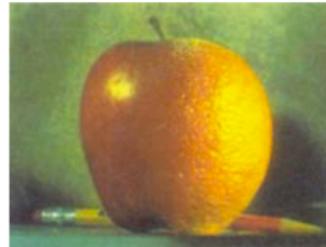


2. Image Formation



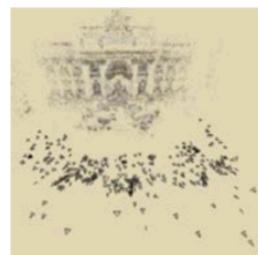
3. Image Processing



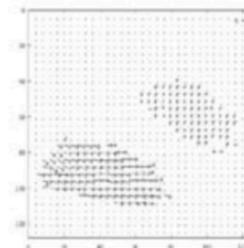
4. Features



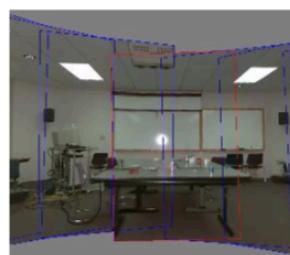
5. Segmentation



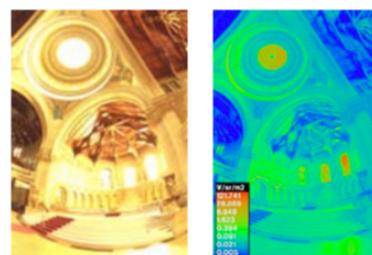
6-7. Structure from Motion



8. Motion



9. Stitching



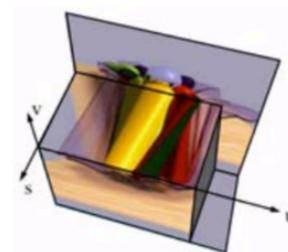
10. Computational Photography



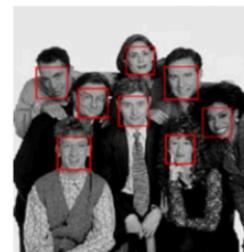
11. Stereo



12. 3D Shape



13. Image-based Rendering



14. Recognition

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# Edge detection

- **Goal:** map image from 2d array of pixels to a set of curves or line segments or contours.
- **Why?**



Figure from D. Lowe

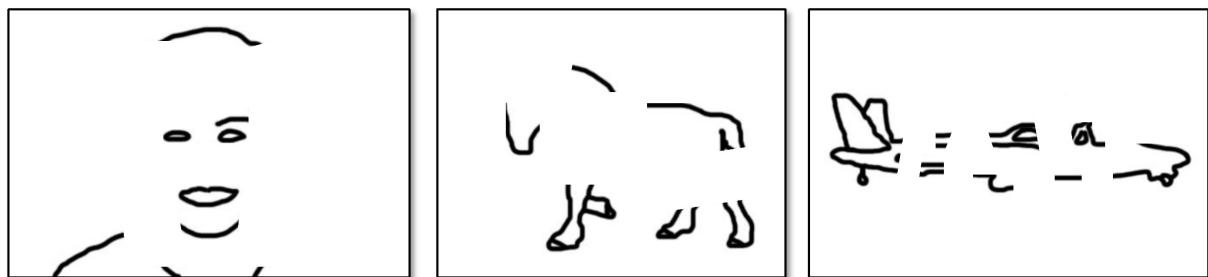
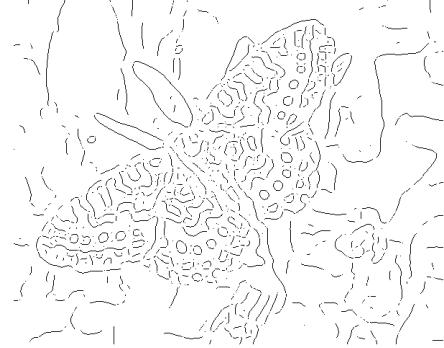


Figure from J. Shotton et al., PAMI 2007

- **Main idea:** look for strong **gradients**, post-process



# Gradients → edges



Primary edge detection steps:

1. Smoothing: suppress noise
2. Edge enhancement: filter for contrast
3. Edge localization

Determine which local maxima from filter output  
are actually edges vs. noise

- Threshold, Thin

# Thresholding

- Choose a threshold value  $t$
- Set any pixels less than  $t$  to zero (off)
- Set any pixels greater than or equal to  $t$  to one (on)

# Original image



# Gradient magnitude image



# Thresholding gradient with a lower threshold



# Thresholding gradient with a higher threshold



# Canny edge detector

- Filter image with derivative of Gaussian
- Find magnitude and orientation of gradient
- **Non-maximum suppression:**
  - Thin wide “ridges” down to single pixel width
- **Linking and thresholding (hysteresis):**
  - Define two thresholds: low and high
  - Use the high threshold to start edge curves and the low threshold to continue them
- MATLAB: `edge(image, 'canny');`
- `>>help edge`

# The Canny edge detector



original image (Lena)

# The Canny edge detector



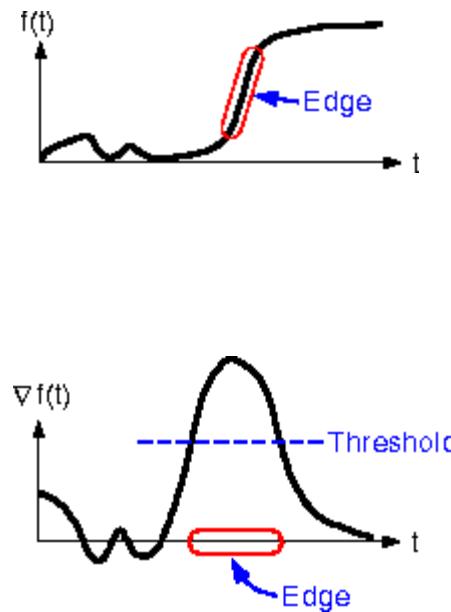
norm of the gradient

# The Canny edge detector



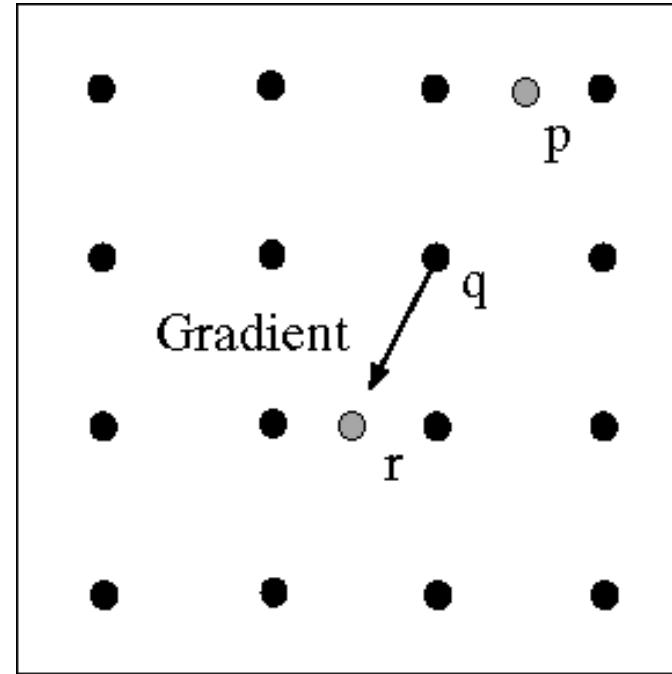
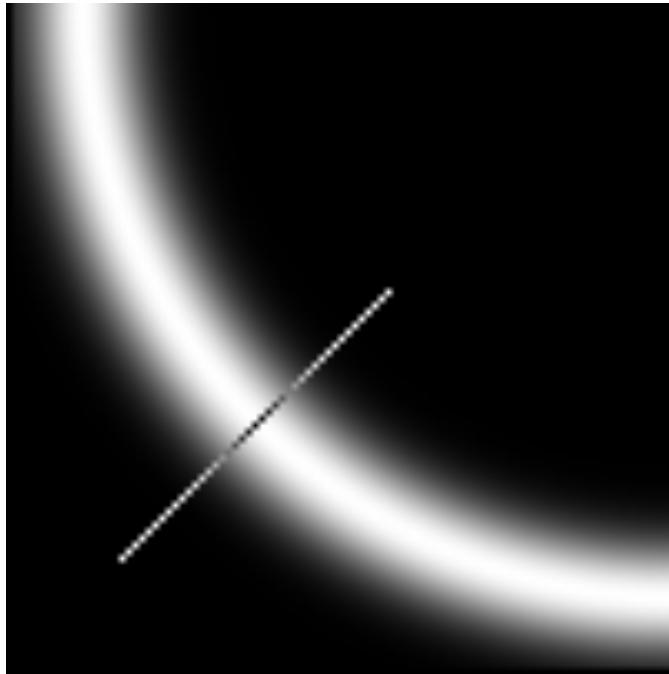
thresholding

# The Canny edge detector



How to turn  
these thick  
regions of the  
gradient into  
curves?

# Non-maximum suppression

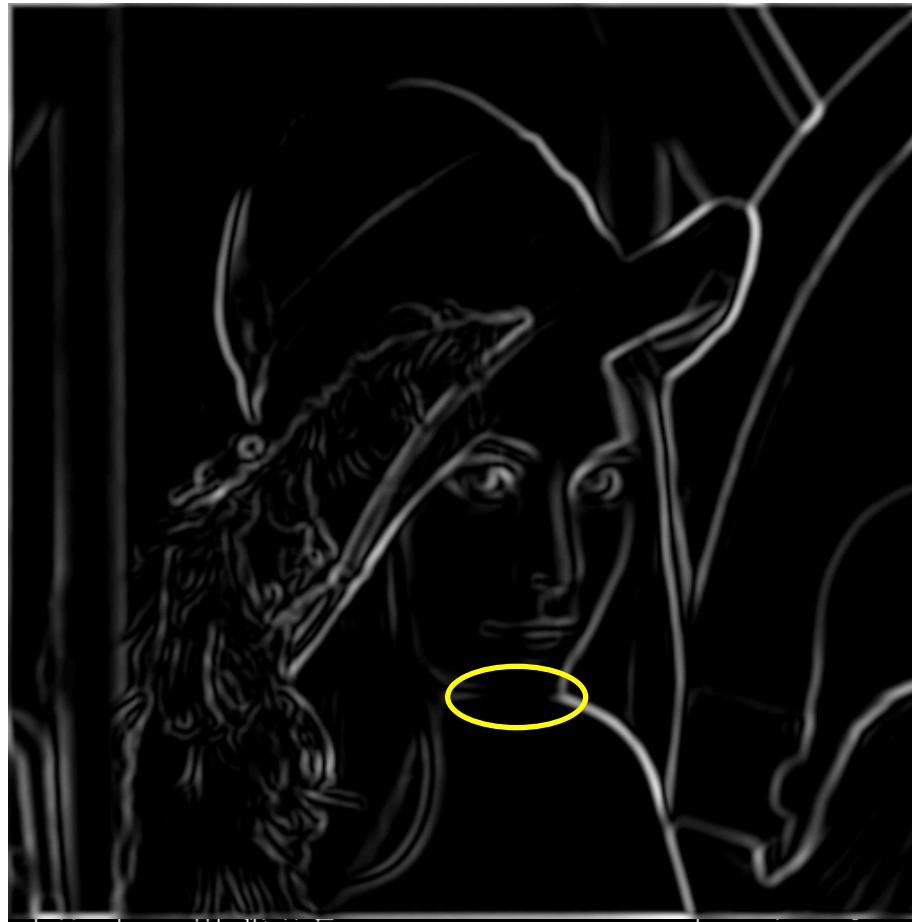


Check if pixel is local maximum along gradient direction

Select single max across width of the edge

Requires checking interpolated pixels p and r

# The Canny edge detector

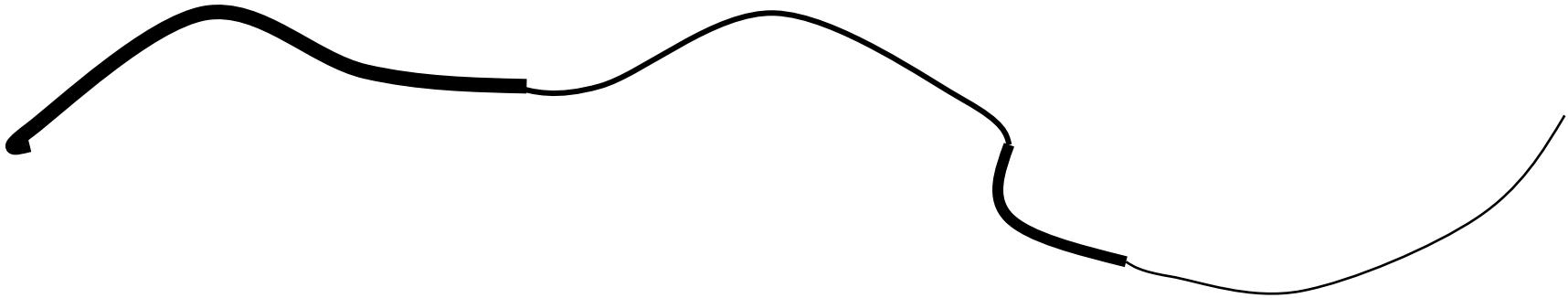


thinning  
(non-maximum suppression)

Problem:  
pixels along  
this edge  
didn't  
survive the  
thresholding

# Hysteresis thresholding

- Use a high threshold to start edge curves, and a low threshold to continue them.



