

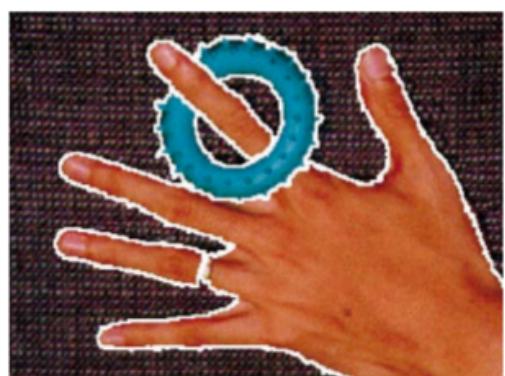
2. Image Formation



3. Image Processing



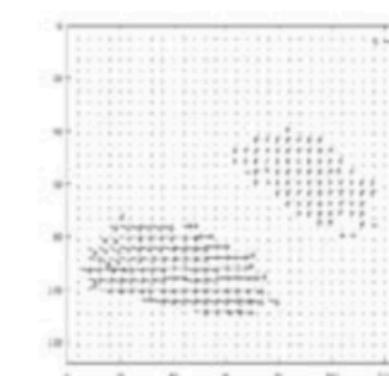
4. Features



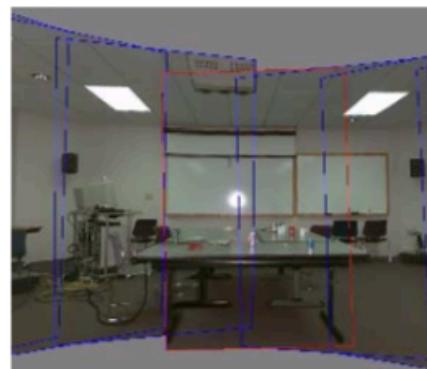
5. Segmentation



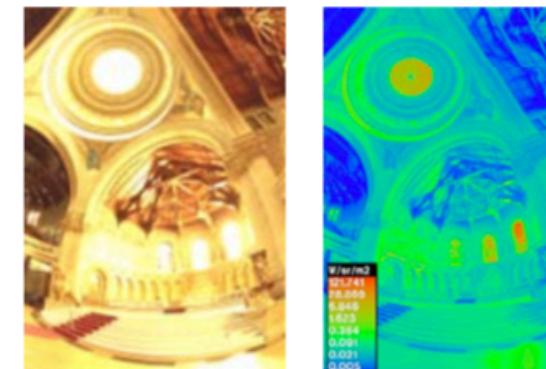
6-7. Structure from Motion



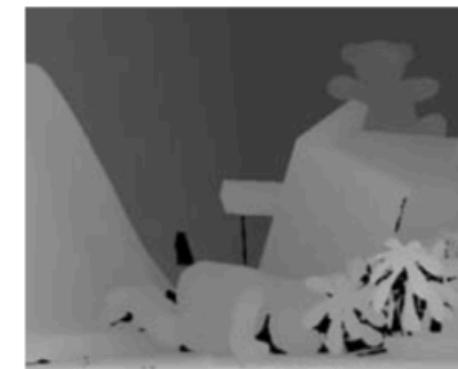
8. Motion



9. Stitching



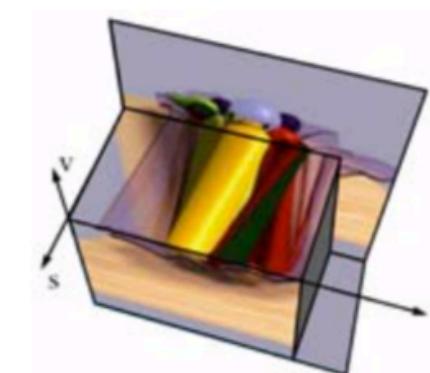
10. Computational Photography



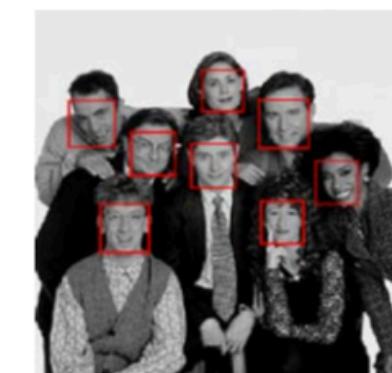
11. Stereo



12. 3D Shape



13. Image-based Rendering



14. Recognition

# Stitching and HDR,



(Lords Cricket Ground, London, UK, by I. Essa)

Slides by Irfan Essa

Adapted for CS 4476 by Frank Dellaert

More details in Szeliski Ch. 9, Ch 10.

# 5 Steps to Make a Panorama



(Lord's Cricket Ground, London, UK, by I. Essa)

- \*  Capture Images
- \*  Detection and matching
- \*  Warping → Aligning Images
- \*  Blending, Fading, Cutting
- \*  Cropping (Optional)

# Align Images: Translate??



L



R



L on top

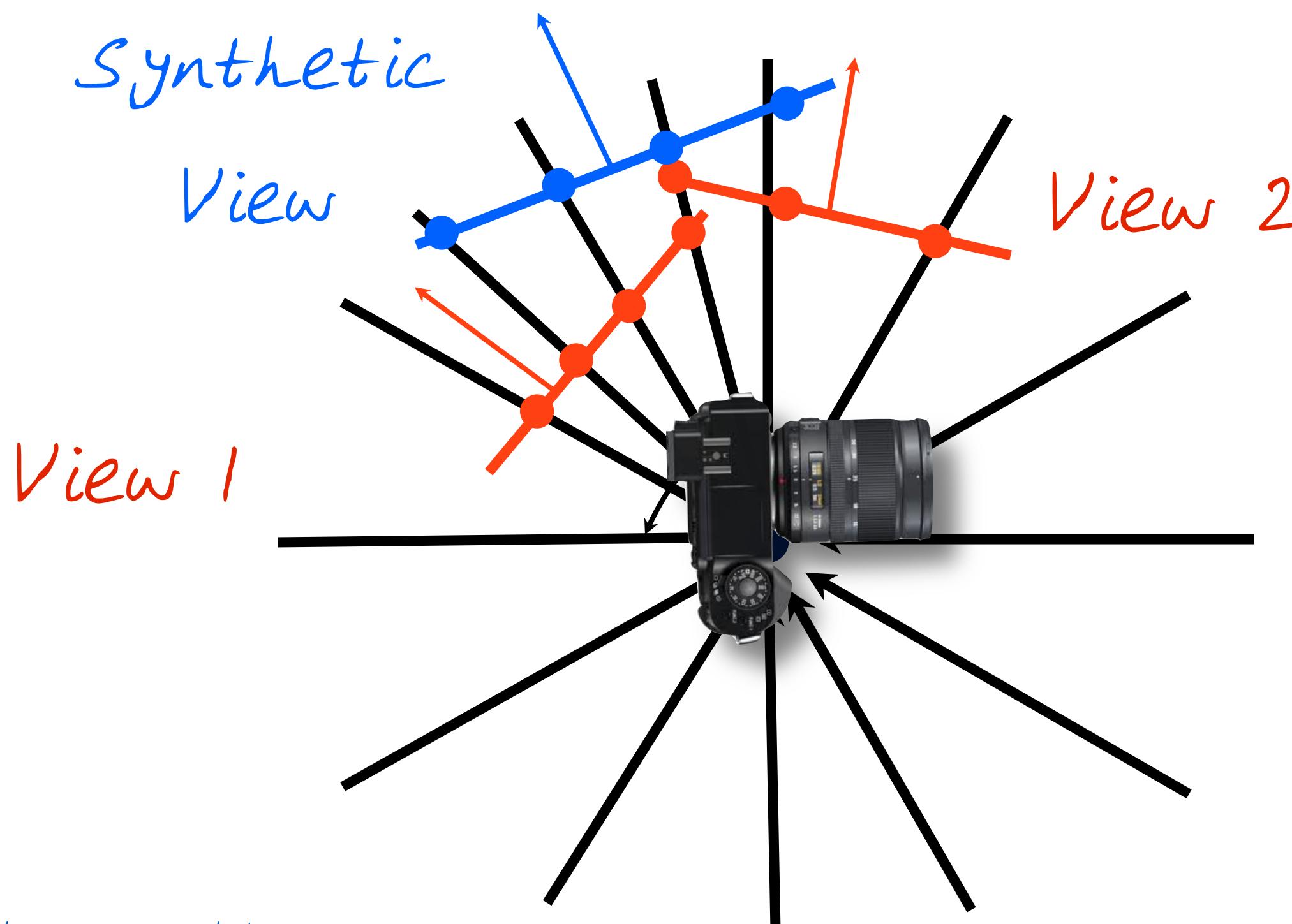


R on top

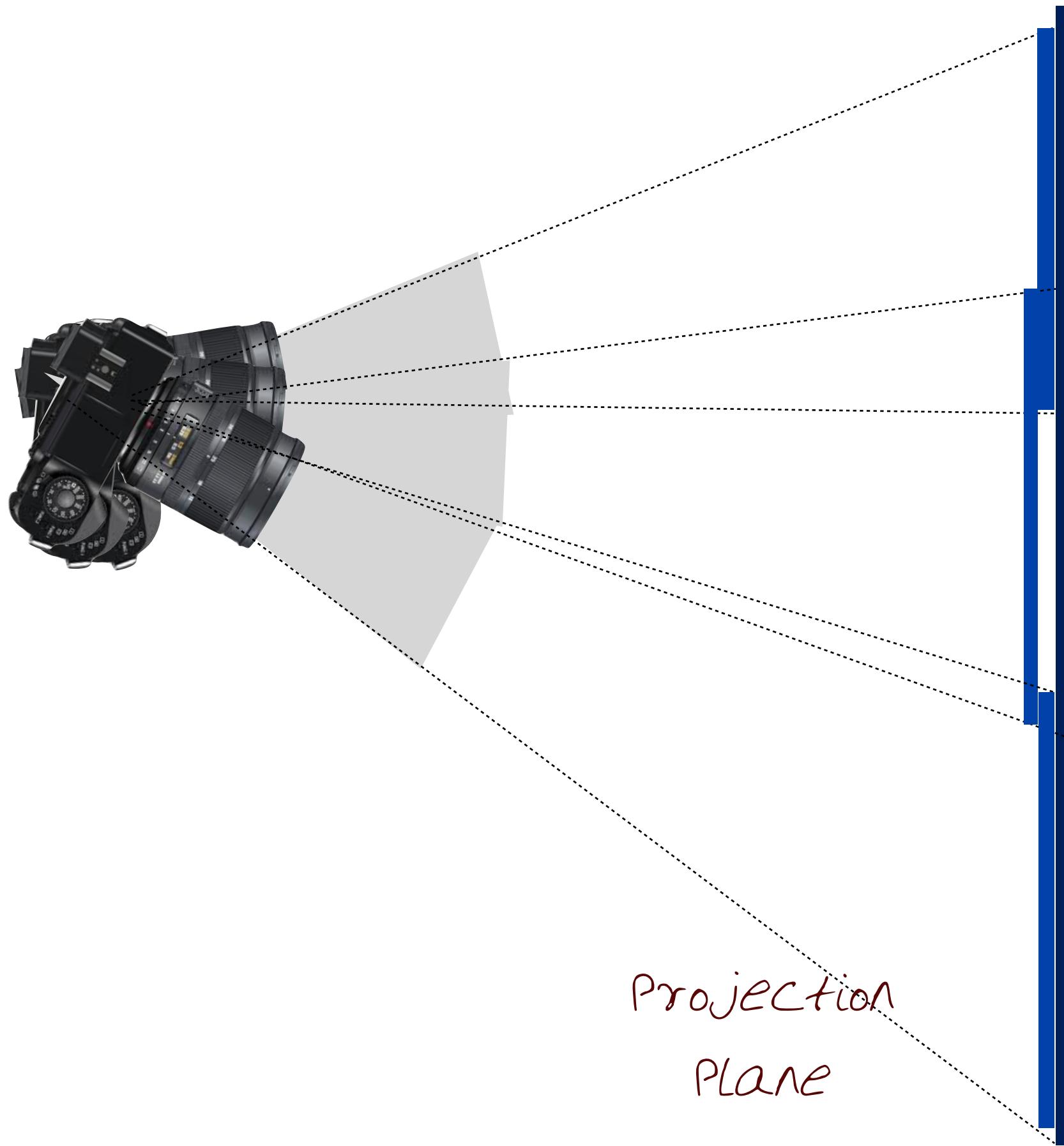
# Better: Warp



# A Bundle of Rays Contains all Views



Possible to generate  
any synthetic  
camera view as long  
as it has  
the same center of  
projection!



