

Assignment 2 report

Median Filters

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Implementations

1. Median filtering pseudocode

Read image

For each pixel

Crop based on the window_size aoi

Sort(aoi)

Median = take the middle value of sorted aoi

Save median to result_image

Evaluate with RSME

Plot all plots, histogram, and image results

Executing main.m, will execute all window size from 3x3 to 25x25. It will show original, denoised image, and their diff of window size 3,15,25. It records all time elapsed and RMSE for each window size, then plot in a figure.

The denoised image will lost floor(window_size/2) border.

2. Median Filtering with histogram

Median filtering in 1 is claimed to be slow because it uses sort algorithm, which requires $O(w n \log n)$.

Therefore, instead of sorting we want to use histogram to get the median of each iteration, which only requires $O(w)$. This approach is claimed to be a lot faster compare to method no 1.

Read image

For each pixel

Crop based on the window_size aoi

Histogram aoi for bin counts and grey-level values

Get the cumulative of bin counts

Find the index of the first cumulative beans with \geq middle of window_size

Extract the grey-level from that index to get median

Save median to result_image

Evaluate with RSME

Plot all plots, histogram, and image results

Executing main_med_filt.m, will execute all window size from 3x3 to 25x25. It will show original, denoised image, and their diff of window size 3,15,25. It records all time elapsed and RMSE for each window size, then plot in a figure.

The denoised image will lost $\text{floor}(\text{window_size}/2)$ border.

3. Adaptive Median Filter

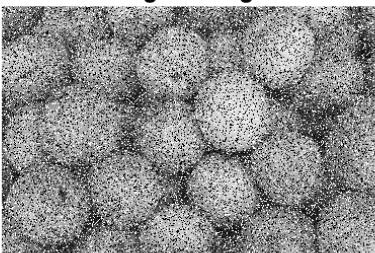
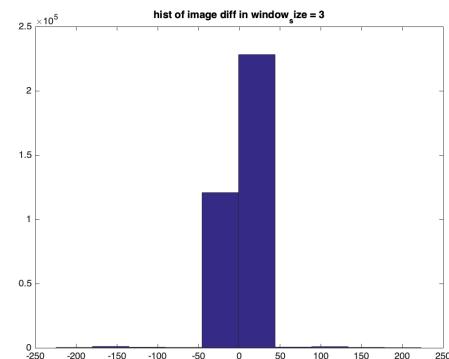
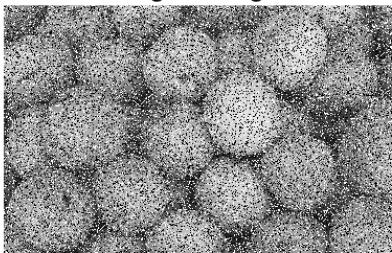
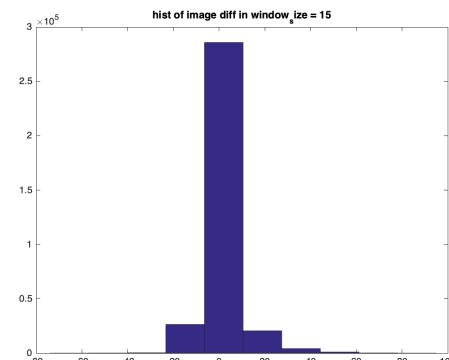
Median filter is claimed to tackle the problem that method no 1 and 2 have, they can remove noise, but the drawback is that we lose edges and details in the process. Meanwhile, adaptive median filter can adjust the size of window filter based on certain conditions. When the median value of the pixel is impulse, window size needs to be increased.

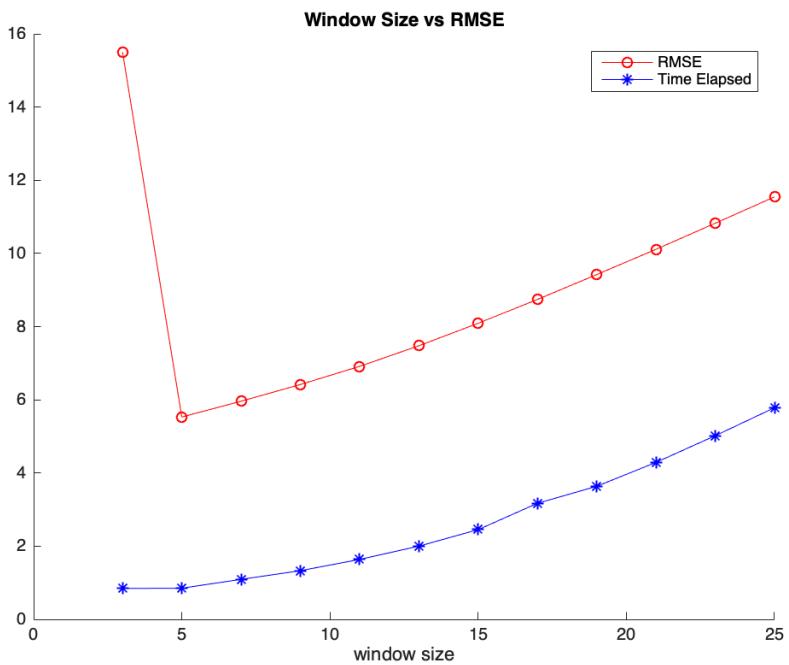
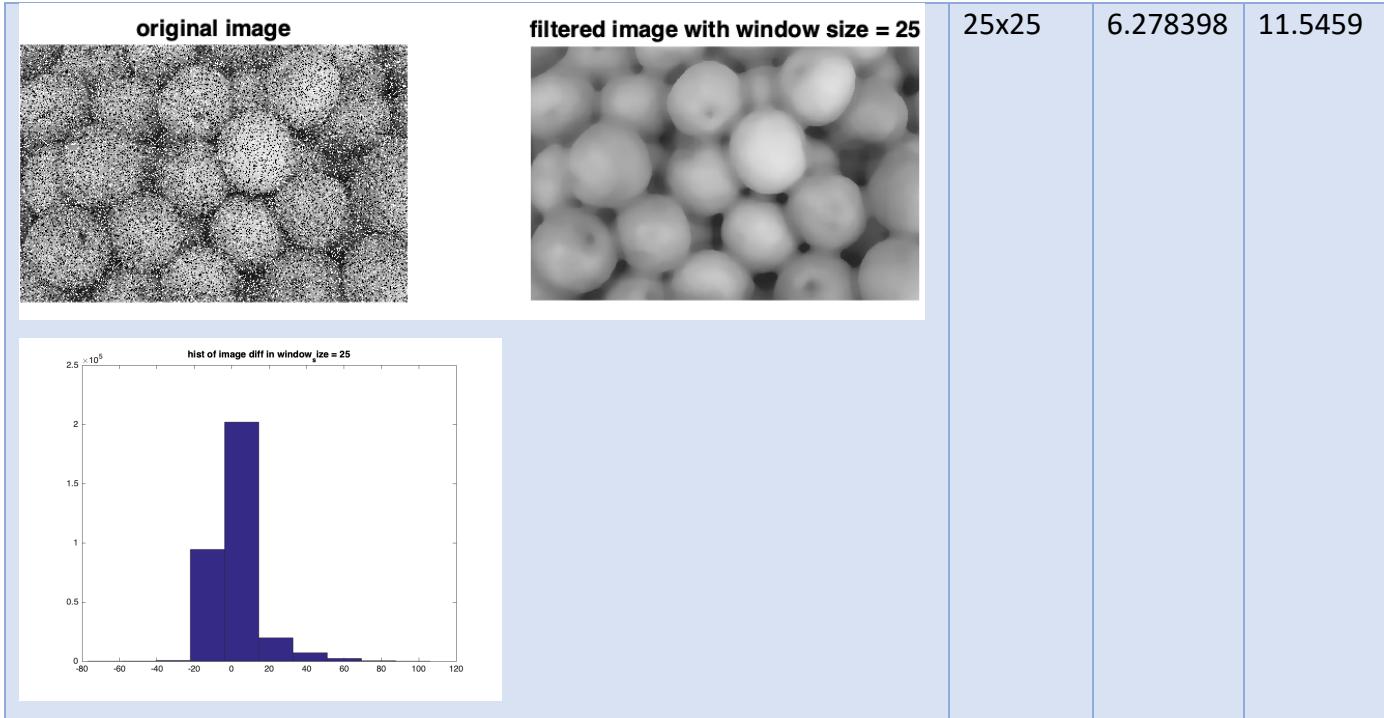
Pseudocode:

```
Read image
define window size max and min
For each pixel
    Get Zmin minimum gray level in the window kernel
    Get Zmax maximum gray level in the window kernel
    Get Zmedian median gray level in the window kernel %using sort instead of histogram
    % Level A
    While window size <= window max
        A1 = Zmedian - Zmin
        A2 = Zmedian - Zmax
        If A1>0 and A2<0
            % Level B
            B1 = current pixel - Zmin
            B2 = current pixel - Zmax
            If B1>0 and B2<0
                Output = current pixel
            Else
                Output = Zmed
            Else
                Increase window size
                If window size > window max
                    Output = current pixel
Evaluate with RSME
Plot all plots, histogram, and image results
```

