeks, it builds on concepts from Week 4.

In this lab you will (1) compute the homography between two images when correspondences are known, (2) estimate correspondences between two sets of Harris Corners using Nearest Neighbor and the ratio test and (3) use RANSAC to find the best homography estimate from the estimated correspondences from (2).

Your Script

Save C Reset MATLAB Documentation (https://www.mathworks.com/help/)

```
buildingDir = fullfile(toolboxdir('vision'), 'visiondata', 'building');
2 buildingScene = imageDatastore(buildingDir);
4 I1 = readimage(buildingScene, 1);
5 I2 = readimage(buildingScene, 2);
7 I1_gray = rgb2gray(I1);
8 I2_gray = rgb2gray(I2);
10 % get points
points1 = detectHarrisFeatures(I1 gray);
12 points2 = detectHarrisFeatures(I2 gray);
13
14 % get features
15 [features1, points1] = extractFeatures(I1_gray, points1);
16 [features2, points2] = extractFeatures(I2 gray, points2);
17
18 loc1 = points1.Location;
19 loc2 = points2.Location;
21 [match,match fwd,match bkwd] = match features(double(features1.Features),double(features2.Features));
22
23 H = ransac_homography(loc1(match(:,1),:),loc2(match(:,2),:));
24
25 I = stitch(I1,I2,H);
26
27 figure()
28 imshow(I)
29
30
  function best H = ransac homography(p1,p2)
31
      thresh = sqrt(2); % threshold for inlier points
      p = 1-1e-4; % probability of RANSAC success
32
33
      w = 0.5; % fraction inliers
34
      % n: number of correspondences required to build the model (homography)
35
36
      n = 4;
37
      % number of iterations required
38
      % from the lecture given the probability of RANSAC success, and fraction of inliers
39
      k = log(1-p)/log(1-w^n)+1; % might want to erase the '+1'
40
41
42
      num_pts = size(p1,1);
43
      best_inliers = 4;
      best H = eye(3);
44
45
      for iter = 1:k
46
          % randomly select n correspondences from p1 and p2
47
          % use these points to compute the homography
48
          N = length(p1);
          p_indices = randperm(N,n);
49
          p1_sample = p1(p_indices,:);
```

```
59
           % get p2 sample from correspondence:
52
           % p1 and p2 are listed in order according to correspondence
53
54
           p2 sample = p2(p indices,:);
55
56
           H = compute homography(p1 sample,p2 sample);
57
58
           % transform p2 to homogeneous coordinates
59
           p2_h = [p2 ones(N,1)];
60
           % estimate the location of correspondences given the homography
61
62
           p1_hat = (H*p2_h(:,:)')';
63
 64
           % convert to image coordinates by dividing x and y by the third coordinate
65
           p1_hat = p1_hat./p1_hat(:,3);
           p1_hat(:,3)=[];
66
67
68
           % compute the distance between the estimated correspondence location and the
           % putative correspondence location
69
           %dist = [];
70
           %for j = 1:length(p1)
71
           % dist = [dist; pdist2(p1(j,:),p1_hat(j,:))];
72
73
           %end
           dist = diag(pdist2(p1(:,:),p1_hat(:,:)));
74
75
76
           % inlying points have a distance less than the threshold thresh defined previously
77
           num_inliers = sum(dist<thresh);</pre>
78
79
            if num_inliers > best_inliers
80
                best inliers = num inliers;
81
                best H = H;
82
           end
       end
83
84 end
85
86
   function H = compute_homography(p1,p2)
87
       % use SVD to solve for H as was done in the lecture
88
       % note pj is an 8 vector representing 4 points
89
90
       % based on http://ros-developer.com/2017/12/26/
91
                finding-homography-matrix-using-singular-value-decomposition-and-ransac-in-opency-and-matlab/
92
       x1 = p2(1,1);
93
94
       y1 = p2(1,2);
95
       x2 = p2(2,1);
96
       y2 = p2(2,2);
97
       x3 = p2(3,1);
98
       y3 = p2(3,2);
99
       x4 = p2(4,1);
       y4 = p2(4,2);
100
101
102
       xp1 = p1(1,1);
103
       yp1 = p1(1,2);
104
       xp2 = p1(2,1);
       yp2 = p1(2,2);
105
       xp3 = p1(3,1);
106
107
       yp3 = p1(3,2);
108
       xp4 = p1(4,1);
109
       yp4 = p1(4,2);
110
111
       % Construct A Matrix Based On Correspondences
112
113
       A=[
                                                y1*xp1
          -x1 -y1 -1
                         0
                              0
                                   0
                                       x1*xp1
114
                                                          xp1;
              0
                    0
                         -x1 -y1 -1 x1*yp1 y1*yp1
115
                                                          yp1;
          -x2 -y2 -1
                         0
                              0
                                          x2*xp2
                                   0
116
                                                      y2*xp2
                                                                xp2;
          0 0 0
                                          x2*yp2 y2*yp2
                     -x2
                            -y2
                                  -1
117
                                                            yp2;
          -x3 -y3 -1 0
                              0
                                   0
                                       x3*xp3 y3*xp3 xp3;
```

```
118
                 0
                       -x3
                             -y3
                                   -1
                                         x3*yp3
                                                  y3*yp3
                                                            yp3;
120
               -v4 -1 0
                               0
                                    0
                                         x4*xp4
                                                  y4*xp4
                                                            xp4;
121
                              -y4
                                   -1
                                         x4*yp4
                                                  y4*yp4
                                                            yp4];
122
        [U,S,V] = svd(A);
123
124
125
126
        X=V(:,end)/V(end,end);
127
        H=reshape(X,3,3)';
128
129 end
130
131
    function [match,match_fwd,match_bkwd] = match_features(f1,f2)
        %% INPUT
132
133
        %% f1,f2: [ number of points x number of features ]
        %% OUTPUT
134
135
        %% match, match fwd, match bkwd: [ indices in f1, corresponding indices in f2 ]
136
        % get matches using pdist and the ratio test with threshold of 0.7
137
        % fwd matching
138
        match_fwd = [];
139
140
        % get indices of f2 which are closest to f1
141
142
        neighbors_wrt_second = knnsearch(f2,f1,'K',2);
143
144
        number = length(neighbors_wrt_second);
145
        for ind = 1:number
146
          feature 1 = f1(ind,:);
147
          current_pair = neighbors_wrt_second(ind,:);
148
          d_1 = pdist2(feature_1, f2(current_pair(1),:) );
          d_2 = pdist2(feature_1, f2(current_pair(2),:) );
149
          d_ratio = d_1/d_2;
150
          if d_ratio < .7</pre>
151
            match_fwd = [match_fwd ; ind, current_pair(1)];
152
153
          end
154
        end
155
        % bkwd matching
156
        match_bkwd = [];
157
158
        % get indices of f1 which are closest to f2
159
160
        neighbors_wrt_first = knnsearch(f1,f2,'K',2);
161
162
        number = length(neighbors_wrt_first);
163
        for ind = 1:number
164
          feature_2 = f2(ind,:);
165
          current_pair = neighbors_wrt_first(ind,:);
166
          d_1 = pdist2(f1(current_pair(1),:), feature_2 );
167
          d_2 = pdist2(f1(current_pair(2),:), feature_2 );
          d ratio = d 1/d 2;
168
169
          if d_ratio < .7</pre>
170
            match_bkwd = [match_bkwd ; current_pair(1), ind];
171
        end
172
173
174
175
        % fwd bkwd consistency check
176
177
        match = intersect(match_fwd, match_bkwd, 'rows');
178 end
```

Is the Homography estimate correct?

Output

