

For more work with the data table estimate $\int_1^{1.8} f(x) dx$ using Romberg integration.

For $h = 0.4$

$$\begin{aligned} T(h) &= T(0.4) = \frac{0.4}{2} [f(1.0) + 2f(1.4) + f(1.8)] \\ &= 0.2 [1.0 + 2(0.67032005) + 0.44932896] \\ &= 0.557993812 \end{aligned}$$

$$\begin{aligned} T\left(\frac{h}{2}\right) &= T(0.2) = \frac{0.2}{2} [f(1.0) + 2f(1.2) + 2f(1.4) + 2f(1.6) + f(1.8)] \\ &= .1 [1 + 2(0.81873075) + 2(0.67032005) + 2(0.54881164) + 0.44932896] \\ &= 0.552505384 \end{aligned}$$

Romberg:

$$\begin{aligned} T_2(h) &= T\left(\frac{h}{2}\right) + \frac{T\left(\frac{h}{2}\right) - T(h)}{2^{2(2-1)} - 1} \\ &= 0.552505384 + \frac{0.552505384 - 0.557993812}{3} \\ &= 0.552505384 - 0.001829476 \\ &= 0.550675908 \end{aligned}$$