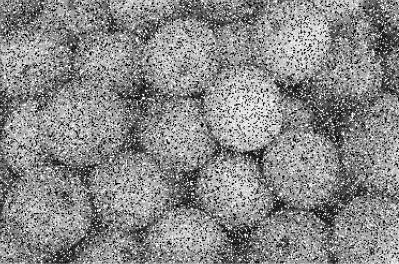
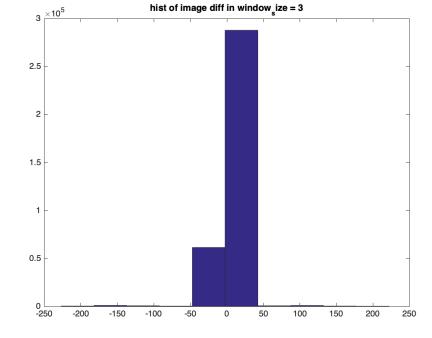
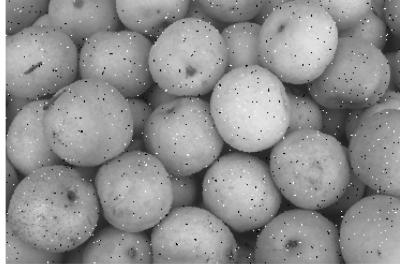
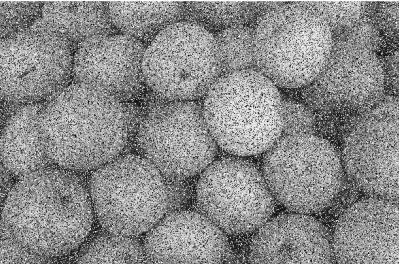
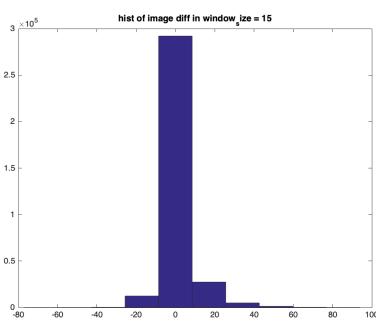
Results

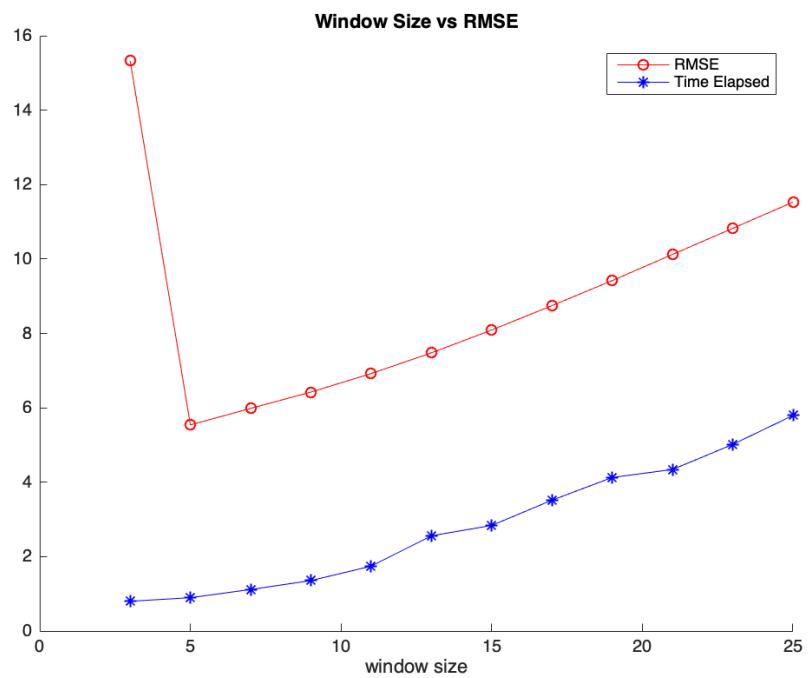
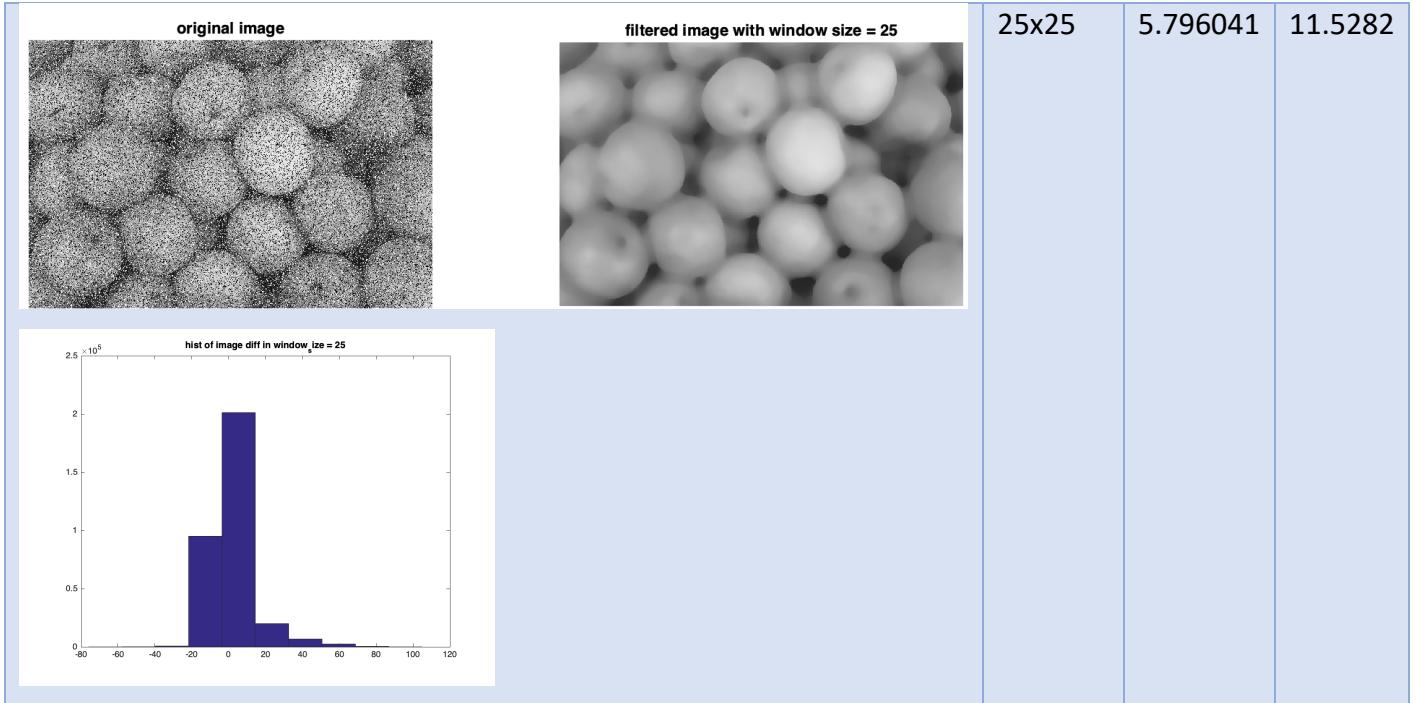
1. Regular Median Filter: Sample of Pears 30% noise results