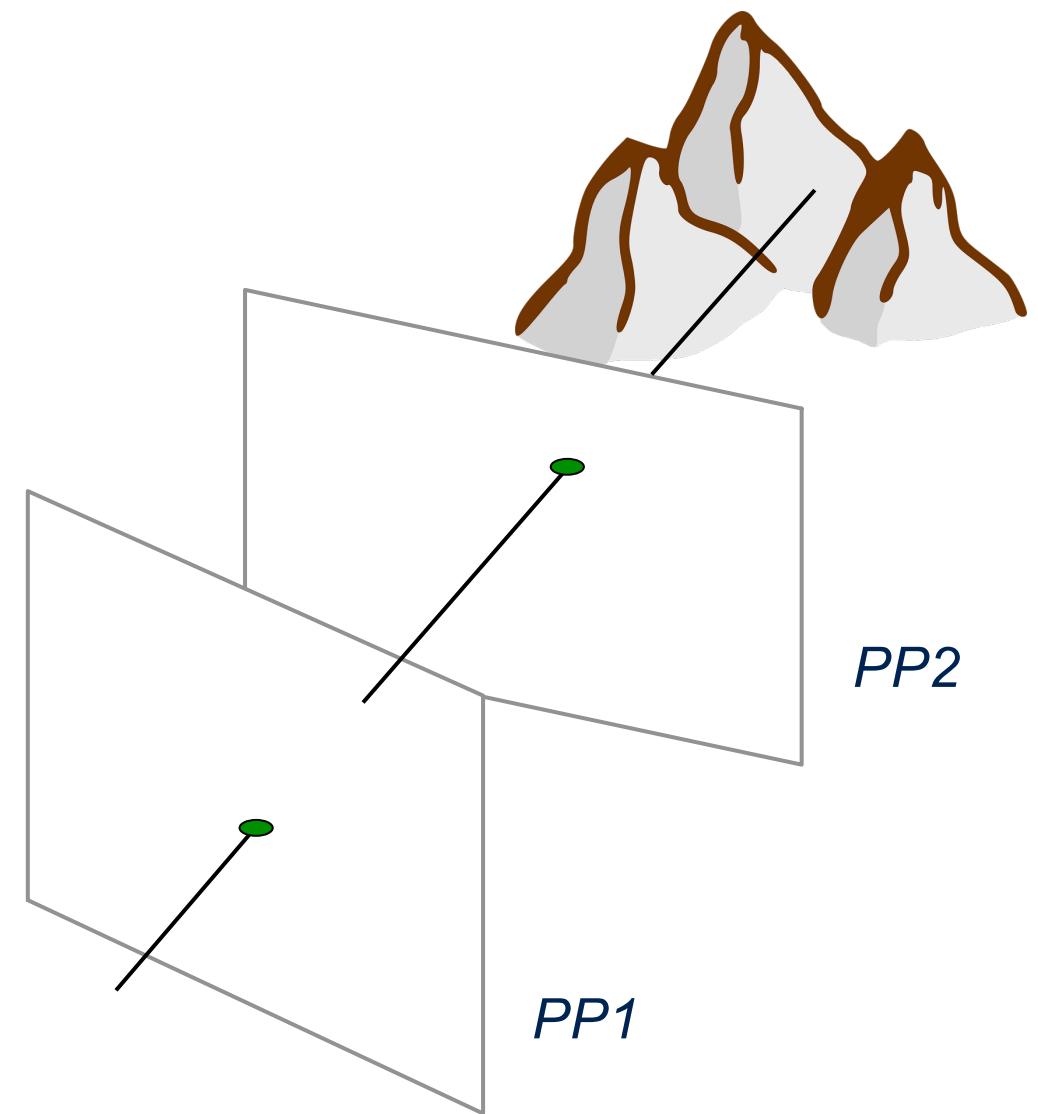
## Image Re-projection to Panorama Projection Plane

- \* The panorama mosaic has a natural interpretation in 3D
- \* Images are reprojected onto a common plane
- \* The mosaic is formed on this plane
- \* Mosaic is a synthetic wide-angle camera

# Image Re-Projection (I)

To relate two images from the same camera center and map a pixel from PP1 to PP2.'

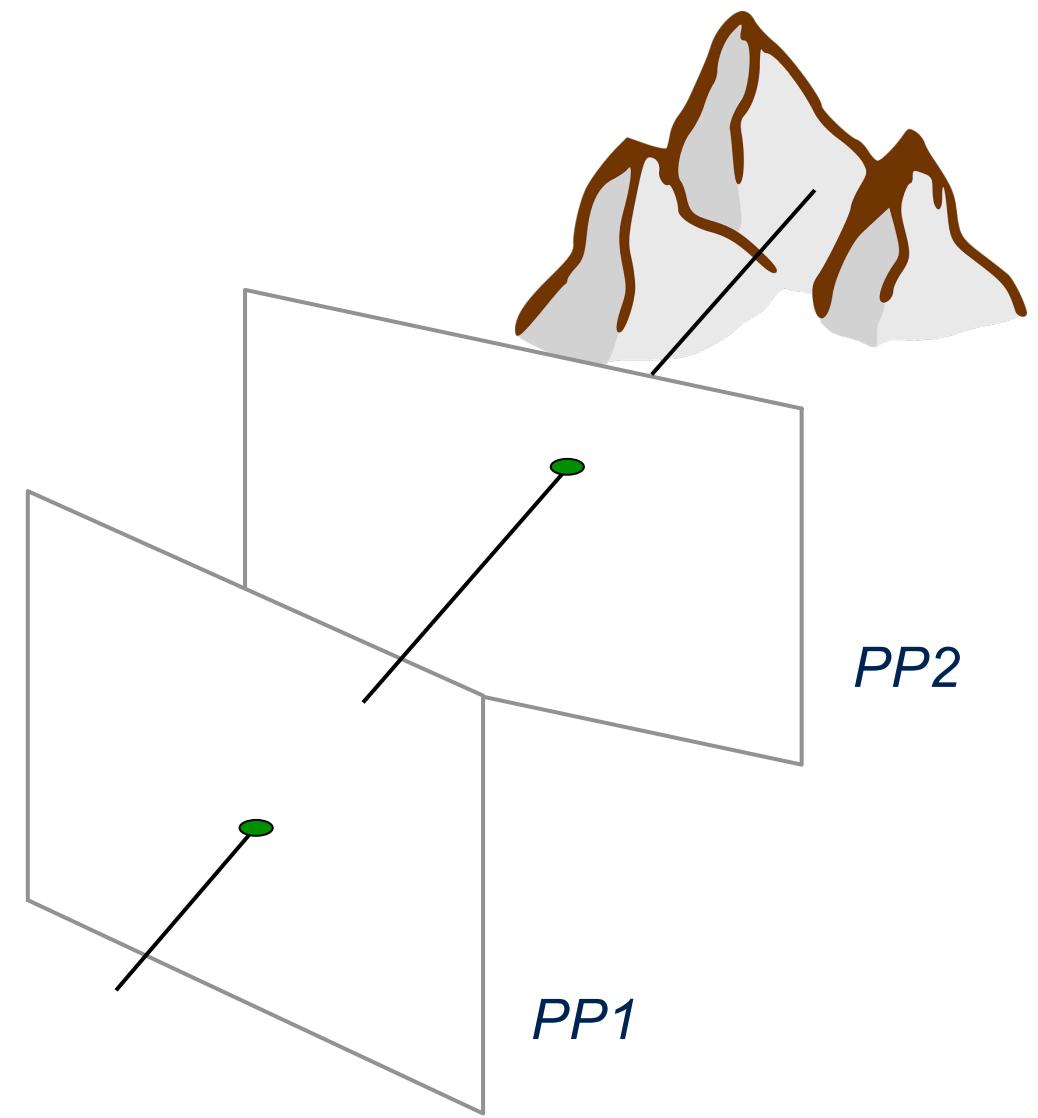
- \* Cast a ray through each pixel in PP1
- \* Draw the pixel where that ray intersects PP2



# Image Re-Projection (2)

To relate two images from the same camera center and map a pixel from PP1 to PP2.'

- \* Rather than a 3D re-projection,
- \* Think of it as a 2D image warp from one image to another
- \* Do not need to know the geometry of the two planes with respect to the eye?



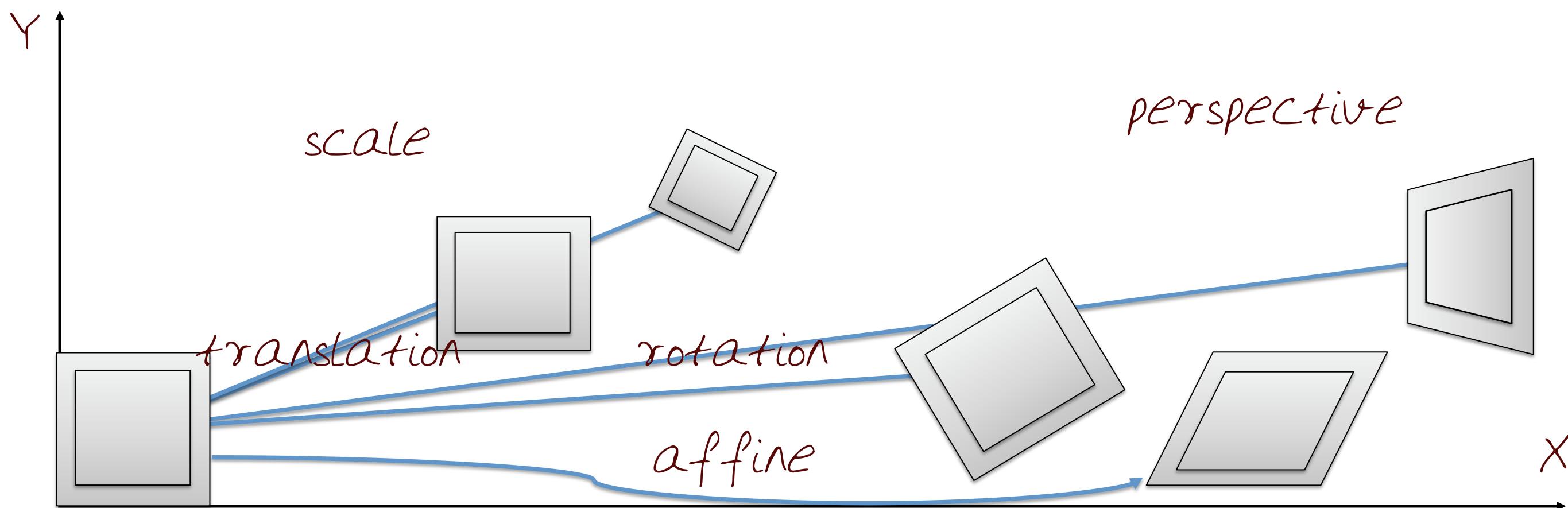
# Recall: Image Transforms

Which transform is the right one for warping PP1 into PP2?

E.g. translation, Euclidean, affine, projective

Translation: 2 unknowns, Euclidean: 3 unknowns

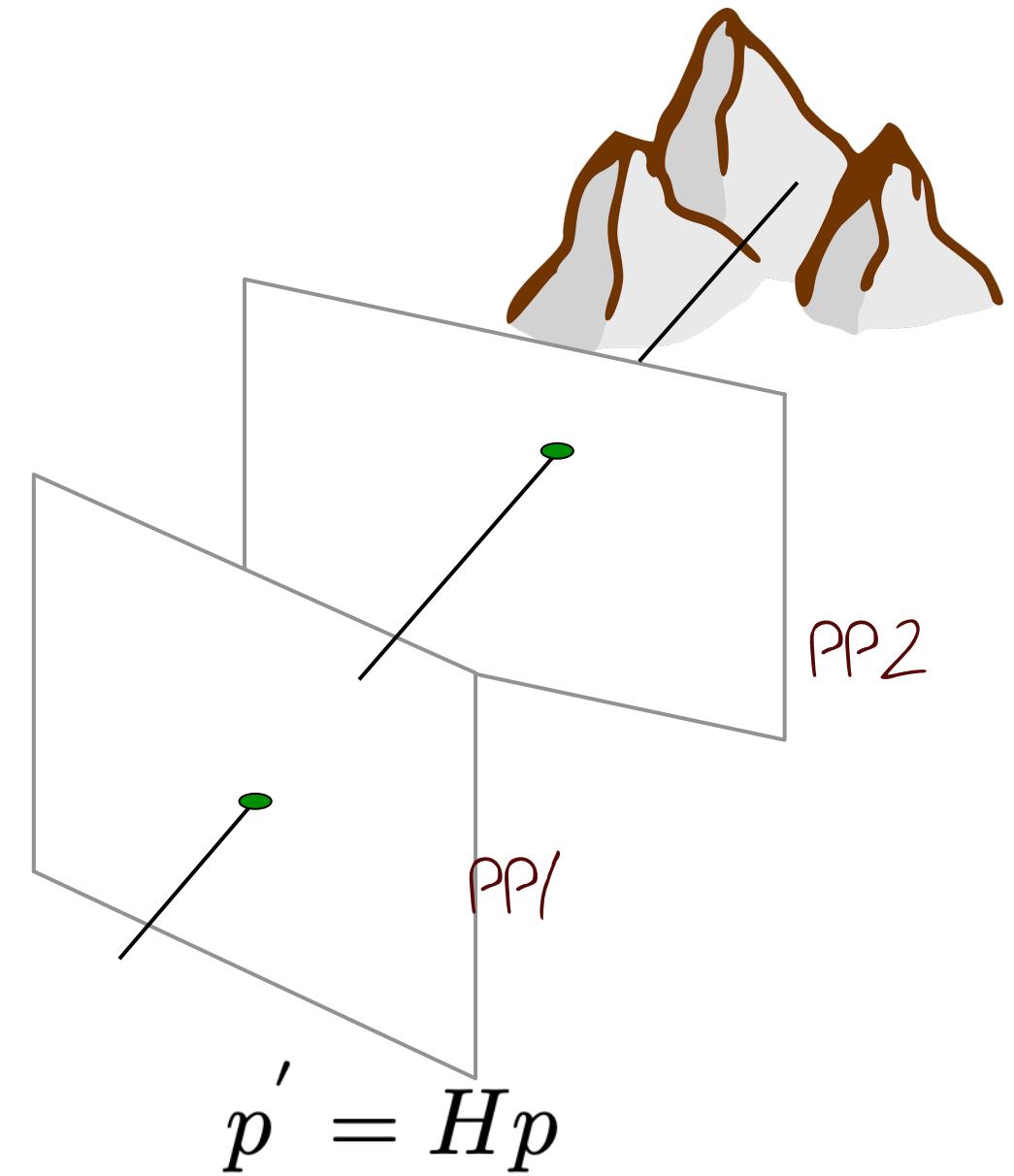
Affine: 6 unknowns, Projective: 8 unknowns