# Hysteresis thresholding



original image



high threshold  
(strong edges)



low threshold  
(weak edges)

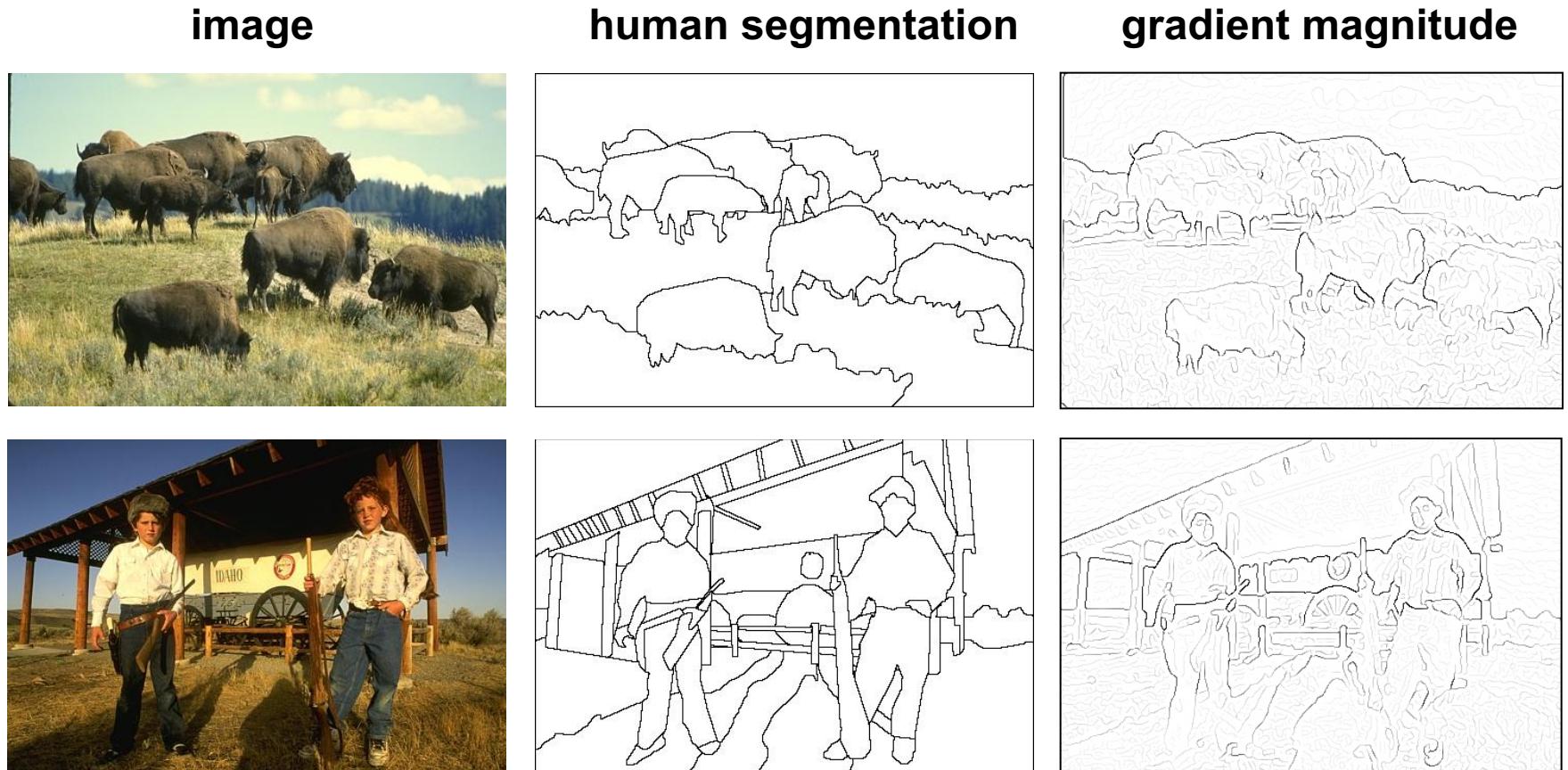


hysteresis threshold

# Recap: Canny edge detector

- Filter image with derivative of Gaussian
- Find magnitude and orientation of gradient
- **Non-maximum suppression:**
  - Thin wide “ridges” down to single pixel width
- **Linking and thresholding (hysteresis):**
  - Define two thresholds: low and high
  - Use the high threshold to start edge curves and the low threshold to continue them
- MATLAB: `edge(image, 'canny');`
- `>>help edge`

# Low-level edges vs. perceived contours

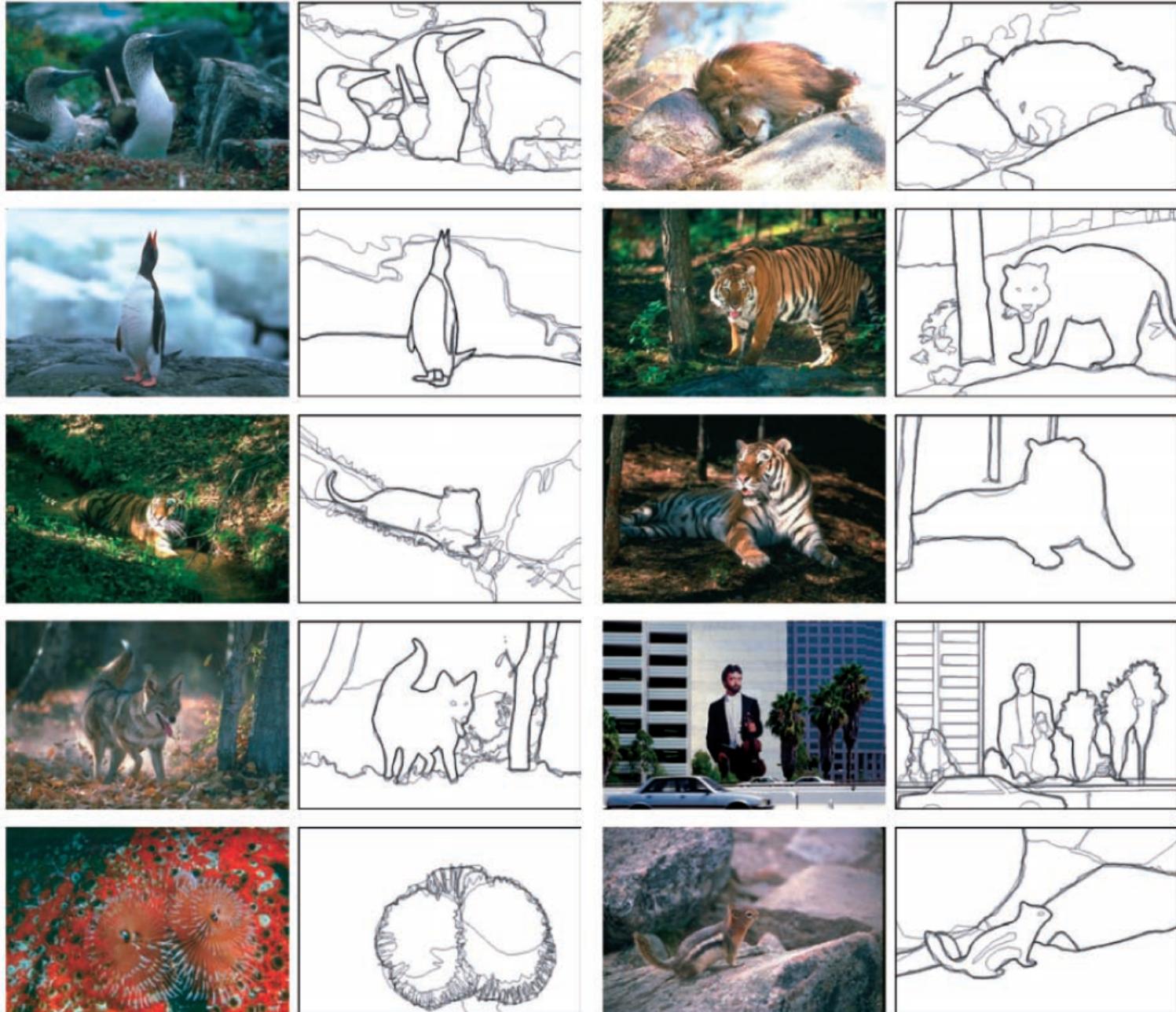


- Berkeley segmentation database:

<http://www.eecs.berkeley.edu/Research/Projects/CS/vision/grouping/segbench/>

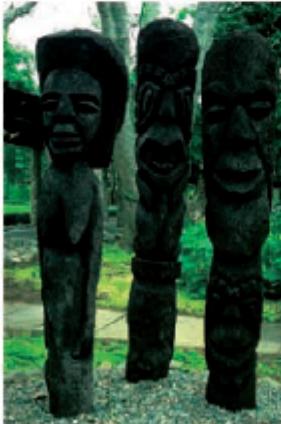
Learn from humans which combination of features is most indicative of a “good” contour?

[D. Martin et al.  
PAMI 2004]

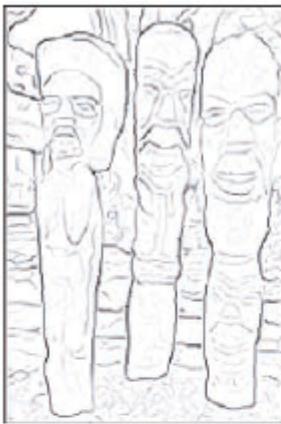


Human-marked segment boundaries

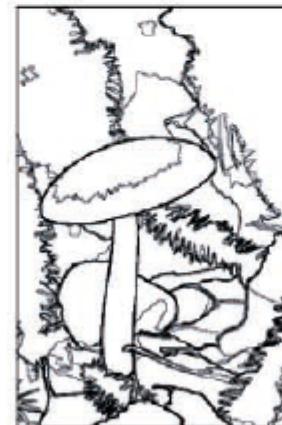
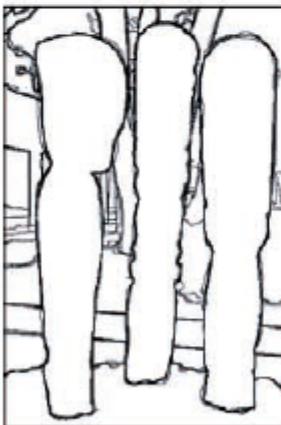
Image