Result	Window size	Time	RMSE
original image 	filtered image with window size = 3 	3x3	0.804303
 hist of image diff in window size = 3			15.5024
original image 	filtered image with window size = 15 	15x15	2.560739
 hist of image diff in window size = 15			8.0910

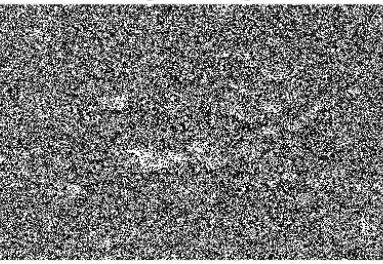
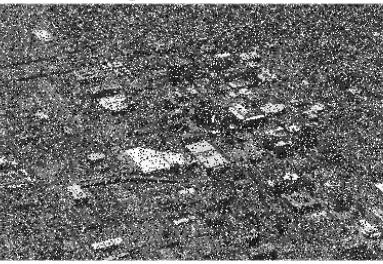
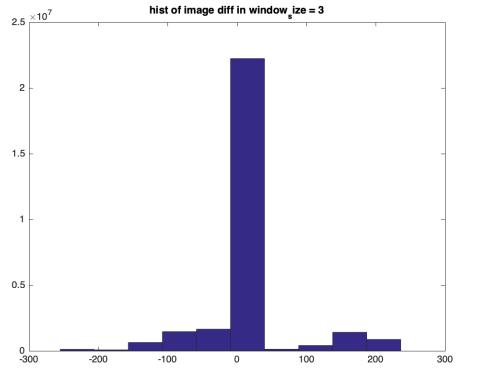
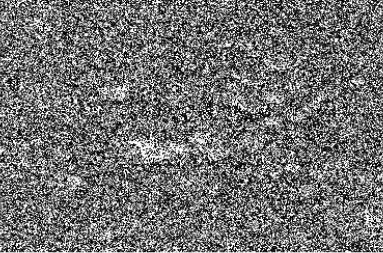
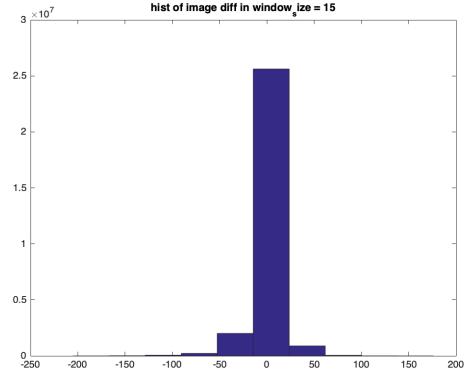


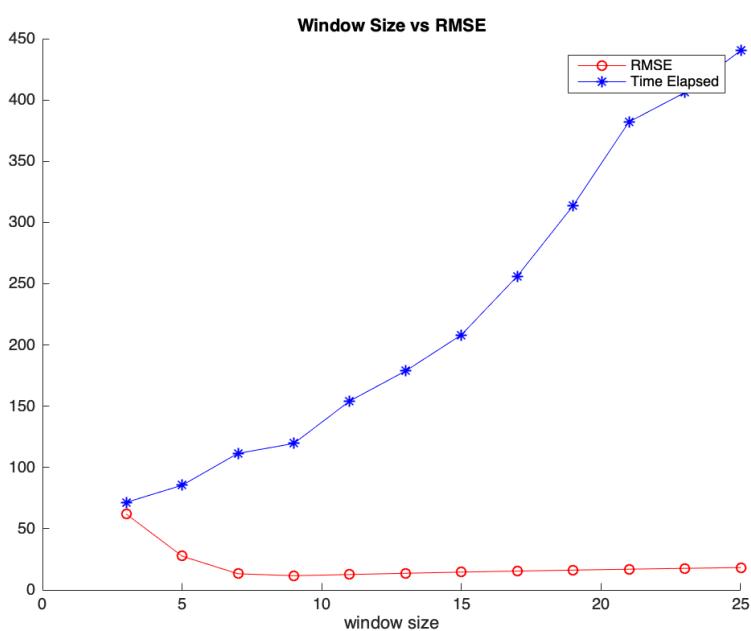
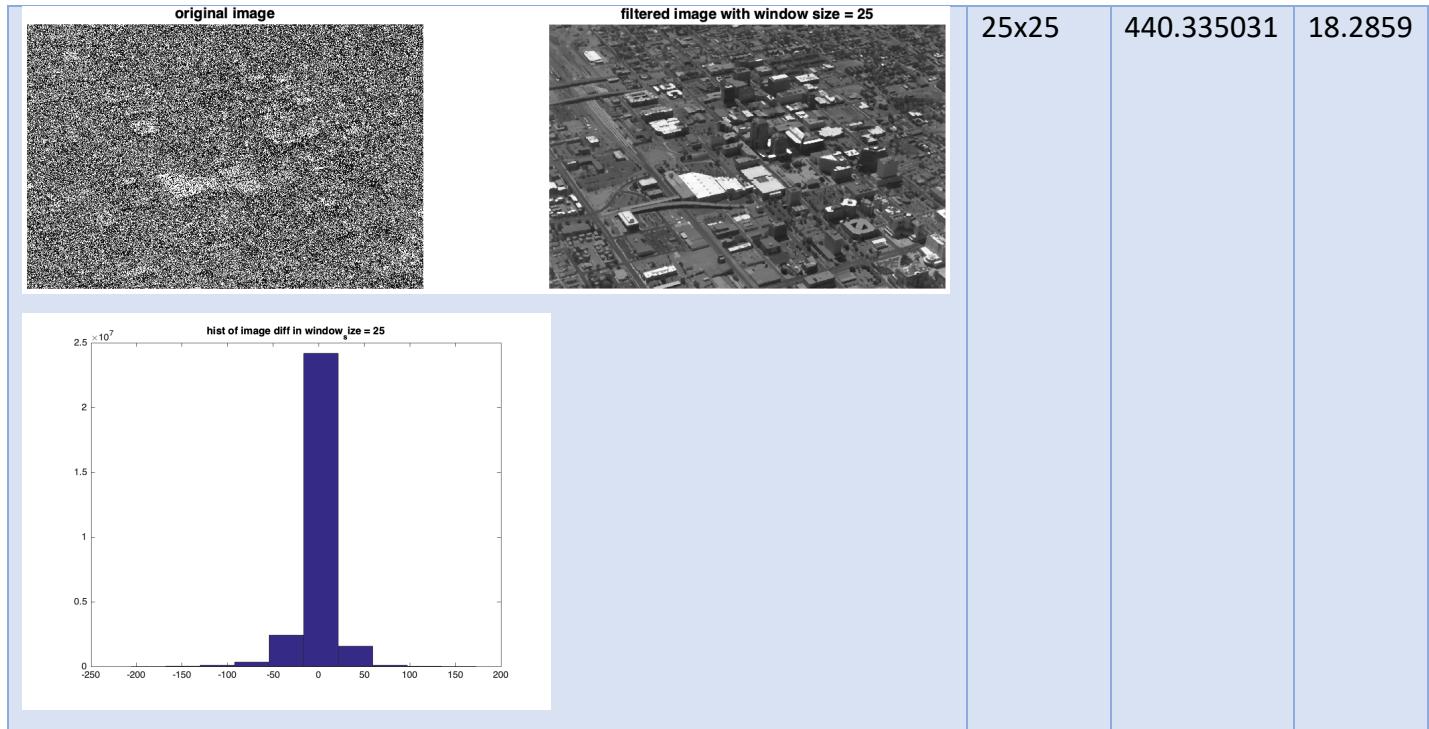
Pears 60% noise

