

Batch: Roll No.: 1811

**Experiment No.: PKCS V1.5** 

**Grade:** AA/AB/BB/BC/CC/CD/DD

Signature of faculty in-charge with date

Title: Public-Key Cryptosystems (PKCSv1.5)

**Objective:** Design a secure system in line with the public-key standard (PKCSv1.5) using virtual lab.

## **Expected Outcome of Experiment:**

CO	Outcome
CO2	Identify the principles of cryptographic techniques and Apply various
	cryptographic algorithms for securing systems

#### **Books/ Journals/ Websites referred:**

1. http://cse29-

<u>iiith.vlabs.ac.in/exp9/Further%20Reading.html?domain=Computer%20Science&lab=Cryptography%20Lab</u>

- 2. <a href="https://medium.com/asecuritysite-when-bob-met-alice/whats-so-special-about-pkcs-1-v1-5-and-the-attack-that-just-won-t-go-away-51ccf35d65b7">https://medium.com/asecuritysite-when-bob-met-alice/whats-so-special-about-pkcs-1-v1-5-and-the-attack-that-just-won-t-go-away-51ccf35d65b7</a>
- 3. <a href="https://en.wikipedia.org/wiki/PKCS">https://en.wikipedia.org/wiki/PKCS</a>

#### **Abstract:**

In cryptography, PKCS stands for "Public Key Cryptography Standards". These are a group of public-key cryptography standards devised and published by RSA Security LLC, starting in the early 1990s. The company published the standards to promote the use of the cryptography techniques to which they had patents, such as the RSA algorithm, the Schnorr signature algorithm and several others. Though not industry standards (because the company retained control over them), some of the standards in



recent years have begun to move into the "standards-track" processes of relevant standards organizations such as the IETF and the PKIX working-group.

## **Related Theory:**

Algorithm: Encryption using PKCS#1v1.5

Input : Recipient's RSA public key (n, e); k = |n| bytes; Data 'D' of length |D|

bytes with  $|D| \le k-11$ 

Output: Encrypted data block of length k bytes.

1. Form the k-byte padded message block EB

 $EB = 00 \parallel 02 \parallel PS \parallel 00 \parallel D$ 

where || denotes concatenation and PS is a string of (k-|D|-3) non-zero randomly generated bytes(i.e., at least 8 random bytes)

2. Encrypt EB with the RSA Algorithm

C = RSA(EB)

3. Output C

#### RSA Algorithm

- Key Generation (at A)
- Select two large primes p, q such that p is not equal to q
- Compute n = p \* q
- Compute phi(n) = (p-1) \* (q-1)
- Select 'e' such that gcd(e, phi(n)) = 1
- Compute d = e-1 mod phi(n)
- A's Public key is (e, n); A's Private key is d

# Encryption

Any party B wishing to send a message M to party A encrypts M using RSA as:

 $C = Me \mod n$ 

# Decryption

Party A decrypts 'C', received from party B, using his private key d as:



 $M = Cd \mod n$ 

*PKCS V1.5*:

PKCS#1 v1.5 aims to address the issues of small messages in RSA. With this we pad the message with random string (r):

 $x = 0x00 \parallel 0x02 \parallel r \parallel 0x00 \parallel m$ 

and then the cipher becomes:

 $c = x^e \pmod{N}$ 

The length of random value (r) is k-Len-3 bytes, and where k is the number of bytes in modulus (N), and Len is the number of bytes in the message. In this way we pad short messages, in order for the value of x to be large enough to make sure it is not possible to easily reverse the cipher for short messages. The receiver then derives the value of x. It then detects the 0x0 and 0x2 at the start of the value, and then removes the padding.

Unfortunately PKCS#1 v1.5 is sussible to Bleichenbacher's attack and has been the core of many attacks on SSL:

Let's say that Eve is attacking the server. In the message she sends, there's padding of the pre-shared key (as it is much smaller than the public modulus — n).