BG+CG+TG

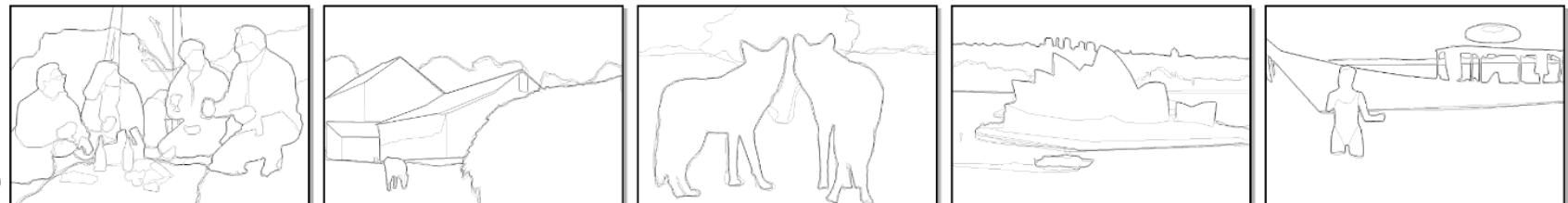


Human

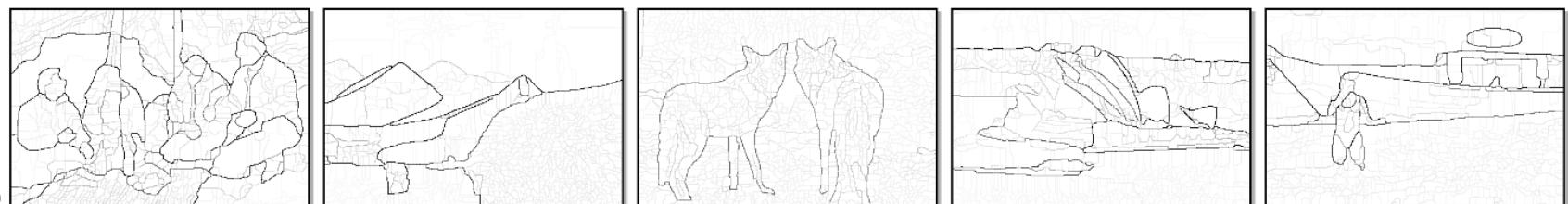




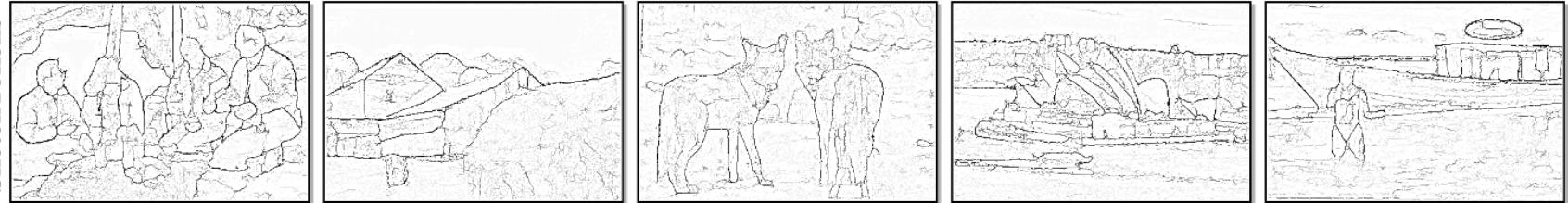
ground truth



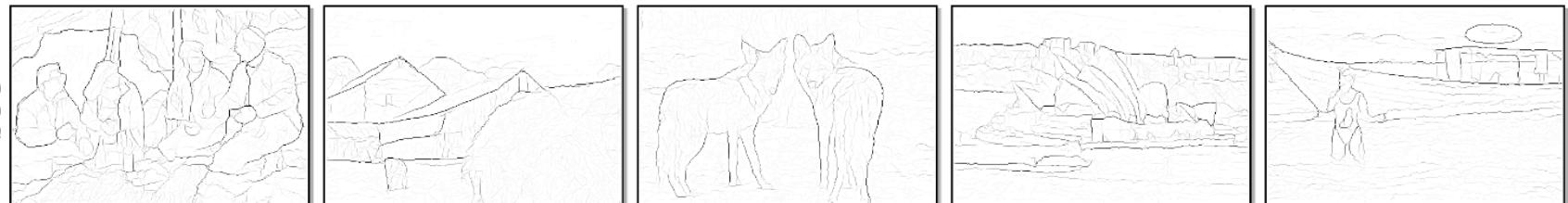
gPb+owt+ucm



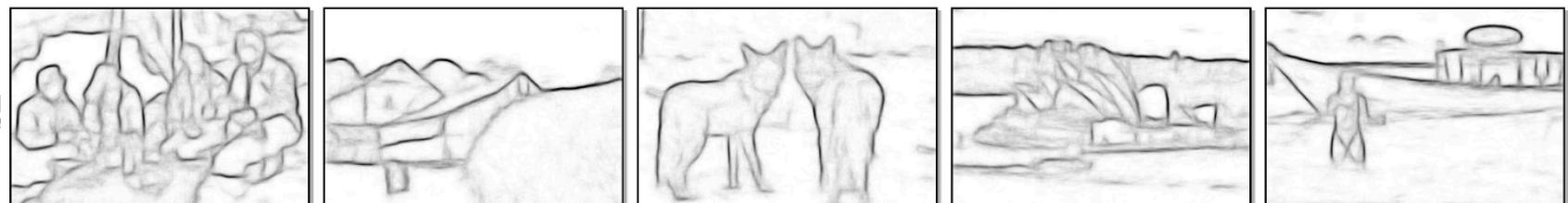
SketchTokens



SCG



SE



# PUSHING THE BOUNDARIES OF BOUNDARY DETECTION USING DEEP LEARNING

ICLR 2016

Iasonas Kokkinos

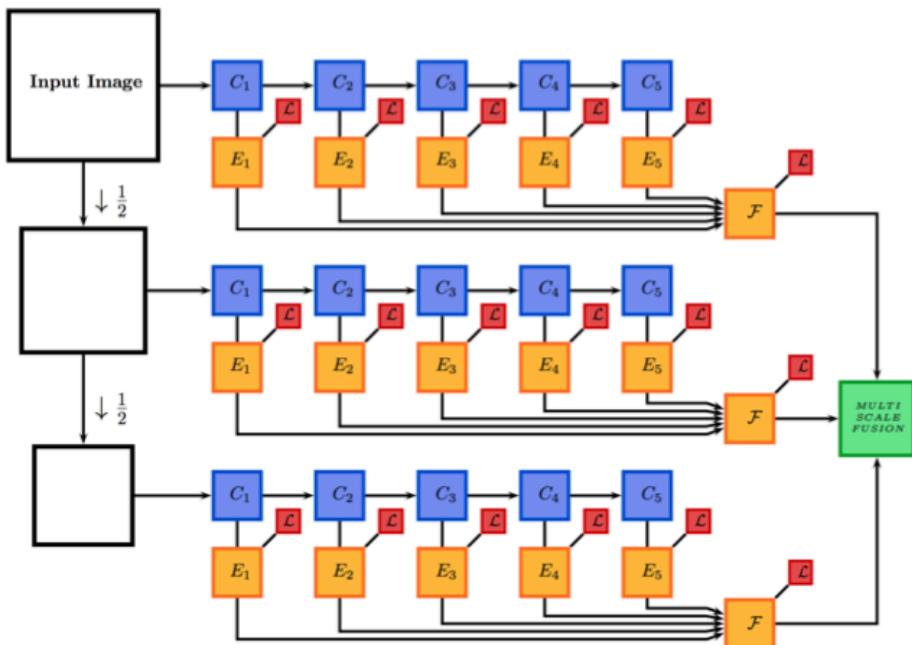


Image Pyramid



Tied CNN outputs



Scale fusion



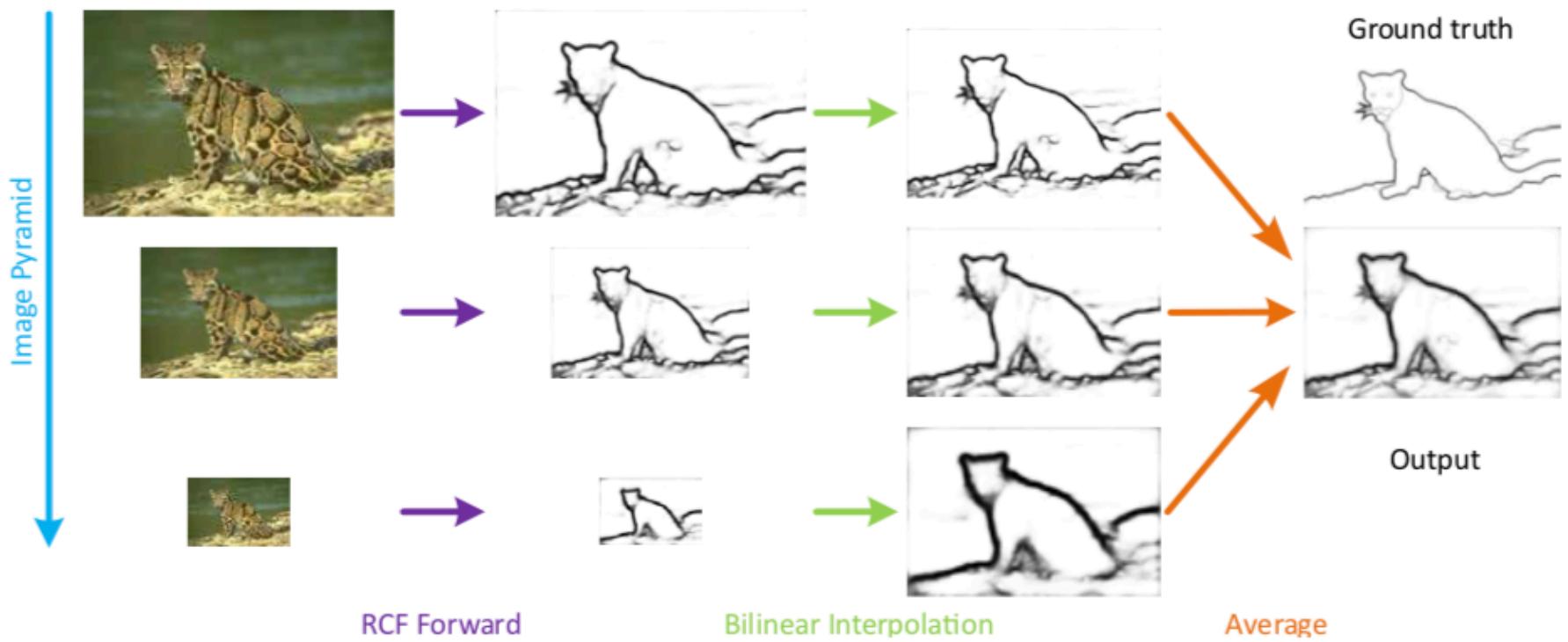
Final outputs

# Richer Convolutional Features for Edge Detection

Yun Liu<sup>1</sup> Ming-Ming Cheng<sup>1</sup> Xiaowei Hu<sup>1</sup> Kai Wang<sup>1</sup> Xiang Bai<sup>2</sup>  
<sup>1</sup>Nankai University <sup>2</sup>HUST

<https://mmcheng.net/rcfEdge/>

CVPR 2017



# Photo-Sketching: Inferring Contour Drawings from Images

WACV 2019

Mengtian Li<sup>1</sup>

Zhe Lin<sup>2</sup>

Radomír Měch<sup>2</sup>

Ersin Yumer<sup>3</sup>

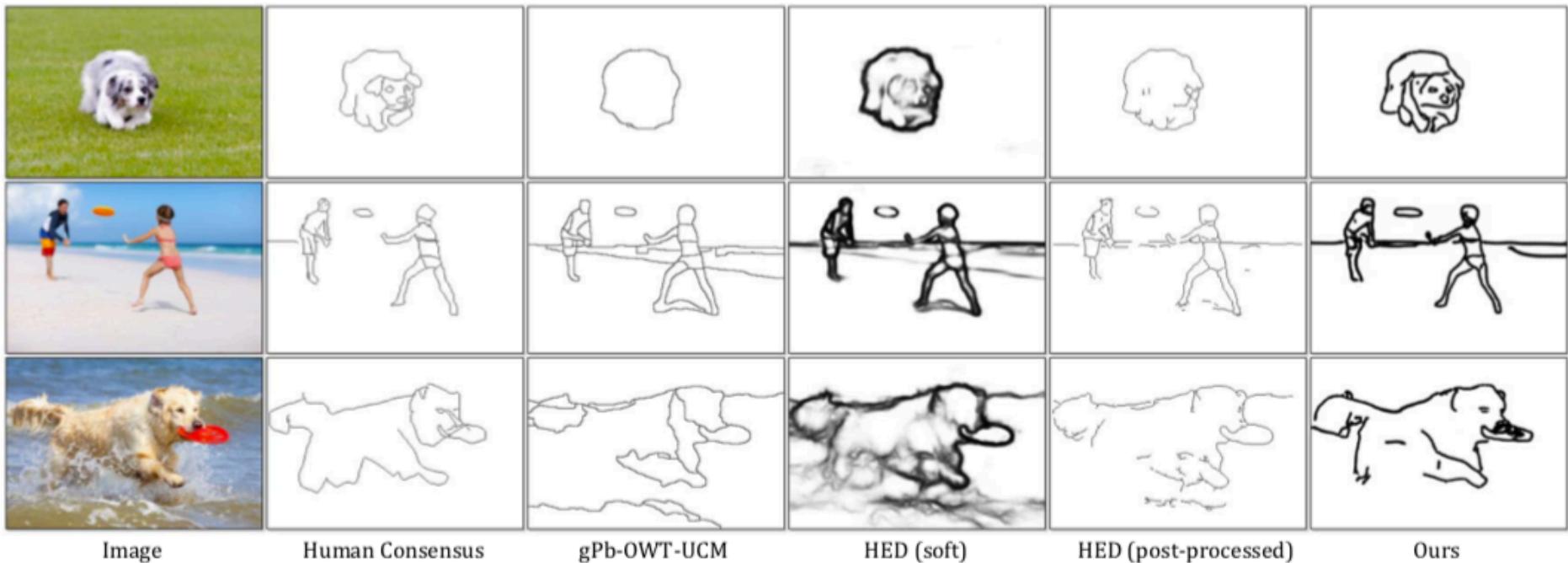
Deva Ramanan<sup>1,4</sup>

<sup>1</sup>Carnegie Mellon University

<sup>2</sup>Adobe Research

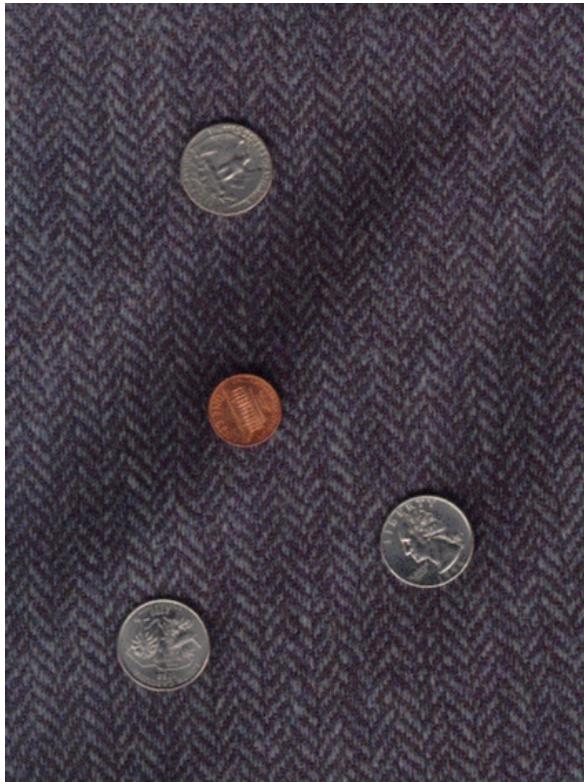
<sup>3</sup>Uber ATG

<sup>4</sup>Argo AI



Uses fairly advanced deep net technique  
(GANs), which we'll discuss only later in  
the course.

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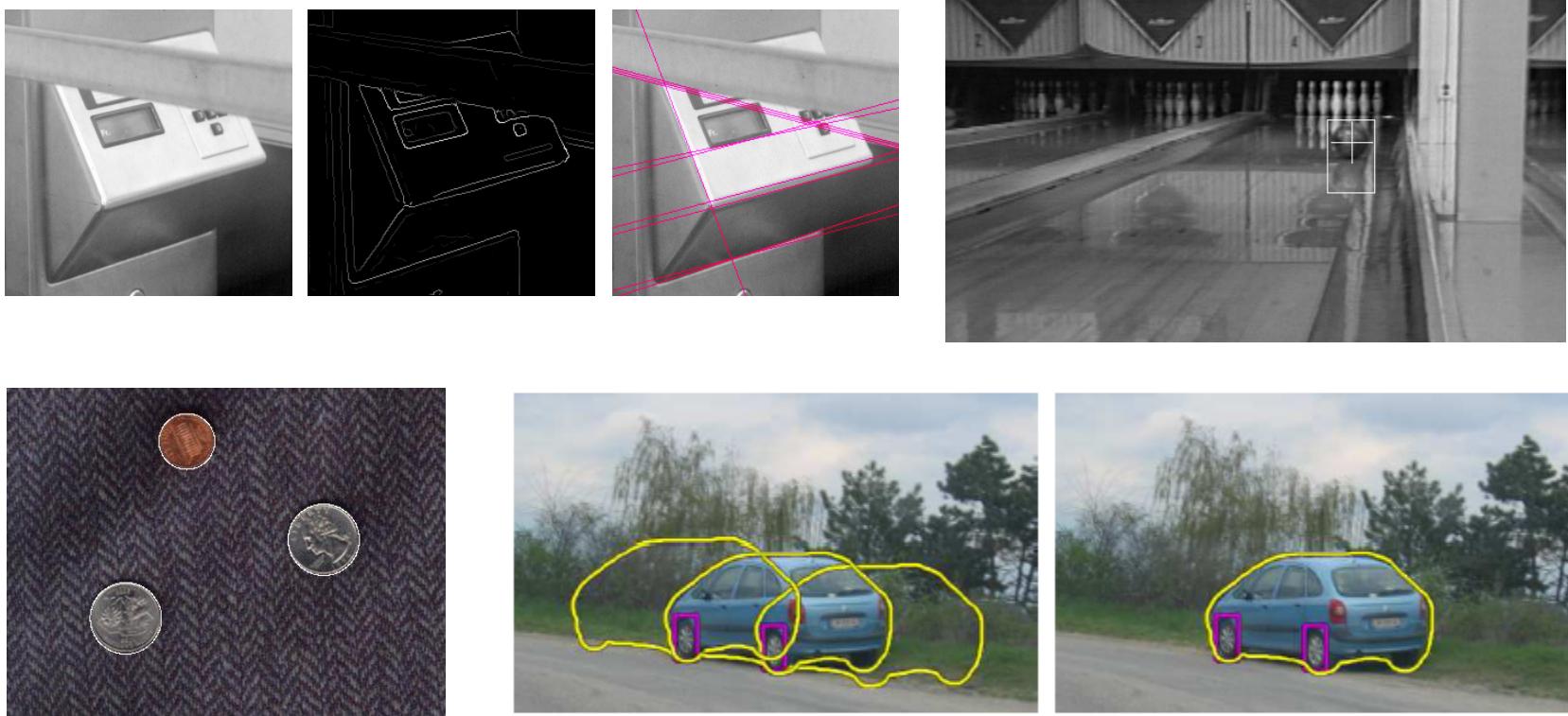


# Voting and the Hough Transform

Disclaimer: Many slides have been borrowed from Devi Parikh and/or Kristen Grauman, who may have borrowed from others.

# Fitting

- Want to associate a model with observed features



[Fig from Marszalek & Schmid, 2007]

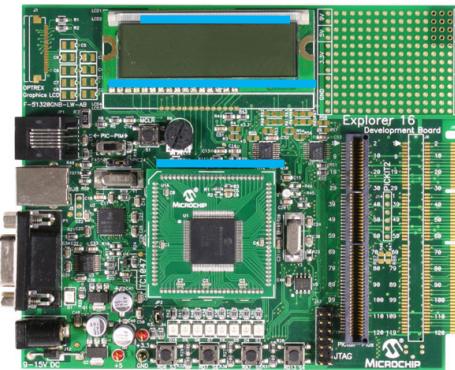
For example, the model could be a line, a circle, or an arbitrary shape.