Result	Window size	Time	RMSE	
 	filtered image with window size = 3 	3x3	0.800223	15.3345
 	filtered image with window size = 15 	15x15	2.837979	8.0914



ABQ 60%

Result	Window size	Time	RMSE
original image 	filtered image with window size = 3 	3x3	71.498193
			61.9841
original image 	filtered image with window size = 15 	15x15	208.242502
			14.5673

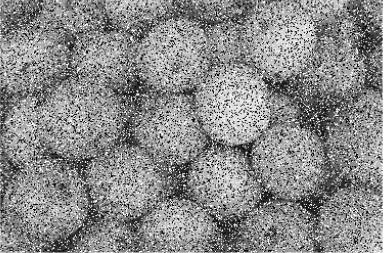
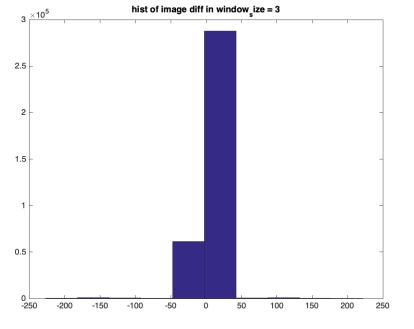
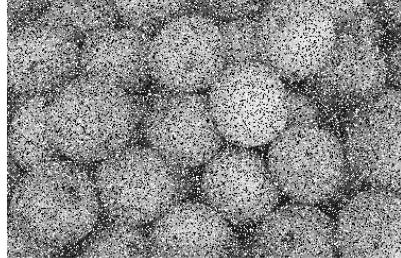


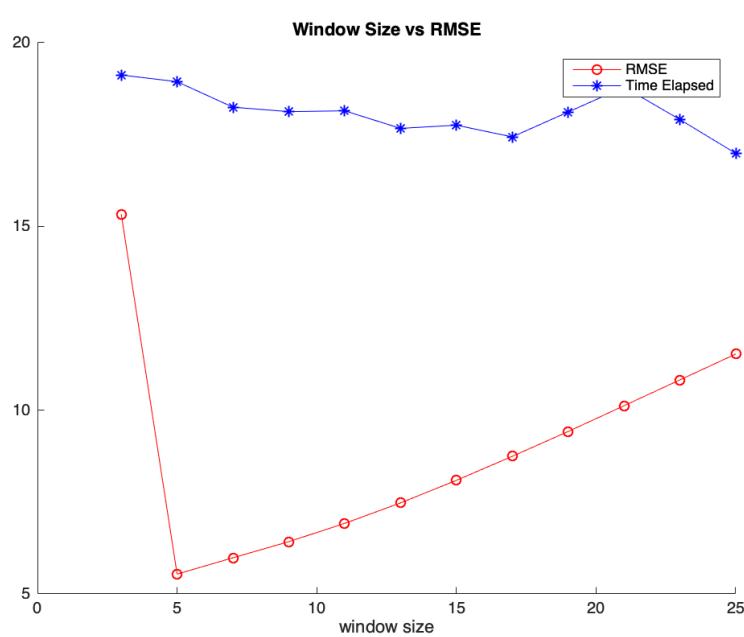
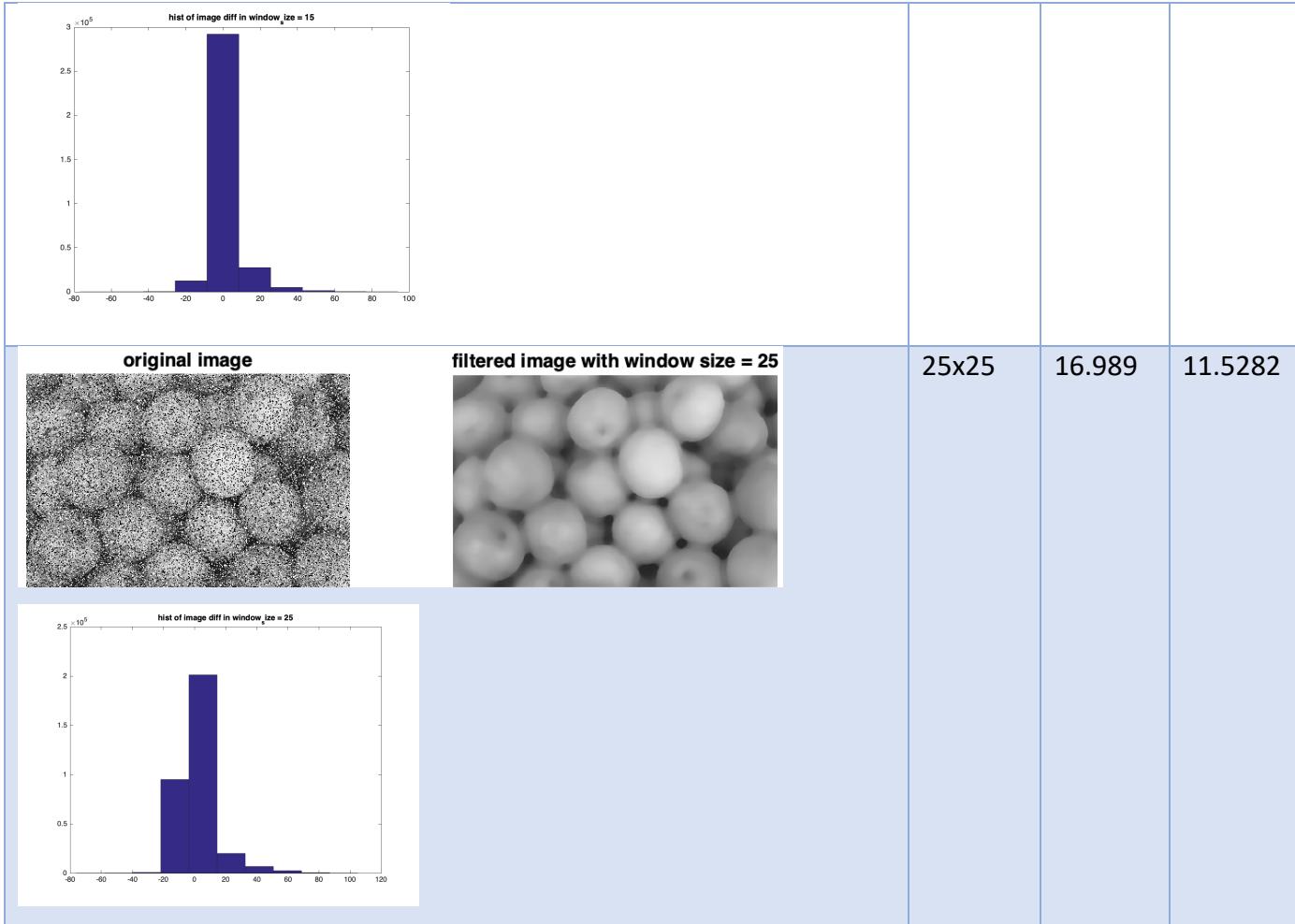
Win size	Time (s)	RMSE
3	71.498	61.98
5	85.461	27.59
7	111.484	13.20
9	119.57	11.64
11	154.25	12.59
13	178.73	13.62
15	208.24	14.56
17	256.14	15.42
19	313.72	16.21
21	382.08	16.95
23	406.02	17.63
25	440.34	18.29

