

Attenuation[0.025, 0.025, 0.1 / 1000, 1.9 * 10^9, 420]

b

$$\begin{aligned} & \left((0.0791762 - 0.0211136 i) \text{BesselJ}\left[1, \right. \right. \\ & \quad 0.025 \sqrt{\left(1583.52 \left(-\text{Sin}[\text{VegetationAtten`Private`alpha} - \text{VegetationAtten`Private`phii}] \times \right. \right. \\ & \quad \quad \text{Sin}[\text{VegetationAtten`Private`thetai}] + \text{Sin}[\text{VegetationAtten`Private`alpha} - \\ & \quad \quad \quad \text{VegetationAtten`Private`phis}] \times \text{Sin}[\text{VegetationAtten`Private`thetas}]]^2 + \\ & \quad \quad \left(\text{Cos}[39.7935 \text{VegetationAtten`Private`beta} \left(\text{Cos}[\text{VegetationAtten`Private`alpha} - \right. \right. \\ & \quad \quad \quad \text{VegetationAtten`Private`phii}] \times \text{Sin}[\text{VegetationAtten`Private`thetai}] - \\ & \quad \quad \quad \text{Cos}[\text{VegetationAtten`Private`alpha} - \text{VegetationAtten`Private`phis}] \times \\ & \quad \quad \quad \text{Sin}[\text{VegetationAtten`Private`thetas}]] \right) + \text{Sin}[\\ & \quad \quad \quad 39.7935 \text{VegetationAtten`Private`beta} \left(\text{Cos}[\text{VegetationAtten`Private`thetai}] + \\ & \quad \quad \quad \text{Cos}[\text{VegetationAtten`Private`thetas}]] \right)^2 \left. \right) \left. \right] \\ & \quad \left(-0.00312567 \text{Cos}\left[\text{ArcCos}\left[\left(\text{Cos}[\text{VegetationAtten`Private`thetai}] \times \right. \right. \right. \right. \\ & \quad \quad \text{Sin}[\text{VegetationAtten`Private`beta}] + \text{Cos}[\text{VegetationAtten`Private`beta}] \times \\ & \quad \quad \text{Cos}[\text{VegetationAtten`Private`alpha} - \text{VegetationAtten`Private`phii}] \times \\ & \quad \quad \text{Sin}[\text{VegetationAtten`Private`thetai}]] \right) / \\ & \quad \left(\sqrt{\left(1 - \left(-\text{Cos}[\text{VegetationAtten`Private`beta}] \times \text{Cos}[\right. \right. \right. \\ & \quad \quad \text{VegetationAtten`Private`thetai}] + \text{Cos}[\text{VegetationAtten`Private`alpha} - \\ & \quad \quad \quad \text{VegetationAtten`Private`phii}] \times \text{Sin}[\text{VegetationAtten`Private`beta}] \times \\ & \quad \quad \quad \text{Sin}[\text{VegetationAtten`Private`thetai}]]^2 \right) \left. \right) \left. \right] - \text{ArcCos}\left[\right. \\ & \quad \left(-\text{Cos}[\text{VegetationAtten`Private`thetas}] \times \text{Sin}[\text{VegetationAtten`Private`beta}] + \\ & \quad \quad \text{Cos}[\text{VegetationAtten`Private`beta}] \times \text{Cos}[\text{VegetationAtten`Private`alpha} - \\ & \quad \quad \quad \text{VegetationAtten`Private`phis}] \times \text{Sin}[\text{VegetationAtten`Private`thetas}]] \right) / \\ & \quad \left(\sqrt{\left(1 - \left(\text{Cos}[\text{VegetationAtten`Private`beta}] \times \text{Cos}[\right. \right. \right. \\ & \quad \quad \text{VegetationAtten`Private`thetas}] + \text{Cos}[\text{VegetationAtten`Private`alpha} - \\ & \quad \quad \quad \text{VegetationAtten`Private`phis}] \times \text{Sin}[\text{VegetationAtten`Private`beta}] \times \\ & \quad \quad \quad \text{Sin}[\text{VegetationAtten`Private`thetas}]]^2 \right) \left. \right) \left. \right] \left. \right] \\ & \quad \left(\text{Cos}[\text{VegetationAtten`Private`beta}] \times \text{Cos}[\text{VegetationAtten`Private`thetai}] - \right. \\ & \quad \quad \text{Cos}[\text{VegetationAtten`Private`alpha} - \text{VegetationAtten`Private`phii}] \times \\ & \quad \quad \text{Sin}[\text{VegetationAtten`Private`beta}] \times \\ & \quad \quad \text{Sin}[\text{VegetationAtten`Private`thetai}] \left. \right) \\ & \quad \left(-\text{Cos}[\text{VegetationAtten`Private`beta}] \times \text{Cos}[\text{VegetationAtten`Private`thetas}] - \right. \\ & \quad \quad \text{Cos}[\text{VegetationAtten`Private`alpha} - \text{VegetationAtten`Private`phis}] \times \\ & \quad \quad \text{Sin}[\text{VegetationAtten`Private`beta}] \times \\ & \quad \quad \text{Sin}[\text{VegetationAtten`Private`thetas}] \left. \right) + 0.993749 \\ & \quad \sqrt{\left(1 - \left(\text{Cos}[\text{VegetationAtten`Private`beta}] \times \text{Cos}[\text{VegetationAtten`Private`thetai}] - \right. \right. \\ & \quad \quad \text{Cos}[\text{VegetationAtten`Private`alpha} - \text{VegetationAtten`Private`phii}] \times \\ & \quad \quad \quad \text{Sin}[\text{VegetationAtten`Private`beta}] \times \text{Sin}[\text{VegetationAtten`Private`thetai}]]^2 \right) \left. \right) \\ & \quad \sqrt{\left(1 - \left(-\text{Cos}[\text{VegetationAtten`Private`beta}] \times \text{Cos}[\text{VegetationAtten`Private`thetas}] - \right. \right. \\ & \quad \quad \text{Cos}[\text{VegetationAtten`Private`alpha} - \text{VegetationAtten`Private`phis}] \times \text{Sin}[\\ & \quad \quad \quad \text{VegetationAtten`Private`beta}] \times \text{Sin}[\text{VegetationAtten`Private`thetas}]]^2 \right) \left. \right) \left. \right) \left. \right) / \\ & \quad \left(\sqrt{\left(1583.52 \left(-\text{Sin}[\text{VegetationAtten`Private`alpha} - \text{VegetationAtten`Private`phii}] \times \right. \right. \right. \\ & \quad \quad \text{Sin}[\text{VegetationAtten`Private`thetai}] + \\ & \quad \quad \text{Sin}[\text{VegetationAtten`Private`alpha} - \text{VegetationAtten`Private`phis}] \times \\ & \quad \quad \text{Sin}[\text{VegetationAtten`Private`thetas}]]^2 + \end{aligned}$$

```

(Cos[39.7935 VegetationAtten`Private`beta (Cos[VegetationAtten`Private`alpha -
VegetationAtten`Private`phii] × Sin[VegetationAtten`Private`thetai] -
Cos[VegetationAtten`Private`alpha - VegetationAtten`Private`phis] ×
Sin[VegetationAtten`Private`thetas]]) +
Sin[39.7935 VegetationAtten`Private`beta (Cos[VegetationAtten`Private`thetai] +
Cos[VegetationAtten`Private`thetas]])^2))
(Cos[VegetationAtten`Private`alpha] ×
Sin[VegetationAtten`Private`beta] ((0. + 0. i) - (3.09324 × 10-6 - 8.24863 × 10-7 i)
Cos[VegetationAtten`Private`alpha] × Sin[VegetationAtten`Private`beta]) -
Cos[VegetationAtten`Private`beta] ((0. + 0. i) - (0.000989625 - 0.0002639 i)
Cos[VegetationAtten`Private`beta] (-0.00312567 Sin[VegetationAtten`Private`alpha]^2
Sin[VegetationAtten`Private`beta]^2 + 0.993749 (1 -
Sin[VegetationAtten`Private`alpha]^2 Sin[VegetationAtten`Private`beta]^2)))) /
(√ (Cos[VegetationAtten`Private`beta]^2 + Cos[VegetationAtten`Private`alpha]^2
Sin[VegetationAtten`Private`beta]^2)^2)
-0.314391

ClearAll[beta, alpha]

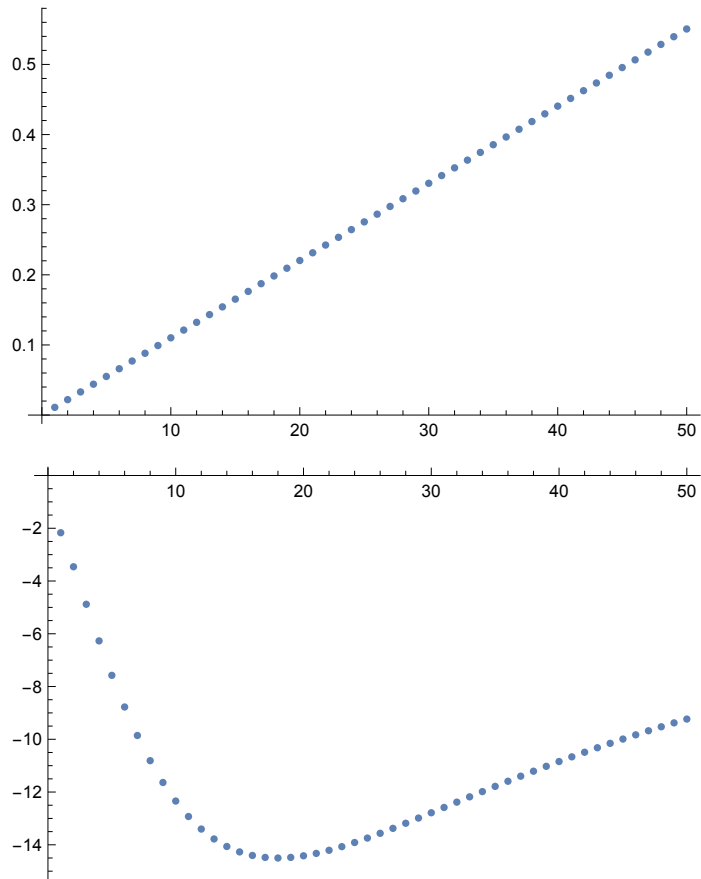
```