# Fitting: Main idea

- Choose a **parametric model** to represent a set of features
- Membership criterion is **not local**
  - Can't tell whether a point belongs to a given model just by looking at that point
- Three main questions:
  - What **model** represents this set of features best?
  - **Which** of several model **instances** gets which feature?
  - **How many** model **instances** are there?
- Computational complexity is important
  - It is infeasible to examine every possible set of parameters and every possible combination of features

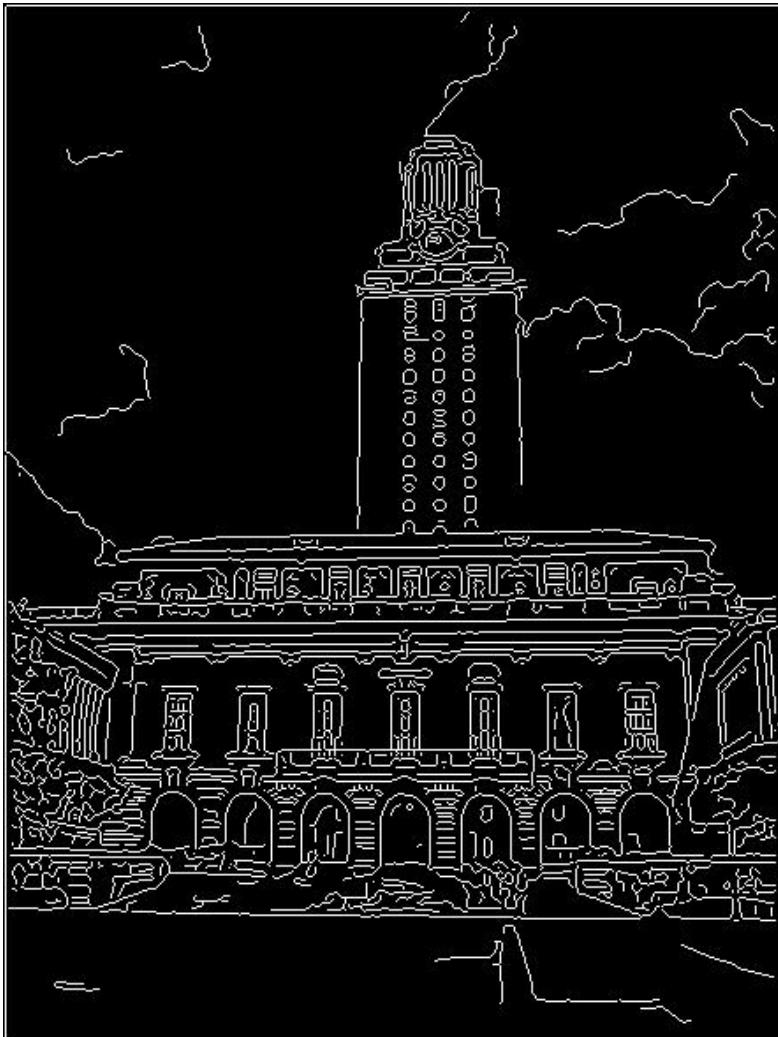
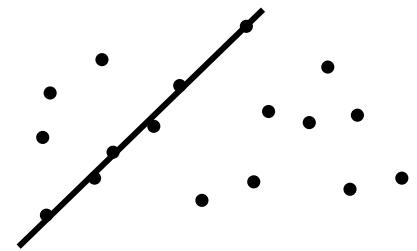
# Example: Line fitting

- Why fit lines?  
Many objects characterized by presence of straight lines



- Wait, why aren't we done just by running edge detection?

# Difficulty of line fitting



- **Extra** edge points (clutter), multiple models:
  - which points go with which line, if any?
- Only some parts of each line detected, and some parts are **missing**:
  - how to find a line that bridges missing evidence?
- **Noise** in measured edge points, orientations:
  - how to detect true underlying parameters?

# Voting

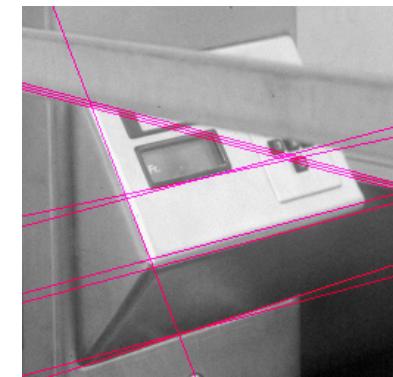
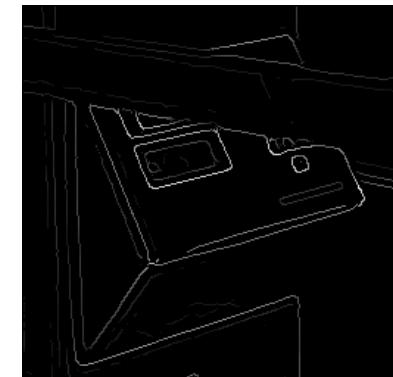
- It's not feasible to check all combinations of features by fitting a model to each possible subset.
- **Voting** is a general technique where we let the features *vote for all models that are compatible with it*.
  - Cycle through features, cast votes for model parameters.
  - Look for model parameters that receive a lot of votes.
- Noise & clutter features will cast votes too, *but* typically their votes should be inconsistent with the majority of “good” features.

# Fitting lines: Hough transform

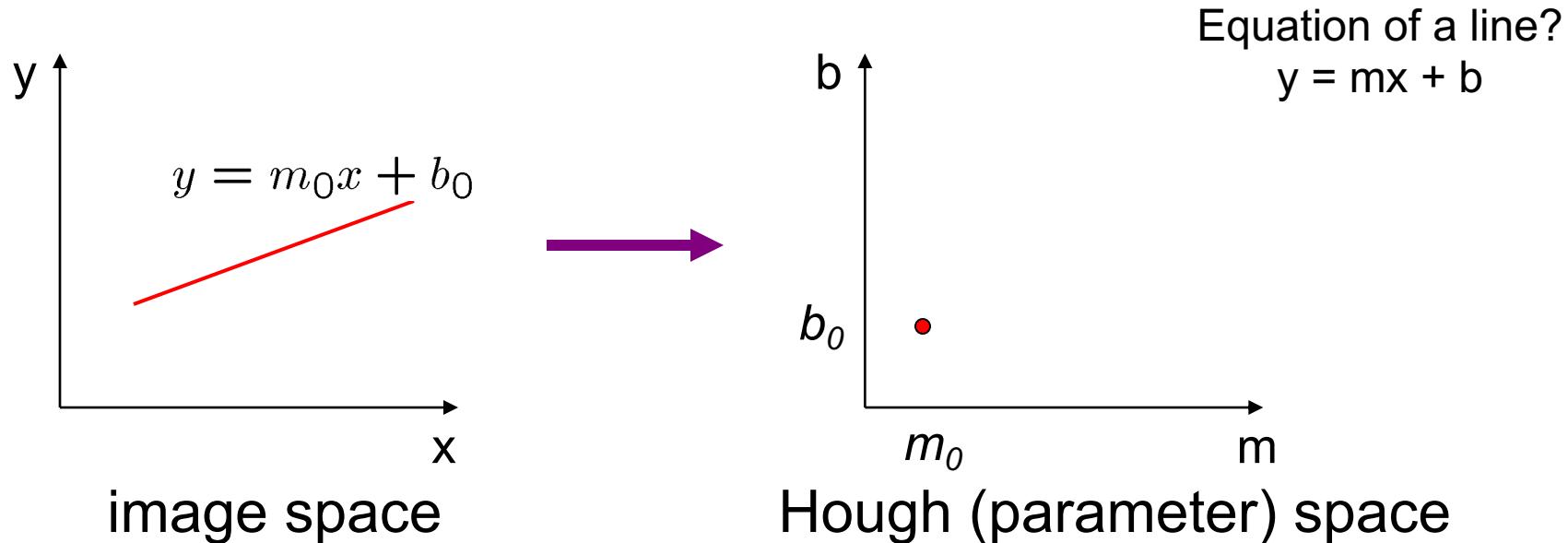
- Given points that belong to a line, what is the line?
- How many lines are there?
- Which points belong to which lines?
- **Hough Transform** is a voting technique that can be used to answer all of these questions.

Main idea:

1. Record vote for each possible line on which each edge point lies.
2. Look for lines that get many votes.



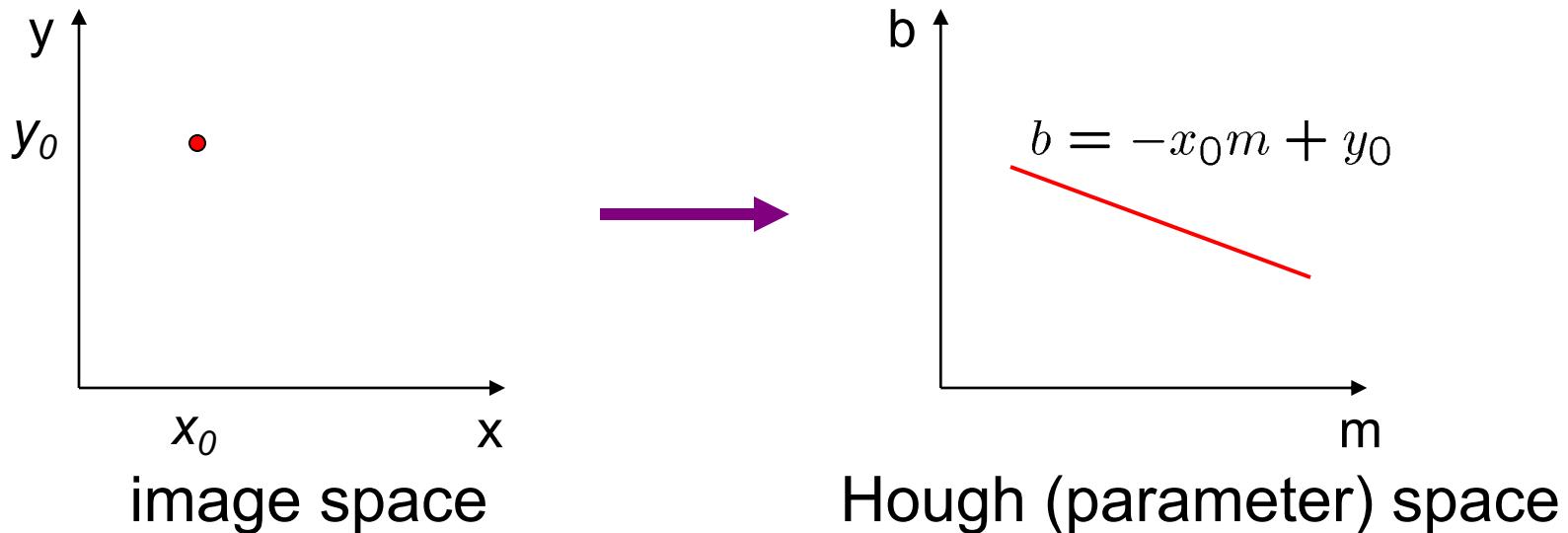
# Finding lines in an image: Hough space



Connection image  $(x,y)$  and Hough  $(m,b)$  spaces:

- Line in image corresponds to a point in Hough space
- To go from image space to Hough space:
  - given a set of points  $(x,y)$ , find all  $(m,b)$  such that  $y = mx + b$

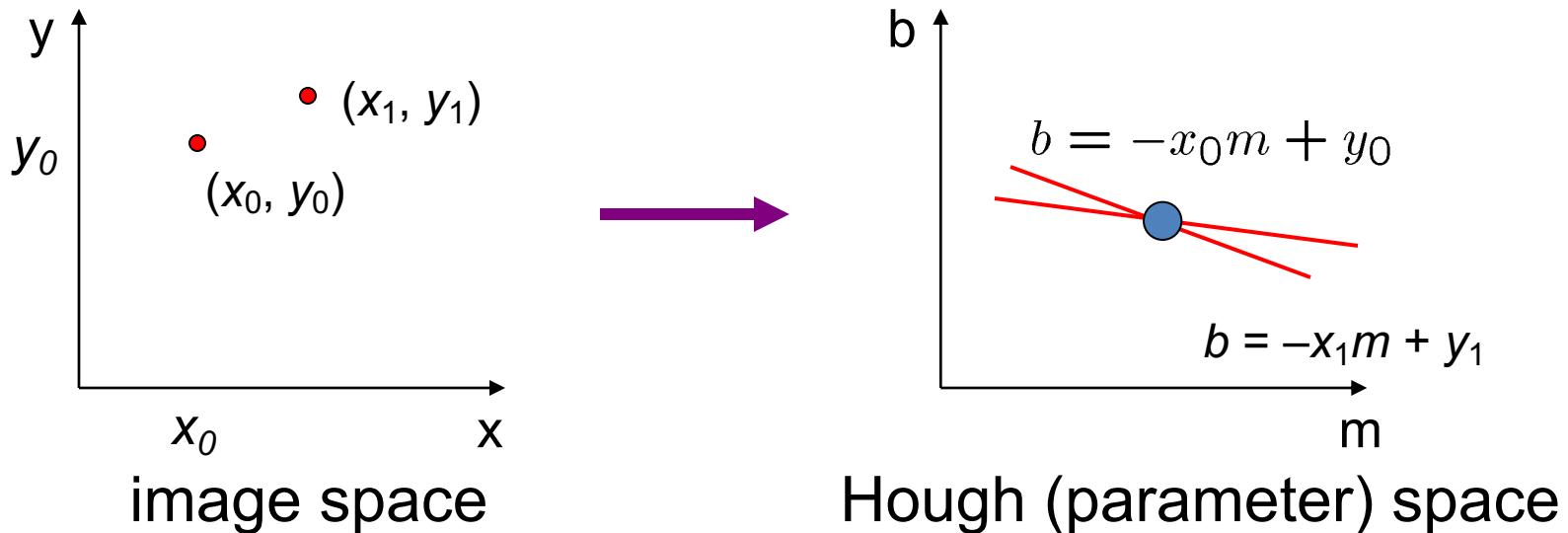
# Finding lines in an image: Hough space



Connection between image  $(x,y)$  and Hough  $(m,b)$  spaces

- A line in the image corresponds to a point in Hough space
- To go from image space to Hough space:
  - given a set of points  $(x,y)$ , find all  $(m,b)$  such that  $y = mx + b$
- What does a point  $(x_0, y_0)$  in the image space map to?
  - Answer: the solutions of  $b = -x_0 m + y_0$
  - this is a line in Hough space

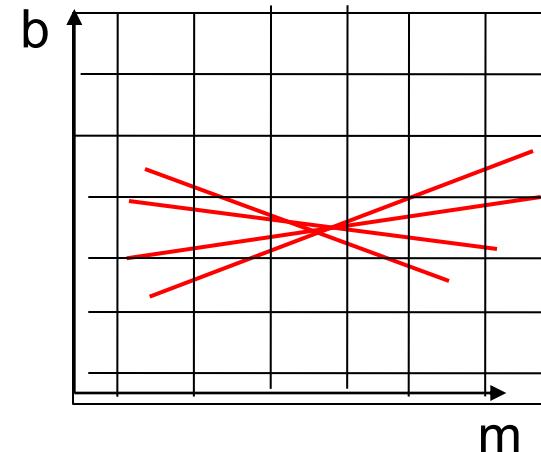
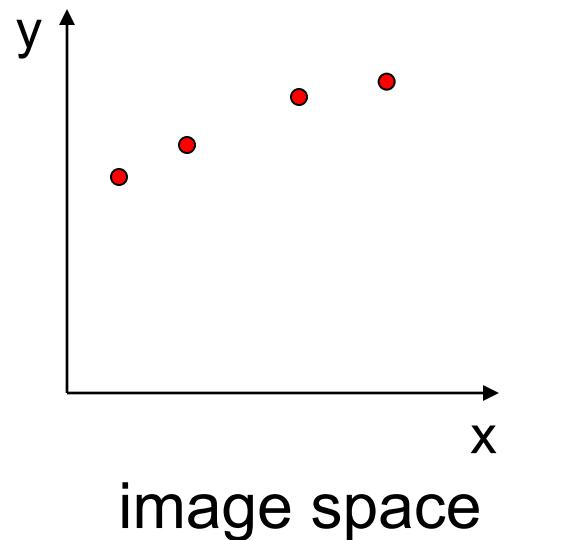
# Finding lines in an image: Hough space



What are the line parameters for the line that contains both  $(x_0, y_0)$  and  $(x_1, y_1)$ ?