# Homography Recap

Relates two images from the same camera center

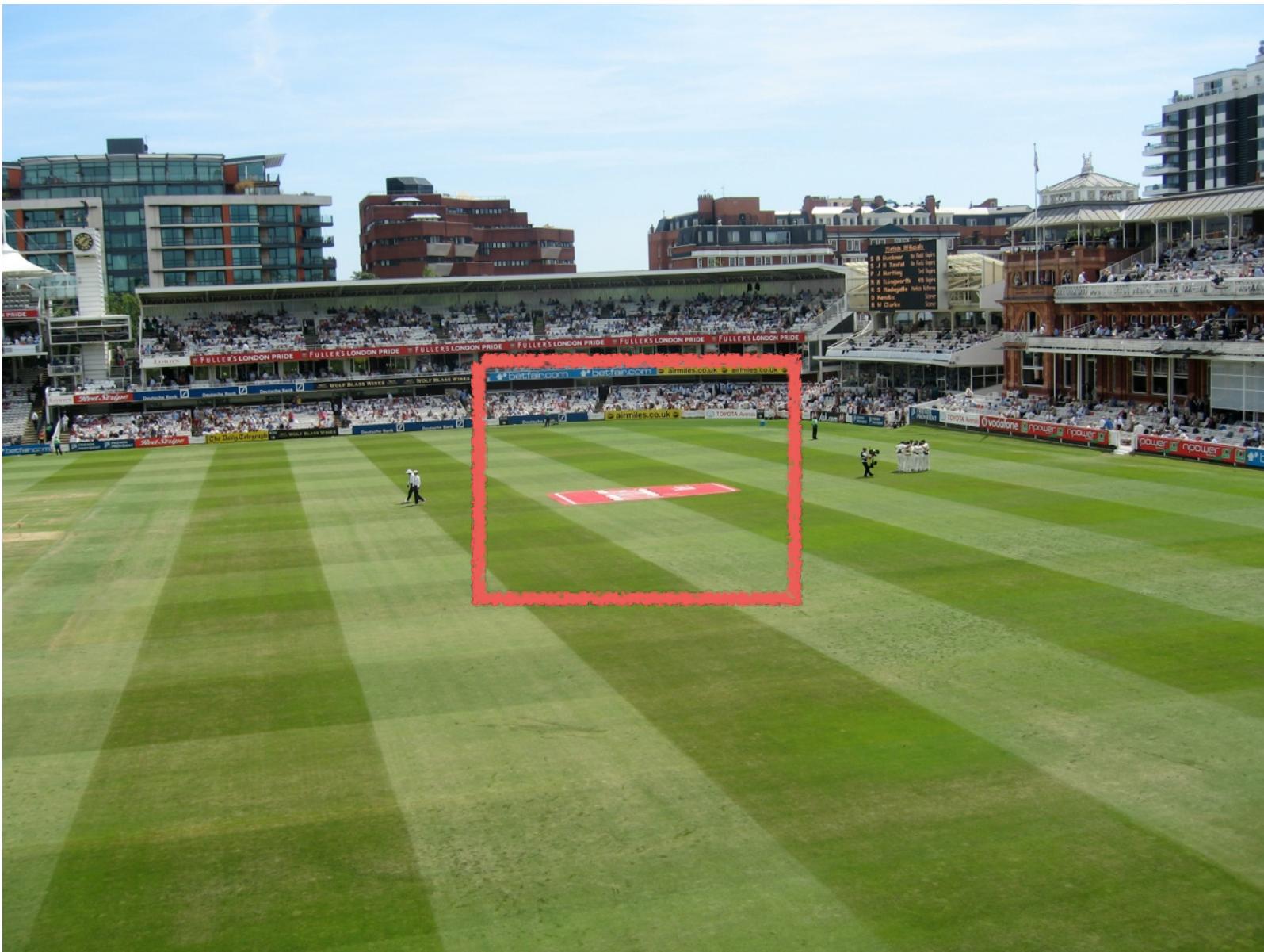
- \* Rectangle should map to arbitrary quadrilateral
- \* Parallel lines aren't parallel
- \* Straight lines must be straight



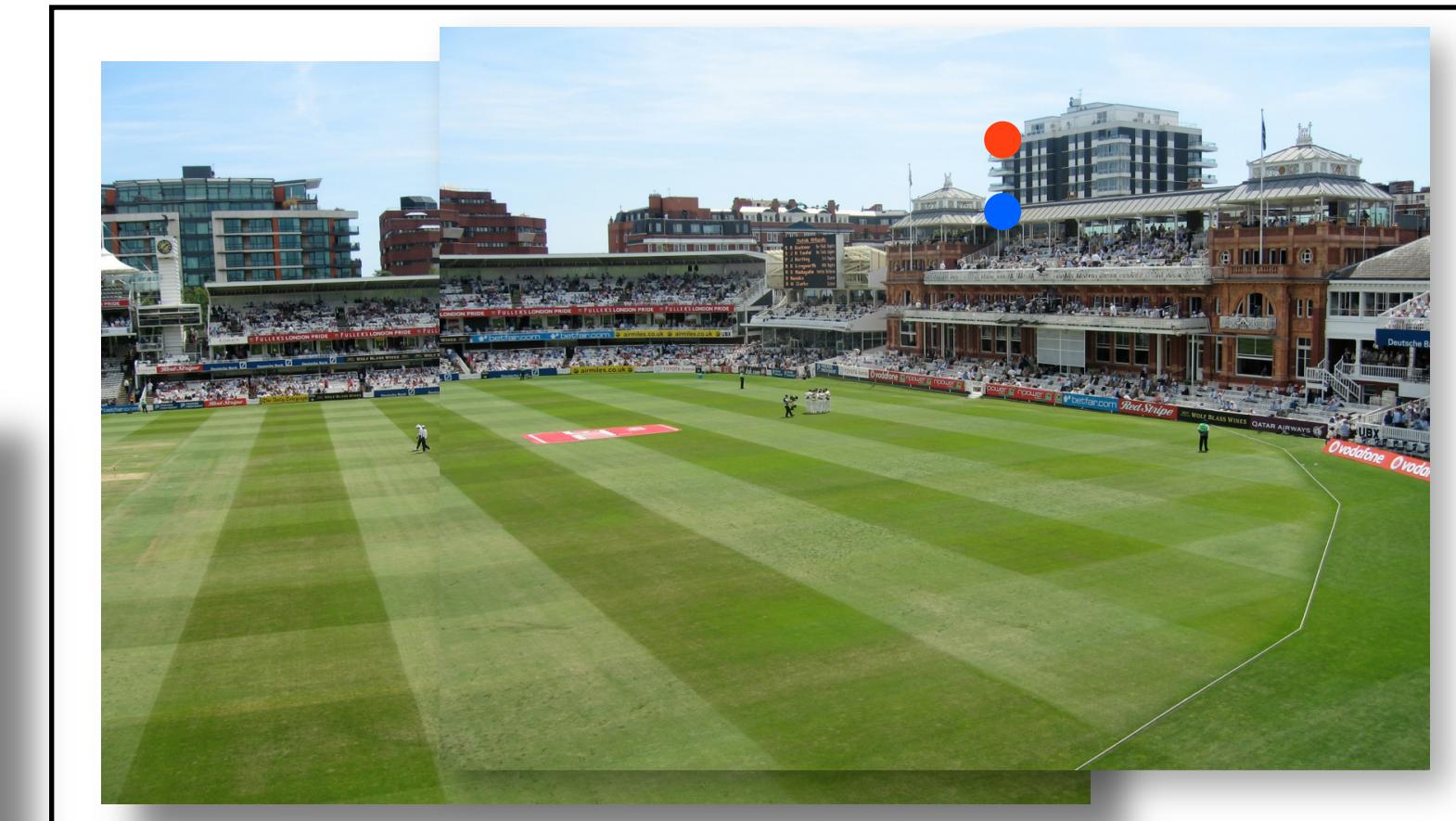
$$\begin{bmatrix} wx' \\ wy' \\ w \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