For median filter version 1, the bigger the window size, the better the filtering results are. From 3 experiments above, a bigger window size leads to a longer time to complete the process, but the smaller RMSE we get. However, visually speaking, larger window_size removes noise, but it makes the image blurry and we lost a lot of information, especially on edges and corners.

2. Histogram Median Filter

Sample of Pears 60% noise results

Result	Window size	Time	RMSE																										
original image   <p>hist of image diff in window size = 3</p> <table border="1"> <caption>Data for histogram of image difference (approximate values)</caption> <thead> <tr> <th>Bin Range</th> <th>Frequency</th> </tr> </thead> <tbody> <tr> <td>-50 to -25</td> <td>0.6</td> </tr> <tr> <td>-25 to 0</td> <td>2.8</td> </tr> <tr> <td>0 to 25</td> <td>0.0</td> </tr> <tr> <td>25 to 50</td> <td>0.0</td> </tr> <tr> <td>50 to 75</td> <td>0.0</td> </tr> <tr> <td>75 to 100</td> <td>0.0</td> </tr> <tr> <td>100 to 125</td> <td>0.0</td> </tr> <tr> <td>125 to 150</td> <td>0.0</td> </tr> <tr> <td>150 to 175</td> <td>0.0</td> </tr> <tr> <td>175 to 200</td> <td>0.0</td> </tr> <tr> <td>200 to 225</td> <td>0.0</td> </tr> <tr> <td>225 to 250</td> <td>0.0</td> </tr> </tbody> </table>	Bin Range	Frequency	-50 to -25	0.6	-25 to 0	2.8	0 to 25	0.0	25 to 50	0.0	50 to 75	0.0	75 to 100	0.0	100 to 125	0.0	125 to 150	0.0	150 to 175	0.0	175 to 200	0.0	200 to 225	0.0	225 to 250	0.0	3x3	19.1206	15.3345
Bin Range	Frequency																												
-50 to -25	0.6																												
-25 to 0	2.8																												
0 to 25	0.0																												
25 to 50	0.0																												
50 to 75	0.0																												
75 to 100	0.0																												
100 to 125	0.0																												
125 to 150	0.0																												
150 to 175	0.0																												
175 to 200	0.0																												
200 to 225	0.0																												
225 to 250	0.0																												
original image  filtered image with window size = 15 	15x15	17.755	8.0914																										



Win size	Time (s)	RMSE
3	19.12	15.3345
5	18.94	5.5399
7	18.25	5.9848
9	18.12	6.4230
11	18.15	6.9202
13	17.67	7.4778
15	17.76	8.0914
17	17.44	8.7462
19	18.11	9.4201
21	18.79	10.1220
23	17.90	10.8246
25	16.98	11.5282

The RMSE for the same image in median filter using sort and histogram is identical. It clarifies that my algorithm using histogram is correct. However, an interesting finding is time elapsed to denoise the same image. In the experiment of range 3-25, sort median filter is a lot faster, it contradicts histogram's claim. In window size 3x3, sort is 20 times faster compare to histogram. However, it does not conclude that way. In 3x3, the sort only sorting 9 elements of array, but bigger the window size will require a lot more resources, because they are sorting more arrays.

We can see it from graph of both algorithms. Time elapsed of using sort is increasing over time, but histogram is fairly stable, even decreasing. Then, I tried to test the algorithm using window size 105 on pears image, sort median filter executes in 80.964551 seconds, but histogram only takes 15.675738 seconds to execute. This is because with 105 window size, sort needs to sort 11,025 elements, but histogram take the hist of 11,025 which requires so much less resources. Therefore, histogram is works better when the window size is bigger.

ABQ 60%

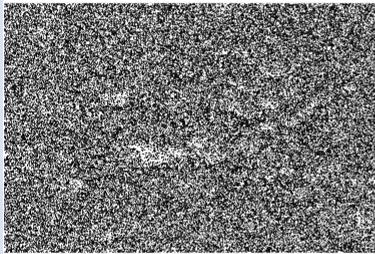
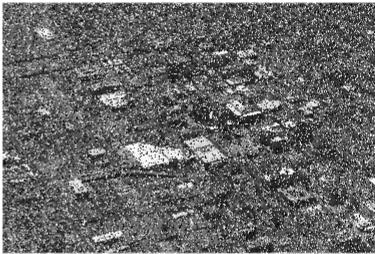
I tried to filter ABQ 60% using histogram, but it takes forever to execute. This is because ABQ image is huge. In 1 hour, it finishes 2 window_size, which are 3 and 5.

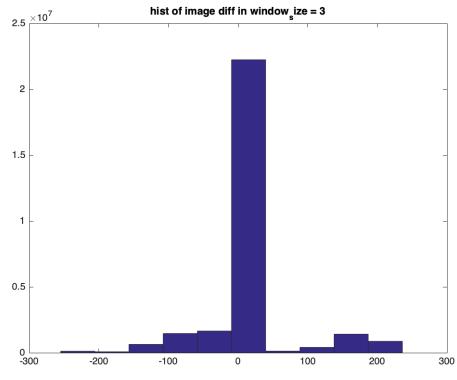
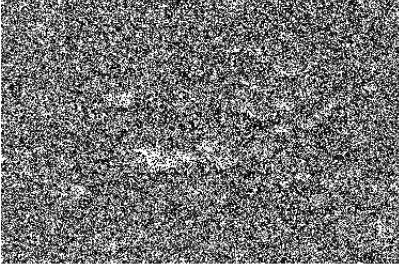
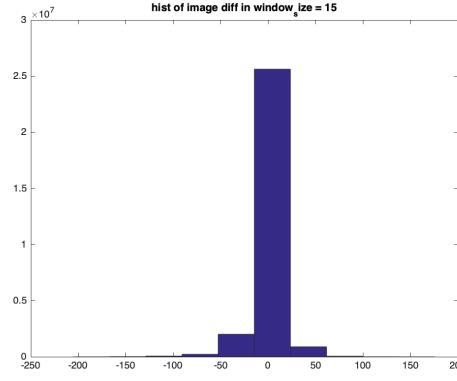
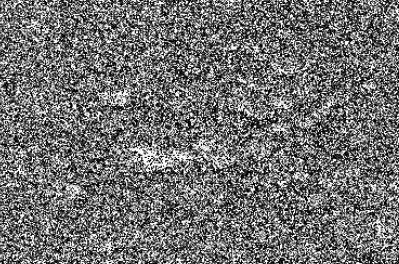
window_size 3