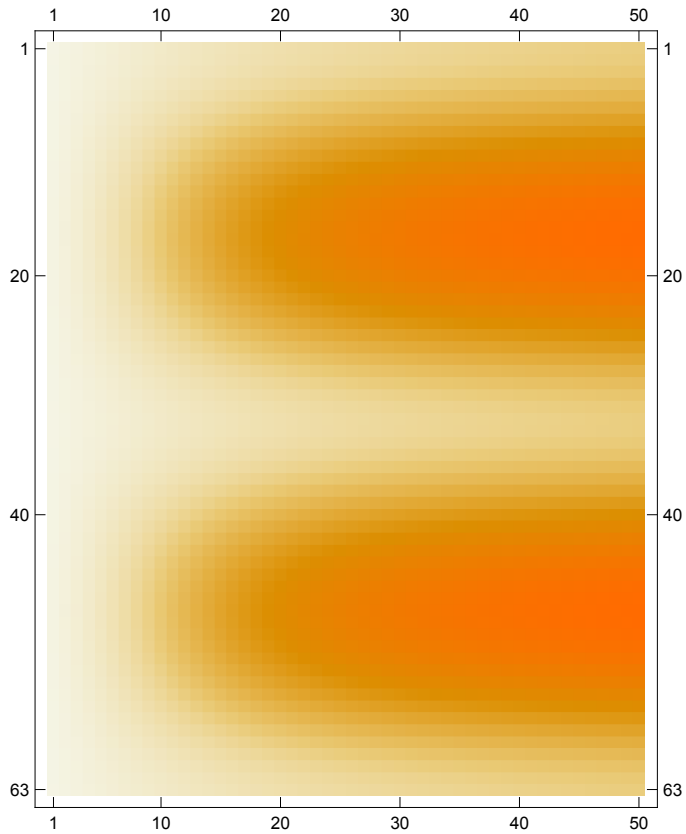
```

epsilonb = 28 - I * 7;
epsilonL[f_] := 3.1686 + (28.938 / (1 + I * (f / 10^9) / 18)) - I * (0.5672 / (f / 10^9));
start = 1 * 10^9;
end = 30 * 10^9;
step = 1 * 10^9;
arr = Table[Attenuation[0.114, 0.114, 1.31, i, epsilonb, Pi / 2, Pi / 2, 0.013],
  {i, start, end, step}] + Table[Attenuation[0.06, 0.06, 0.99,
  i, epsilonb, Pi / 2, Pi / 2, 0.073], {i, start, end, step}] +
Table[Attenuation[0.028, 0.028, 0.82, i, epsilonb, Pi / 2, Pi / 2, 0.041],
  {i, start, end, step}] + Table[Attenuation[0.007, 0.007,
  0.54, i, epsilonb, Pi / 2, Pi / 2, 5.1], {i, start, end, step}] +
Table[Attenuation[0.002, 0.002, 0.12, i, epsilonb, Pi / 2, Pi / 2, 56],
  {i, start, end, step}] + Table[Attenuation[0.037, 0.037, 0.0002,
  i, epsilonL[i], Pi / 2, Pi / 2, 0.013], {i, start, end, step}]

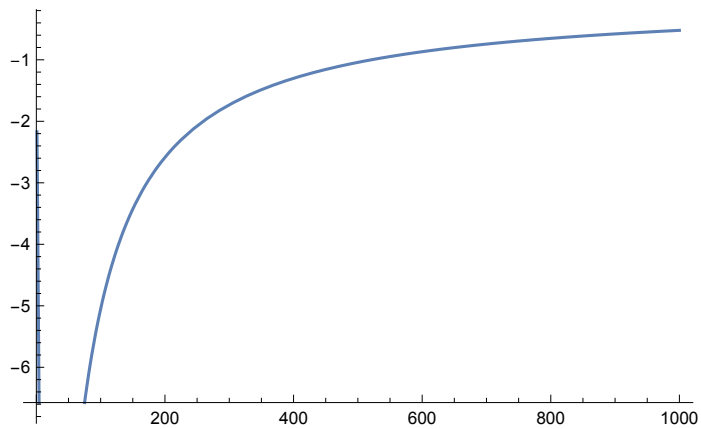
mat = Table[Attenuation[0.114, 0.114, 1.31, i, epsilonb, angle, Pi / 2, 0.013],
  {angle, 0, 2 * Pi, .1}, {i, start, end, step}] +
Table[Attenuation[0.06, 0.06, 0.99, i, epsilonb, angle, Pi / 2, 0.073],
  {angle, 0, 2 * Pi, .1}, {i, start, end, step}] +
Table[Attenuation[0.028, 0.028, 0.82, i, epsilonb, angle, Pi / 2, 0.041],
  {angle, 0, 2 * Pi, .1}, {i, start, end, step}] +
Table[Attenuation[0.007, 0.007, 0.54, i, epsilonb, angle, Pi / 2, 5.1],
  {angle, 0, 2 * Pi, .1}, {i, start, end, step}] +
Table[Attenuation[0.002, 0.002, 0.12, i, epsilonb, angle, Pi / 2, 56],
  {angle, 0, 2 * Pi, .1}, {i, start, end, step}] +
Table[Attenuation[0.037, 0.037, 0.0002, i, epsilonL[i], angle, Pi / 2, 420],
  {angle, 0, 2 * Pi, .1}, {i, start, end, step}];
ListPlot[arr]
leafEpsilons = Table[Im[epsilonL[i]], {i, start, end, step}];
ListPlot[leafEpsilons]
MatrixPlot[mat]
{0.0109979, 0.0220004, 0.0330083, 0.0440212, 0.0550384, 0.0660592, 0.0770828,
  0.0881085, 0.0991356, 0.110163, 0.121191, 0.132219, 0.143246, 0.154273,
  0.165298, 0.176321, 0.187344, 0.198365, 0.209384, 0.220402, 0.231419,
  0.242434, 0.253448, 0.264461, 0.275472, 0.286483, 0.297492, 0.3085, 0.319508,
  0.330514, 0.34152, 0.352525, 0.36353, 0.374533, 0.385537, 0.396539,
  0.407541, 0.418543, 0.429544, 0.440545, 0.451545, 0.462545, 0.473545,
  0.484544, 0.495543, 0.506542, 0.51754, 0.528539, 0.539537, 0.550535}