- It is the intersection of the lines  $b = -x_0m + y_0$  and  $b = -x_1m + y_1$

# Finding lines in an image: Hough algorithm



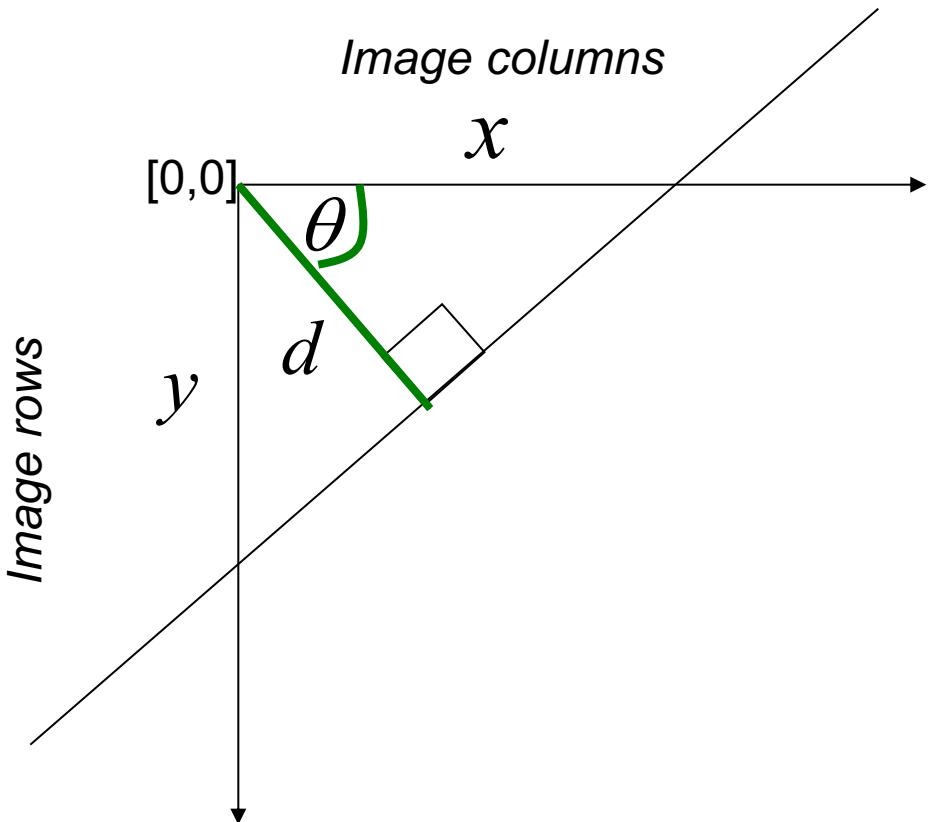
Hough (parameter) space

How can we use this to find the most likely parameters ( $m, b$ ) for the most prominent line in the image space?

- Let each edge point in image space *vote* for a set of possible parameters in Hough space
- Accumulate votes in discrete set of bins; parameters with the most votes indicate line in image space.

# Polar representation for lines

Issues with usual  $(m, b)$  parameter space: can take on infinite values, undefined for vertical lines.



$d$  : perpendicular distance from line to origin

$\theta$  : angle the perpendicular makes with the x-axis

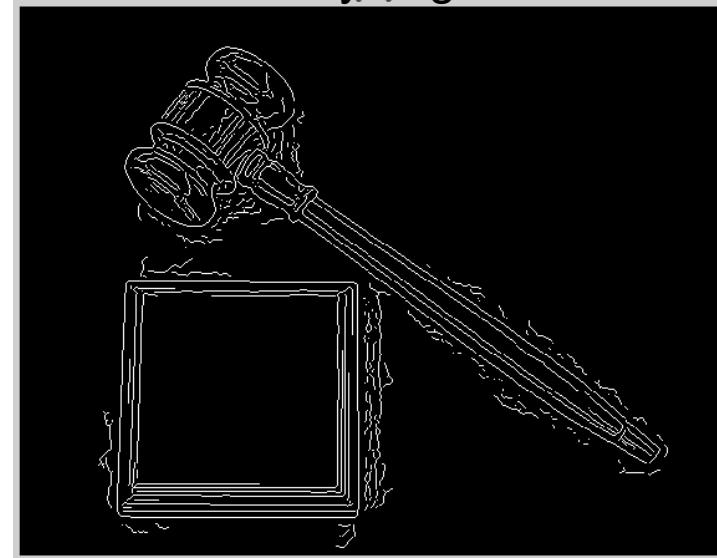
$$x \cos \theta - y \sin \theta = d$$

Point in image space  $\rightarrow$  sinusoid segment in Hough space

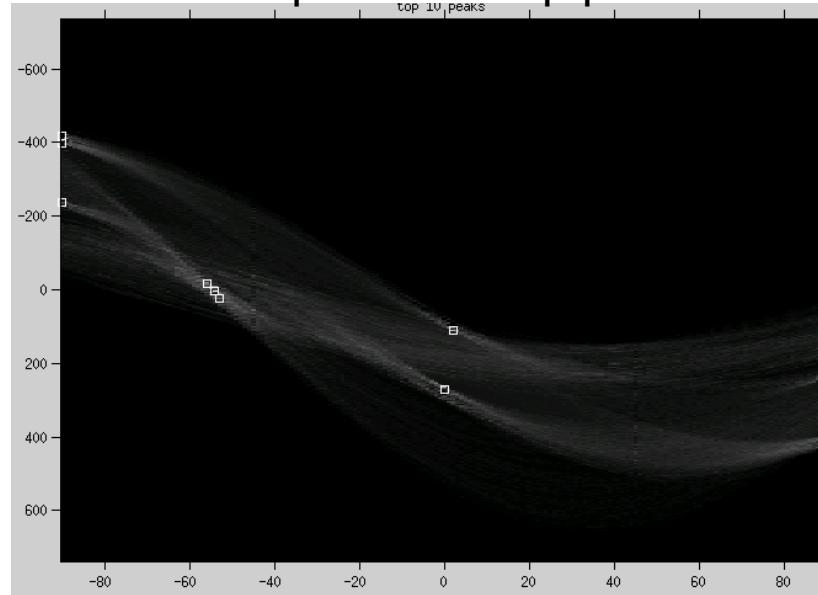
Original image



Canny edges



Vote space and top peaks



# Hough transform algorithm

Using the polar parameterization:

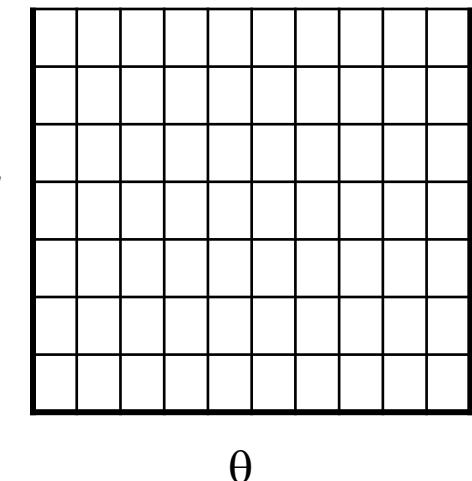
$$x \cos \theta - y \sin \theta = d$$

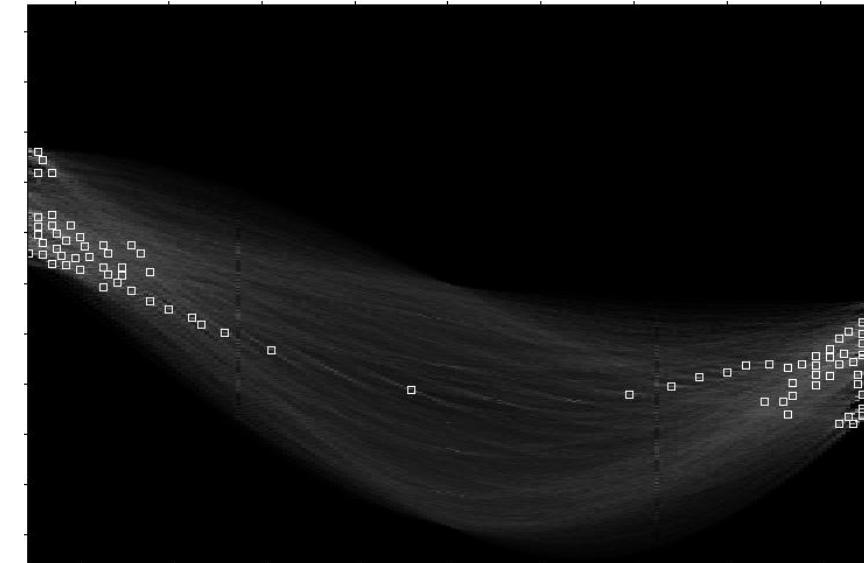
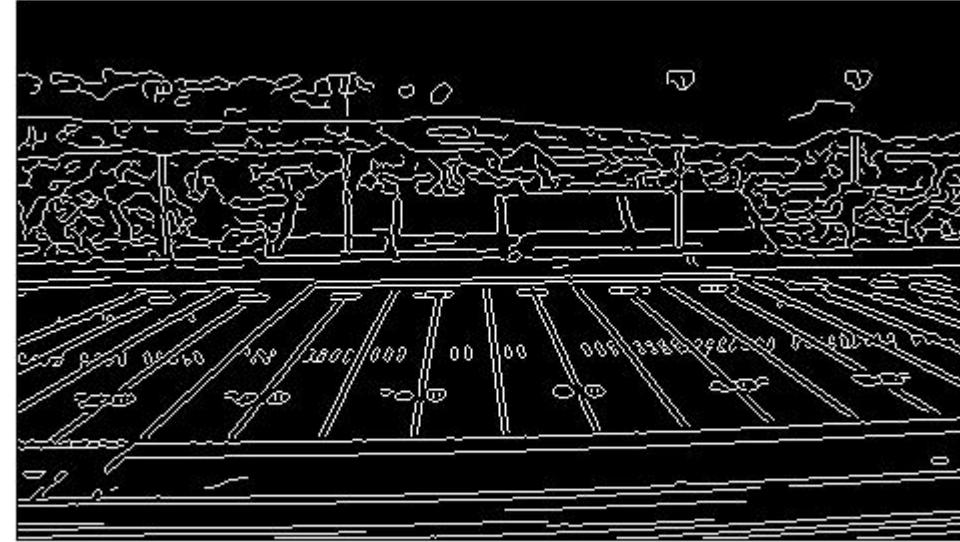
## Basic Hough transform algorithm

1. Initialize  $H[d, \theta] = 0$
2. for each edge point  $I[x, y]$  in the image
  - for  $\theta = [\theta_{\min} \text{ to } \theta_{\max}]$  // some quantization
    - $d = x \cos \theta - y \sin \theta$
    - $H[d, \theta] += 1$
3. Find the value(s) of  $(d, \theta)$  where  $H[d, \theta]$  is maximum
4. The detected line in the image is given by

$$d = x \cos \theta - y \sin \theta$$

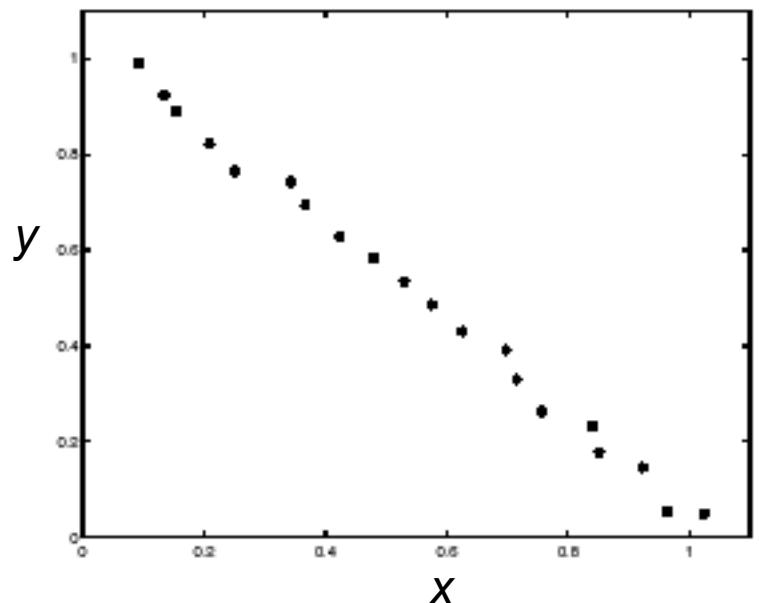
$H$ : accumulator array (votes)