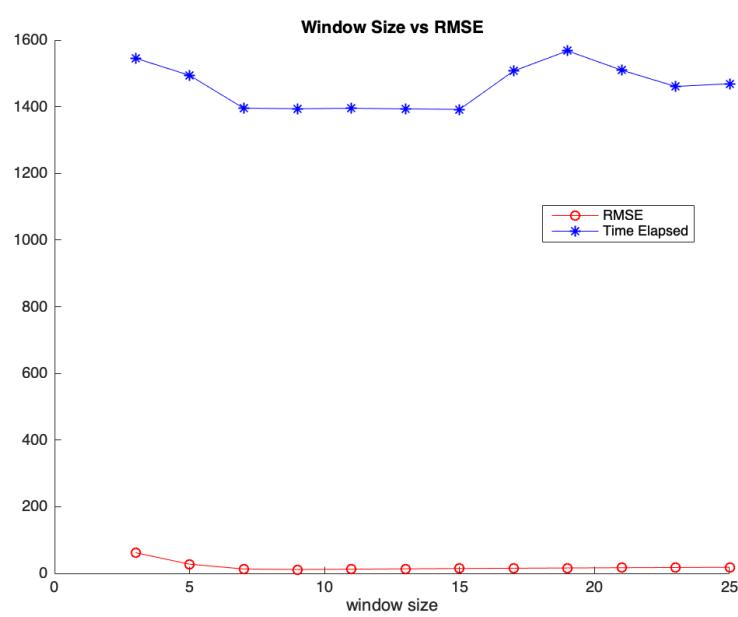
Elapsed time is 1545.524351 seconds.

RMSE = 61.9841

RMSE is still identical compare to sort median filter, but it takes 26 minutes to execute `window_size=3` alone. After more than 5 hours, this is the result of window size 3 to 25

Result	Window size	Time	RMSE
original image 	filtered image with window size = 3 	3x3	1545.52435

					
	<p>original image</p> 	<p>filtered image with window size = 15</p> 	15x15	1391.951115	14.5673
					
	<p>original image</p> 	<p>filtered image with window size = 25</p> 	25x25	1469.104358	18.2859

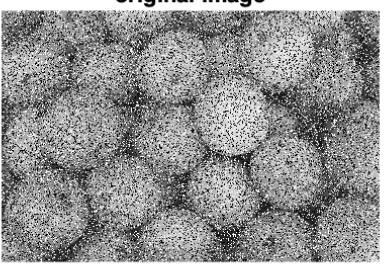
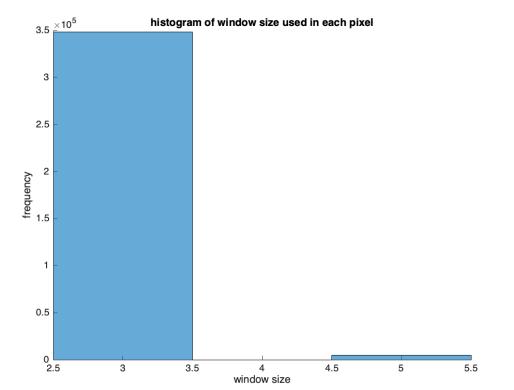
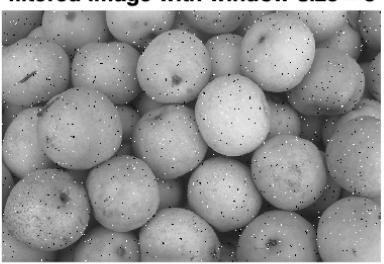
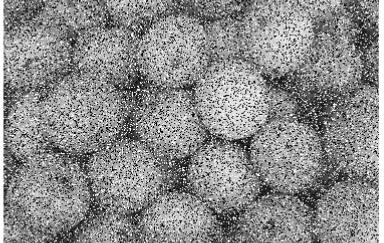
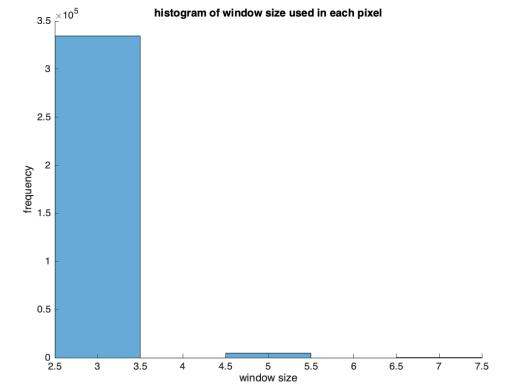


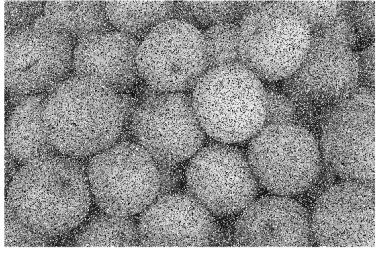
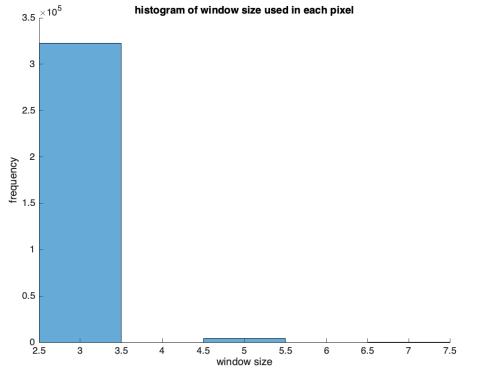
Win size	Time (s)	RMSE
3	1545.52	61.98
5	1494.13	27.59
7	1395.63	13.20
9	1393.98	11.64
11	1395.33	12.59
13	1393.54	13.62
15	1391.95	14.56
17	1507.18	15.42
19	1567.59	16.21
21	1509.78	16.95
23	1460.67	17.63
25	1469.10	18.29

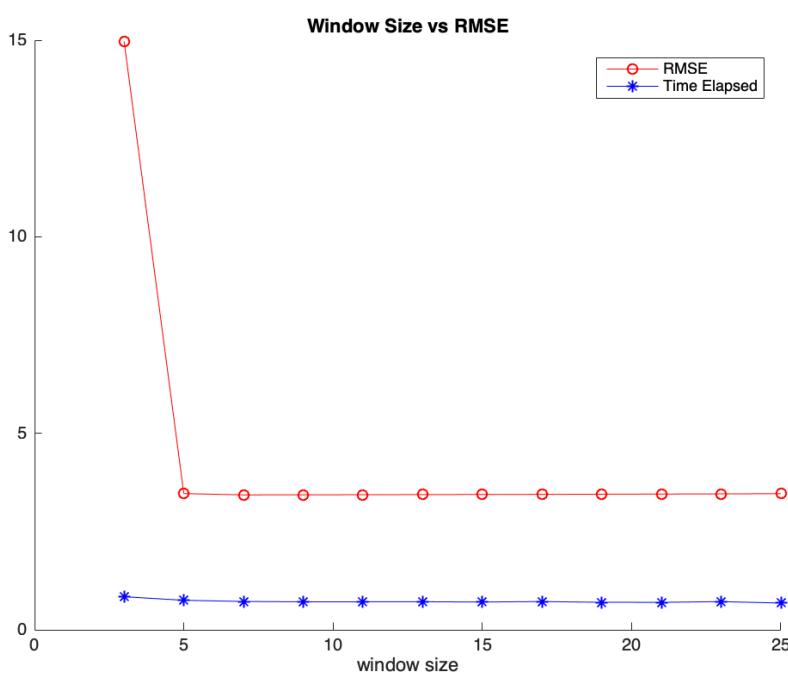
In this experiment median filter with histogram is super slow.

