A Verbose smacof

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Started December 02 2023, Version of December 02, 2023

1 Input

1.1 delta

```
##
        [,1]
                         [,2]
                                         [,3]
                                                          [,4]
## [1,]
          +0.000000000
                           +3.000000000
                                           +2.0000000000
                                                            +3.000000000
## [2,]
          +3.000000000
                           +0.000000000
                                           +1.0000000000
                                                            +2.0000000000
## [3,]
          +2.0000000000
                           +1.0000000000
                                           +0.000000000
                                                            +3.000000000
## [4,]
          +3.000000000
                           +2.0000000000
                                           +3.000000000
                                                            +0.000000000
```

1.2 weights

```
##
        [,1]
                         [,2]
                                          [,3]
                                                          [,4]
## [1,]
          +0.000000000
                           +1.0000000000
                                           +1.0000000000
                                                            +1.0000000000
## [2,]
          +1.0000000000
                           +0.000000000
                                           +1.0000000000
                                                            +1.000000000
## [3,]
                           +1.000000000
                                                            +1.0000000000
          +1.0000000000
                                           +0.000000000
## [4,]
          +1.000000000
                           +1.000000000
                                           +1.0000000000
                                                            +0.000000000
```

2 Normalize

2.1 nweights

```
##
        [,1]
                         [,2]
                                          [,3]
                                                           [,4]
## [1,]
          +0.000000000
                           +0.0833333333
                                            +0.0833333333
                                                             +0.0833333333
## [2,]
          +0.0833333333
                           +0.000000000
                                            +0.083333333
                                                             +0.0833333333
## [3,]
                           +0.0833333333
                                            +0.000000000
          +0.0833333333
                                                             +0.0833333333
## [4,]
          +0.0833333333
                           +0.0833333333
                                            +0.0833333333
                                                             +0.000000000
```

2.2 ndelta

```
## [2,] +1.2247448714 +0.0000000000 +0.4082482905 +0.8164965809

## [3,] +0.8164965809 +0.4082482905 +0.0000000000 +1.2247448714

## [4,] +1.2247448714 +0.8164965809 +1.2247448714 +0.0000000000
```

3 Vmatrix

3.1 vmat

```
##
        [,1]
                        [,2]
                                        [,3]
                                                        [,4]
## [1,]
         +0.2500000000
                          -0.0833333333
                                          -0.0833333333
                                                          -0.0833333333
## [2,]
         -0.0833333333
                         +0.2500000000
                                                          -0.0833333333
                                         -0.0833333333
## [3,]
        -0.0833333333
                         -0.0833333333
                                         +0.2500000000
                                                         -0.0833333333
## [4,]
        -0.0833333333
                          -0.0833333333
                                         -0.0833333333
                                                          +0.2500000000
```

3.2 vinv

```
##
        [,1]
                        [,2]
                                         [,3]
                                                         [,4]
## [1,]
                          -0.7500000000
                                          -0.7500000000
          +2.2500000000
                                                           -0.7500000000
## [2,]
        -0.7500000000
                          +2.2500000000
                                          -0.7500000000
                                                           -0.7500000000
## [3,]
        -0.7500000000
                          -0.7500000000
                                          +2.2500000000
                                                          -0.7500000000
                          -0.7500000000
                                          -0.7500000000
## [4,]
        -0.7500000000
                                                           +2.2500000000
```

4 Initialize

4.1 xini

```
## [,1] [,2]

## [1,] +0.6212655007 +0.4082482905

## [2,] -0.2985956365 -0.4082482905

## [3,] +0.2985956365 -0.4082482905

## [4,] -0.6212655007 +0.4082482905
```

4.2 dini

```
##
                                      3
## 1
       +0.0000000000
                       +1.2299638932
                                        +0.8779422008
                                                        +1.2425310015
## 2
       +1.2299638932
                       +0.0000000000
                                                        +0.8779422008
                                        +0.5971912731
## 3
       +0.8779422008
                       +0.5971912731
                                        +0.000000000
                                                        +1.2299638932
## 4
       +1.2425310015
                       +0.8779422008
                                        +1.2299638932
                                                        +0.000000000
```