# Computing Homographies

## Nonlinear Least-Squares (Ch. 6)



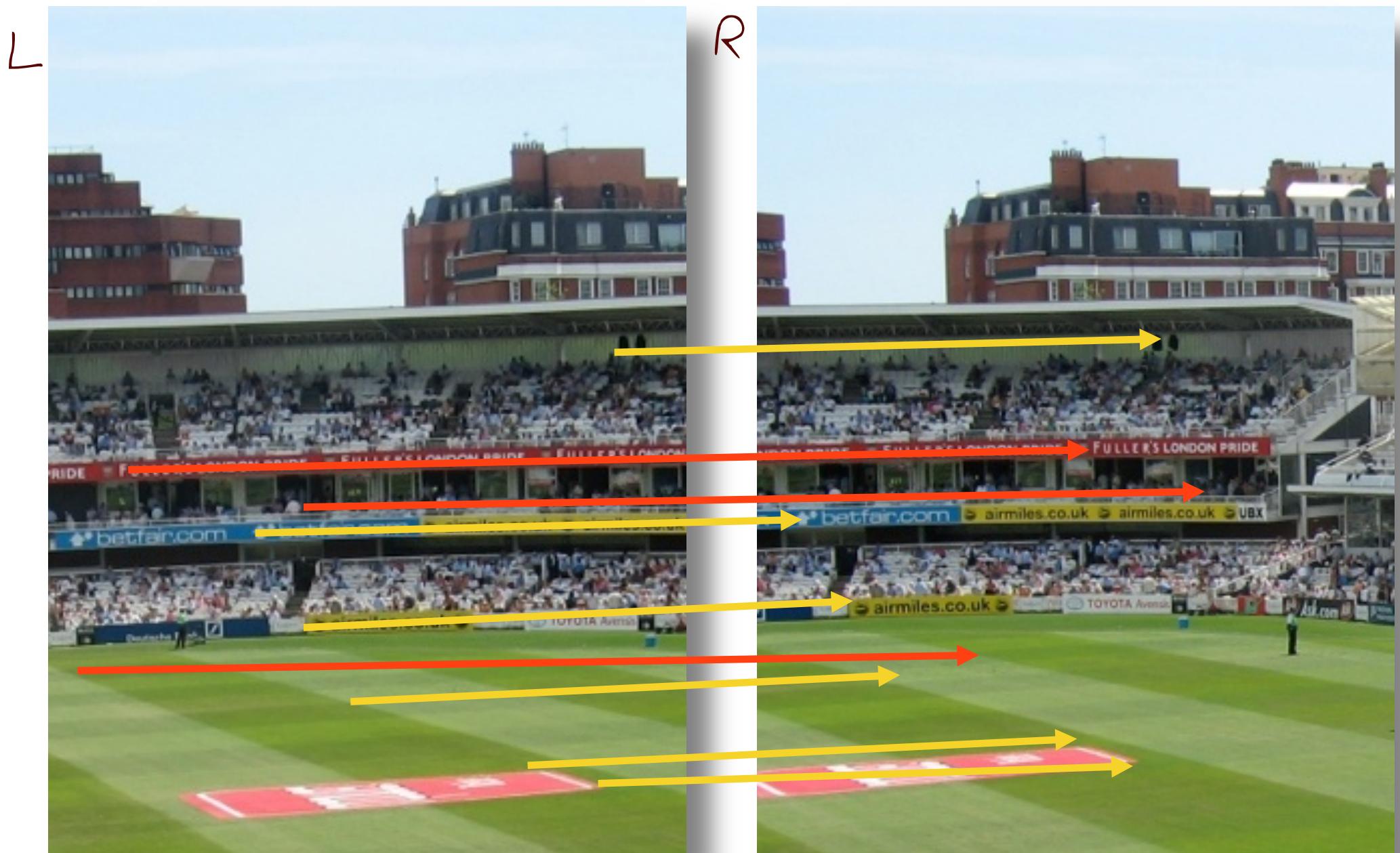
# Warp into a Shared Coordinate Space



# Warping and Interpolation



# Dealing with BAD matches



# RANDom SAMple Consensus (RANSAC)

- \* Select ONE match,  
Count INLIERS
- \* Find "average"  
translation vector



L

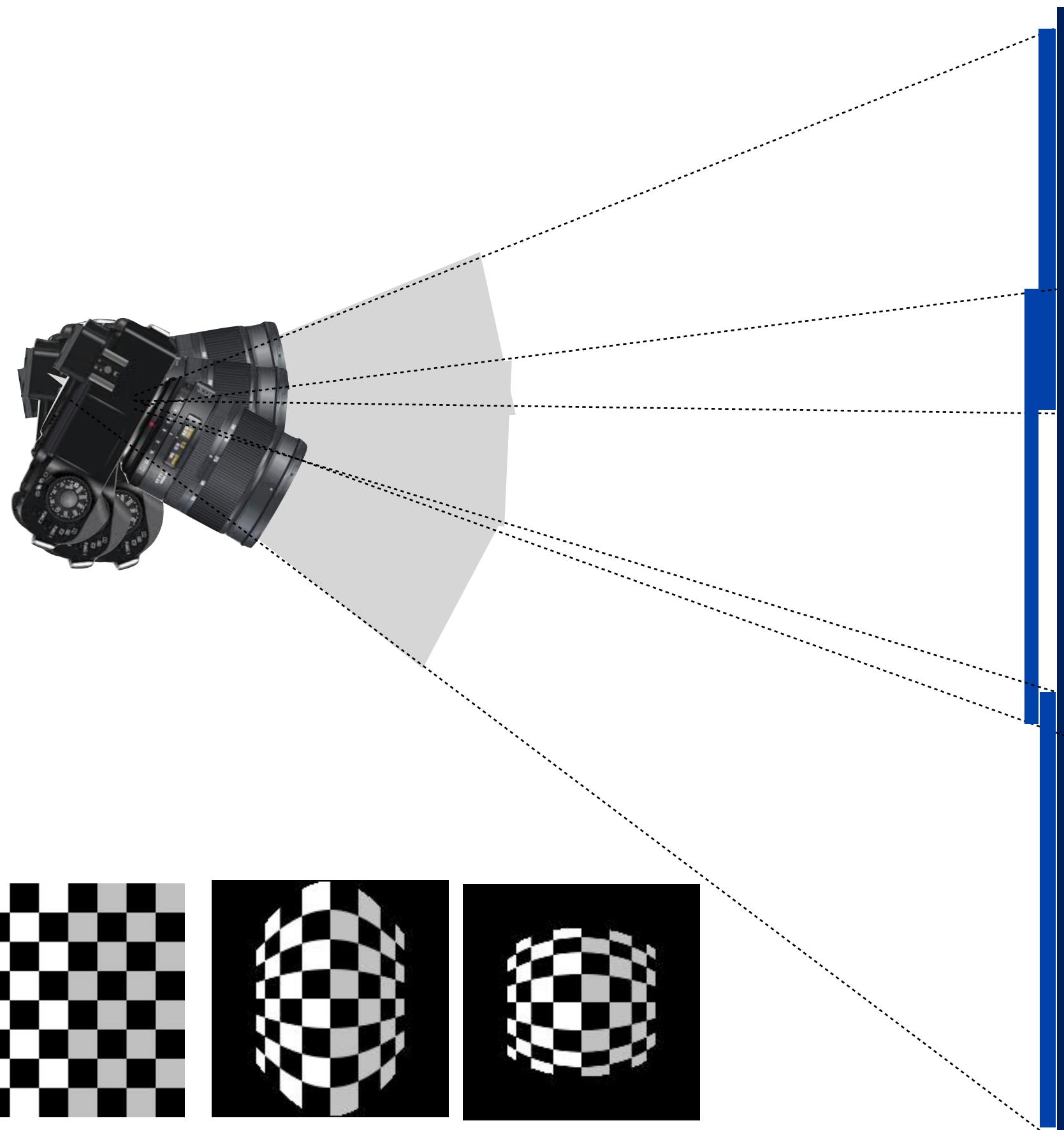
R

# RANDom SAMple Consensus (RANSAC)

Loop till find a convergence/popular  $H$ :

1. Select four feature pairs (at random)
2. Compute homography  $H$  (exact)
3. Compute inliers where:  $SSD(pin', H pin) < \varepsilon$
4. Keep largest set of inliers
5. Re-compute least-squares  $H$  estimate on all of the inliers

Key idea: Not that there are more inliers than outliers, but that the outliers are wrong in different ways.



Plain    Cylinder    Sphere

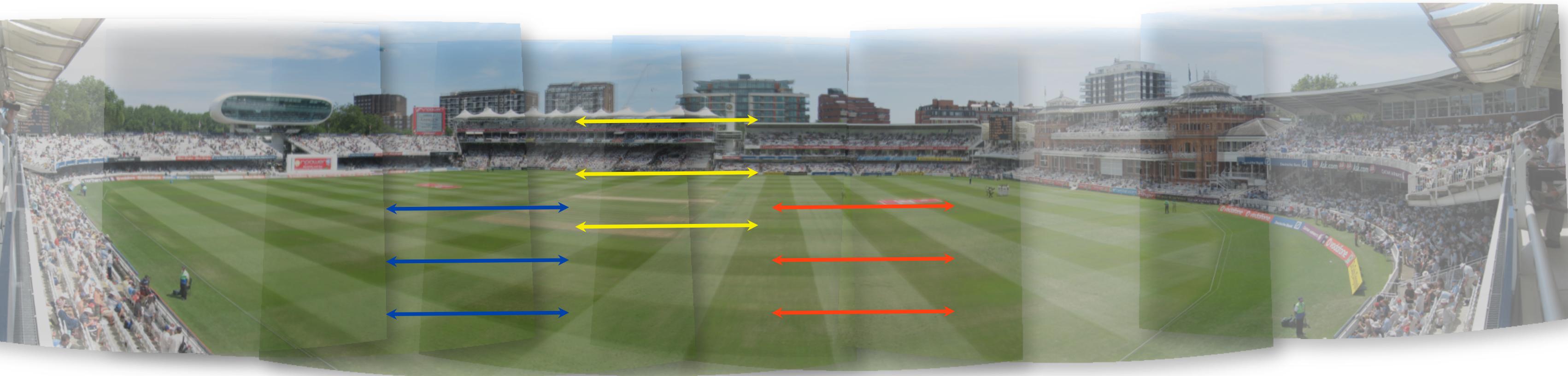
Not Just a Plane

Projection Plane

- \* Cylinder
- \* Sphere

Planar,  
Spherical,  
Cylindrical  
Panoramas





## “Finding Panoramas”

Using RANSAC and related matching techniques, we can find images next to each other that form a panorama. So we don't have to take pictures in a sequence.

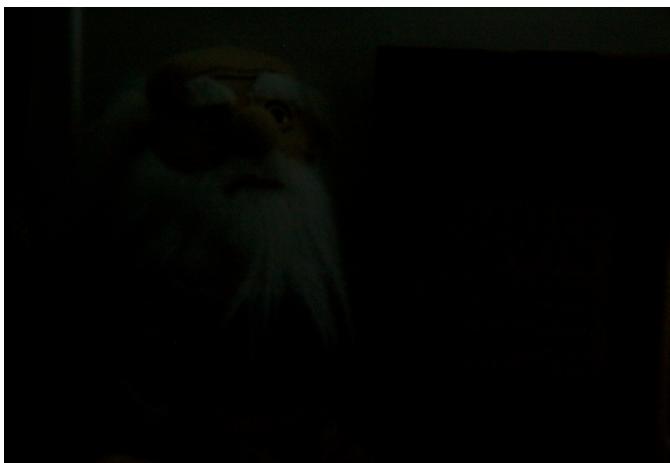
# Further Reading



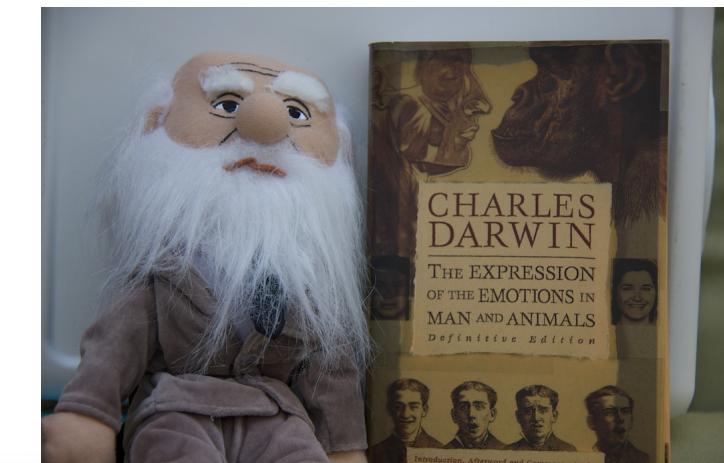
- \* Brown and Lowe (2003). "Recognising Panoramas. " International Conference on Computer Vision (ICCV2003) ([pdf](#) | [bib](#) | [ppt](#))
- \* Microsoft Research Image Composite Editor (ICE)
- \* Panorama Tools Graphical User Interface (PTGui)
- \* Hugin Panorama Photo Stitcher

# High Dynamic Range

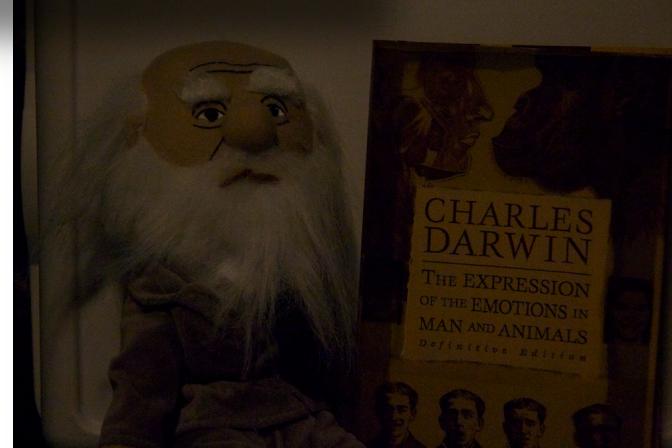
Inside, No Lights  
Long Exposure



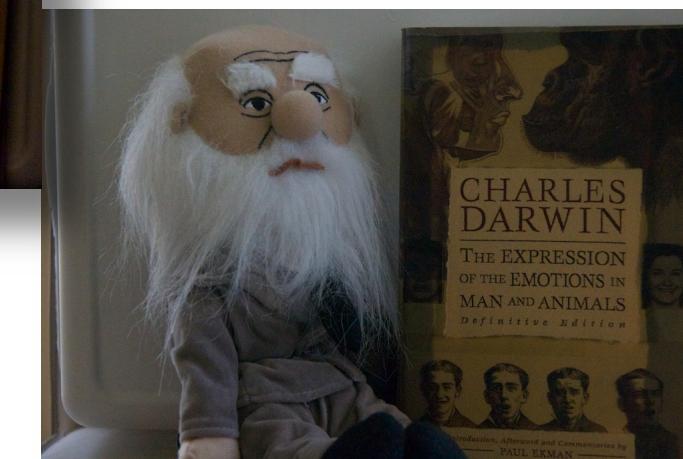
Outside,  
in the Sun



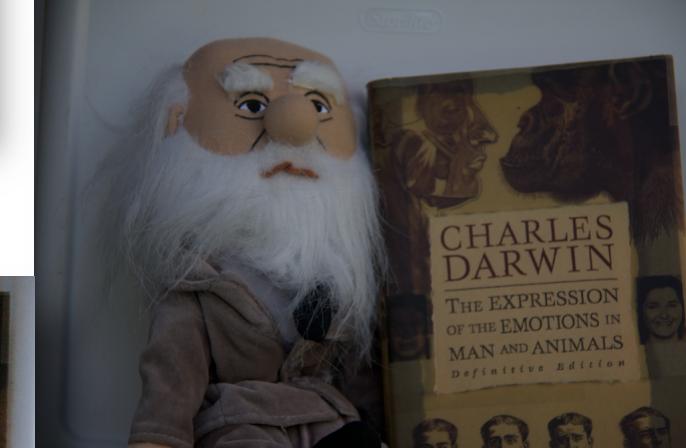
Into the Sun



Inside,  
Incandescent Light



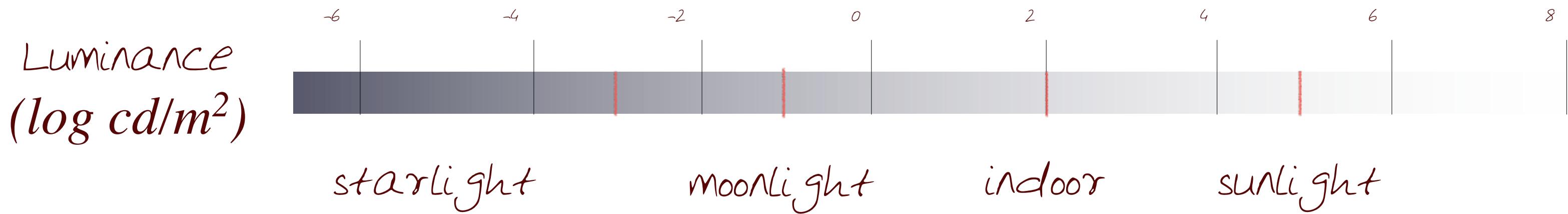
Outside,  
Under Shade



Inside, Near Window  
(Natural Light)

# Dynamic Range

Luminance: A photometric measure of the luminous intensity per unit area of light traveling in a given direction. measured in candela per square meter ( $\text{cd}/\text{m}^2$ ).



