

Final Project of ELEC5470 FALL 2017

Optimization in Image Deblurring

Initial Proposal

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Abstract

In this report, I present some representative image deblurring algorithms and the convex/non-convex optimization techniques used in these papers.

Index Terms

Optimization, Image Deblurring, Prior

I. INTRODUCTION

Nowadays, smart phone has become the digital hub of everyone's daily life, and camera is one of the most important modules on smart phones. However, limited by the space of smart phones, the smart phone camera optic system is often very simple and CMOS size is usually very small. That means the image quality is easily affected environment, for example, low light condition leads to severe noise, camera shaking and long exposure time causes uncomfortable blur effect. In this report, I focus on how to remove the image blur effects caused by camera shaking.

Image deblurring is a fundamental computer vision research problem. Now, there are two different ways to solve the image deblurring problem: 1) traditional convolutional model approach; 2) neural network approach. In this report, I mainly focus on the first approach and give some brief introductions of the second approach.

A. Traditional Convolutional Model Approach

In traditional convolutional model, the image blur effect is expressed by 2D convolution:

$$\mathbf{b} = \mathbf{l} \otimes \mathbf{k} + \mathbf{n}, \quad (1)$$

where \mathbf{b} , \mathbf{l} and \mathbf{k} are the blurry image, latent sharp/unblurred image and blur kernel respectively. \mathbf{n} denotes the noise. The blur kernel \mathbf{k} is usually expressed by a small matrix which is related to the camera shaking trajectory, as shown in the Fig. 1. Because the 2D convolution is difficult to handle, Eqn. 1 is often written in frequency domain:

$$\mathcal{F}(\mathbf{b}) = \mathcal{F}(\mathbf{l}) \cdot \mathcal{F}(\mathbf{k}) + \mathcal{F}(\mathbf{n}), \quad (2)$$

where $\mathcal{F}(\cdot)$ denotes the Fourier transform.

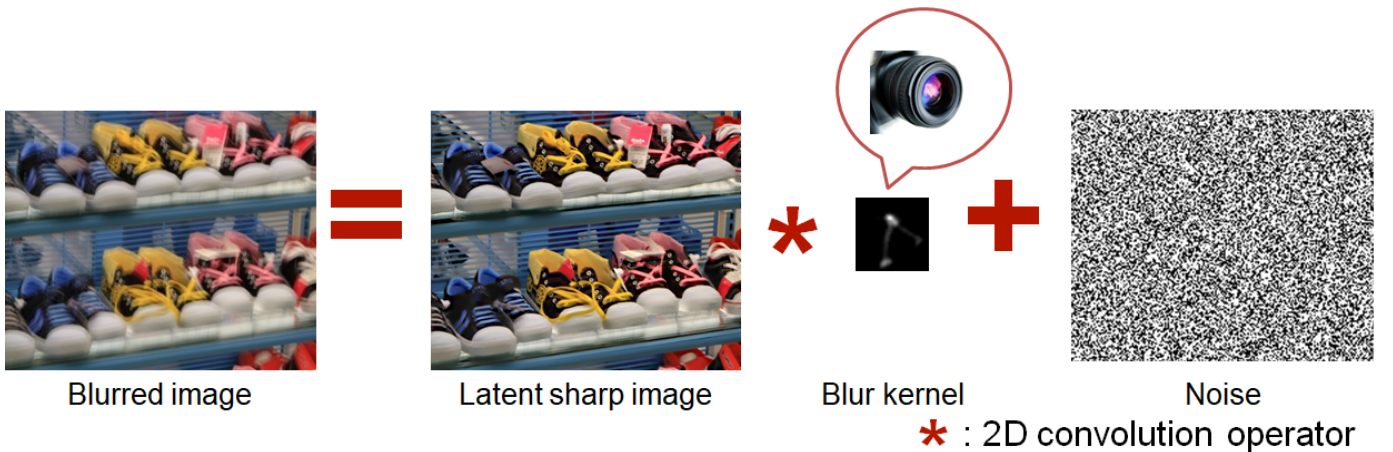


Fig. 1: Image Convolutional Blur Model

The deblurring problem can be divide into two kinds: 1) non-blind deblurring: only \mathbf{l} is unknown, use existing \mathbf{k} to solve latent sharp image \mathbf{l} :

$$\min_{\mathbf{l}} \|\mathbf{b} - \mathbf{l} \otimes \mathbf{k}\|. \quad (3)$$

2) Blind deblurring: both \mathbf{l} and \mathbf{k} are unknown:

$$\min_{\mathbf{l}, \mathbf{k}} \|\mathbf{b} - \mathbf{l} \otimes \mathbf{k}\|, \quad (4)$$

The non-blind deblurring looks easy, but in fact, it is very tough in image deblurring problems. I recommend the readers to read the simple introduction [1]<https://blogs.mathworks.com/steve/2007/08/13/image-deblurring-introduction/> first. The results are shown in Fig. 2: (a) and (d) show the blurry image and groundtruth image respectively. (b) is the deblurring result using pseudo inverse filter. We can see that although the main structure of the image is recovered, a lot of artifacts (ringing and noise) are introduced. (c) is the result of the state-of-the-art non blind deblurring algorithm [2], which I will introduce in next section.

