We calculate the GHY boundary term for the flat causal diamond in D dimensions via two limiting procedures. Take standard polar coordinates (t, r, θ) . The tips of the diamond are at $(\pm T, \mathbf{0})$. Consider two ϵ -families of surfaces:

• Timelike lozenges (TL):

$$t^2 - (T - r)^2 + \epsilon^2 = 0$$

• Spacelike lozenges (SL):

$$r^2 - (T - |t|)^2 + \epsilon^2 = 0$$

both approaching the diamond as $\epsilon \to 0$. If we calculate the boundary action associated with these surfaces for non-zero ϵ and take the limit of that expression as $\epsilon \to 0$ we obtain the following results. For the TL family we get

$$S_{GHY} \sim 2V_{D-2}T^{D-2}\left[2(D-2) - \log\left(\frac{2T}{\epsilon}\right)\right]$$

and for the SL family we obtain

$$S_{GHY} \sim \begin{cases} 4\log\left(\frac{2T}{\epsilon}\right) & \text{for } D = 2\\ 2V_{D-2}T^{D-2}\frac{D-1}{D-2} & \text{for } D > 2 \end{cases}$$

where V_n is the volume of the *n*-sphere. So the limits agree for D = 2 but disagree for D > 2. The SL limit gives a finite constant boundary term for D > 2 whereas the TL limit gives a logarithmic divergence in all D.