\*Human Static Contrast Ratio: 100:1 ( $10^2:1$ ) → about 6.5 f-stops

\*Human Dynamic Contrast Ratio: 1,000,000:1 ( $10^6:1$ ) → about 20 f-stops

# Limited Dynamic Range of Current Cameras



Short Exposure: Snow and Outside Visible



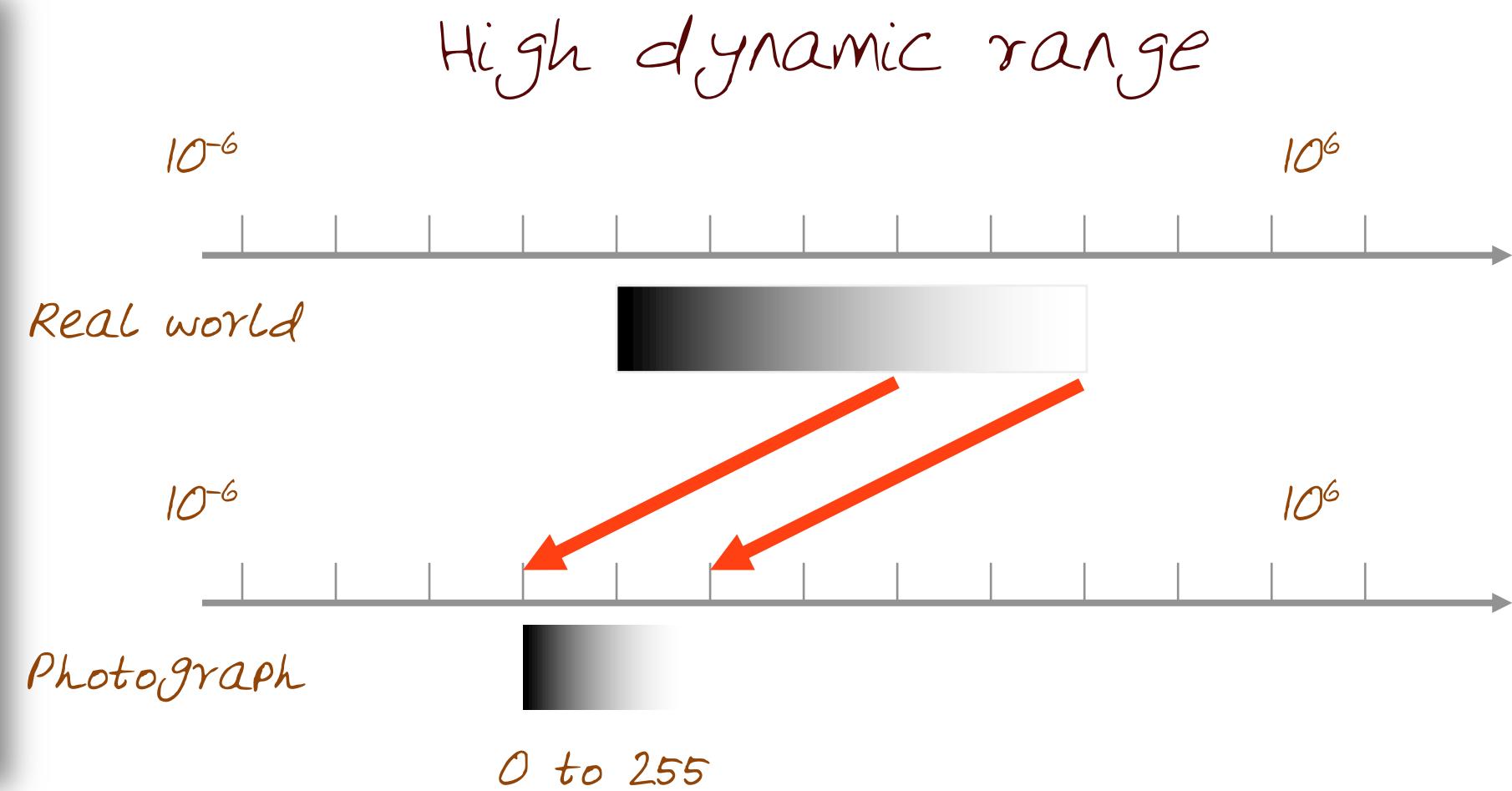
Long Exposure: Inside Visible

- \* Need about 5-10 million values to store all brightnesses around us
- \* 8-bit images provide only 256 values!!

# Limited Dynamic Range of Current Cameras

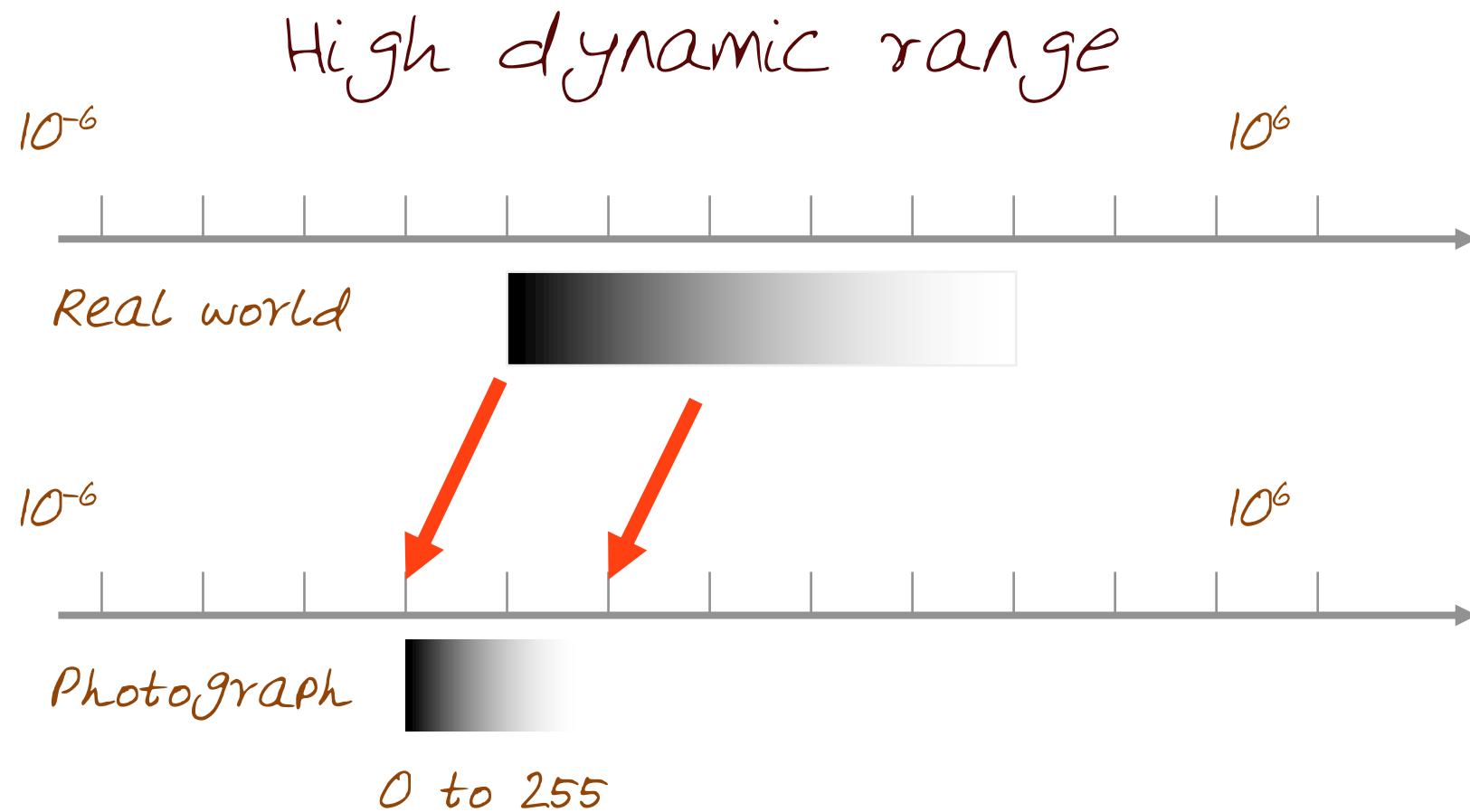


Short Exposure: Snow and Outside Visible



- \* Need about 5-10 million values to store all brightnesses around us.
- \* 8-bit images provide only 256 values!!

# Limited Dynamic Range of Current Cameras

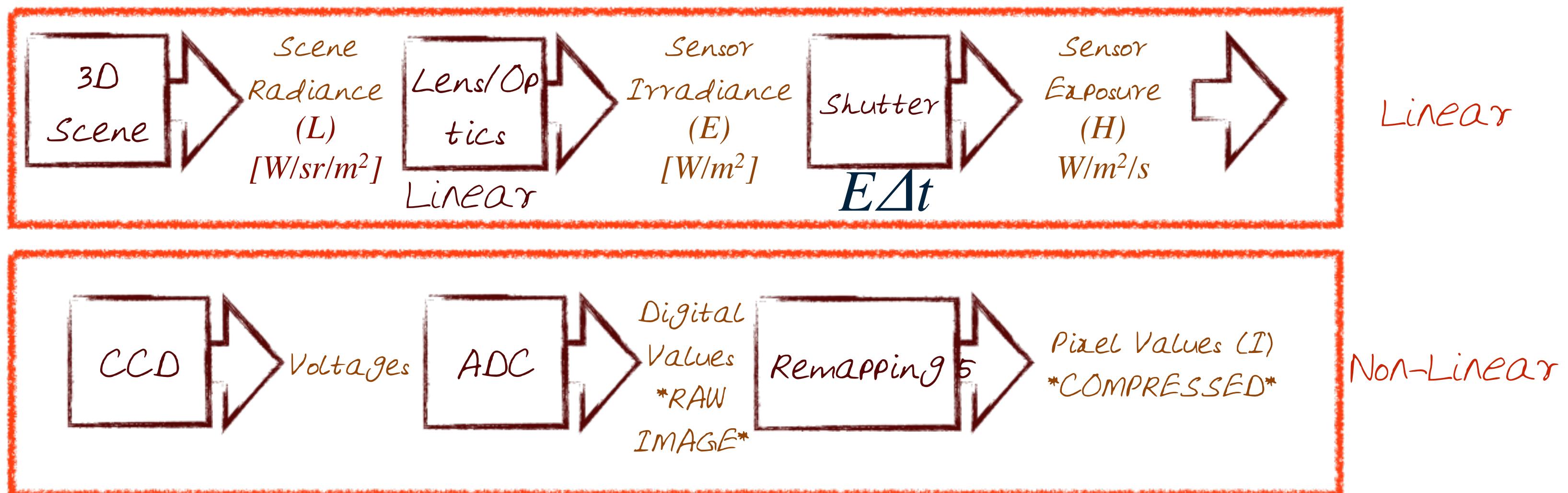


Long Exposure: Inside Visible

- \* Need about 5-10 million values to store all brightnesses around us.
- \* 8-bit images provide only 256 values!!

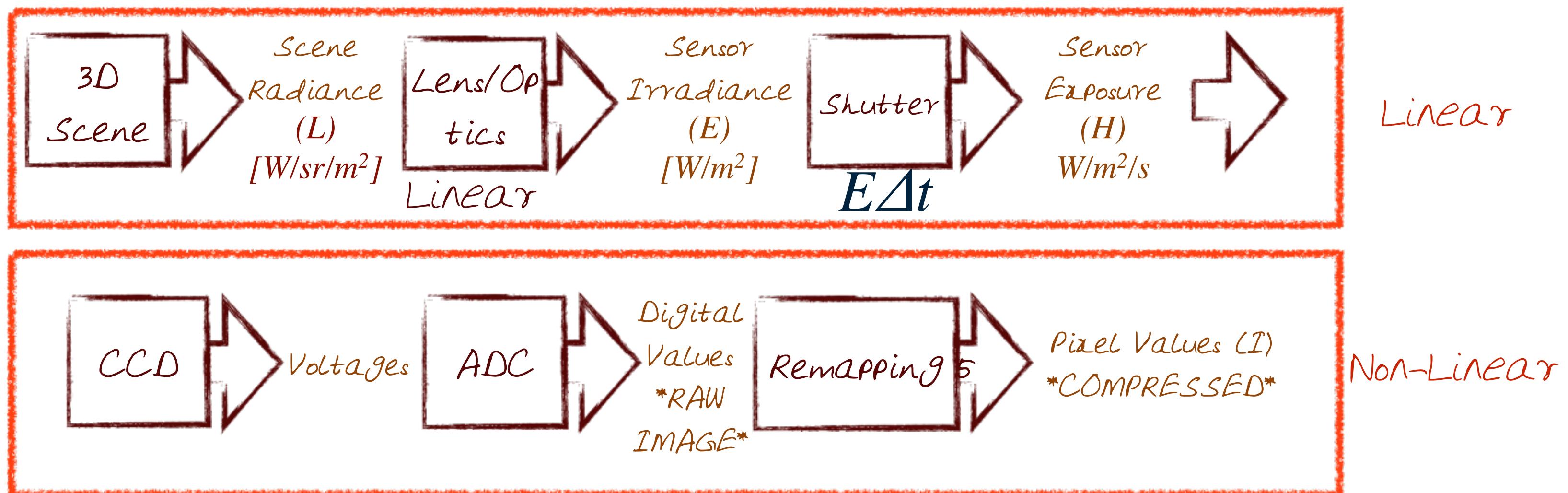
# Relationship Between Image and Scene Brightness

## The Image Acquisition Pipeline



# Relationship Between Image and Scene Brightness

$$g: L \rightarrow E \rightarrow H \rightarrow I \quad \longleftrightarrow \quad g^{-1}: I \rightarrow H \rightarrow E \rightarrow L$$