In PKCS#1 v1.5 padding we then have two bytes at the start:

0x00 0x02

Eve then captures the cipher in the handshake and which contains the SSL pre-shared key (M):

 $C=M^e \pmod{N}$ 

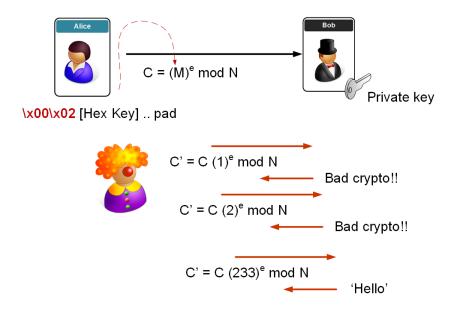
She then plays it back to the server, but adds an 's' value (where she multiplies the cipher (c) by s to the power of e (mod N)):

 $C'=C\times(se) \pmod{N}$ 



where e and N are the known public key elements. The server decrypts and gets:  $M'=(C(s^e))^d \pmod{N}=C^d\times s^e$  ( modN)= $M\times s \pmod{N}$  M=C's

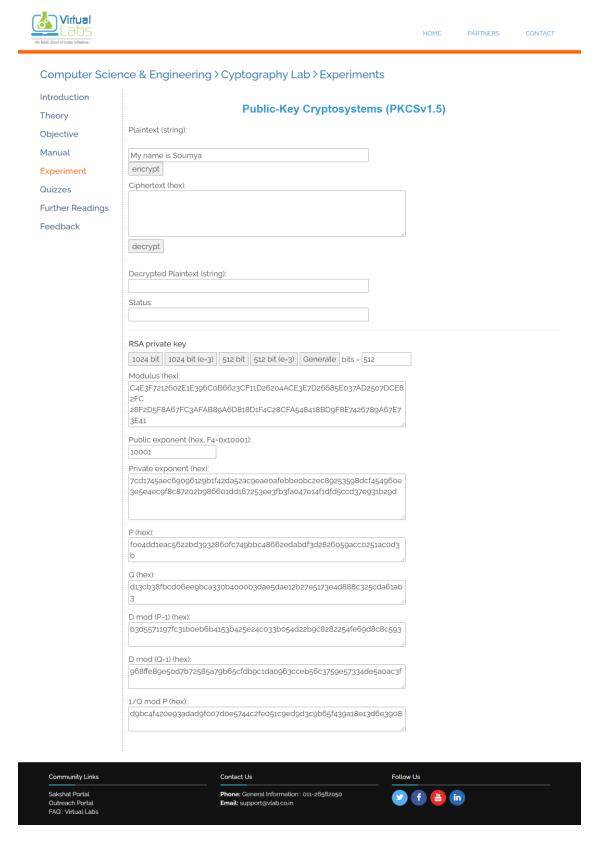
When the server reads this, the first two bytes are likely to be incorrect, so it responds to say "Bad Crypto!". Eve then keeps trying with different s values, until the server gives her a positive response, and she's then on her way to finding the key. As we have 16 bits at the start, it will take us between 30,000 (1 in 215 which is 1-in-32,728) and 130,000 attempts (1 in 217 which is 1-in-131,073) to get a successful access. We use padding to make sure that M (the pre-shared key) is the same length as the modulus (n). As M is only 48 bytes, we need to pad to give a length equal to n (256 bytes for a 2048-bit key).



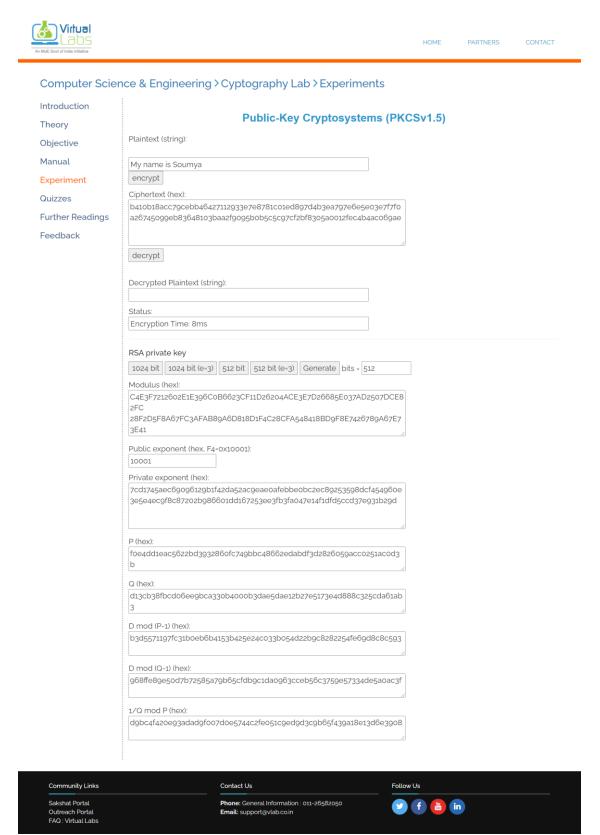
In the end we just need to divide the original cipher by the value we have found, and we get M. In this case we capture the cipher with M (which starts with x00, and then play it back with the addition of s^e, and then detect when there is a success in the cipher code:

### **Implementation Details:**

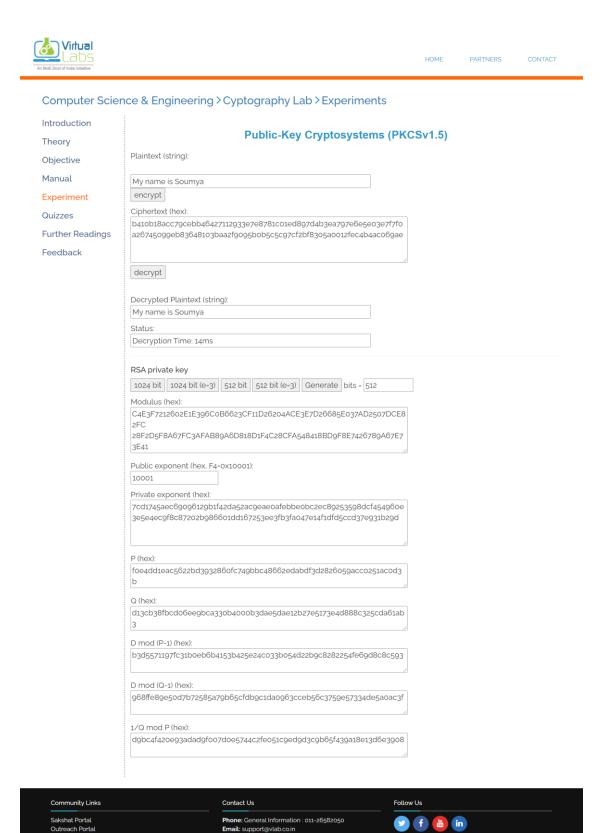




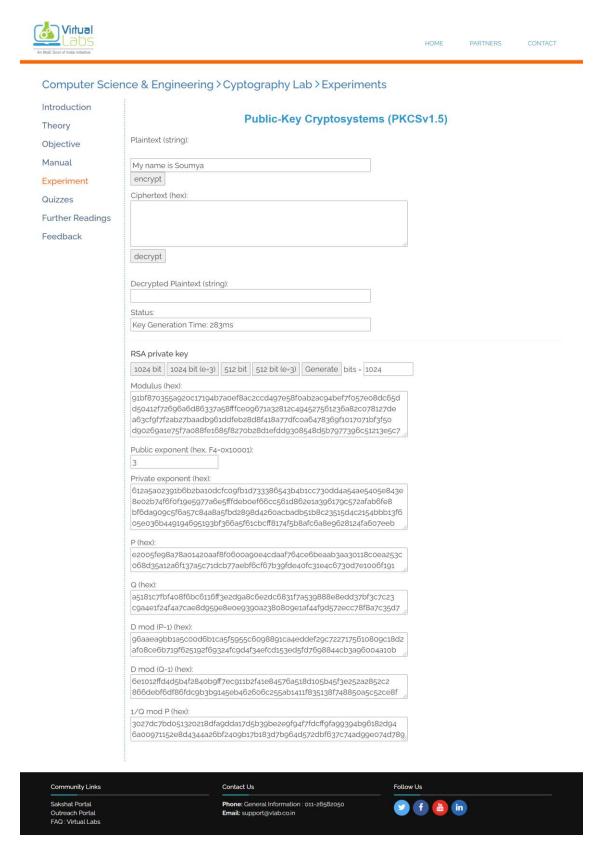
















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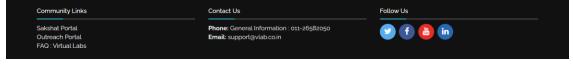
# Computer Science & Engineering > Cyptography Lab > Experiments Introduction Public-Key Cryptosystems (PKCSv1.5) Theory Plaintext (string): Objective Manual My name is Soumya encrypt Experiment 69433e43e598cdd1f8o56aae7f4b164622caefb6a53399b9faf3d4e843214c3c Further Readings 6521f49bfac22dac15fd6c3oeec5a579735e87176794ce1d42eb89ccfdac955o 082383c9497b287c192638e43f1201b011fc10f22ed5a45fec87fda1a0813c53 Feedback oa9552c7fc753o9d5b2febf9c7fdfb55b4ce39edo4oe78d85338a826d5d99aa2 decrypt Decrypted Plaintext (string): Encryption Time: 4ms RSA private key 1024 bit 1024 bit (e-3) 512 bit 512 bit (e-3) Generate bits = 1024 Modulus (hex): 91bf870355a920c17194b7a0ef8ac2ccd497e58f0ab2ac94bef7f057e08dc65d d50412f72696a6d86337a58fffce09671a32812c494527561236a82c078127de a63cfgf7f2ab27baadbg61ddfeb28d8f418a77dfcoa647836gf1o17o71bf3f50 