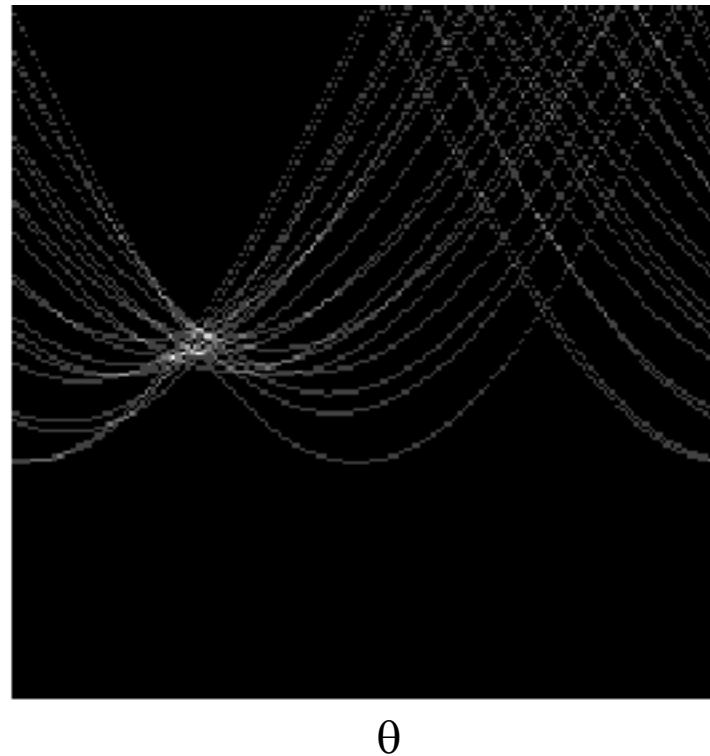


Showing longest segments found

# Impact of noise on Hough



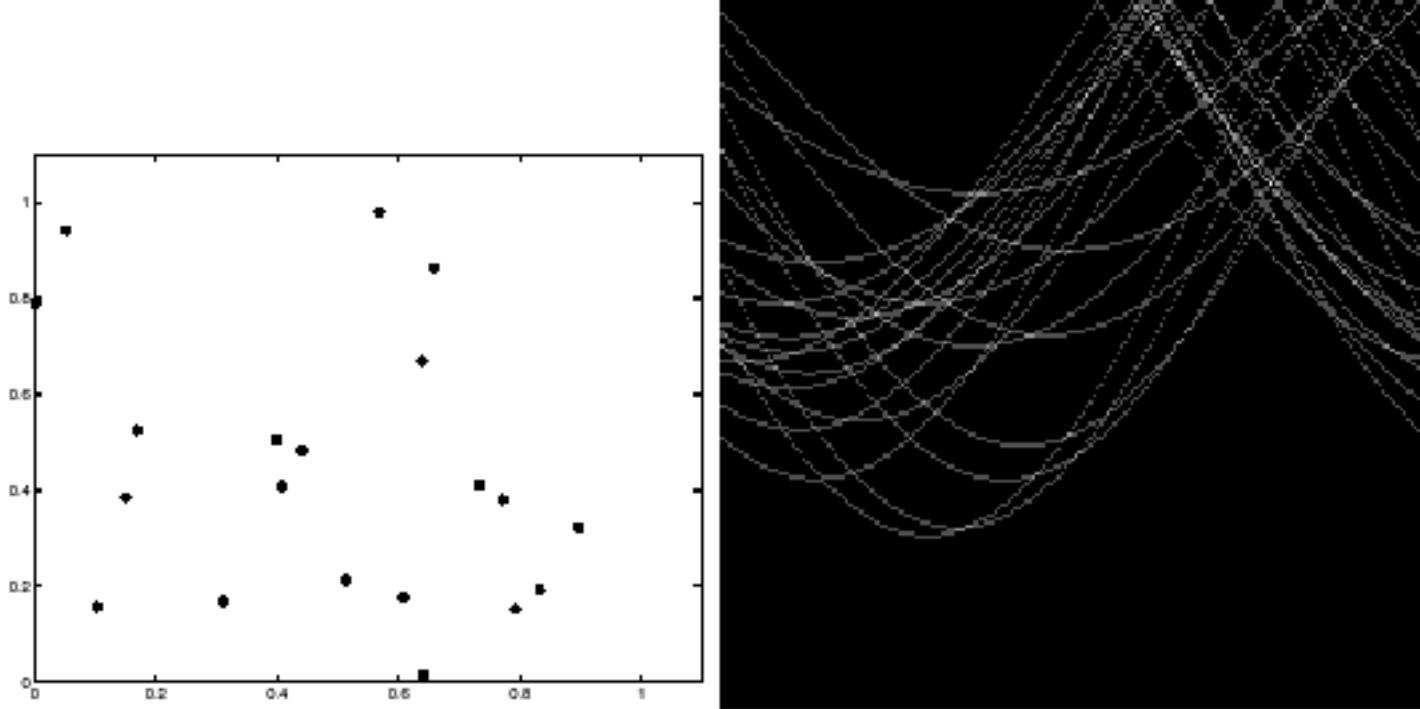
**Image space  
edge coordinates**



**Votes**

What difficulty does this present for an implementation?

# Impact of noise on Hough



**Image space  
edge coordinates**

**Votes**

Here, everything appears to be “noise”, or random edge points, but we still see peaks in the vote space.

# Hough transform for circles

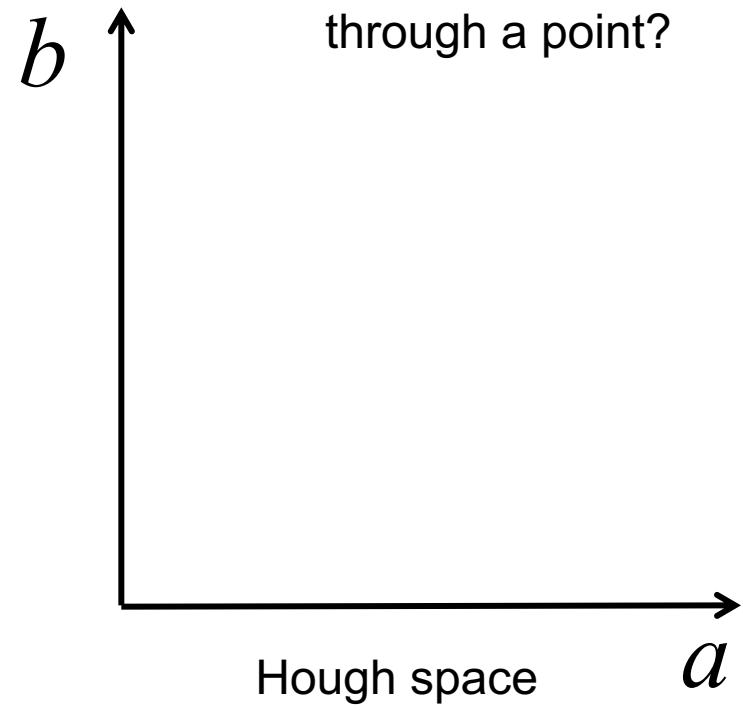
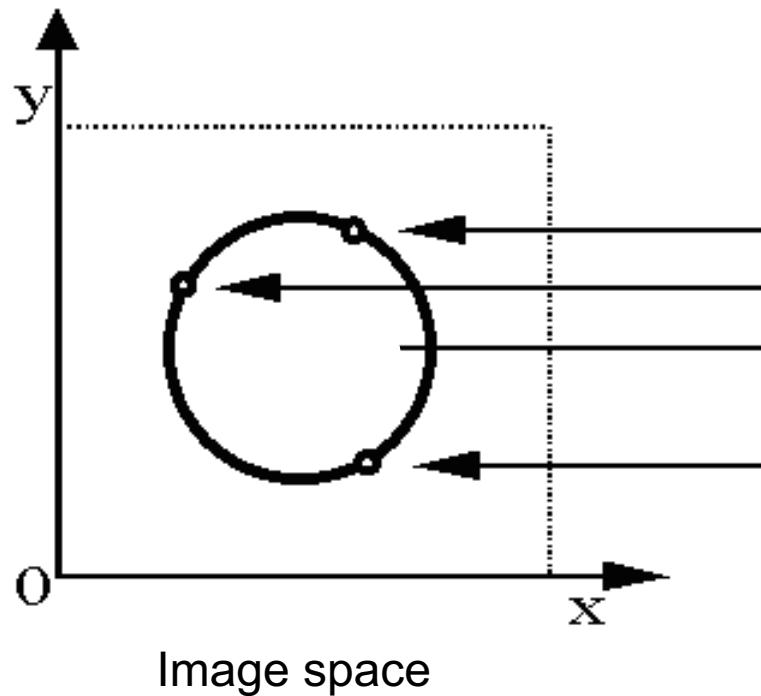
- Circle: center  $(a, b)$  and radius  $r$

Equation of circle?

$$(x_i - a)^2 + (y_i - b)^2 = r^2$$

- For a fixed radius  $r$

Equation of set of circles that all pass through a point?