# Camera Calibration

\*

Geometric

\*

How pixel coordinates relate to

directions in the world

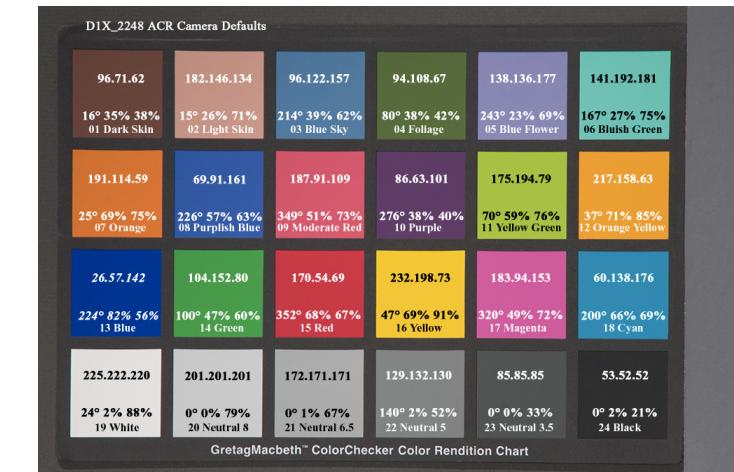
\*

Radiometric / Photometric

\*

How pixel values relate to

radiance amounts in the world

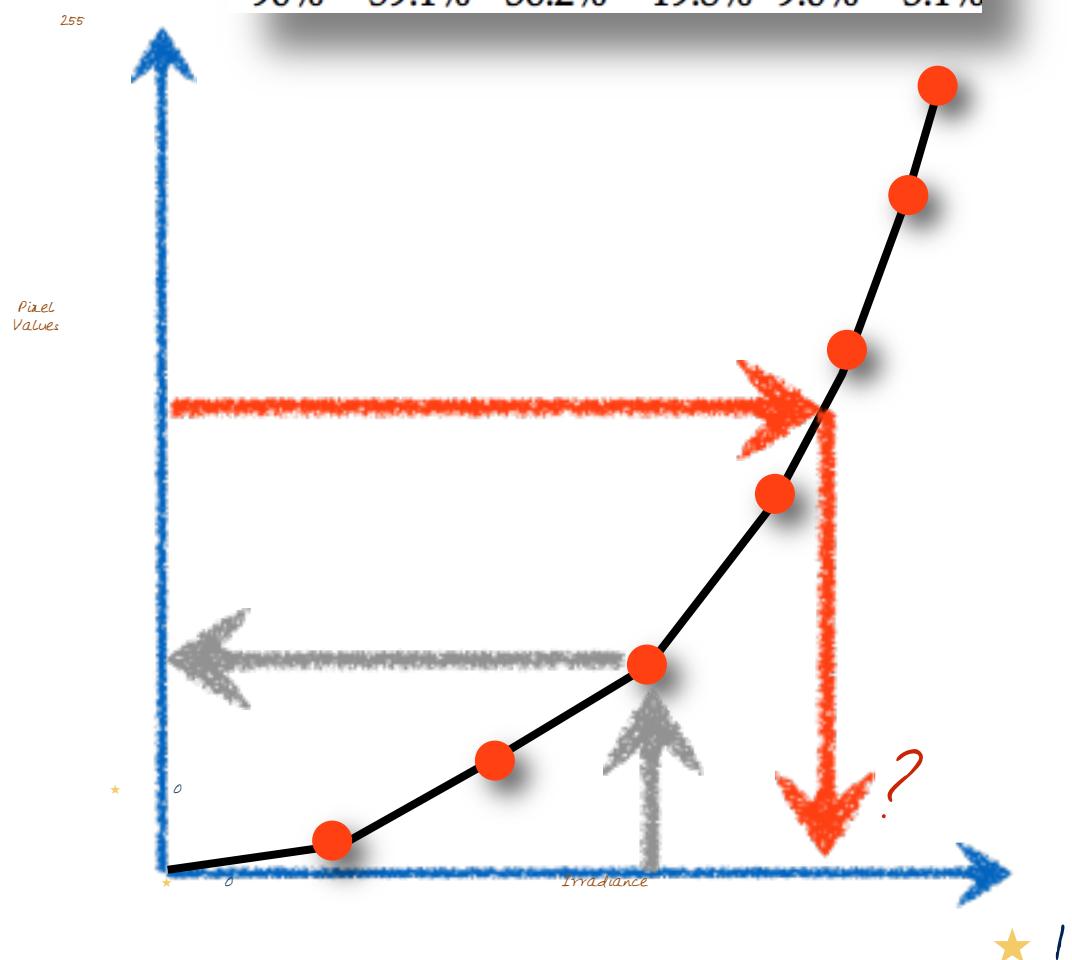
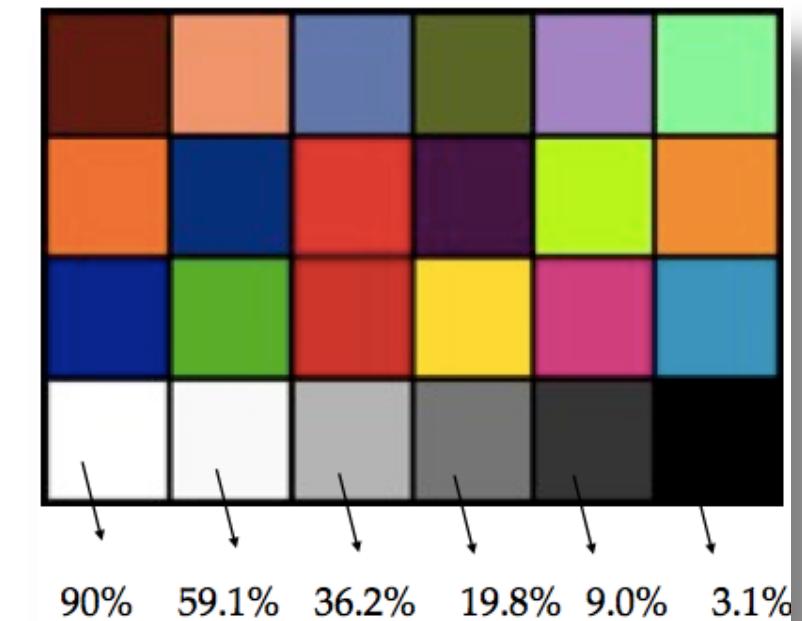


# Radiometric Calibration

$$g: L \rightarrow E \rightarrow H \rightarrow I \longleftrightarrow g^{-1}: I \rightarrow H \rightarrow E \rightarrow L$$

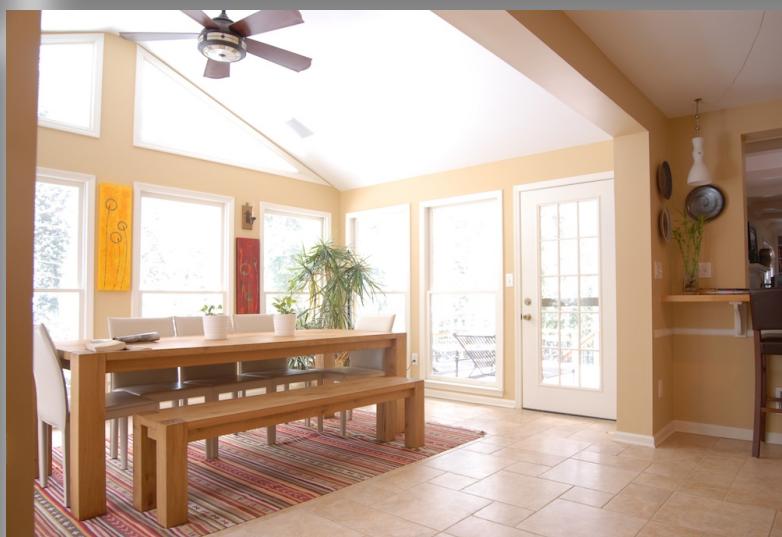
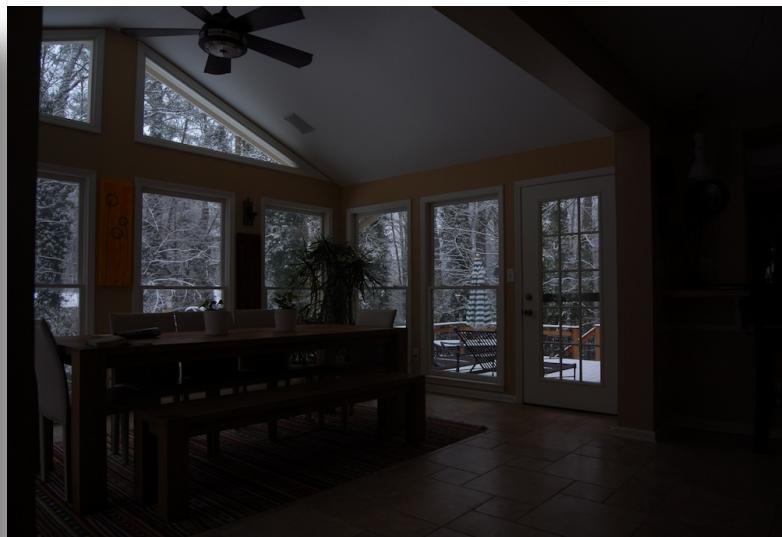
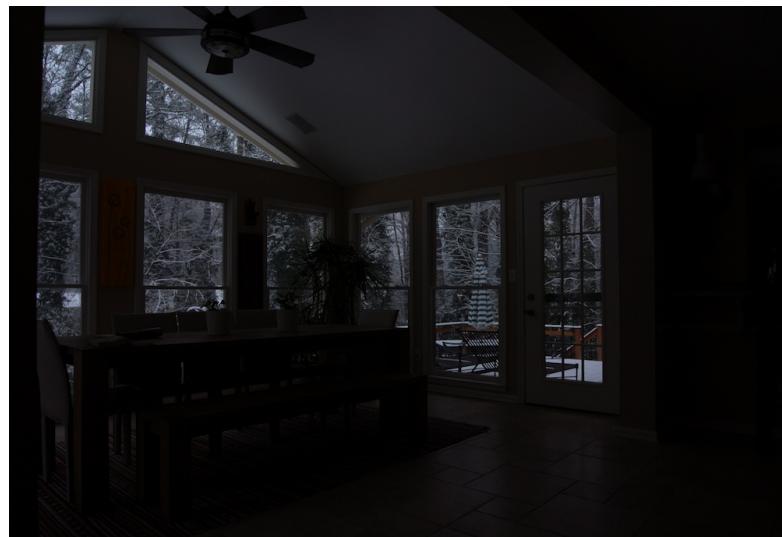
- \* A Color Chart with known reflectances
- \* Multiple camera exposures to fill up the curve
- \* Method assumes constant lighting on all patches and works best when source is far away (example sunlight)
- \* Unique inverse exists because  $g$  is monotonic and smooth for all cameras

(Grossberg and Nayar 2003)



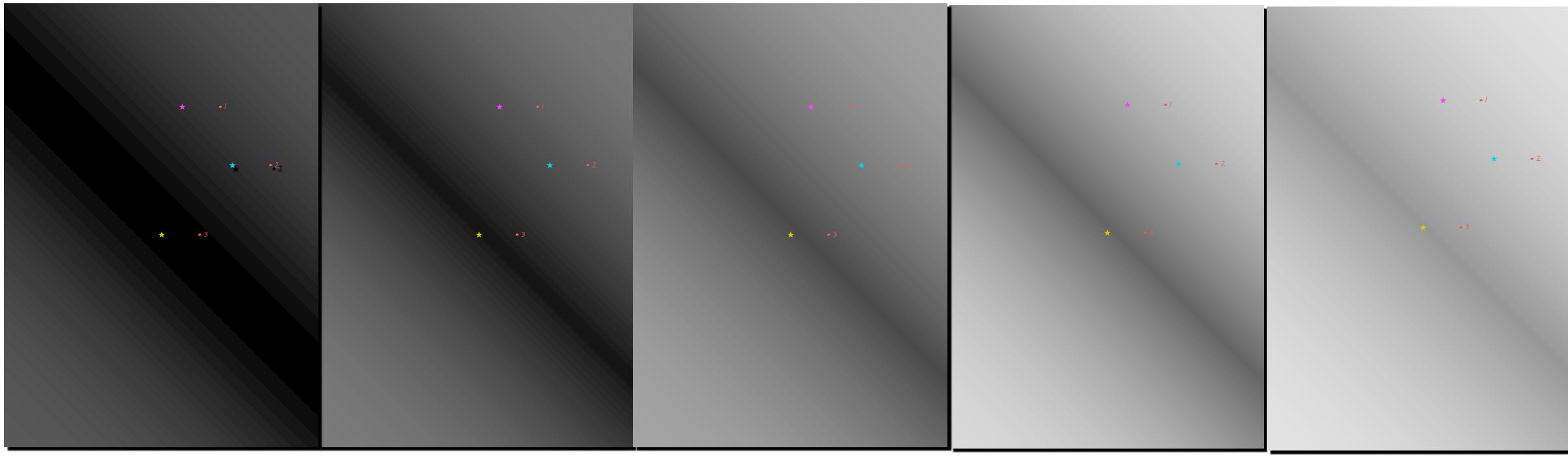


# A Sequence of Images of Different Exposures



# Series of Images

Pixel Values ( $I$ )