```





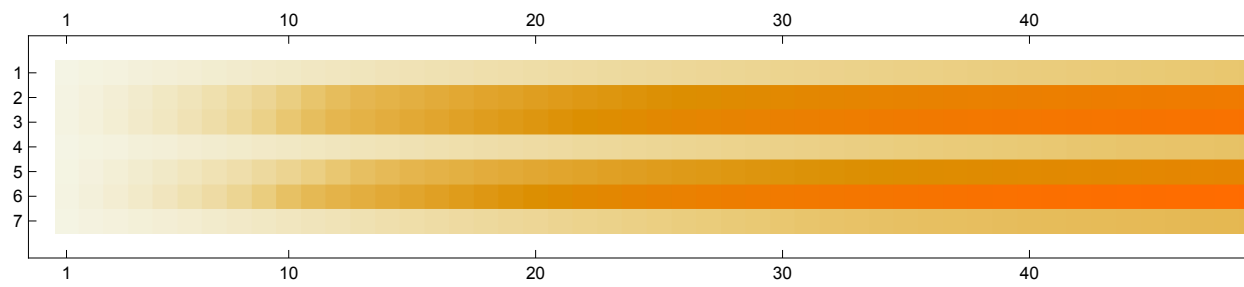
```
Plot[Im[epsilonI[f]], {f, 1, 1000}]
```



```
epsilonI[2 * 10^9]
```

```
31.7537 - 3.45972 i
```

MatrixPlot[mat]



Attenuation[0.037, 0.037, 0.0002, 1.9 * 10^9, epsilon][1.9 * 10^9], Pi / 2, Pi / 2, 420]

```

(-Sin[VegetationAtten`Private`beta] ×
  Sin[VegetationAtten`Private`alpha - VegetationAtten`Private`phii]
  ((0. + 0. i) + (0.0000187576 - 2.02239 × 10-6 i) Sin[VegetationAtten`Private`beta] ×
    Sin[VegetationAtten`Private`alpha - VegetationAtten`Private`phii]) +
  (-Cos[VegetationAtten`Private`alpha - VegetationAtten`Private`phii] ×
    Cos[VegetationAtten`Private`thetai] × Sin[VegetationAtten`Private`beta] -
    Cos[VegetationAtten`Private`beta] × Sin[VegetationAtten`Private`thetai])
  ((0. + 0. i) + (0.00444877 - 0.000479652 i)
    (-Cos[VegetationAtten`Private`alpha - VegetationAtten`Private`phii] ×
      Cos[VegetationAtten`Private`thetai] × Sin[VegetationAtten`Private`beta] -
      Cos[VegetationAtten`Private`beta] × Sin[VegetationAtten`Private`thetai])
    (-0.00421636 (Cos[VegetationAtten`Private`beta] × Cos[
      VegetationAtten`Private`thetai] - Cos[VegetationAtten`Private`alpha -
      VegetationAtten`Private`phii] × Sin[VegetationAtten`Private`beta] ×
      Sin[VegetationAtten`Private`thetai])2 + 0.991567
      (1 - (Cos[VegetationAtten`Private`beta] × Cos[VegetationAtten`Private`thetai] -
        Cos[VegetationAtten`Private`alpha - VegetationAtten`Private`phii] ×
        Sin[VegetationAtten`Private`beta] ×
        Sin[VegetationAtten`Private`thetai])2)))))) /
  (√ (Sin[VegetationAtten`Private`beta]2 Sin[VegetationAtten`Private`alpha -
    VegetationAtten`Private`phii]2 +
    (-Cos[VegetationAtten`Private`alpha - VegetationAtten`Private`phii] ×
      Cos[VegetationAtten`Private`thetai] × Sin[VegetationAtten`Private`beta] -
      Cos[VegetationAtten`Private`beta] × Sin[VegetationAtten`Private`thetai])2)2)
--
(Cos[VegetationAtten`Private`alpha] ×
  Sin[VegetationAtten`Private`beta] ((0. + 0. i) - (0.0000187576 - 2.02239 × 10-6 i)
    Cos[VegetationAtten`Private`alpha] × Sin[VegetationAtten`Private`beta]) -
  Cos[VegetationAtten`Private`beta] ((0. + 0. i) - (0.00444877 - 0.000479652 i)
    Cos[VegetationAtten`Private`beta] (-0.00421636 Sin[VegetationAtten`Private`alpha]2
      Sin[VegetationAtten`Private`beta]2 + 0.991567 (1 -
        Sin[VegetationAtten`Private`alpha]2 Sin[VegetationAtten`Private`beta]2)))))) /
  (√ (Cos[VegetationAtten`Private`beta]2 + Cos[VegetationAtten`Private`alpha]2
    Sin[VegetationAtten`Private`beta]2)2)
0.568898

Sin[1]
Sin[1]

