

# Majorizing Least Squares Loss functions

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TBD

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**Note:** This is a working manuscript which will be expanded/updated frequently. All suggestions for improvement are welcome. All Rmd, tex, html, pdf, R, and C files are in the public domain. Attribution will be appreciated, but is not required. The files can be found at <https://github.com/deleeuw/majorls>

# 1 Introduction

## 2 Positive Definite Weights

$$\sigma(y) = (x - y)'W(x - y)$$

With  $W \succeq 0$ . Minimize over  $y \in \mathcal{Y}$ .

### 2.1 Scalar Majorization

### 2.2 Diagonal Majorization

### 2.3 Examples

#### 2.3.1 Linear Regression

#### 2.3.2 Low-rank Approximation