3. Adaptive Median Filter

Pears 60%

Result	Max Win size	Time(s)	RMSE
 	filtered image with window size = 3 	5x5	0.734430
 	filtered image with window size = 15 	15x15	0.758240

  	25x25 1.003224 3.4637
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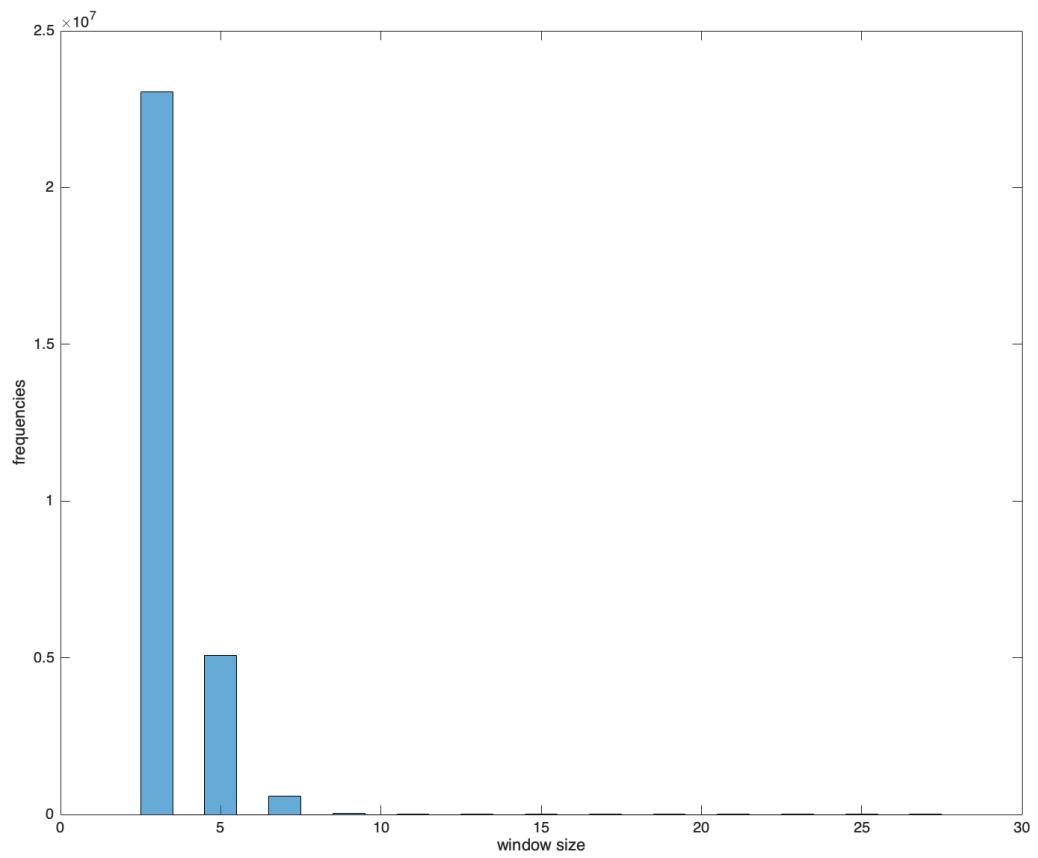
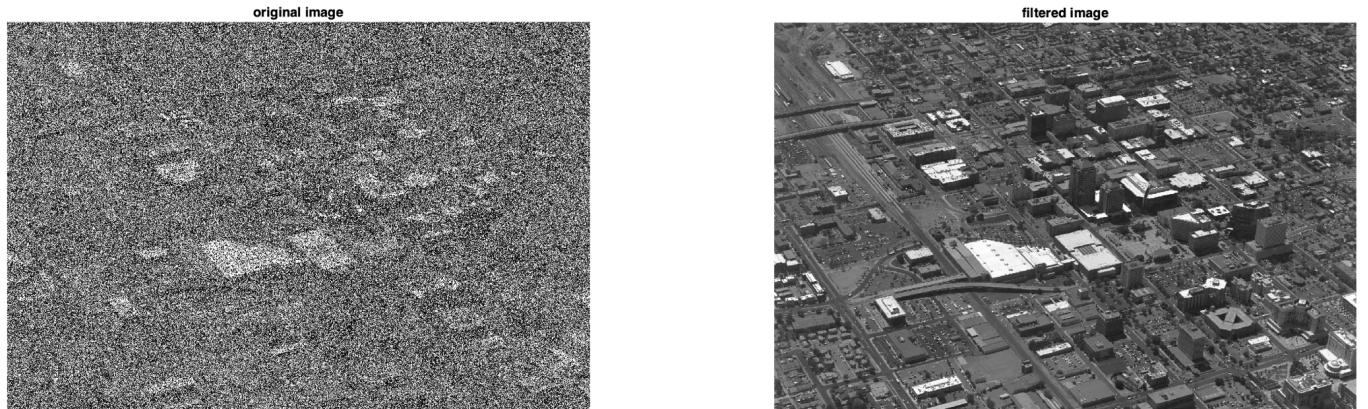


Max Win Size	Time (s)	RMSE
3	0.727007	14.9734
5	0.734430	3.4658
7	0.753620	3.4330
9	0.741663	3.4361
11	0.737330	3.4369
13	0.743319	3.4409
15	0.758240	3.4430
17	0.764870	3.4454
19	0.791594	3.4502
21	0.810517	3.4545
23	0.768411	3.4586
25	1.003224	3.4637

As we can see, the result of using adaptive filter is impressive. Denoised image has detail and no blur. It preserves the edges really well. RMSE evaluations proves this point, adaptive median filter has the lowest RMSE compare to previous 2 method. And time evaluation shows that this method performs faster compare to other 2 methods. The reason is, based on the histogram window_size vs frequency above, the majority of window size used in all cases window_max is 3x3, using sort that we use, it does sort only 9 elements. Therefore, it performs fast.

ABQ 60%

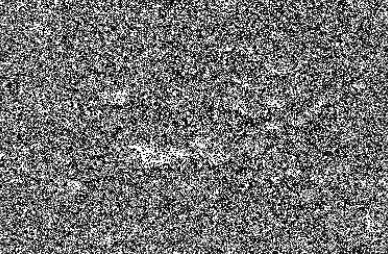
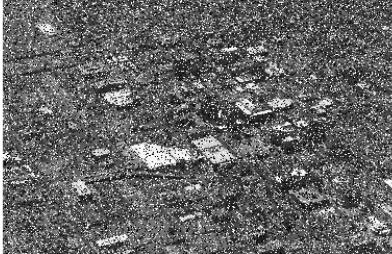
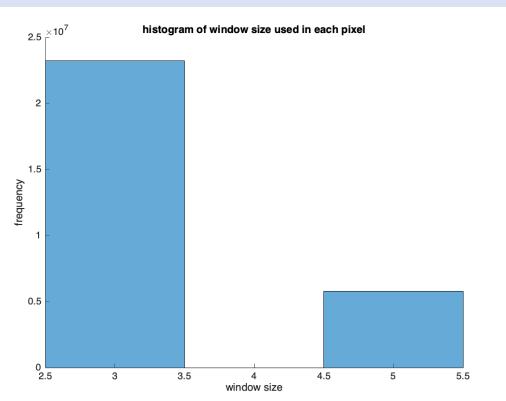
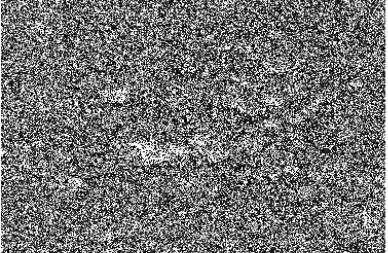
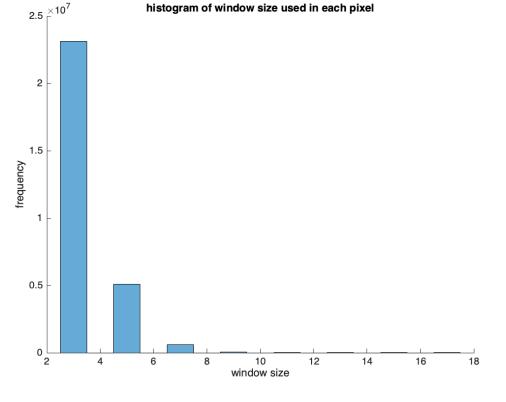
Result of ABQ with 60% noise with window size min 3 and max 25