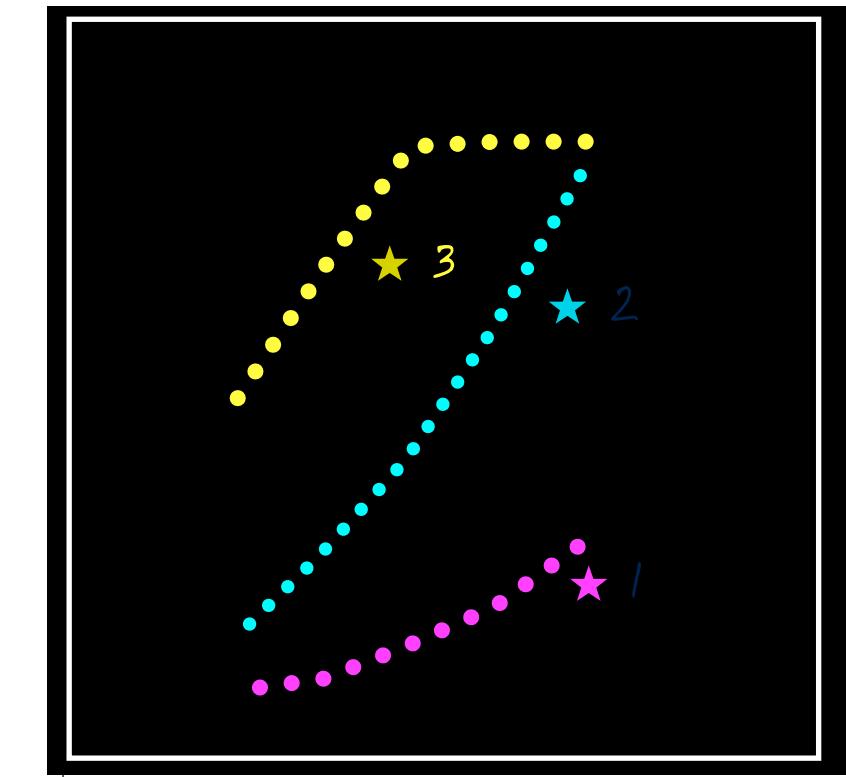
$$\Delta t = 1/64 \text{ sec}$$

$$\Delta t = 1/16 \text{ sec}$$

$$\Delta t = 1/4 \text{ sec}$$

$$\Delta t = 1 \text{ sec}$$

$$\Delta t = 4 \text{ sec}$$



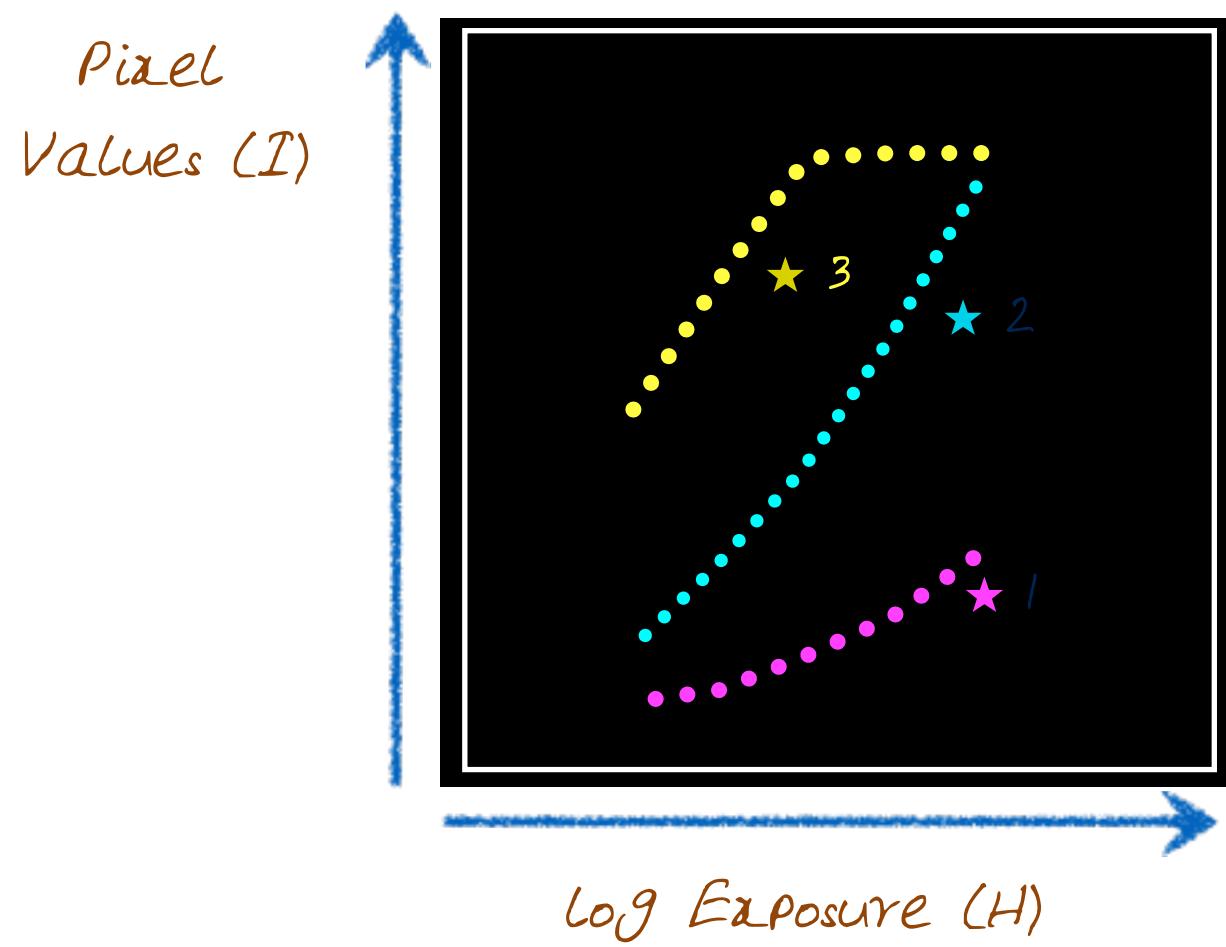
Log Exposure ( $H$ )

Pixel Values ( $I$ ) =  $g(\text{Exposure})$

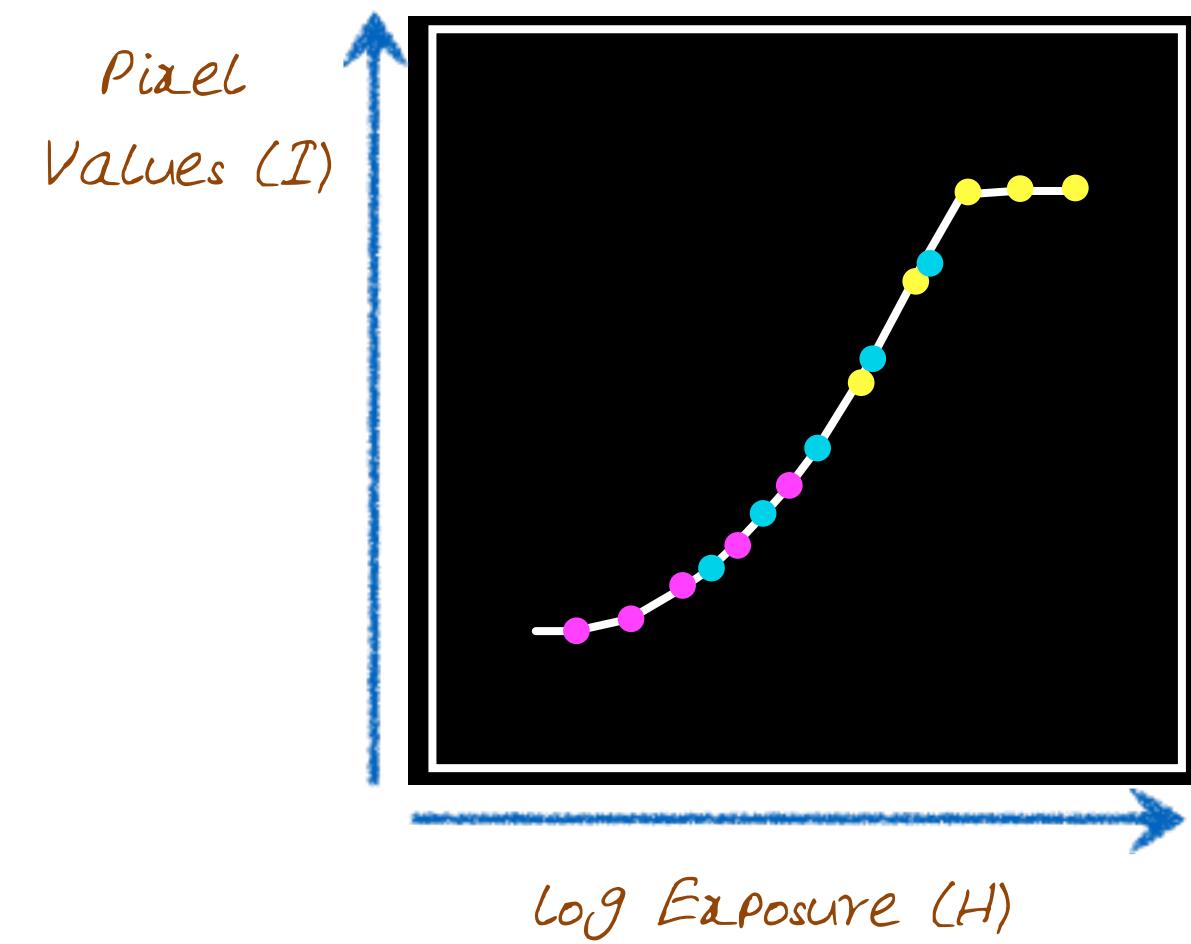
Exposure ( $H$ ) = Irradiance ( $E$ ) \*  $\Delta t$

Log Exposure ( $H$ ) = Log Irradiance ( $E$ ) + Log  $\Delta t$

# Response Curves



Assuming unit  
radiance for  
each pixel



After adjusting  
radiances to obtain a  
smooth response curve

# Iterative Method

- \* For each pixel site  $i$  in each image  $j$ , we have

$$Z_{ij} = f(X_{ij}) = f(I_i \Delta t_j) \quad (1)$$

- \* So, if have  $f$ , we can estimate the *irradiance image*  $I$  as

$$I_i = \frac{1}{m} \sum_{j=0}^{m-1} \frac{f^{-1}(Z_{ij})}{\Delta t_j} \quad (2)$$

- \* Note  $f^{-1}$  is a lookup table

- \* We can re-estimate as:  $f^{-1}(Z_{ij}) = I_i \Delta t_j = X_{ij}$

- \* Iterate (2) and (3), until convergence.

(3)

# Demo-time!

HDR  
by Akshay J D

i </>

Next Source Image

Toggle Annotation

Gamma slider

Exposure slider

Re-evaluate HDR

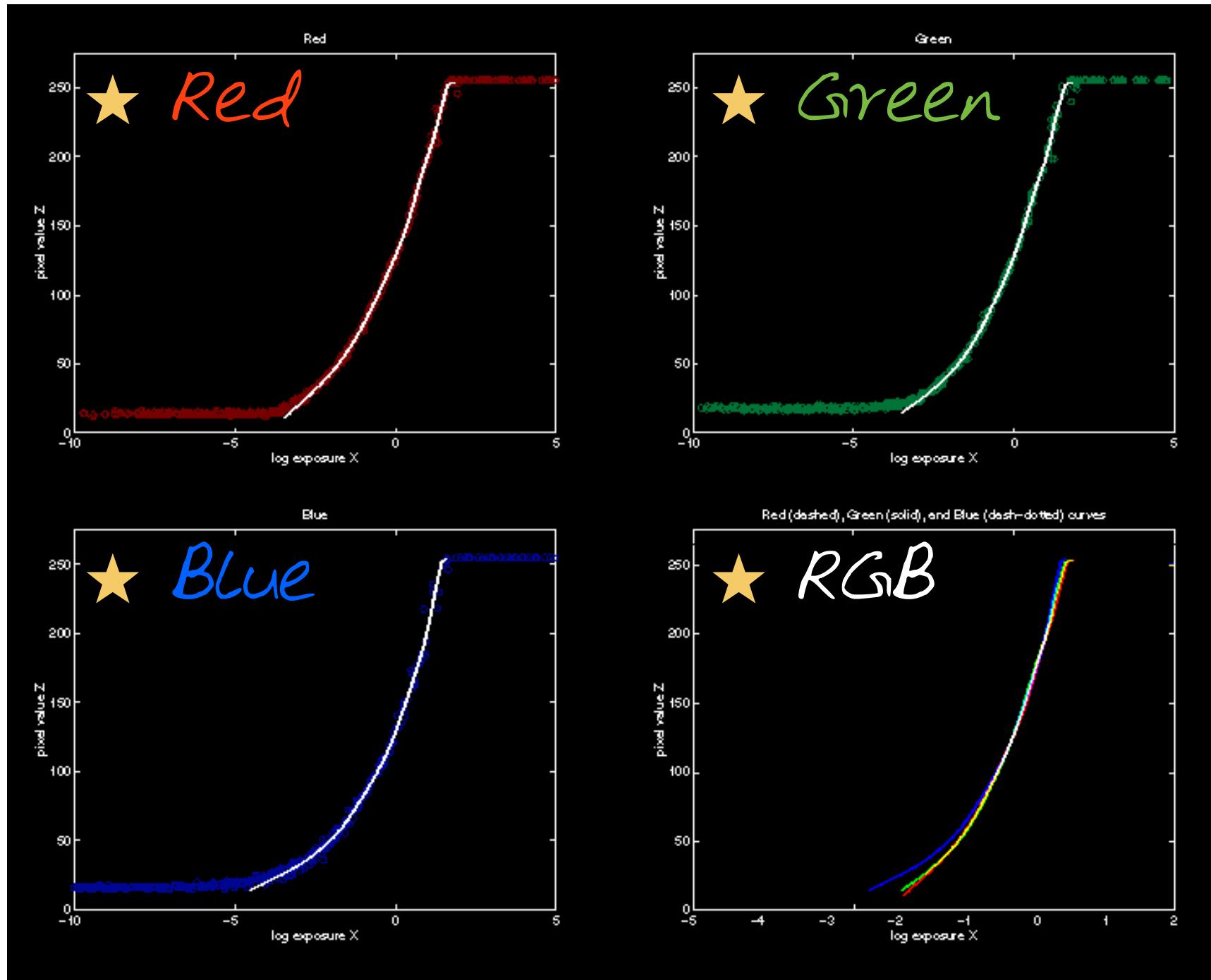
# How to Compute: Debevec 99

- \* Let  $g(z)$  be the discrete inverse response function
- \* For each pixel site  $i$  in each image  $j$ , compute
$$\ln(E_i) + \ln(\Delta t_j) = g(Z_{ij})$$
- \* Solve the overdetermined linear system for  $N$  pixels over  $P$  different exposure images.  
Fitting Term  $\sum_{i=1}^N \sum_{j=1}^P [\ln(E_i) + \ln(\Delta t_j) - g(Z_{ij})]^2$  Smoothness Term  $+ \lambda \sum_{z=Z_{min}}^{Z_{max}} g''(z)^2$

$$\sum_{i=1}^N \sum_{j=1}^P [\ln(E_i) + \ln(\Delta t_j) - g(Z_{ij})]^2 + \lambda \sum_{z=Z_{min}}^{Z_{max}} g''(z)^2$$