d90269a1e75f7a088fe1685f8270b28d1efdd9308548d5b7977396c51213e5c7 Public exponent (hex, F4=0x10001): Private exponent (hex): 612a5ao2391b6b2ba10dcfco9fb1d733386543b4b1cc730dd4a54ae5405e843e 8e02b74f6f0f19e5977a6e5fffdeb0ef66cc561d862e1a396179c572afab6fe8 bf6dagogc5f6a57c84a8a5fbd28g8d426oacbadb51b8c23515d4c2154bbb13f6 05e036b449194695193bf366a5f61cbcff8174f5b8afc6a8e9628124fa607eeb P (hex): e2005fe98a78a01420aaf8f0600a90e4cdaaf764ce6beaab3aa30118c0ea253c o68d35a12a6f137a5c71dcb77aebf6cf67b39fde4ofc31e4c673od7e1oo6f191 a5181c7fbf408f6bc6116ff3e2dga8c6e2dc6831f7a539888e8edd37bf3c7c23 c9a4e1f24f4a7cae8d959e8e0e9390a2380809e1af44f9d572ecc78f8a7c35d7 D mod (P-1) (hex): 96aaea9bb1a5cood6b1ca5f5955c6o98891ca4eddef29c7227175610809c18d2 afo8ce6b719f625192f69324fc9d4f34efcd153ed5fd7698844cb3a96004a10b D mod (Q-1) (hex): 6e1012ffd4d5b4f2840b9ff7ec911b2f41e84576a518d105b45f3e252a2852c2 866debf6df86fdc9b3b9145eb462606c255ab1411f835138f748850a5c52ce8f 3027dc7bd051320218dfa9dda17d5b39be2e9f94f7fdcff9fa99394b96182d94 6a00971152e8d4344a26bf2409b17b183d7b964d572dbf637c74ad99e074d789