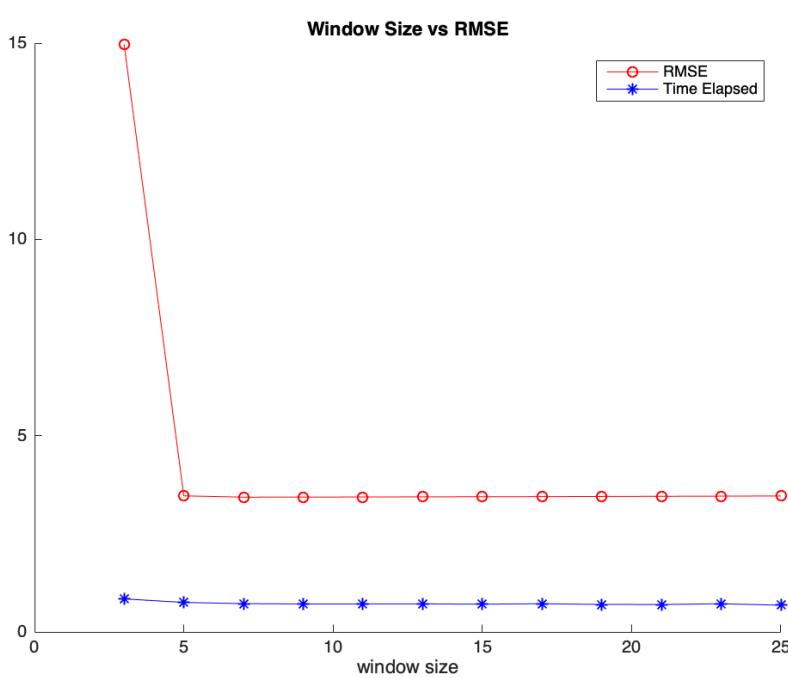
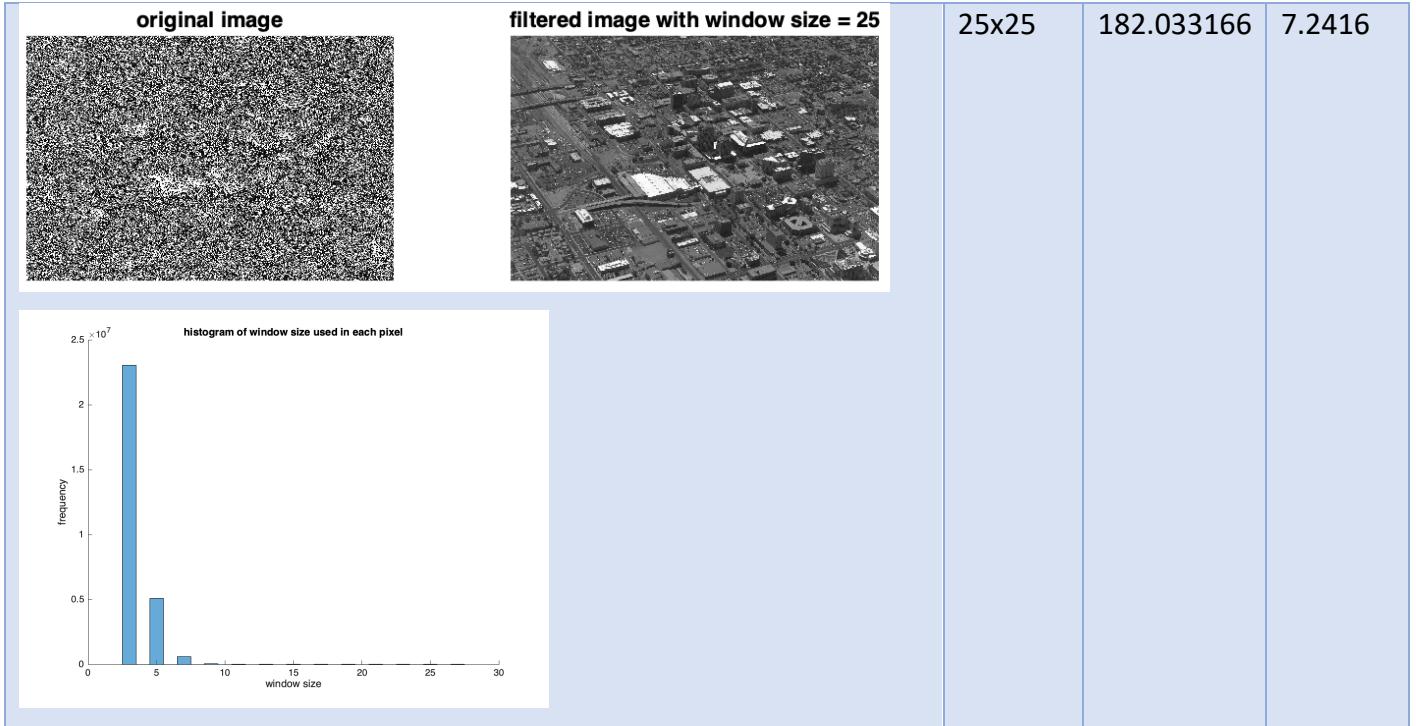


Elapsed time is 166.411179 seconds.

RMSE 7.2416

Result of ABQ with 60% noise based on different max window size allowed by the user

Result	Max Win size	Time(s)	RMSE
original image  filtered image with window size = 3  histogram of window size used in each pixel 	5x5	180.591851	21.6884
original image  filtered image with window size = 15  histogram of window size used in each pixel 	15x15	167.527600	7.2393



Max Win Size	Time (s)	RMSE
3	166.415227	61.8819
5	180.591851	21.6884
7	183.238089	8.9176
9	180.110875	7.3066
11	175.463682	7.2391
13	166.340203	7.2387
15	167.527600	7.2393
17	166.389025	7.2398
19	166.310213	7.2403
21	166.162990	7.2407
23	168.274904	7.2412
25	182.033166	7.2416

With max window size 5x5, adaptive median filter still have some salt and pepper noise and high RMSE. But, with max window size 7 and up, it performs a lot better and RMSE seems stable at around 7 greyscale error, which is really good. Visually, the result of max window size 7 and up is giving us sharper texture, edges, and corners. This tackles the problem of 2 previous median filter that we build.

Conclusion

Median filters proven have the ability to remove noise if we have the right window size. If the window size is too small, we will have some noise left, otherwise we will lost so many information, such as texture, edges, and corners since the image is become blurred.

Median filter using sort is good if the window size is small since we only need to sort small number of elements, but it will takes so much time when the window size is big. Therefore, if the window size that we are going to use is big, we can use histogram to find the median. This will save time since the complexity is $O(\text{window_size})$ compare to sorting $O(w^2 \log w^2)$. But still, in small window size sorting algorithm performs faster.

Finally, we tackle the problem of losing image texture with adaptive median filter. It increases the window size if the median of the window is impulse. This method is mathematically and visually better compare to median filter using sort and histogram. The drawback is slower compare to median sort filter, but still faster compare to my histogram median filter.