```

```
Table[{i, angle}, {i, 0, 10}, {angle, 0, Pi, 1}]
```

```
{{{0, 0}, {0, 1}, {0, 2}, {0, 3}},
 {{1, 0}, {1, 1}, {1, 2}, {1, 3}}, {{2, 0}, {2, 1}, {2, 2}, {2, 3}},
 {{3, 0}, {3, 1}, {3, 2}, {3, 3}}, {{4, 0}, {4, 1}, {4, 2}, {4, 3}},
 {{5, 0}, {5, 1}, {5, 2}, {5, 3}}, {{6, 0}, {6, 1}, {6, 2}, {6, 3}},
 {{7, 0}, {7, 1}, {7, 2}, {7, 3}}, {{8, 0}, {8, 1}, {8, 2}, {8, 3}},
 {{9, 0}, {9, 1}, {9, 2}, {9, 3}}, {{10, 0}, {10, 1}, {10, 2}, {10, 3}}}
```

```
Table[Attenuation[0.114, 0.114, 1.31,
```

```
1.9*10^9, epsilonb, angle, 2*Pi, 0.013], {angle, 0, Pi, 1}]
```

```
Sin[Pi/8]
```

```
--
```

```
0
```

```
(-Cos[VegetationAtten`Private`alpha] × Sin[VegetationAtten`Private`beta]
 ((0. + 0. i) - (0.00287799 - 0.000746146 i) Cos[VegetationAtten`Private`alpha]
 ((-0.508031 + 0.00592524 i) Cos[VegetationAtten`Private`beta]^2 -
 (0.0160619 - 0.0118505 i) (1 - Cos[VegetationAtten`Private`beta]^2))
 Sin[VegetationAtten`Private`beta]) - Sin[VegetationAtten`Private`alpha] ×
 Sin[VegetationAtten`Private`beta] ((0. + 0. i) + (0.00145769 - 0.000396118 i)
 Sin[VegetationAtten`Private`alpha] × Sin[VegetationAtten`Private`beta])) /
 (√ (Cos[VegetationAtten`Private`alpha]^2 Sin[VegetationAtten`Private`beta]^2 +
 Sin[VegetationAtten`Private`alpha]^2 Sin[VegetationAtten`Private`beta]^2)^2)
```

```
-0.0000373838 + 0.0000460901 i
```

```
--
```

```
1
```

```
(-Sin[VegetationAtten`Private`alpha] × Sin[VegetationAtten`Private`beta]
 ((0. + 0. i) + (0.00145769 - 0.000396118 i) Sin[VegetationAtten`Private`alpha] ×
 Sin[VegetationAtten`Private`beta]) + (-Cos[VegetationAtten`Private`beta] × Sin[1] -
 Cos[1] × Cos[VegetationAtten`Private`alpha] × Sin[VegetationAtten`Private`beta])
 ((0. + 0. i) + (0.00287799 - 0.000746146 i) (-Cos[VegetationAtten`Private`beta] × Sin[1] -
 Cos[1] × Cos[VegetationAtten`Private`alpha] × Sin[VegetationAtten`Private`beta])
 ((-0.508031 + 0.00592524 i) (Cos[1] × Cos[VegetationAtten`Private`beta] -
 Cos[VegetationAtten`Private`alpha] × Sin[1] × Sin[
 VegetationAtten`Private`beta])^2 - (0.0160619 - 0.0118505 i) (1 - (Cos[1] ×
 Cos[VegetationAtten`Private`beta] - Cos[VegetationAtten`Private`alpha] ×
 Sin[1] × Sin[VegetationAtten`Private`beta])^2)))) /
 (√ (Sin[VegetationAtten`Private`alpha]^2 Sin[VegetationAtten`Private`beta]^2 +
 (-Cos[VegetationAtten`Private`beta] × Sin[1] - Cos[1] ×
 Cos[VegetationAtten`Private`alpha] × Sin[VegetationAtten`Private`beta])^2)^2)
```

```
-0.00104306 + 0.000293935 i
```


--

2

$$\begin{aligned}
& (-\sin[\text{VegetationAtten`Private`alpha}] \times \sin[\text{VegetationAtten`Private`beta}] \\
& \quad ((0. + 0. i) + (0.00145769 - 0.000396118 i) \sin[\text{VegetationAtten`Private`alpha}] \times \\
& \quad \quad \sin[\text{VegetationAtten`Private`beta}]) + (-\cos[\text{VegetationAtten`Private`beta}] \times \sin[2] - \\
& \quad \cos[2] \times \cos[\text{VegetationAtten`Private`alpha}] \times \sin[\text{VegetationAtten`Private`beta}]) \\
& \quad ((0. + 0. i) + (0.00287799 - 0.000746146 i) (-\cos[\text{VegetationAtten`Private`beta}] \times \sin[2] - \\
& \quad \cos[2] \times \cos[\text{VegetationAtten`Private`alpha}] \times \sin[\text{VegetationAtten`Private`beta}]) \\
& \quad ((-0.508031 + 0.00592524 i) (\cos[2] \times \cos[\text{VegetationAtten`Private`beta}] - \\
& \quad \cos[\text{VegetationAtten`Private`alpha}] \times \sin[2] \times \sin[\\
& \quad \quad \text{VegetationAtten`Private`beta}])^2 - (0.0160619 - 0.0118505 i) (1 - (\cos[2] \times \\
& \quad \cos[\text{VegetationAtten`Private`beta}] - \cos[\text{VegetationAtten`Private`alpha}] \times \\
& \quad \sin[2] \times \sin[\text{VegetationAtten`Private`beta}])^2))))) / \\
& \quad \left(\sqrt{(\sin[\text{VegetationAtten`Private`alpha}]^2 \sin[\text{VegetationAtten`Private`beta}]^2 + \right. \\
& \quad \quad (-\cos[\text{VegetationAtten`Private`beta}] \times \sin[2] - \cos[2] \times \\
& \quad \quad \cos[\text{VegetationAtten`Private`alpha}] \times \sin[\text{VegetationAtten`Private`beta}])^2)^2} \\
& \quad \left. - 0.00121172 + 0.000335501 i \right)
\end{aligned}$$