4.3 xold

```
## [,1] [,2]
## [1,] +0.5967072366 +0.3921104729
```

```
## [2,] -0.2867923246 -0.3921104729
## [3,] +0.2867923246 -0.3921104729
## [4,] -0.5967072366 +0.3921104729
```

4.4 dold

```
##
                                      3
## 1
       +0.000000000
                                        +0.8432376560
                                                        +1.1934144733
                       +1.1813441355
## 2
                       +0.000000000
       +1.1813441355
                                        +0.5735846492
                                                        +0.8432376560
## 3
       +0.8432376560
                       +0.5735846492
                                        +0.000000000
                                                        +1.1813441355
## 4
       +1.1934144733
                       +0.8432376560
                                        +1.1813441355
                                                        +0.000000000
```

4.5 bold

```
##
## 1
       +0.2526065660
                       -0.0863948697
                                        -0.0806906348
                                                         -0.0855210615
## 2
       -0.0863948697
                       +0.2263979197
                                        -0.0593124152
                                                         -0.0806906348
## 3
      -0.0806906348
                       -0.0593124152
                                        +0.2263979197
                                                         -0.0863948697
       -0.0855210615
                       -0.0806906348
                                        -0.0863948697
                                                         +0.2526065660
```

4.6 sold

[1] +0.0055858539

5 First Iteration

5.1 **xnew1**

```
## [,1] [,2]

## [1,] +0.6101973991 +0.3930958570

## [2,] -0.2560298680 -0.3930958570

## [3,] +0.2560298680 -0.3930958570

## [4,] -0.6101973991 +0.3930958570
```

5.2 dnew1

```
##
## 1
       +0.000000000
                       +1.1698064325
                                        +0.8622830459
                                                        +1.2203947983
## 2
       +1.1698064325
                       +0.000000000
                                        +0.5120597360
                                                        +0.8622830459
## 3
       +0.8622830459
                       +0.5120597360
                                        +0.000000000
                                                        +1.1698064325
## 4
       +1.2203947983
                       +0.8622830459
                                        +1.1698064325
                                                        +0.000000000
```

5.3 bnew1

```
##
                                       -0.0789084072
## 1
      +0.2497857556
                       -0.0872469750
                                                        -0.0836303734
## 2
                       +0.2325942926
                                       -0.0664389103
                                                       -0.0789084072
      -0.0872469750
## 3
      -0.0789084072
                       -0.0664389103
                                       +0.2325942926
                                                       -0.0872469750
## 4
      -0.0836303734
                       -0.0789084072
                                       -0.0872469750
                                                       +0.2497857556
```

5.4 snew1

[1] +0.0035041674

6 Second Iteration

6.1 **xnew2**

```
## [,1] [,2]

## [1,] +0.6167537315 +0.3918899543

## [2,] -0.2449488115 -0.3918899543

## [3,] +0.2449488115 -0.3918899543

## [4,] -0.6167537315 +0.3918899543
```

6.2 dnew2

```
##
## 1
      +0.0000000000
                      +1.1648357042
                                      +0.8674963076
                                                      +1.2335074629
## 2
      +1.1648357042
                      +0.0000000000
                                      +0.4898976231
                                                      +0.8674963076
                                      +0.0000000000
## 3 +0.8674963076
                      +0.4898976231
                                                      +1.1648357042
      +1.2335074629
                      +0.8674963076
                                      +1.1648357042
                                                      +0.000000000
## 4
```

6.3 bnew2

```
##
## 1
       +0.2487948391
                       -0.0876192859
                                        -0.0784342033
                                                        -0.0827413499
## 2
      -0.0876192859
                       +0.2354979798
                                       -0.0694444906
                                                        -0.0784342033
## 3
       -0.0784342033
                       -0.0694444906
                                        +0.2354979798
                                                        -0.0876192859
## 4
      -0.0827413499
                       -0.0784342033
                                       -0.0876192859
                                                        +0.2487948391
```

