

Extension of the entropy viscosity method to the  
multi-D 7-equation two-phase flow model.  
I do not know if we should have 'multi-D' in the title  
since we will only present 1-D results

Marc O. Delchini<sup>a</sup>, Jean C. Ragusa<sup>\*,a</sup>, Ray A. Berry<sup>b</sup>

<sup>a</sup>*Department of Nuclear Engineering, Texas A&M University, College Station, TX 77843, USA*

<sup>b</sup>*Idaho National Laboratory, Idaho Falls, ID 83415, USA*

---

**Abstract**

blabla

*Key words:* two-phase flow model, with variable area, entropy viscosity method, stabilization method, low Mach regime, shocks.

---

**1. Introduction**

- a few lines about the need for accurately resolving two-phase flows
- background on the different two-phase flow models: 5, 6 and 7-equation two-phase flow models
- then, focus on the different types of 7-equation two-phase flow models: they mostly differ because of the closure relaxations used
- discuss the different numerical solvers developed for the 7-equation two-phase flow model: HLL, HLLC, and approximated Riemann solvers accounting for the source terms
- emphasize the fact that the above numerical solvers only works on discontinuous schemes
- then, introduce the entropy viscosity method and details the organization of the paper

---

\*Corresponding author

*Email addresses:* `delchmo@tamu.edu` (Marc O. Delchini), `jean.ragusa@tamu.edu` (Jean C. Ragusa), `ray.berry@inl.gov` (Ray A. Berry)

14 **2. The multi-D 7-equation two-phase flow model**

- 15 • give the equations and detail the different terms
- 16 • include the relaxation terms, the mass and heat exchange terms
- 17 • eigenvalues
- 18 • entropy equation WITHOUT the dissipative terms and give the details of
- 19 the derivation in the appendix

20 **3. A viscous regularization for the multi-D 7-equation two-phase flow**  
21 **model**

- 22 • explain why we work with the phase entropy equation instead of consid-
- 23 ering the total entropy residual by summing over the two phases
- 24 • viscous regularization must be consistent with single-phase flow equation
- 25 • recall the notion of entropy condition and entropy inequality → require
- 26 dissipative terms in order to get a sign
- 27 • give the system of equations with the dissipative terms
- 28 • guide the reader through the derivation of the dissipative terms
- 29 • give the entropy residual with all terms in the right hand-side
- 30 • make the link with the single-phase flow equations
- 31 • explain how to derive the dissipative term for the volume fraction equation
- 32 • emphasizes the fact that the regularization is valid for any EOS with
- 33 convex entropy
- 34 • a few words about the parabolic regularization

35 **4. A definition of the viscosity coefficients for all Mach flows**

- 36 • non-dimensionalize the equations but use  $P_\infty$  for the pressure instead of
- 37  $(\rho c^2)_\infty$
- 38 • introduce a new Pechlet number for  $\beta$ : its behavior should be the same
- 39 as the Pechlet number for  $\kappa$
- 40 • two cases: zero and infinite relaxation coefficients
- 41 • derive the normalization parameters for the isentropic and non-isentropic
- 42 flows
- 43 • discussion about the

44 **5. 1-D numerical results**