--

3

$$\begin{aligned}
& (-\sin[\text{VegetationAtten`Private`alpha}] \times \sin[\text{VegetationAtten`Private`beta}] \\
& \quad ((0. + 0. i) + (0.00145769 - 0.000396118 i) \sin[\text{VegetationAtten`Private`alpha}] \times \\
& \quad \quad \sin[\text{VegetationAtten`Private`beta}]) + (-\cos[\text{VegetationAtten`Private`beta}] \times \sin[3] - \\
& \quad \cos[3] \times \cos[\text{VegetationAtten`Private`alpha}] \times \sin[\text{VegetationAtten`Private`beta}]) \\
& \quad ((0. + 0. i) + (0.00287799 - 0.000746146 i) (-\cos[\text{VegetationAtten`Private`beta}] \times \sin[3] - \\
& \quad \cos[3] \times \cos[\text{VegetationAtten`Private`alpha}] \times \sin[\text{VegetationAtten`Private`beta}]) \\
& \quad ((-0.508031 + 0.00592524 i) (\cos[3] \times \cos[\text{VegetationAtten`Private`beta}] - \\
& \quad \cos[\text{VegetationAtten`Private`alpha}] \times \sin[3] \times \sin[\\
& \quad \quad \text{VegetationAtten`Private`beta}])^2 - (0.0160619 - 0.0118505 i) (1 - (\cos[3] \times \\
& \quad \cos[\text{VegetationAtten`Private`beta}] - \cos[\text{VegetationAtten`Private`alpha}] \times \\
& \quad \sin[3] \times \sin[\text{VegetationAtten`Private`beta}])^2))))) / \\
& \quad \left(\sqrt{(\sin[\text{VegetationAtten`Private`alpha}]^2 \sin[\text{VegetationAtten`Private`beta}]^2 + \right. \\
& \quad \quad (-\cos[\text{VegetationAtten`Private`beta}] \times \sin[3] - \cos[3] \times \\
& \quad \quad \cos[\text{VegetationAtten`Private`alpha}] \times \sin[\text{VegetationAtten`Private`beta}])^2)^2} \\
& \quad \left. - 0.000065669 + 0.0000530609 i \right) \\
& \quad \{0.0000313042, 0.0000313042, 0.0000313042, 0.0000313042\}
\end{aligned}$$

$$\sin\left[\frac{\pi}{8}\right]$$

```

$ContextPath
{VegetationAtten`, NaturalLanguageLoader`, StreamingLoader`,
 SymbolicMachineLearningLoader`, NeuralNetworks`, IconizeLoader`,
 HTTPHandlingLoader`, PacletManager`, System`, Global`}

Attenuation[0.037, 0.037, 0.0002, 1.9 * 10^9, 31 - i * 8, 0, Pi / 4, 420]
--
0.156086

N[1 / 7]
0.142857

3.7 / 100
0.037

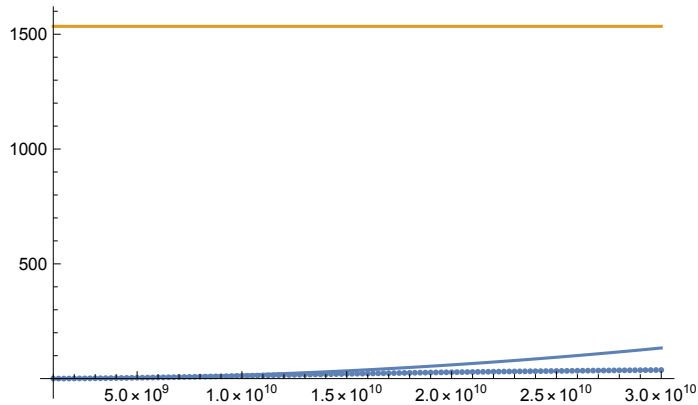
 $x^2 + y^2 /. x \rightarrow 1 /. y \rightarrow 2$ 
5

N[Pi / 2]
1.5708

epsilonb = 28 - I * 7;
epsilonl[f_] := 3.1686 + (28.938 / (1 + I * (f / 10^9) / 18)) - I * (0.5672 / (f / 10^9));
start = 1 * 10^9;
end = 30 * 10^9;
step = 0.25 * 10^9;
li =
Table[{i, Attenuation[0.114, 0.114, 1.31, i, epsilonb, 0, Pi / 2, Pi / 4, 0.013] +
  Attenuation[0.06, 0.06, 0.99, i, epsilonb, 0, Pi / 2, Pi / 4, 0.073] +
  Attenuation[0.028, 0.028, 0.82, i, epsilonb, 0, Pi / 2, Pi / 2, 0.041] +
  Attenuation[0.007, 0.007, 0.54, i, epsilonb, 0, Pi / 2, Pi / 2, 5.1] +
  Attenuation[0.002, 0.002, 0.12, i, epsilonb, 0, Pi / 2, Pi / 2, 56] +
  Attenuation[0.037, 0.037, 0.0002, i, epsilonl[i], 0, Pi / 2, Pi / 2, 420]},
  {i, start, end, step}];
Clear[Attenuation]

```

```
fits = FindFormula[li, x, 1, "Error", PerformanceGoal -> "Quality"]
Show[Plot[fits, {x, 1 * 10^9, 30 * 10^9}, PlotRange -> All], ListPlot[li]]
{0.051166 + 1.01536 * 10^-10 x + 1.45033 * 10^-19 x^2, 1534.37}
```