6.4 snew2

[1] +0.0031872596

7 Third Iteration

7.1 **xnew3**

```
## [,1] [,2]

## [1,] +0.6201781703 +0.3904481658

## [2,] -0.2410806891 -0.3904481658

## [3,] +0.2410806891 -0.3904481658

## [4,] -0.6201781703 +0.3904481658
```

7.2 dnew3

```
##
## 1
      +0.0000000000
                       +1.1625686662
                                       +0.8680518309
                                                        +1.2403563407
      +1.1625686662
                       +0.000000000
                                       +0.4821613781
                                                        +0.8680518309
                                       +0.0000000000
## 3
      +0.8680518309
                       +0.4821613781
                                                        +1.1625686662
      +1.2403563407
                       +0.8680518309
                                       +1.1625686662
## 4
                                                        +0.000000000
```

7.3 bnew3

```
##
                                                     -0.0822844769
## 1 +0.2484586307 -0.0877901457
                                      -0.0783840081
                      +0.2367328763
## 2
      -0.0877901457
                                      -0.0705587225
                                                      -0.0783840081
## 3
      -0.0783840081
                      -0.0705587225
                                      +0.2367328763
                                                      -0.0877901457
      -0.0822844769
                                                     +0.2484586307
                      -0.0783840081
                                      -0.0877901457
## 4
```

7.4 snew3

[1] +0.0031257518

8 Fourth Iteration

8.1 xnew4

```
## [,1] [,2]

## [1,] +0.6221618803 +0.3892943614

## [2,] -0.2397466548 -0.3892943614

## [3,] +0.2397466548 -0.3892943614

## [4,] -0.6221618803 +0.3892943614
```

8.2 dnew4

```
## 1 2 3 4
## 1 +0.0000000000 +1.1615019251 +0.8674340344 +1.2443237606
## 2 +1.1615019251 +0.0000000000 +0.4794933096 +0.8674340344
```

```
## 3 +0.8674340344 +0.4794933096 +0.0000000000 +1.1615019251
## 4 +1.2443237606 +0.8674340344 +1.1615019251 +0.0000000000
```

8.3 bnew4

```
##
     1
                                      3
       +0.2483327275
                       -0.0878707735
                                                        -0.0820221198
## 1
                                        -0.0784398341
## 2
       -0.0878707735
                       +0.2372619435
                                        -0.0709513359
                                                        -0.0784398341
       -0.0784398341
                       -0.0709513359
                                        +0.2372619435
## 3
                                                        -0.0878707735
      -0.0820221198
                       -0.0784398341
                                        -0.0878707735
## 4
                                                        +0.2483327275
```

8.4 snew4

[1] +0.0031079624

9 Fifth Iteration

9.1 xnew5

```
## [,1] [,2]

## [1,] +0.6233856874 +0.3884626907

## [2,] -0.2392820211 -0.3884626907

## [3,] +0.2392820211 -0.3884626907

## [4,] -0.6233856874 +0.3884626907
```

9.2 dnew5

```
##
     1
                                     3
## 1
       +0.000000000
                       +1.1609516027
                                       +0.8666883378
                                                        +1.2467713749
## 2
      +1.1609516027
                       +0.000000000
                                       +0.4785640423
                                                        +0.8666883378
## 3
      +0.8666883378
                       +0.4785640423
                                       +0.000000000
                                                        +1.1609516027
                                       +1.1609516027
                                                        +0.000000000
## 4
      +1.2467713749
                       +0.8666883378
```

9.3 bnew5

```
##
     1
## 1
       +0.2482808473
                       -0.0879124266
                                        -0.0785073235
                                                        -0.0818610971
## 2
      -0.0879124266
                       +0.2375088582
                                        -0.0710891080
                                                        -0.0785073235
      -0.0785073235
                       -0.0710891080
                                        +0.2375088582
                                                        -0.0879124266
## 3
                       -0.0785073235
                                                        +0.2482808473
       -0.0818610971
                                        -0.0879124266
## 4
```

9.4 snew5

[1] +0.0031011765