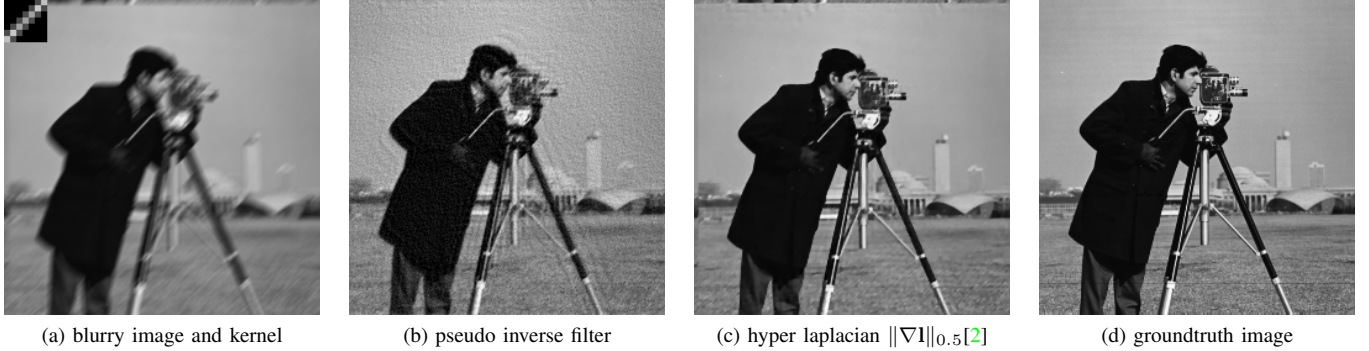


Fig. 2: Image Deblurring Example

To solve the problem is Fig. 2(b), existing state-of-the-art algorithms usually solve the following optimization problem with image prior ϕ and kernel prior ρ instead of original one: 1) Non-blind deblurring

$$\min_{\mathbf{l}} \|\mathbf{b} - \mathbf{l} \otimes \mathbf{k}\| + \lambda \phi(\mathbf{l}). \quad (5)$$

2) Blind deblurring

$$\min_{\mathbf{l}, \mathbf{k}} \|\mathbf{b} - \mathbf{l} \otimes \mathbf{k}\| + \lambda \phi(\mathbf{l}) + \mu \rho(\mathbf{k}). \quad (6)$$

Usually, Eqn. 6 will be split into two minimization problems and solve \mathbf{l} and \mathbf{k} alternatively:

$$\begin{cases} \min_{\mathbf{l}} & \|\mathbf{b} - \mathbf{l} \otimes \mathbf{k}\| + \lambda \phi(\mathbf{l}) \\ \min_{\mathbf{k}} & \|\mathbf{b} - \mathbf{l} \otimes \mathbf{k}\| + \mu \rho(\mathbf{k}) \end{cases} \quad (7)$$

B. Neural Network Approach

The convolutional model looks very beautiful, but solving it is really not easy. Therefore, some researchers proposed to use neural network to predict the latent sharp image directly. For example, the neural network in Fig. 3 takes the stacked nearby videos frames as input, and directly output the deblurred central video.

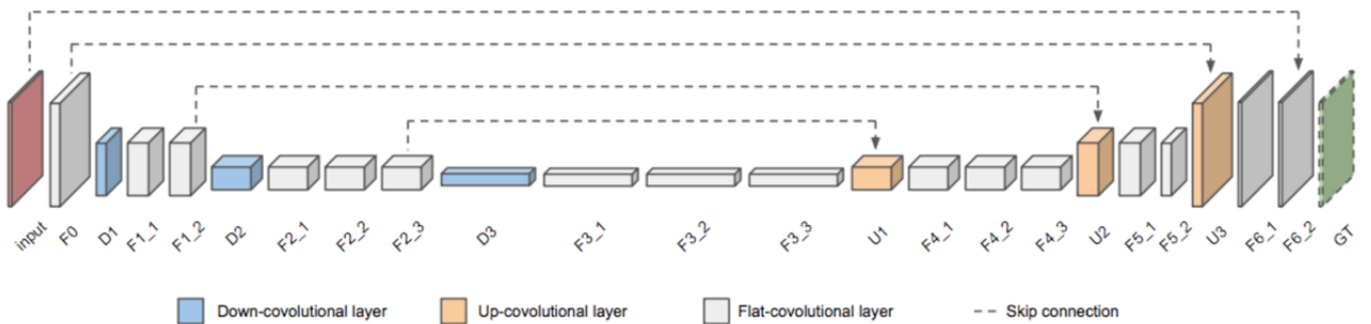


Fig. 3: Structure of CNN used in Deep Video Deblurring[3]

Until now, the neural network is still a black box to researchers. No one could give a theoretical explanation, so I am not going to talk the details here.

II. OVERVIEW OF EXISTING WORK

In this section, I categorize the representative deblurring algorithms into 3 kinds: 1) image priors; 2) kernel priors; 3) neural networks priors.