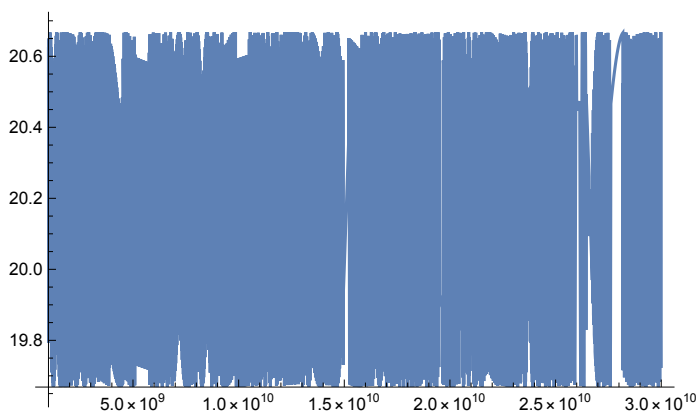


```
nlm = NonlinearModelFit[li, a + Sin[x / c]^2, {a, b, c, d, e}, x]
nlm[{"BestFit", "ParameterTable"}]
Show[Plot[nlm[x], {x, 1 * 10^9, 30 * 10^9}], ListPlot[li]]
```

⋯ **NonlinearModelFit** : The step size in the search has become less than the tolerance prescribed by the PrecisionGoal option, but the gradient is larger than the tolerance specified by the AccuracyGoal option. There is a possibility that the method has stalled at a point that is not a local minimum.

FittedModel [19.6684 + Sin[1. x]^2]

		Estimate	Standard Error	t-Statistic	P-Value
{ 19.6684 + Sin[1. x]^2 ,	a	19.6684	1.13873	17.2722	2.31753×10^{-33}
	b	1.	0.	∞	$0. \times 10^{-308}$
	c	1.	9.09891×10^{-11}	1.09903×10^{10}	$1.094959412559185 \times 10^{-1011}$
	d	1.	0.	∞	$0. \times 10^{-308}$
	e	1.	0.	∞	$0. \times 10^{-308}$

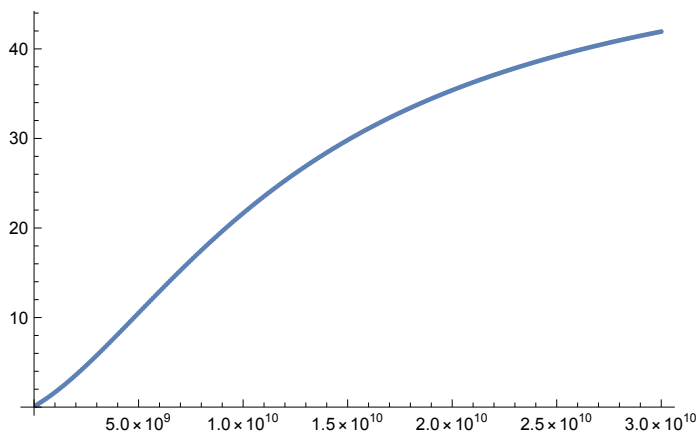




```
Clear[nlm]
```

```

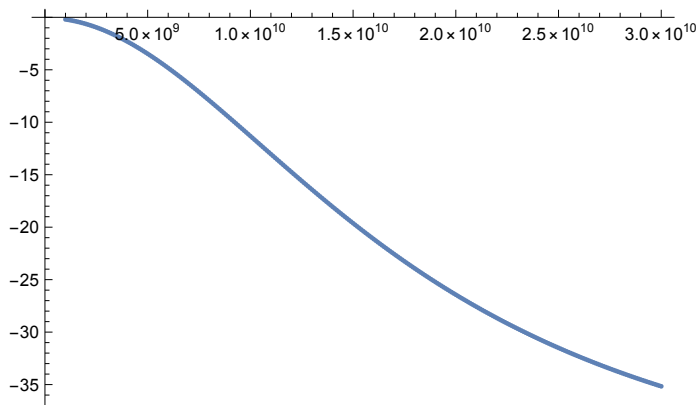
epsilonb = 28 - I * 7;
epsilonl[f_] := 3.1686 + (28.938 / (1 + I * (f / 10^9) / 18)) - I * (0.5672 / (f / 10^9));
start = 0.1 * 10^9;
end = 30 * 10^9;
step = 1 * 10^8;
li = Table[{i,
  Attenuation[0.0025, 0.0025, 0.305, i, epsilonb, 0, Pi / 2, Pi / 2, 10] +
  Attenuation[0.015, 0.015, 2.6162, i, epsilonb, 0, Pi / 2, Pi / 4, 0.01] +
  Attenuation[0.0005, 0.0005, 0.09, i, epsilonb, 0, Pi / 2, Pi / 2, 56] +
  Attenuation[0.001, 0.001, 0.015, i, epsilonl[i], 0, Pi / 2, Pi / 2, 420]
}, {i, start, end, step}];
ListPlot[li]
f = Interpolation[li]

```



InterpolatingFunction [  Domain: $\{\{1. \times 10^8, 3. \times 10^{10}\}\}$
Output: scalar]

```
ListPlot[li]
```



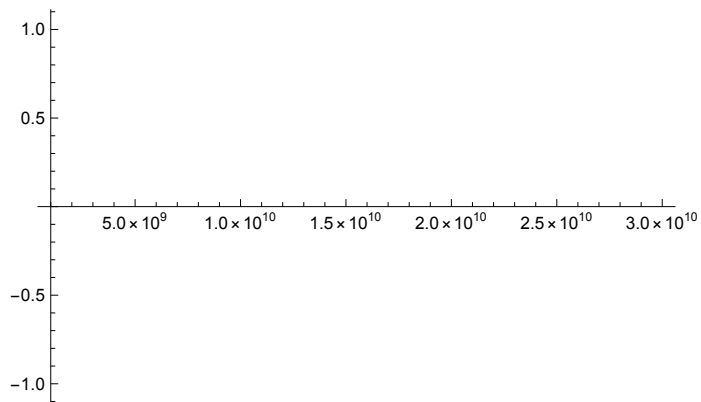
```
Attenuation[0.001, 0.001, 0.015,
  1.9 * 10^9, epsilonL[1.9 * 10^9], 0, Pi / 2, Pi / 2, 420]
1.74779
```

```
Sqrt[1 - (0.001 / 0.015) ^ 2]
0.997775
```

```
N[100 * (1 - 10 ^ (3.5 / 10))]
-123.872
```

```
f[2 * 10^9]
3.58942
```

```
Plot[f[x], {x, 1 * 10^9, 30 * 10^9}]
```




```
FourierSeries[Interpolation[li][x], x, 1]
```


```
FourierSeries[InterpolatingFunction[ Domain: {{1. x 10^9, 3. x 10^10}} Output: scalar][x], x, 1]
```

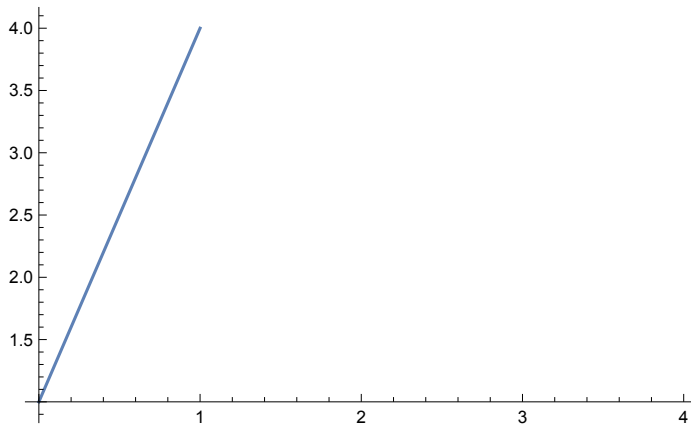
```
b = BSplineFunction[{1, 2, 3, 4}]
```

```
b[1*10^9]
```

```
Plot[b[x], {x, 0, 4}]
```

```
BSplineFunction[ Argument count: 1  
Output: scalar]
```


```
BSplineFunction[ Argument count: 1  
Output: scalar] [1 000 000 000]
```



```
li
```

```
{ {1 000 000 000, 1.65299}, {2 000 000 000, 3.58942}, {3 000 000 000, 5.77848},  
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  {7 000 000 000, 15.2529}, {8 000 000 000, 17.5015}, {9 000 000 000, 19.6376},  
  {10 000 000 000, 21.649}, {11 000 000 000, 23.5312}, {12 000 000 000, 25.2843},  
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```

```
GeneralizedLinearModelFit[%130, {x}, {x}]
```

```
FittedModel[ 5.53309 + 1.38657 × 10-9 x]
```

Transpose[%128]

```
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  38.5526, 39.2137, 39.8311, 40.4084, 40.949, 41.4558, 41.9315} }
```

str = OpenWrite[]

Write[str, li]

Close[str]

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DeleteFile[str]

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DeleteFile : String or non -empty list of strings is expected at position 1 in DeleteFile [OutputStream [
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epsilonb = 28 - I * 7;

epsilonI[f_] := 3.1686 + (28.938 / (1 + I * (f / 10^9) / 18)) - I * (0.5672 / (f / 10^9));

start = 0.1 * 10^9;

end = 30 * 10^9;

step = 1 * 10^7;

pine = Table[{i,

```
Attenuation[0.0025, 0.0025, 0.305, i, epsilonb, 0, Pi / 2, Pi / 2, 10] +
Attenuation[0.015, 0.015, 2.6162, i, epsilonb, 0, Pi / 2, Pi / 4, 0.01] +
Attenuation[0.0005, 0.0005, 0.09, i, epsilonb, 0, Pi / 2, Pi / 2, 56] +
Attenuation[0.001, 0.001, 0.015, i, epsilonI[i], 0, Pi / 2, Pi / 2, 420]],
{i, start, end, step}];
```

oak = Table[{i,

```
Attenuation[0.114, 0.114, 1.31, i, epsilonb, 0, Pi / 2, Pi / 4, 0.013] +
Attenuation[0.06, 0.06, 0.99, i, epsilonb, 0, Pi / 2, Pi / 4, 0.073] +
Attenuation[0.028, 0.028, 0.82, i, epsilonb, 0, Pi / 2, Pi / 2, 0.041] +
Attenuation[0.007, 0.007, 0.54, i, epsilonb, 0, Pi / 2, Pi / 2, 5.1] +
Attenuation[0.002, 0.002, 0.12, i, epsilonb, 0, Pi / 2, Pi / 2, 56] +
Attenuation[0.037, 0.037, 0.0002, i, epsilonI[i], 0, Pi / 2, Pi / 2, 420]],
{i, start, end, step}];
```

Export["pine.txt", pine, "CSV"];

Export["oak.txt", oak, "CSV"];

Export["test.txt", pine, "CSV"]

test.txt

FindFile["test.txt"]

/Users/michaeldeleo/test.txt