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#### Computer Science & Engineering > Cyptography Lab > Experiments Introduction Public-Key Cryptosystems (PKCSv1.5) Theory Plaintext (string): Objective Manual My name is Soumya encrypt Experiment Quizzes 69433e43e598cdd1f8o56aae7f4b164622caefb6a53399b9faf3d4e843214c3c Further Readings 6521f49bfac22dac15fd6c30eec5a579735e87176794ce1d42eb89ccfdac9550 082383c9497b287c192638e43f1201b011fc10f22ed5a45fec87fda1a0813c53 Feedback oa9552c7fc753o9d5b2febf9c7fdfb55b4ce39edo4oe78d85338a826d5d99aa2 decrypt Decrypted Plaintext (string): My name is Soumya Status: Decryption Time: 30ms RSA private key 1024 bit | 1024 bit (e=3) | 512 bit | 512 bit (e=3) | Generate | bits = 1024 Modulus (hex): 91bf870355a920c17194b7a0ef8ac2ccd497e58f0ab2ac94bef7f057e08dc65d d50412f72696a6d86337a58fffce09671a32812c494527561236a82c078127de a63cfgf7f2ab27baadbg61ddfeb28d8f418a77dfcoa647836gf1o17o71bf3f5o d90269a1e75f7a088fe1685f8270b28d1efdd9308548d5b7977396c51213e5c7 Public exponent (hex, F4=0x10001): Private exponent (hex): 612a5ao2391b6b2ba1odcfco9fb1d733386543b4b1cc73odd4a54ae54o5e843e 8eo2b74f6fof19e5977a6e5fffdeboef66cc561d862e1a396179c572afab6fe8 bf6dagogc5f6a57c84a8a5fbd28g8d426oacbadb51b8c23515d4c2154bbb13f6 05e036b449194695193bf366a5f61cbcff8174f5b8afc6a8e9628124fa607eeb P (hex): e2005fe98a78a01420aaf8f0600a90e4cdaaf764ce6beaab3aa30118coea253c o68d35a12a6f137a5c71dcb77aebf6cf67b39fde4ofc31e4c673od7e1oo6f191 a5181c7fbf408f6bc6116ff3e2d9a8c6e2dc6831f7a539888e8edd37bf3c7c23 c9a4e1f24f4a7cae8d959e8eoe939oa238o8o9e1af44f9d572ecc78f8a7c35d7 D mod (P-1) (hex): 96aaeagbb1a5cood6b1ca5f5955c6og88g1ca4eddef29c722717561080gc18d2 afo8ce6b719f625192f69324fc9d4f34efcd153ed5fd7698844cb3a96oo4a1ob D mod (Q-1) (hex): 6e1012ffd4d5b4f2840b9ff7ec911b2f41e84576a518d105b45f3e252a2852c2 866debf6df86fdc9b3b9145eb462606c255ab1411f835138f748850a5c52ce8f 3027dc7bd051320218dfa9dda17d5b39be2e9f94f7fdcff9fa99394b96182d94 6a00971152e8d4344a26bf2409b17b183d7b964d572dbf637c74ad99e074d789



# 1. Enlist all the Steps followed and various options explored

Step 1: Read the lab introduction, theory and manual to understand how to perform the experiment.

Step 2: Enter the input text to be encrypted in the 'Plaintext' area

Step 3: Select keysize of public key from RSA Private key section by clicking on one of the key button.

Step 4: Click on encrypt button to generate a ciphertext.

## 2. Explain your program logic, classes and methods used.

The logic for the RSA algorithm is given as follows:

- 1. Choose two distinct prime numbers p and q.
- 2. Find n such that n = pq. n will be used as the modulus for both the public and private keys.
- 3. Find the totient of n,  $\phi(n) = (p-1)(q-1)$ .
- 4. Choose an e such that  $1 < e < \phi(n)$ , and such that e and  $\phi(n)$  share no divisors other than 1 (e and  $\phi(n)$  are relatively prime). e is kept as the public key exponent.
- 5. Determine d (using modular arithmetic) which satisfies the congruence relation  $de \equiv 1 \pmod{\phi(n)}$ .

The following logic is used for encryption using PKCS V1.5

1. Form the k-byte padded message block EB

$$EB = 00 \parallel 02 \parallel PS \parallel 00 \parallel D$$

where || denotes concatenation and PS is a string of (k-|D|-3) non-zero randomly generated bytes (i.e., at least 8 random bytes)

- 2. Encrypt EB with the RSA Algorithm
- C = RSA(EB)
- 3. Output C

### 3. Explain the Importance of the approach followed by you



- This approach helps us understand the basic mathematical foundations of cryptography, to gain insightful experience by working with fundamental cryptographic applications and to train in the art of design and analysis of information security protocols.
- We can easily generate some plaintext, encrypt it with the given key size and check if we get back the original text after decryption. This helps us verify the working of the algorithm.

#### Conclusion:-

Hence successfully performed a virtual lab to design a secure system in line with the public-key standard (PKCSv1.5) which uses RSA algorithm.