See Debevec and malik (1997) for more details

# Response Curves



(Not actual curves for these images, used here just for demonstration)

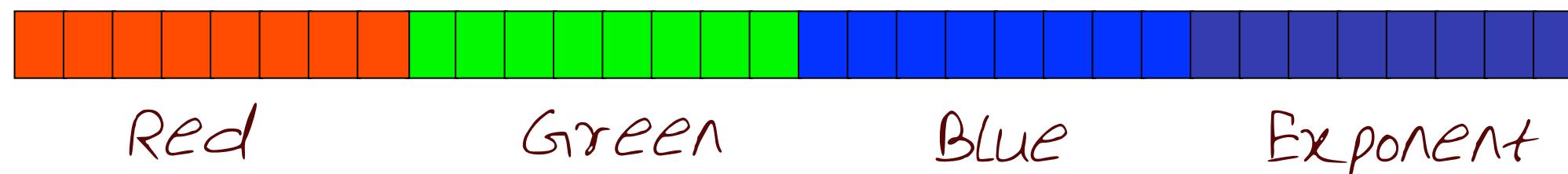
# Radiance Map



# Need a New File Format

Radiance Format

32 bits / pixel



- ★  $(145, 215, 87, 149) =$
- ★  $(145, 215, 87) * 2^{(149-128)} =$
- ★  $(1190000, 1760000, 713000)$

- ★  $(145, 215, 87, 103) =$
- ★  $(145, 215, 87) * 2^{(103-128)} =$
- ★  $(0.00000432, 0.00000641, 0.00000259)$

Ward (2001), There are many other formats too

*Now to Display it!*





# Tone Mapping

- \* map one set of colors to another
- \* Displaying on a medium that has limited dynamic range
- \* Printers, monitors, and projectors all have a limited dynamic range
- \* Inadequate to reproduce the full range of light intensities present in natural scenes



★ [http://commons.wikimedia.org/  
wiki/File:Kanitz-Kyawsche\\_Gruft\\_in\\_Hainewalde  
\\_HDR.jpg](http://commons.wikimedia.org/wiki/File:Kanitz-Kyawsche_Gruft_in_Hainewalde_HDR.jpg)

# Tone Mapping

- \* Addresses the problem of
- \* strong contrast reduction from the scene  
radiance to the displayable range
- \* preserves the image details and color appearance
- \* many well-known ALgorithms exist for this
- \* See Banterle, et al. (2011), Reinhard et al. (2002) and Durand and Dorsey (2002)

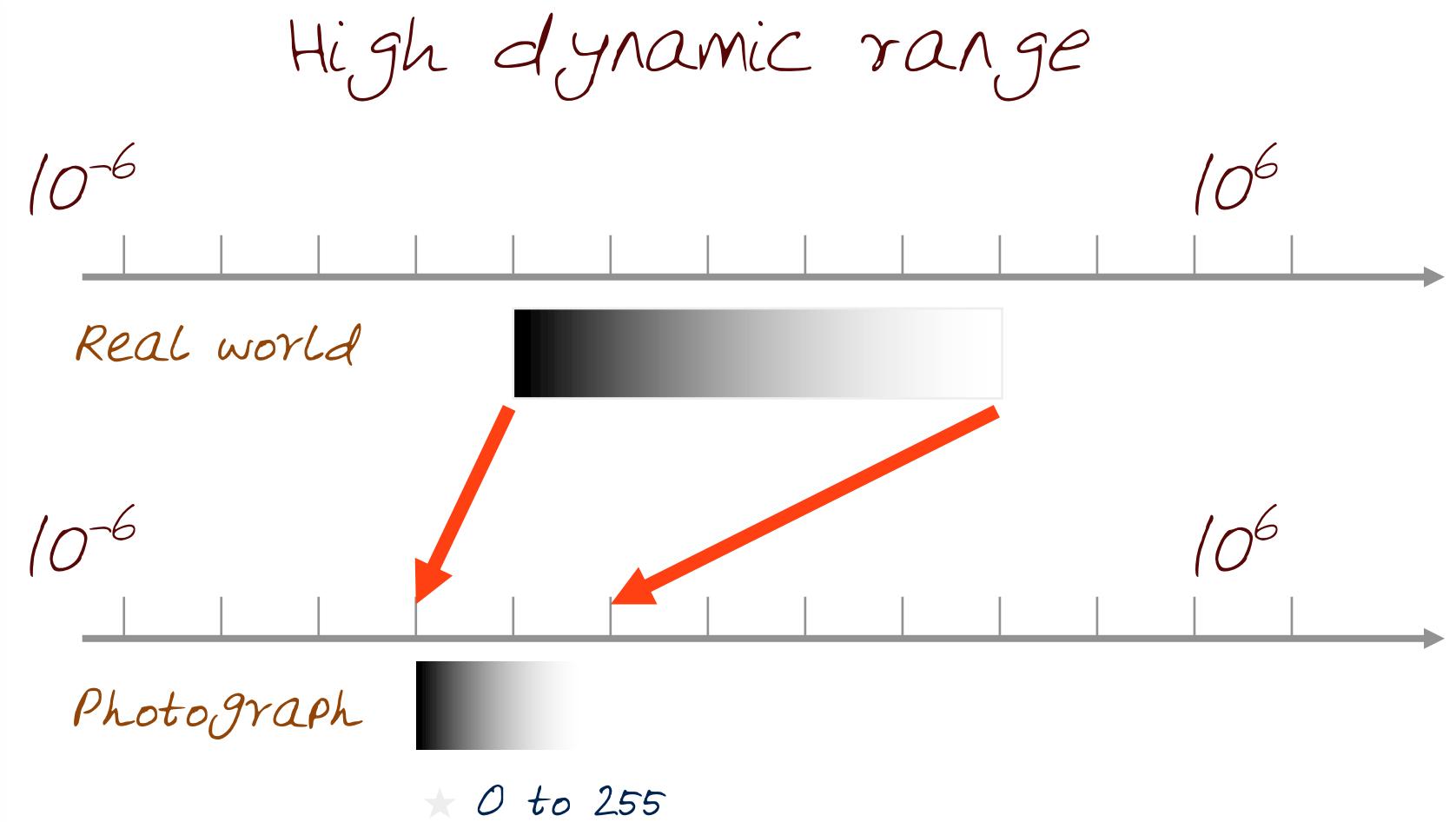


★ [http://commons.wikimedia.org/wiki/File:Kanitz-Kyawsche\\_Gruft\\_in\\_Hainewalde\\_HDR.jpg](http://commons.wikimedia.org/wiki/File:Kanitz-Kyawsche_Gruft_in_Hainewalde_HDR.jpg)

# Tone Mapping

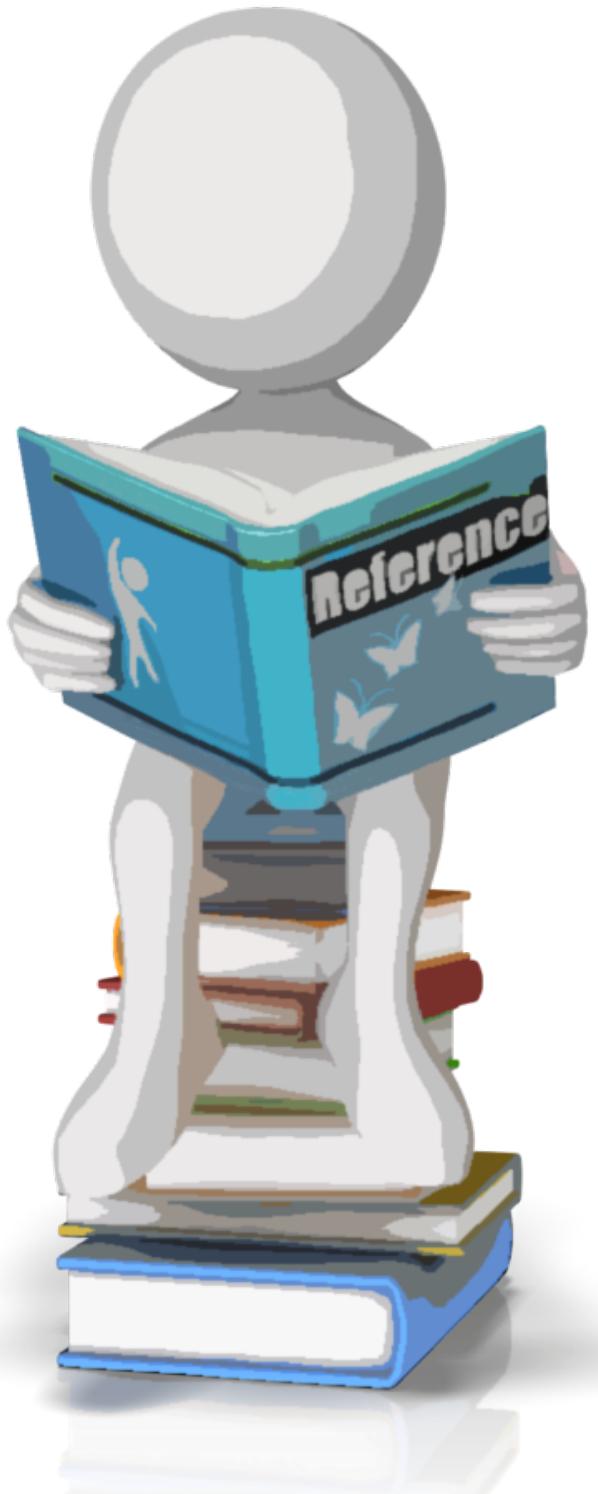


- \*Match limited contrast of the medium
- \*Preserve details



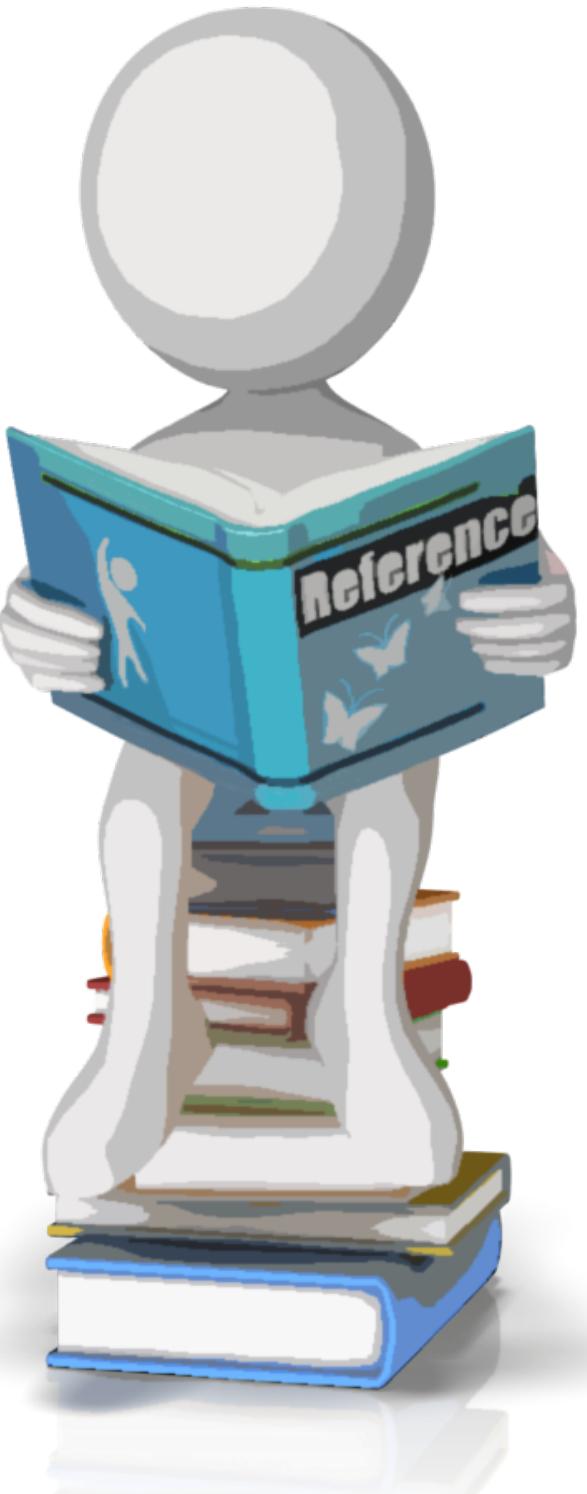
- \*Use filtering approaches to "compress" locally and globally

# Further Information



- \* Grossberg and Nayar (2003), "Determining the Camera Response from Images: What is Knowable?," IEEE Transactions on Pattern Analysis and Machine Intelligence,
- \*Debevec and Malik (1997). "Recovering High Dynamic Range Radiance maps from Photographs." In SIGGRAPH 1997
- \* Ward (2001), "High Dynamic Range Imaging," Proceedings of the Ninth Color Imaging Conference, November 2001.

# Further Information



- \* Durand and Dorsey (2002), "Fast Bilateral Filtering for the Display of High-Dynamic-Range Images" IN SIGGRAPH 2002 .
- \* Reinhard, Stark, Shirley and Ferwerda (2002), "Photographic Tone Reproduction for Digital Images" , IN SIGGRAPH 2002 .
- \* Banterle, Artusi, Debattista, and Chalmers (2011) Advanced High Dynamic Range Imaging CRC Press . (with Matlab Code)
- \* many Software suites on the Internet .
- \* Also, Look for "Exposure Fusion"

# Credits



- \* Softwares used
  - \* matlab by mathwork's INC.
- \* For more information, see
  - \* Richard Szeliski (2010) Computer Vision: Algorithms and Applications, Springer.
- \* Some concepts in slides motivated by similar slides by J. Hays.
- \* Photographs by Irfan Essa