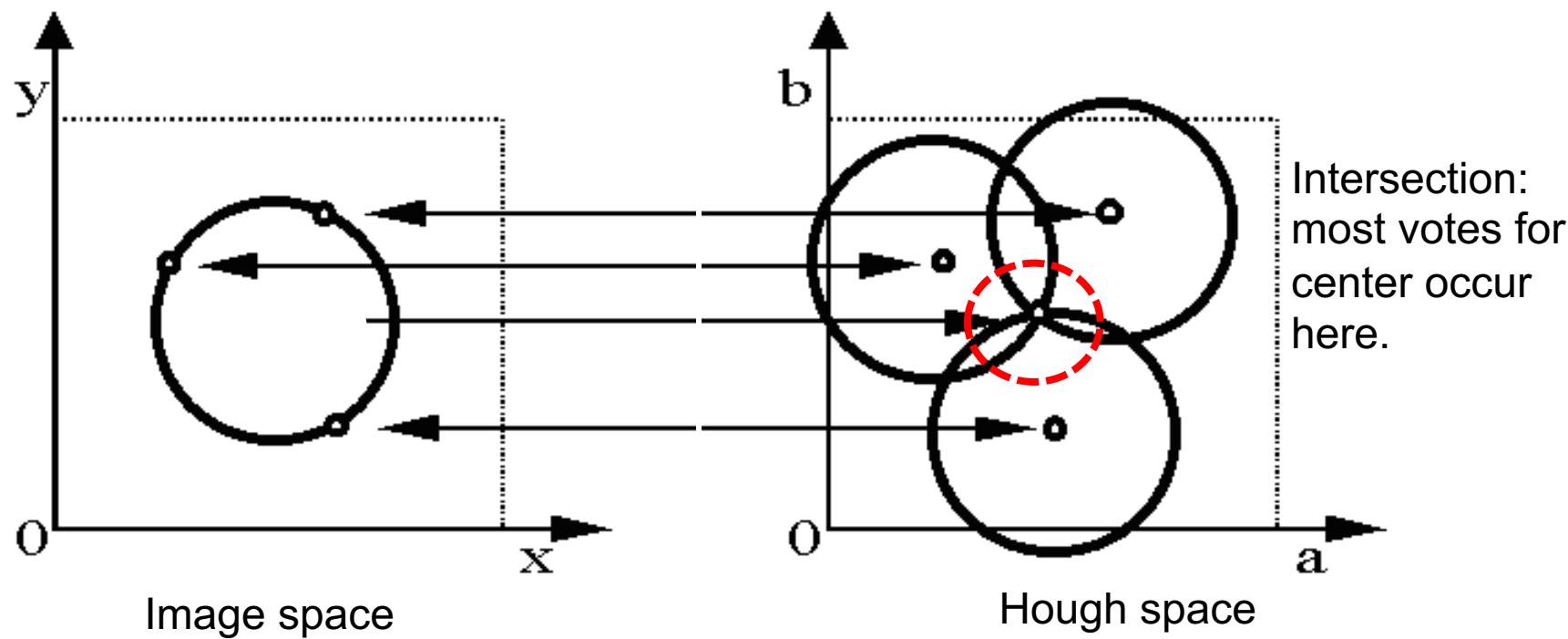


# Hough transform for circles

- Circle: center  $(a, b)$  and radius  $r$

$$(x_i - a)^2 + (y_i - b)^2 = r^2$$

- For a fixed radius  $r$

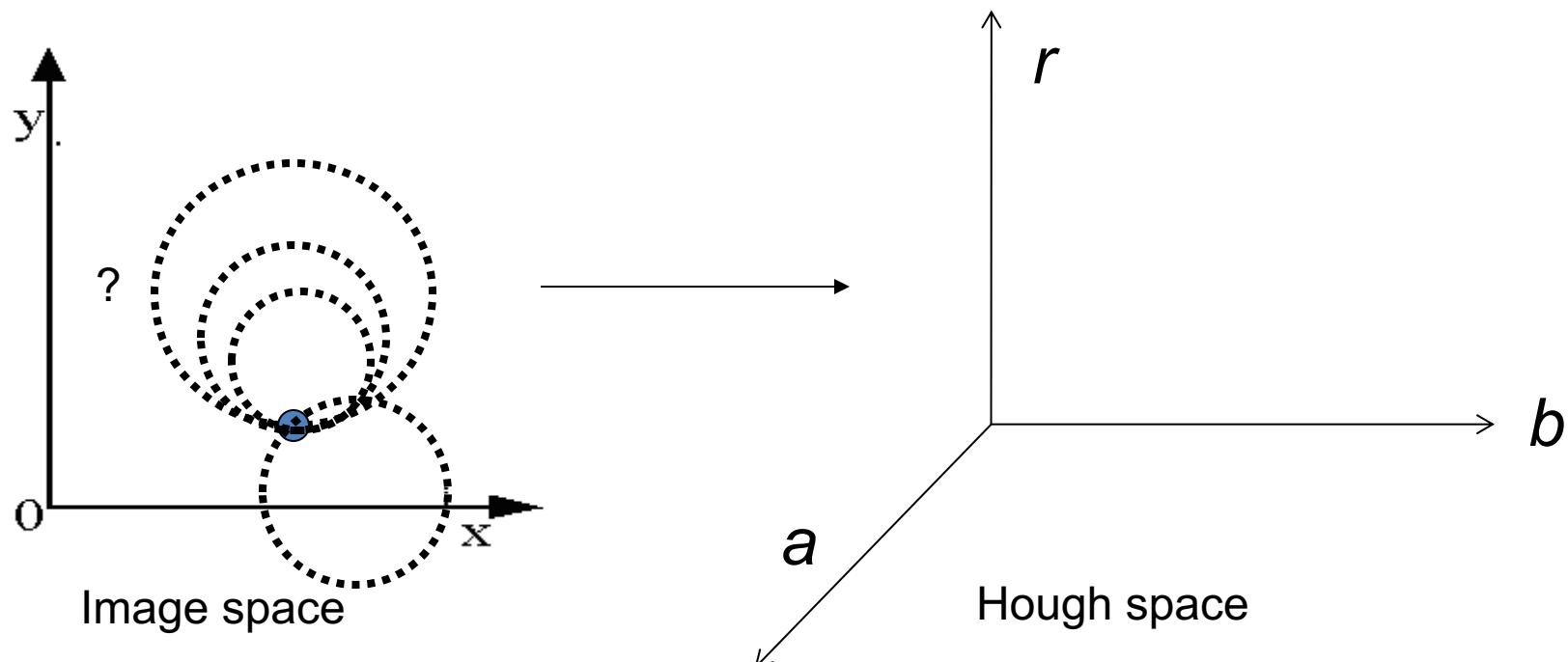


# Hough transform for circles

- Circle: center  $(a, b)$  and radius  $r$

$$(x_i - a)^2 + (y_i - b)^2 = r^2$$

- For an unknown radius  $r$

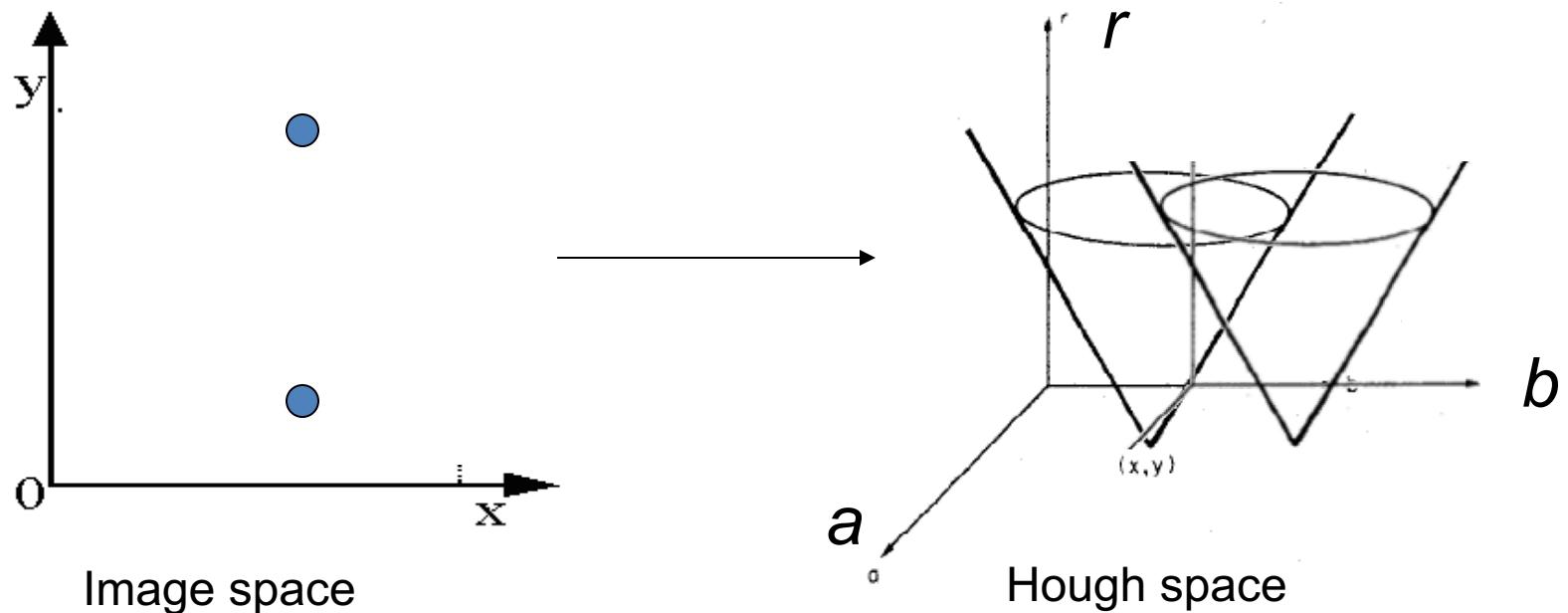


# Hough transform for circles

- Circle: center  $(a, b)$  and radius  $r$

$$(x_i - a)^2 + (y_i - b)^2 = r^2$$

- For an unknown radius  $r$

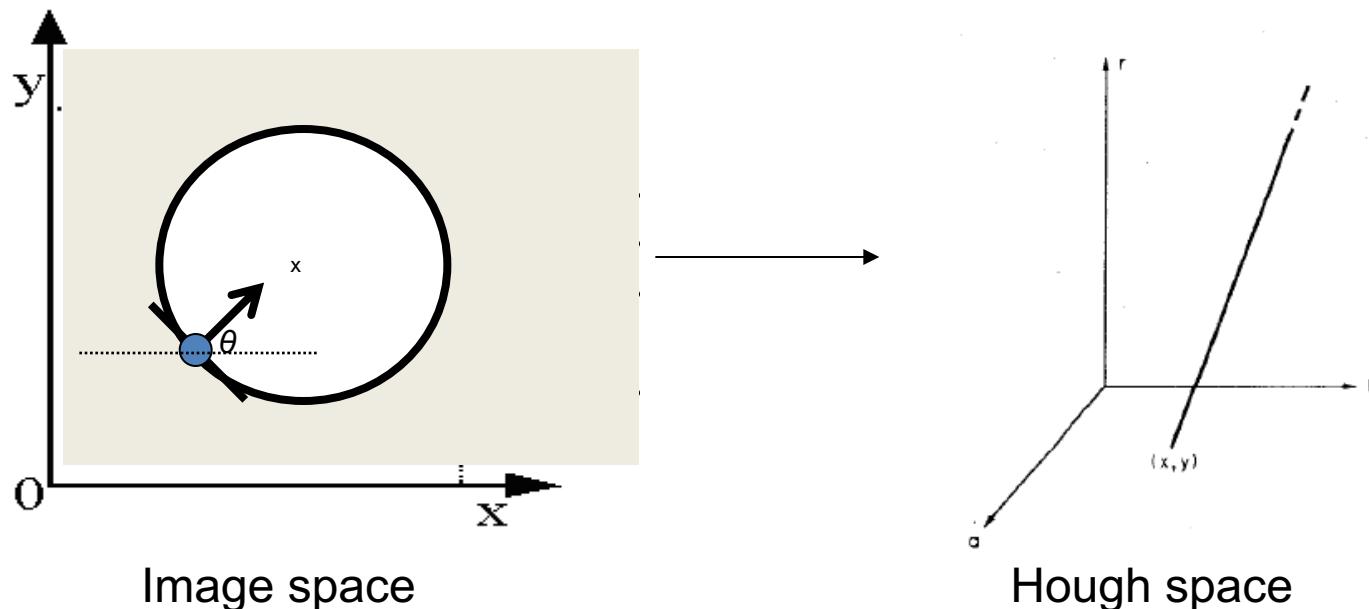


# Hough transform for circles

- Circle: center  $(a, b)$  and radius  $r$

$$(x_i - a)^2 + (y_i - b)^2 = r^2$$

- For an unknown radius  $r$ , **known** gradient direction



# Hough transform for circles

For every edge pixel  $(x, y)$  :

    For each possible radius value  $r$ :

        For each possible gradient direction  $\vartheta$ :

*// or use estimated gradient at  $(x, y)$*

$$a = x - r \cos(\vartheta) \text{ // column}$$

$$b = y + r \sin(\vartheta) \text{ // row}$$

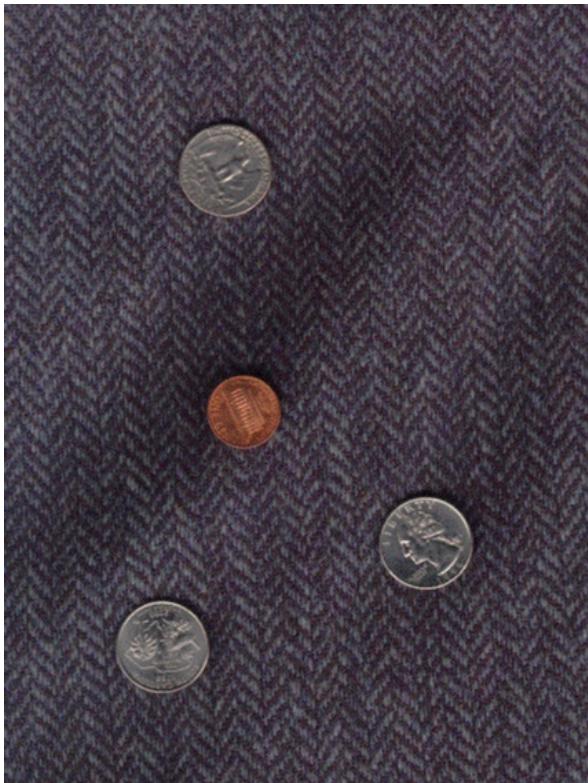
$$H[a, b, r] += 1$$

end

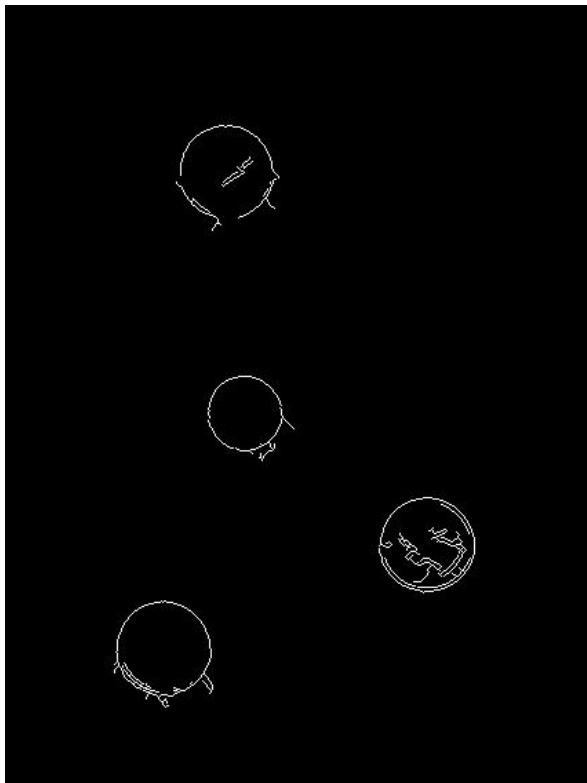
end

# Example: detecting circles with Hough

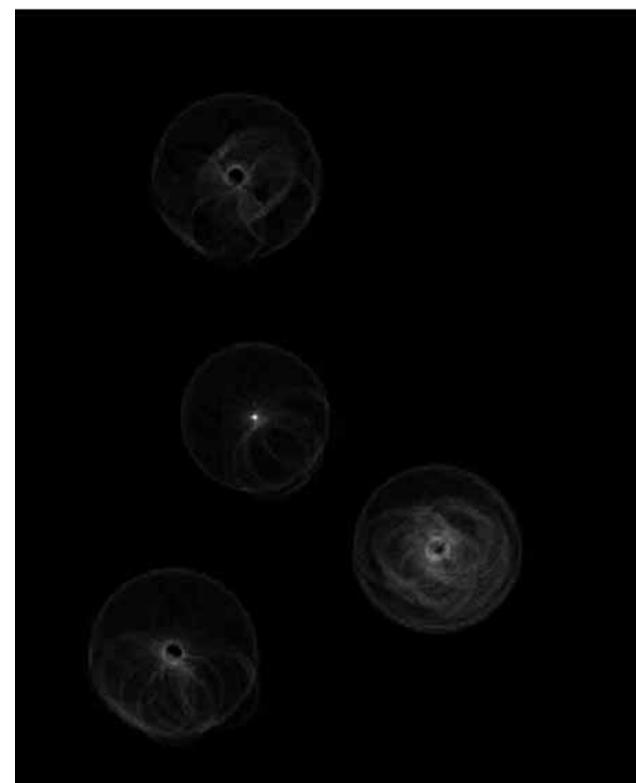
Original



Edges



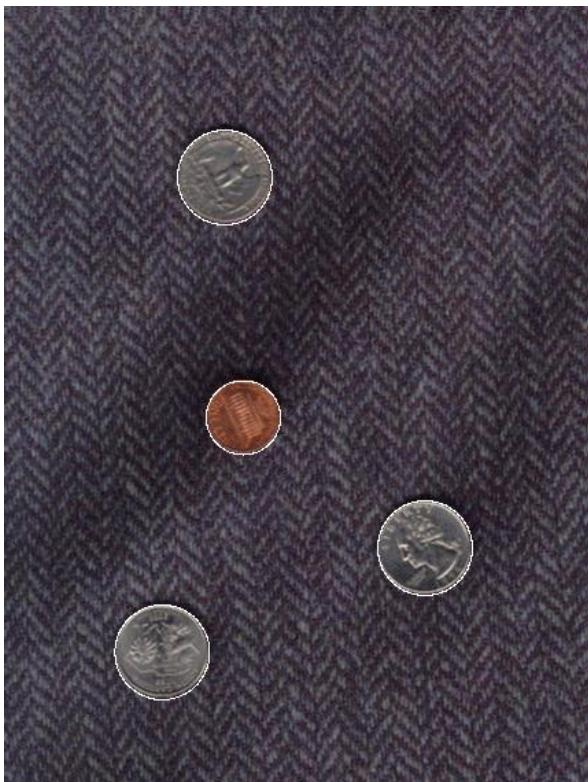
Votes: Penny



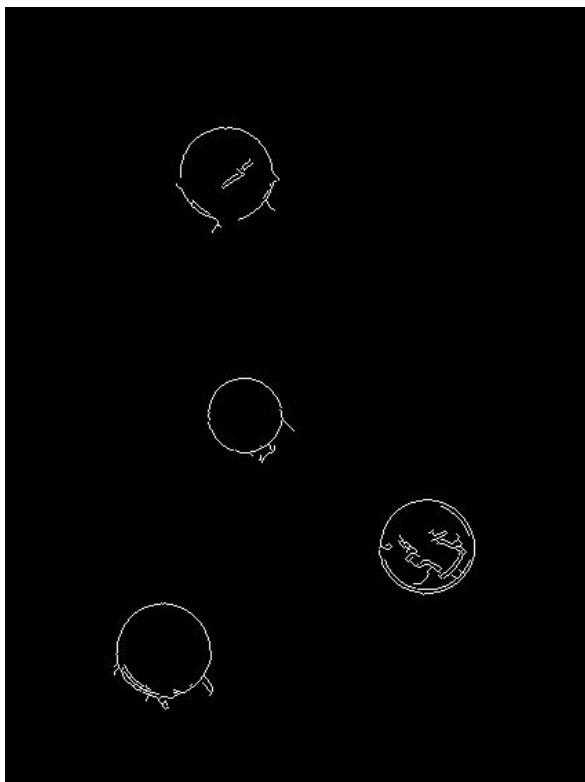
Note: a different Hough transform (with separate accumulators) was used for each circle radius (quarters vs. penny).