A. Image Priors

As mentioned above, I formulate the image deblurring objective function as following minimization problem:

$$\min_{\mathbf{l}, \mathbf{k}} \|\mathbf{b} - \mathbf{l} \otimes \mathbf{k}\| + \lambda \phi(\mathbf{l}) + \mu \rho(\mathbf{k}). \quad (8)$$

Hyper-laplacian Prior[2]: this paper proposed a excellent non-blind image deblurring algorithm. Kernel is already given in non-blind deblurring so I only need to solve the first problem in Eqn. 7. A hyper-laplacian image prior $\phi(\mathbf{l}) = \|\nabla \mathbf{l}\|_\alpha$ is proposed in this paper. As shown in Fig. 4, the dark blue curve denotes the empirical image gradient distribution of natural images. The reason why hyper-laplacian is proposed is that the curve shape of hyper-laplacian (green) is closet to the empirical one (dark blue).

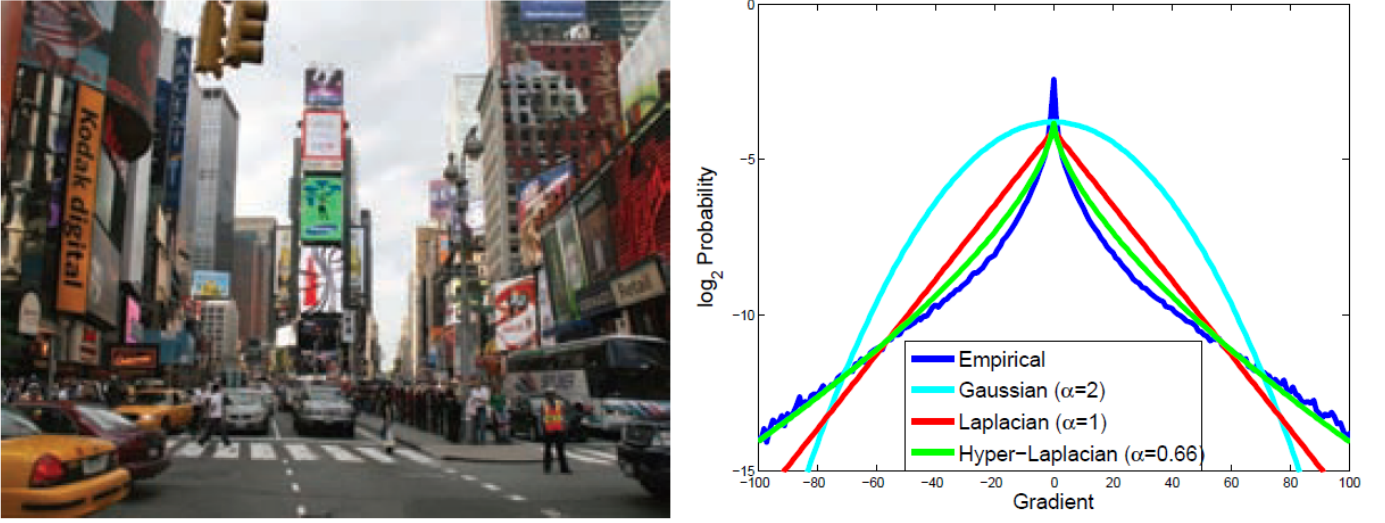


Fig. 4: Hyper-Laplacian Image Prior[3]

However, solving the problem is still not trivial because the image prior $\phi(\mathbf{l}) = \|\nabla \mathbf{l}\|_\alpha$ is non-convex. The most commonly used method in image deblurring is to re-formulate the objective function again:

$$\min_{\mathbf{l}} \|\mathbf{b} - \mathbf{l} \otimes \mathbf{k}\|_2^2 + \lambda_1 \|\nabla \mathbf{l} - \mathbf{g}\|_2^2 + \lambda_2 \|\mathbf{g}\|_\alpha. \quad (9)$$

Eqn. 10 can be divided into two sub-optimization problems and solve alternatively:

$$\begin{cases} \min_{\mathbf{l}} & \|\mathbf{b} - \mathbf{l} \otimes \mathbf{k}\|_2^2 + \lambda_1 \|\nabla \mathbf{l} - \mathbf{g}\|_2^2 \\ \min_{\mathbf{g}} & \lambda_1 \|\nabla \mathbf{l} - \mathbf{g}\|_2^2 + \lambda_2 \|\mathbf{g}\|_\alpha. \end{cases} \quad (10)$$

B. Kernel Priors

C. Neural Networks Priors

III. CONCLUSION

The conclusion goes here.

REFERENCES

- [1] S. Eddins, "Image deblurring introduction," <https://blogs.mathworks.com/steve/2007/08/13/image-deblurring-introduction/>.
- [2] D. Krishnan and R. Fergus, "Fast image deconvolution using hyper-laplacian priors," in *Advances in Neural Information Processing Systems*, 2009, pp. 1033–1041.
- [3] S. Su, M. Delbracio, J. Wang, G. Sapiro, W. Heidrich, and O. Wang, "Deep video deblurring," *arXiv preprint arXiv:1611.08387*, 2016.