# Example: detecting circles with Hough

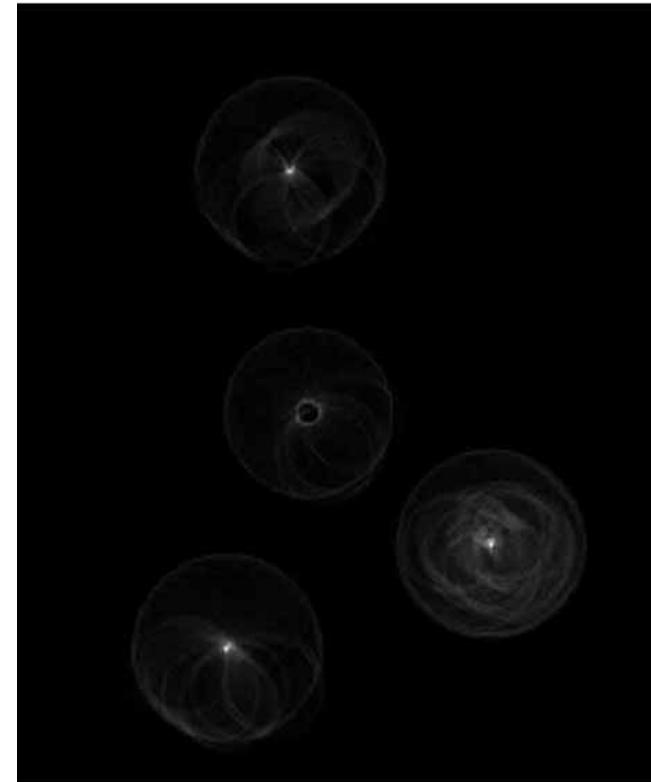
Combined detections



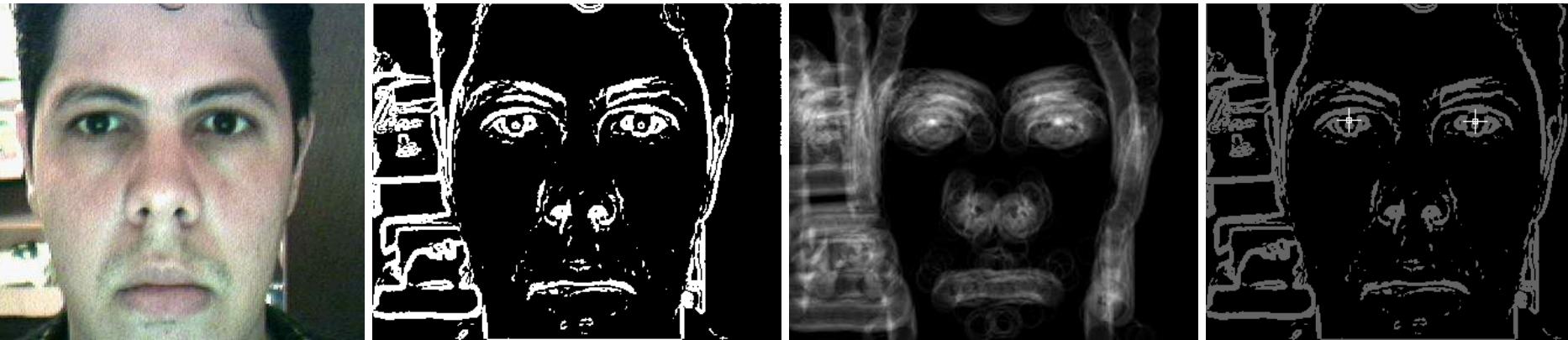
Edges



Votes: Quarter



# Example: iris detection



Gradient+threshold

Hough space  
(fixed radius)

Max detections

- Hemerson Pistori and Eduardo Rocha Costa  
<http://rsbweb.nih.gov/ij/plugins/hough-circles.html>

# Example: iris detection



Figure 2. Original image



Figure 3. Distance image



Figure 4. Detected face region

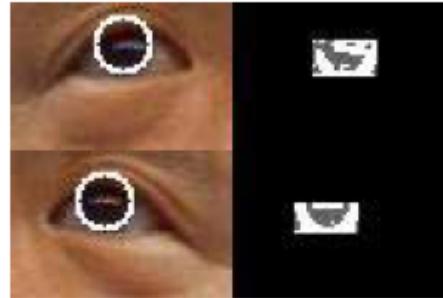


Figure 14. Looking upward

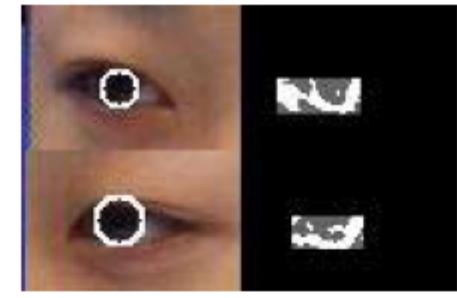


Figure 15. Looking sideways

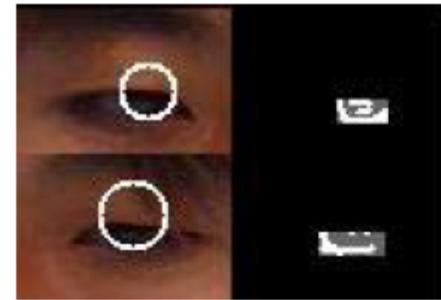
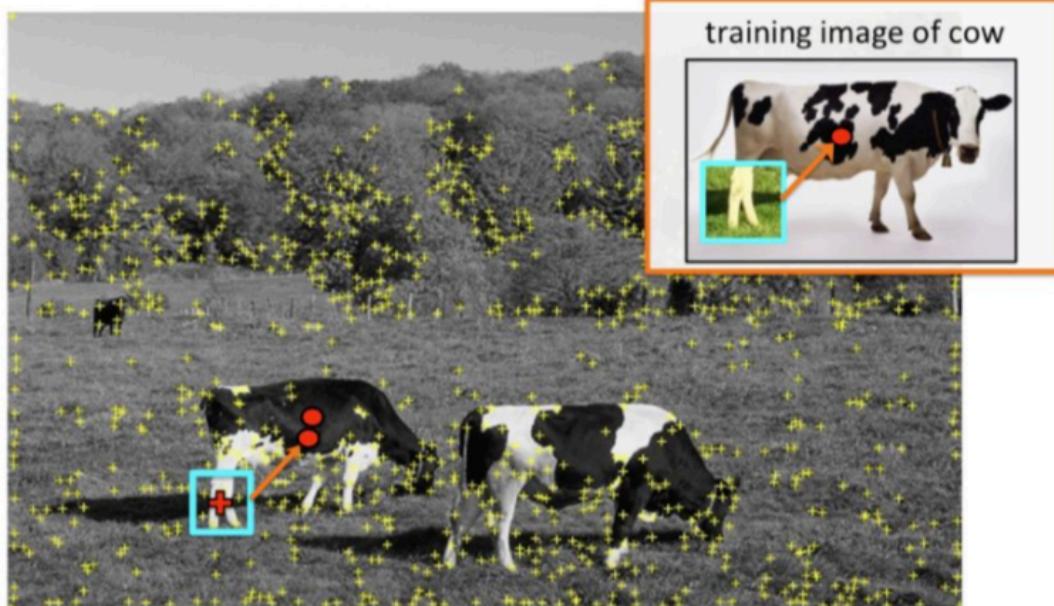


Figure 16. Looking downward

- An Iris Detection Method Using the Hough Transform and Its Evaluation for Facial and Eye Movement, by Hideki Kashima, Hitoshi Hongo, Kunihito Kato, Kazuhiko Yamamoto, ACCV 2002.

# Hough Voting for Object recognition

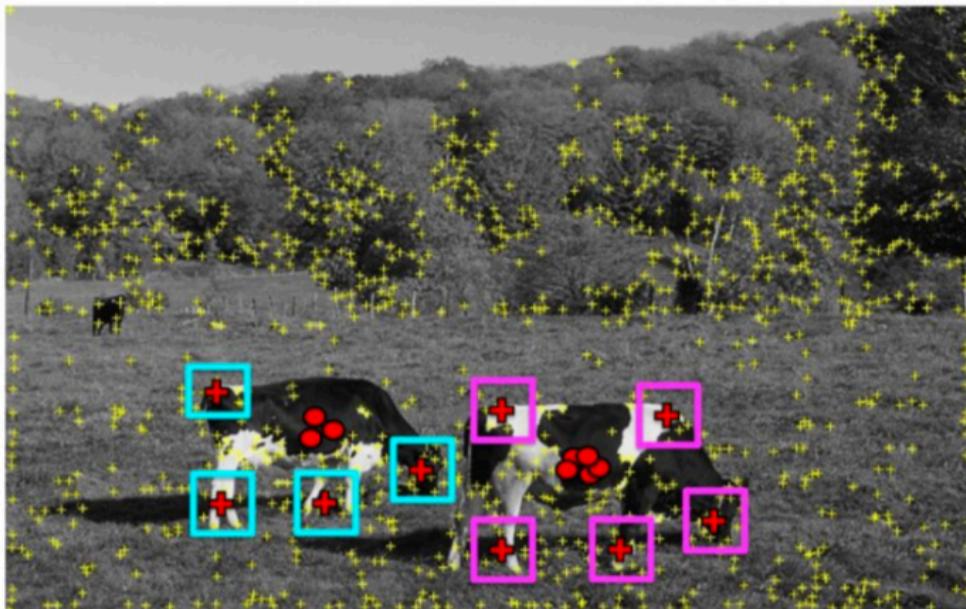


**vote for center of object**

## Hough voting pipeline (in 2D):

- Select interest points
- Match patch around each interest point to a training patch (codebook)
- Vote for object center given that training instance

# Hough Voting for Object recognition

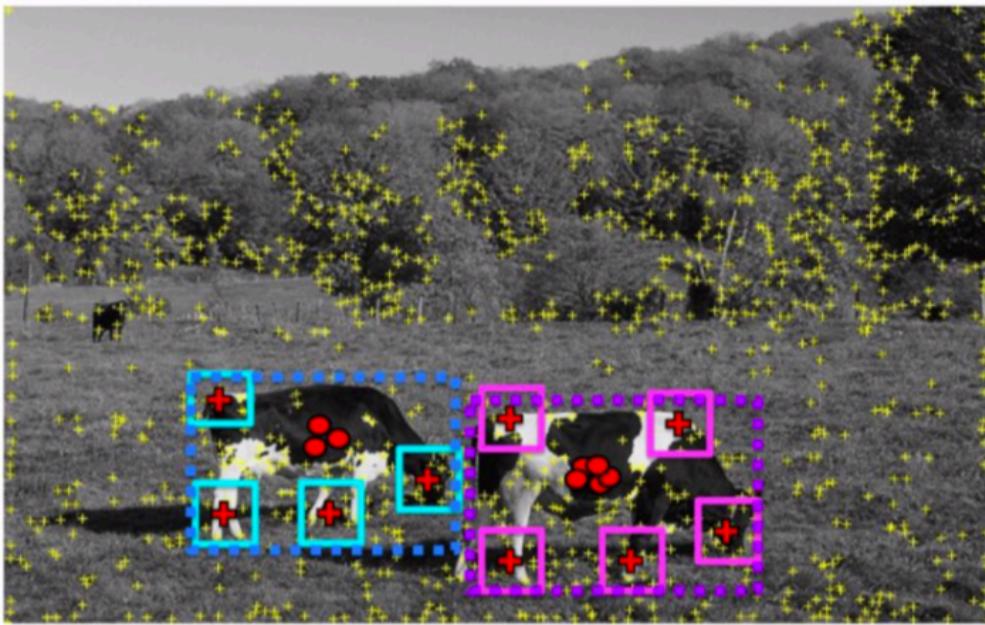


Find patches that voted for the peaks (back-projection).

## Hough voting pipeline (in 2D):

- Select interest points
- Match patch around each interest point to a training patch (codebook)
- Vote for object center given that training instance
- Votes clustering to find peaks
- **Find patches that voted for the peaks back-projection**

# Hough Voting for Object recognition



Find full objects based on the back-projected patches.

## Hough voting pipeline (in 2D):

- Select interest points
- Match patch around each interest point to a training patch (codebook)
- Vote for object center given that training instance
- Votes clustering to find peaks
- Find patches that voted for the peaks back-projection
- **Find full objects based on back-projected patches**

# Hough transform: pros and cons

## Pros

- All points are processed independently, so can cope with occlusion, gaps
- Some robustness to noise: noise points unlikely to contribute *consistently* to any single bin
- Can detect multiple instances of a model in a single pass

## Cons

- Complexity of search time increases exponentially with the number of model parameters
- Non-target shapes can produce spurious peaks in parameter space
- Quantization: can be tricky to pick a good grid size

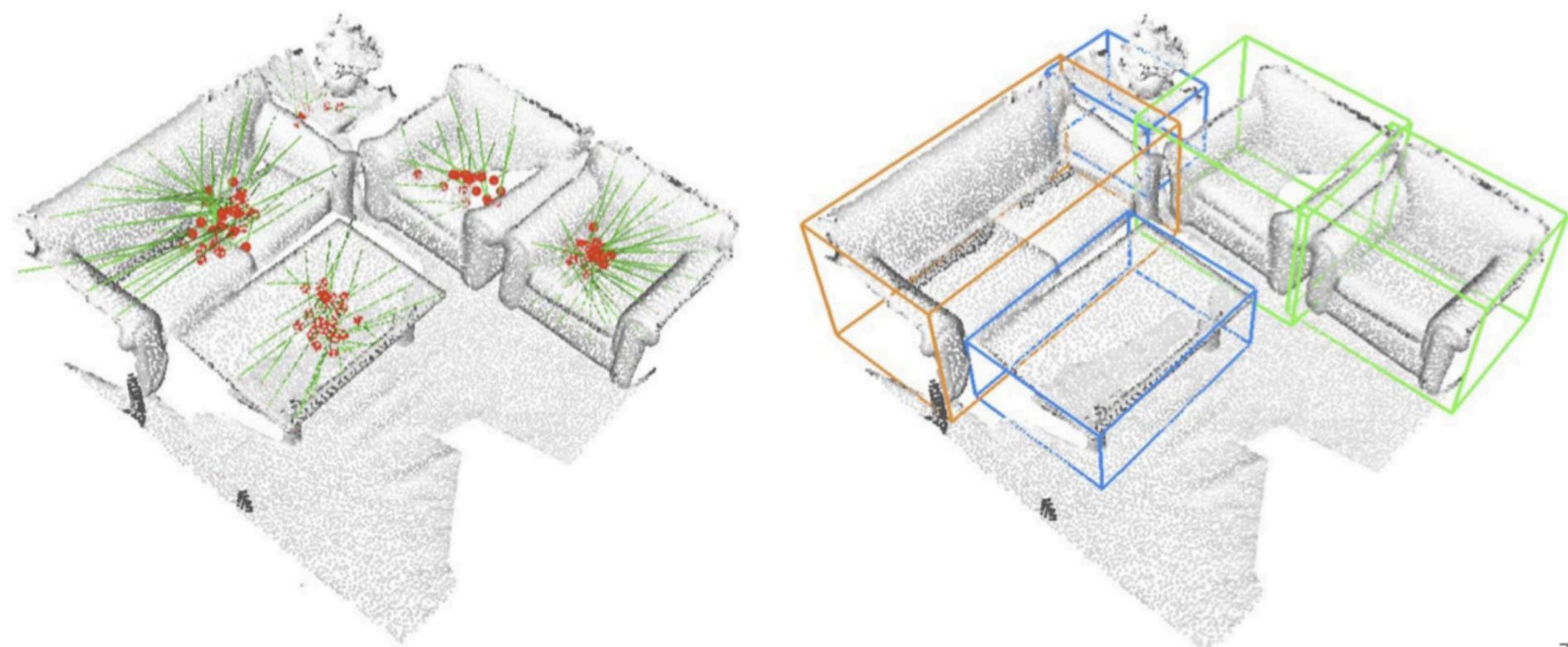
# Deep Hough Voting for 3D Object Detection in Point Clouds

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<sup>1</sup>Facebook AI Research <sup>2</sup>Stanford University

ICCV 2019

## Deep Hough Voting: 3D Object Detection in Point Clouds



# Deep Hough voting:

