

# Prompt cusps and the dark matter annihilation signal

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SFB1258 Neutrinos and Dark Matter colloquium

October 2022

# Outline

Dark matter halos

Prompt cusps of the first halos

Dark matter annihilation and indirect detection

Annihilation in prompt cusps

# Outline

**Dark matter halos**

Prompt cusps of the first halos

Dark matter annihilation and indirect detection

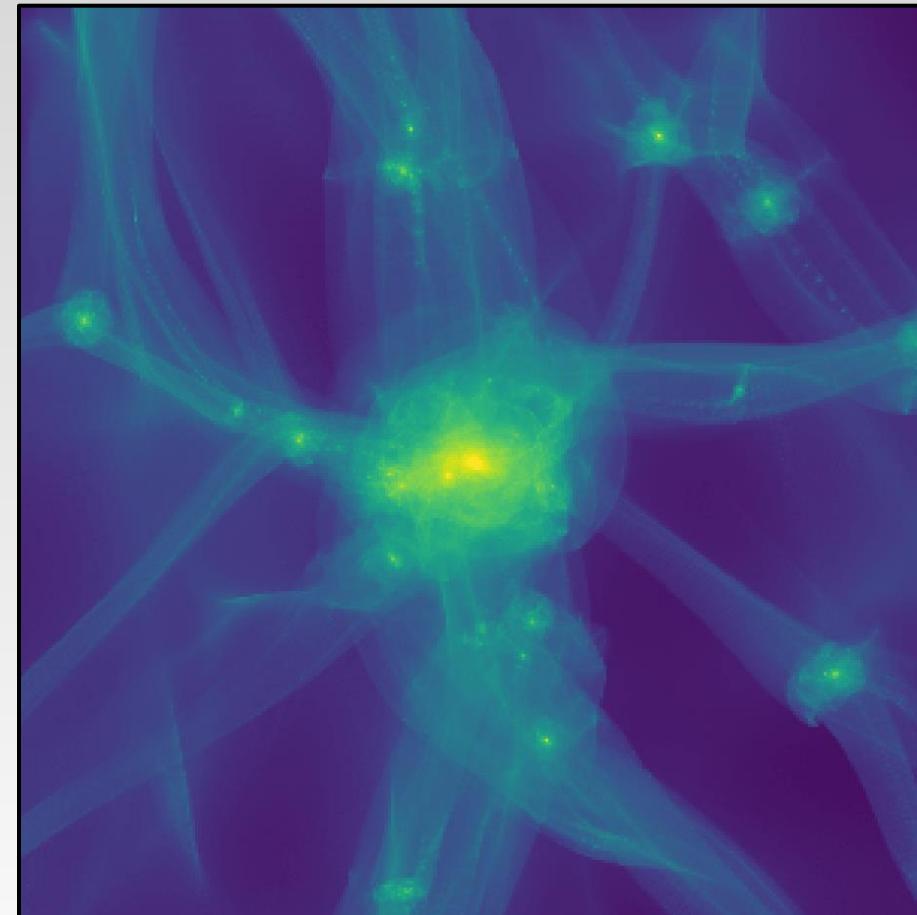
Annihilation in prompt cusps

# Dark matter halos

- There is  $\sim 5$  times more dark matter than baryons
- Dark matter drives gravitational structure formation

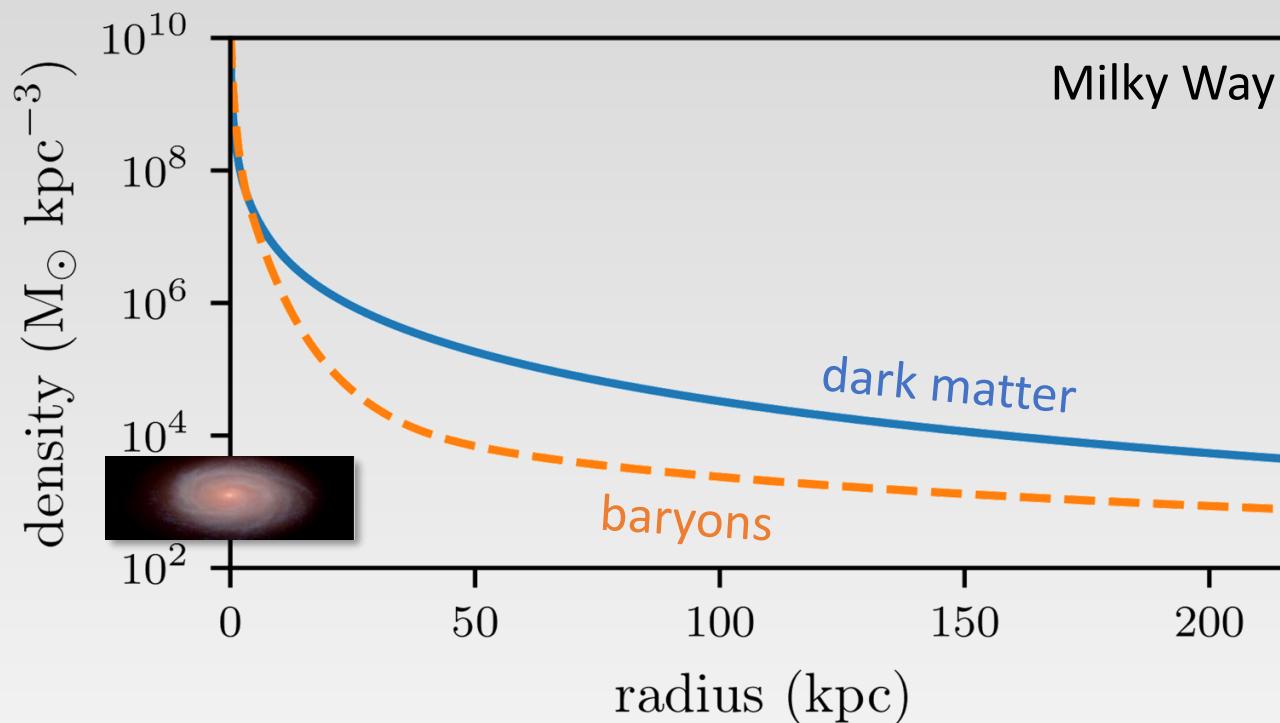
Regions with excess density  
collapse under gravity to form  
**hot clouds of dark matter**

[Unlike visible matter, DM is essentially  
collisionless and cannot cool]



# Dark matter halos

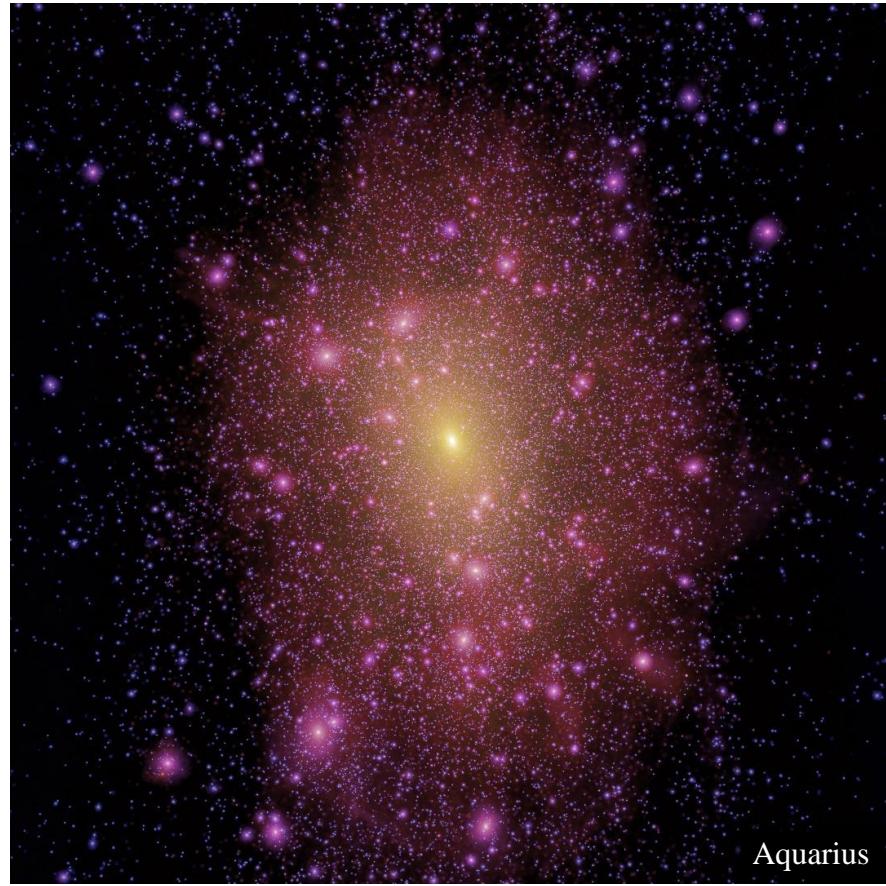
Galaxies form in the centers of these “halos”



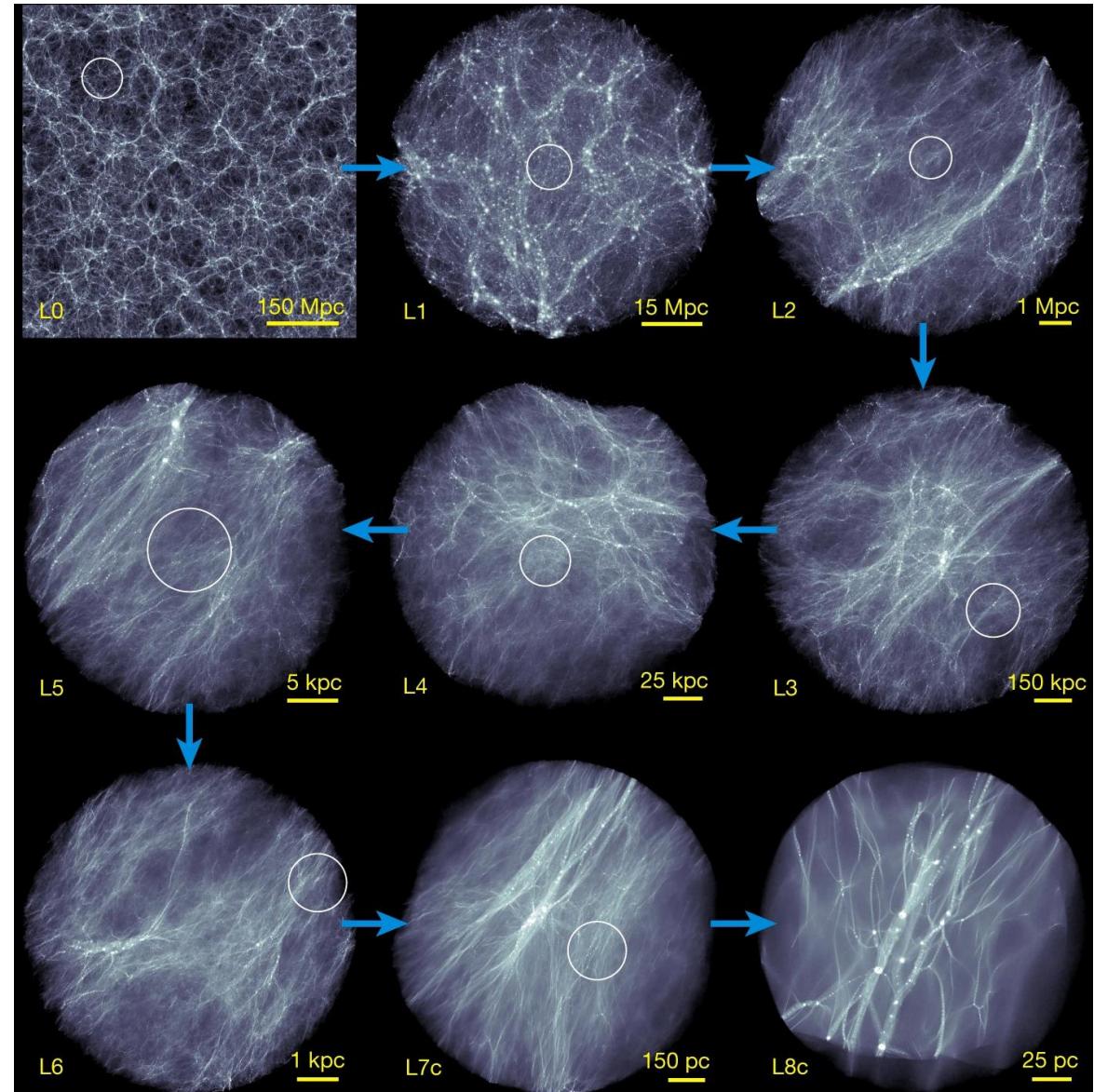
MW mass model: Cautun et al (2020)  
picture of simulated MW-like galaxy: Grand et al (2021)

# Dark matter halos

Subhalos persist inside other halos:



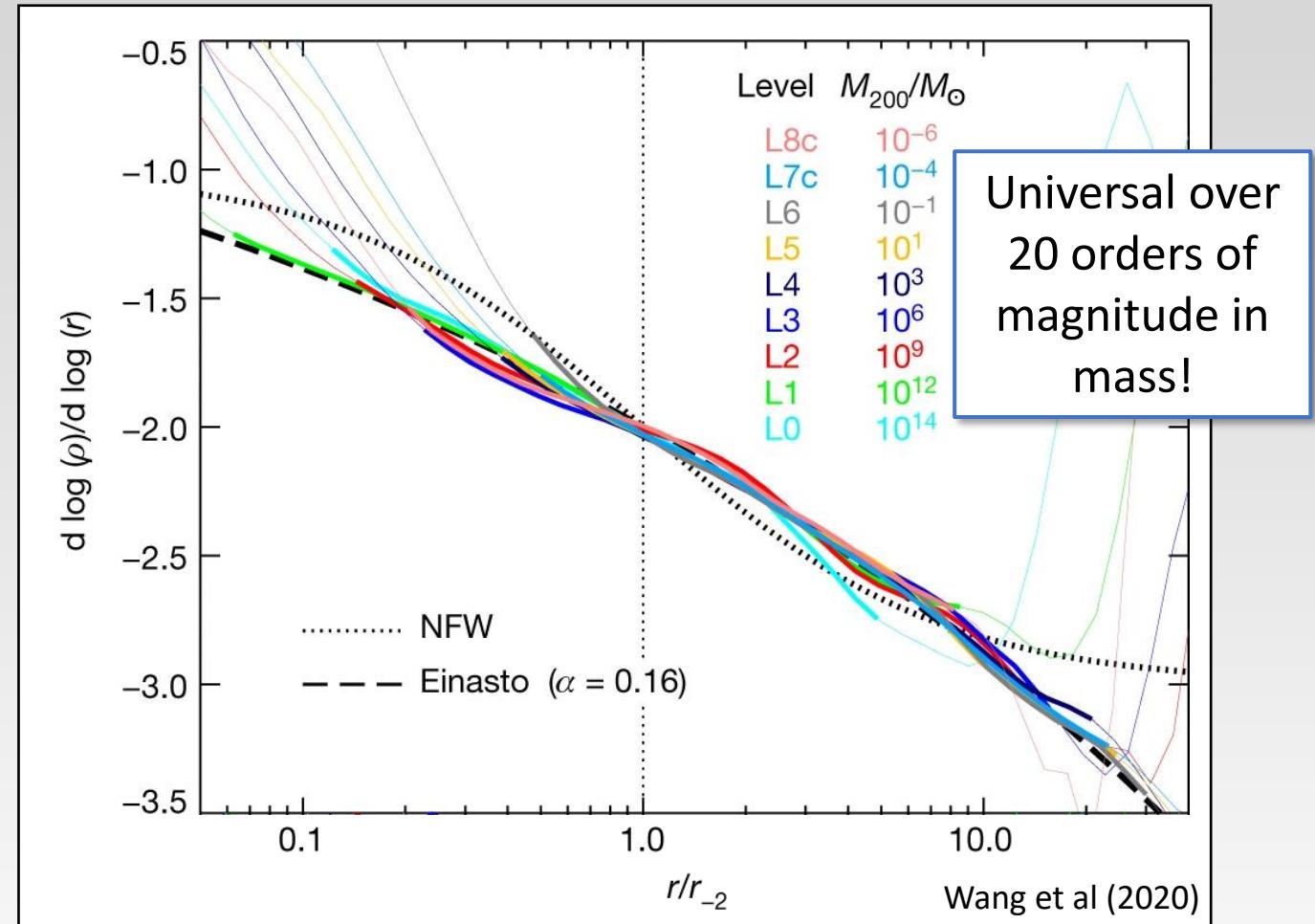
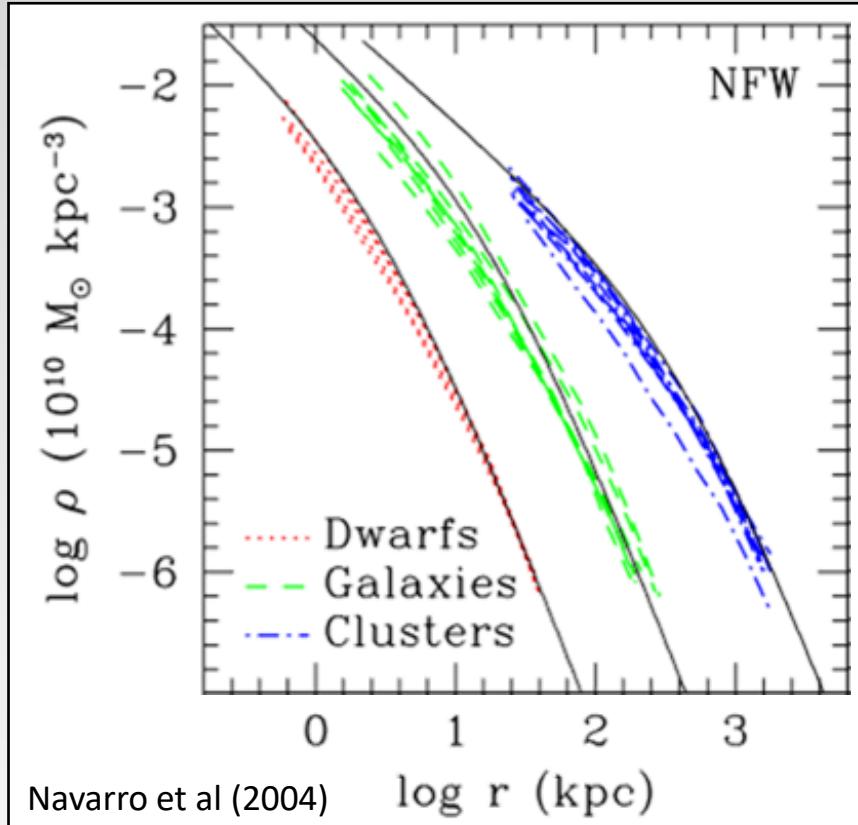
Halos form at all scales:



Wang et al (2020)

# Halo density profiles

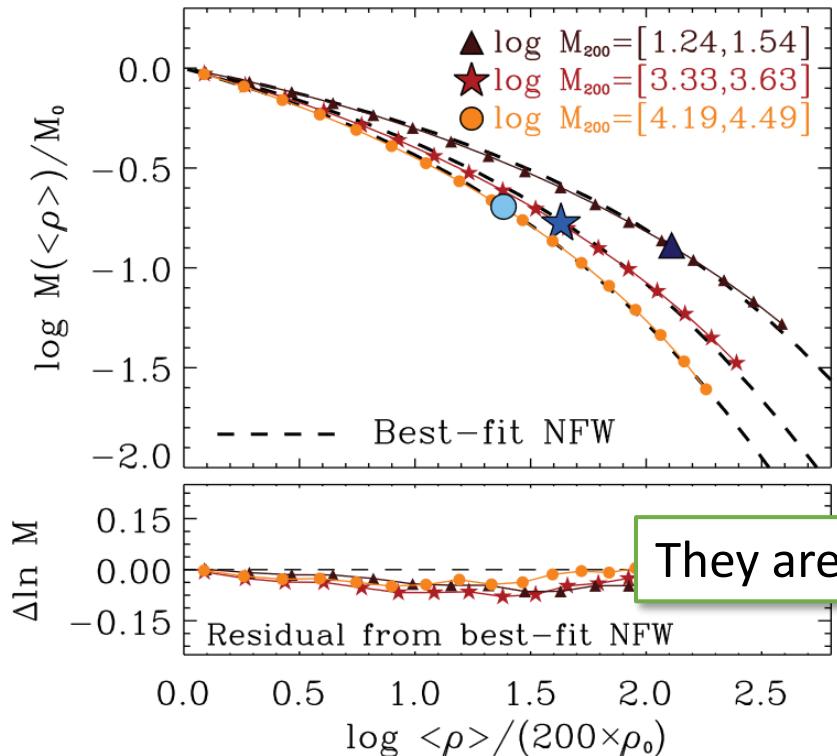
$\rho(r)$ : shallow (logarithmic) decrease at small  $r$ , steep decrease at large  $r$



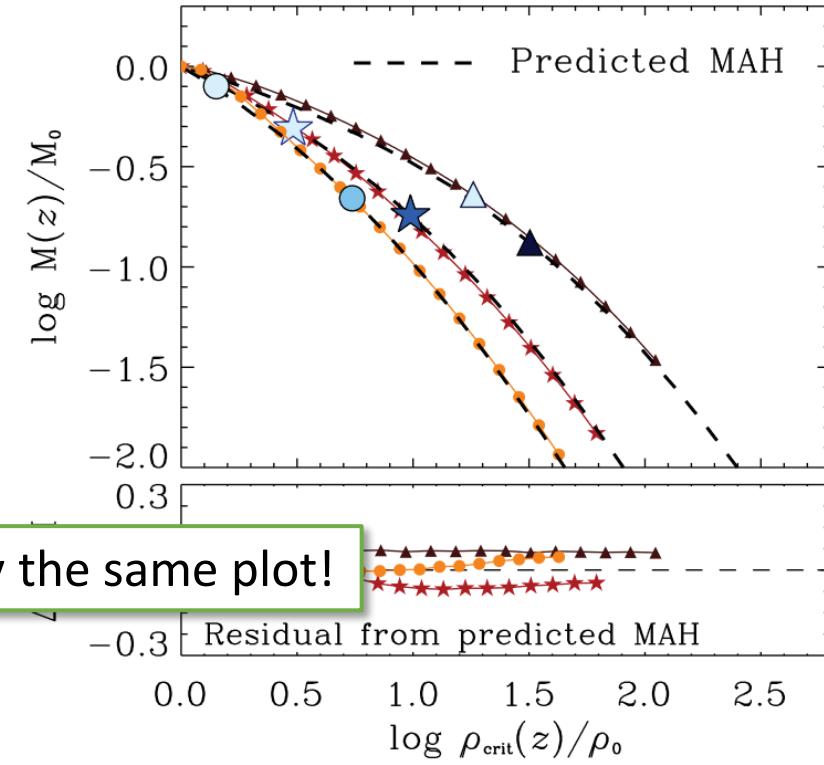
# Density profiles from accretion history

Universal **density profiles** follow from universal **accretion history**

Mass inside regions denser than  $\rho$



Mass accreted when the universe was denser than  $\rho$



They are essentially the same plot!

# Outline

Dark matter halos

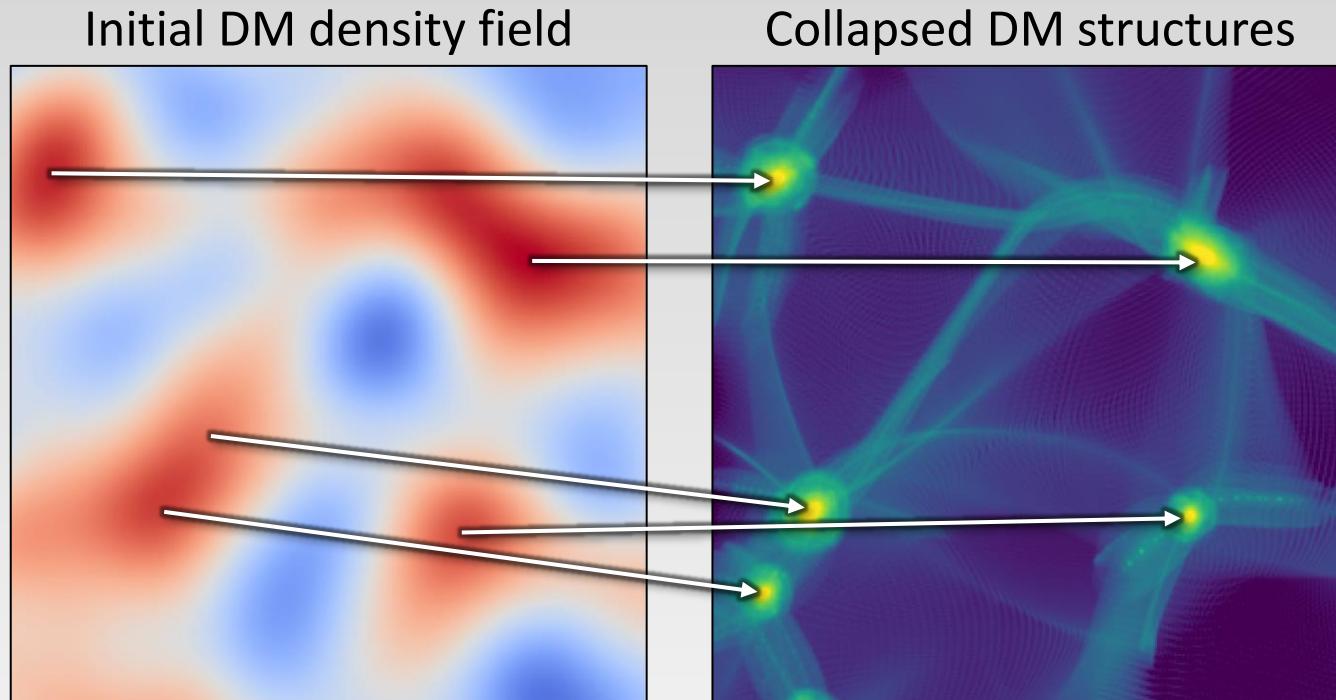
**Prompt cusps of the first halos**

Dark matter annihilation and indirect detection

Annihilation in prompt cusps

# The first halos

The first dark matter halos form from density peaks.

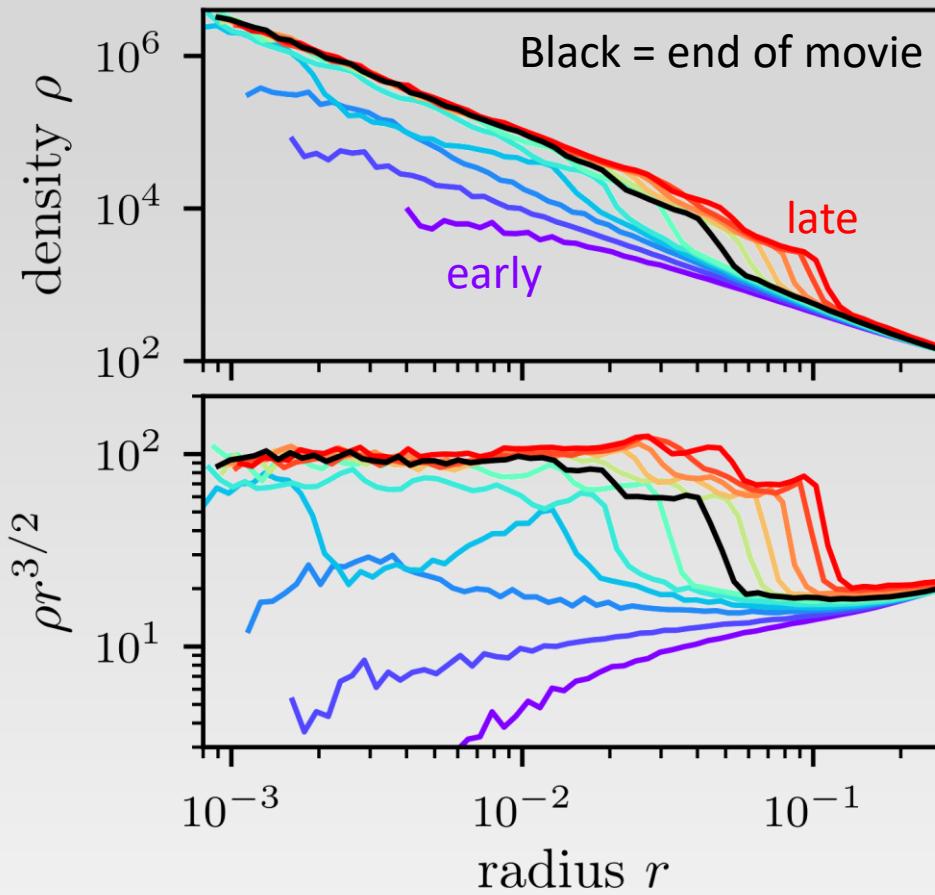


(smoothed by thermal motion)

Normally not resolved in simulations [ $\sim$ earth mass]

$t/t_c = 1.19$ 

# Prompt cusps

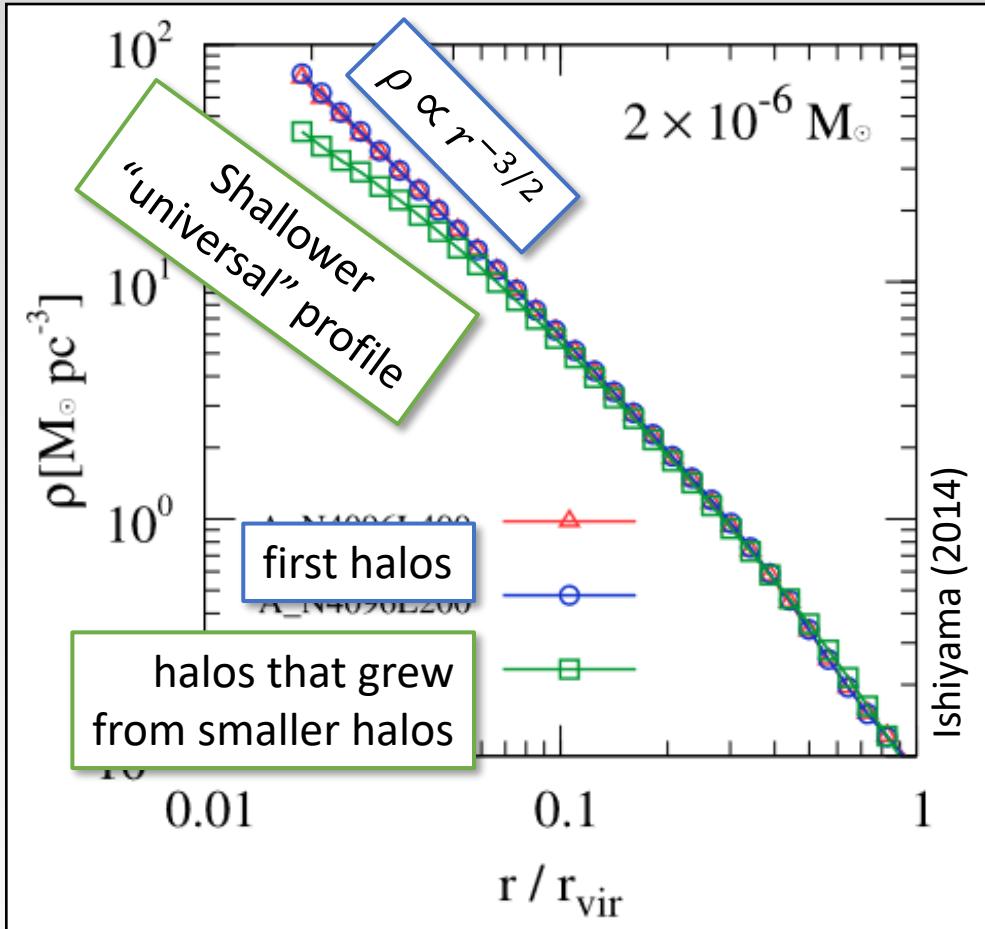


$\rho \propto r^{-3/2}$  cusp stabilizes  
immediately after formation

"prompt"

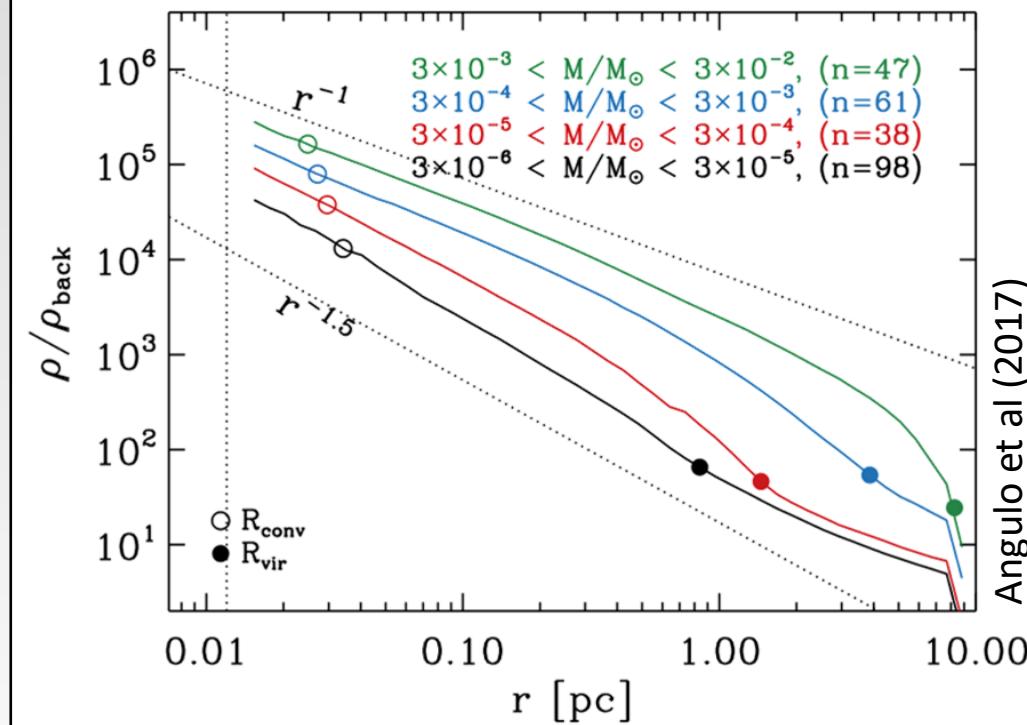
# Do prompt cusps survive?

$\rho \propto r^{-3/2}$  cusps have been seen in simulations before...



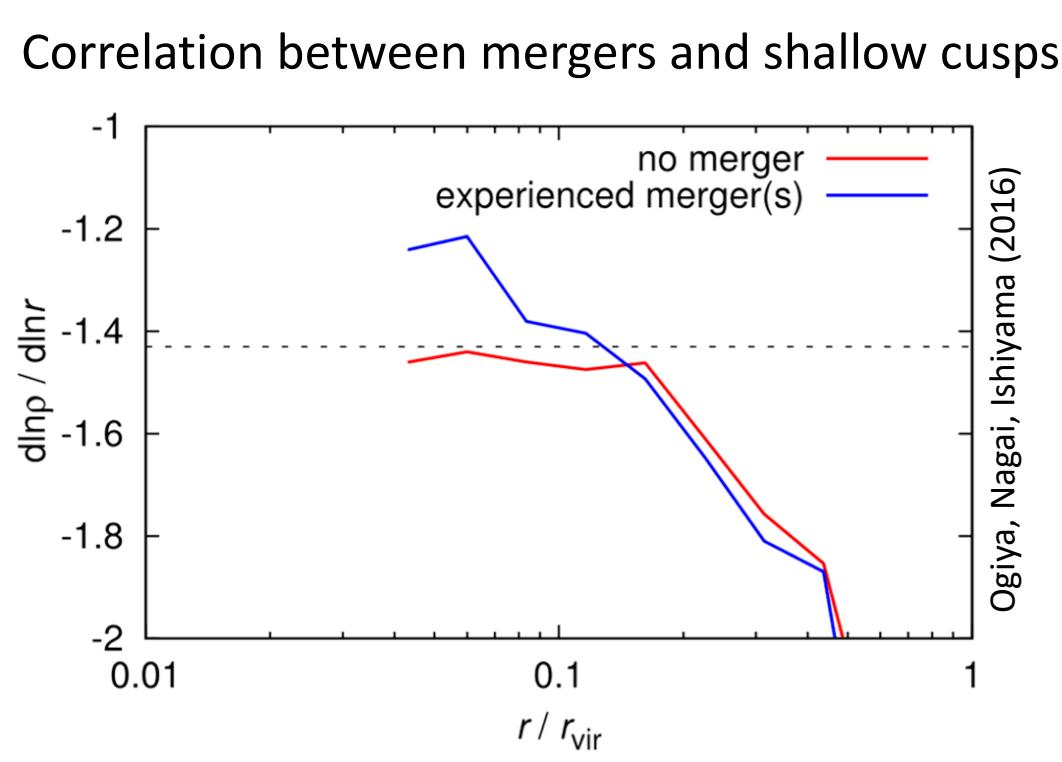
...but their survival was questioned

Halos converge to “universal” density profile as they grow?

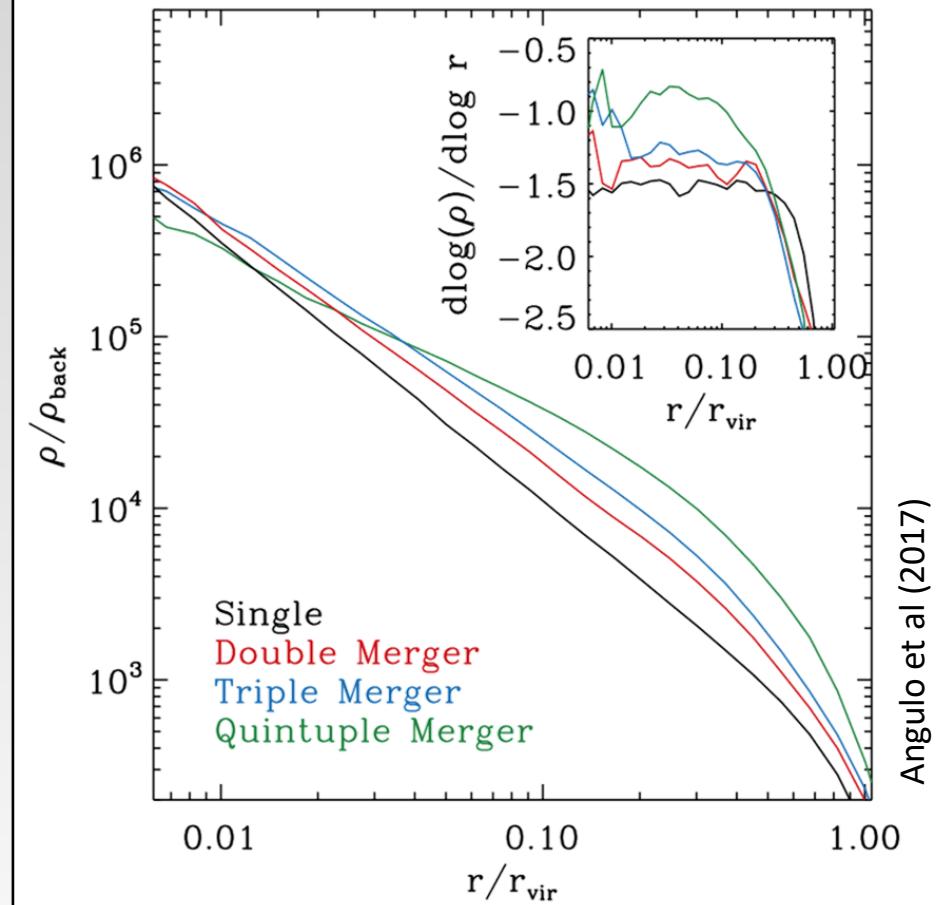


# Cusps shallow due to mergers?

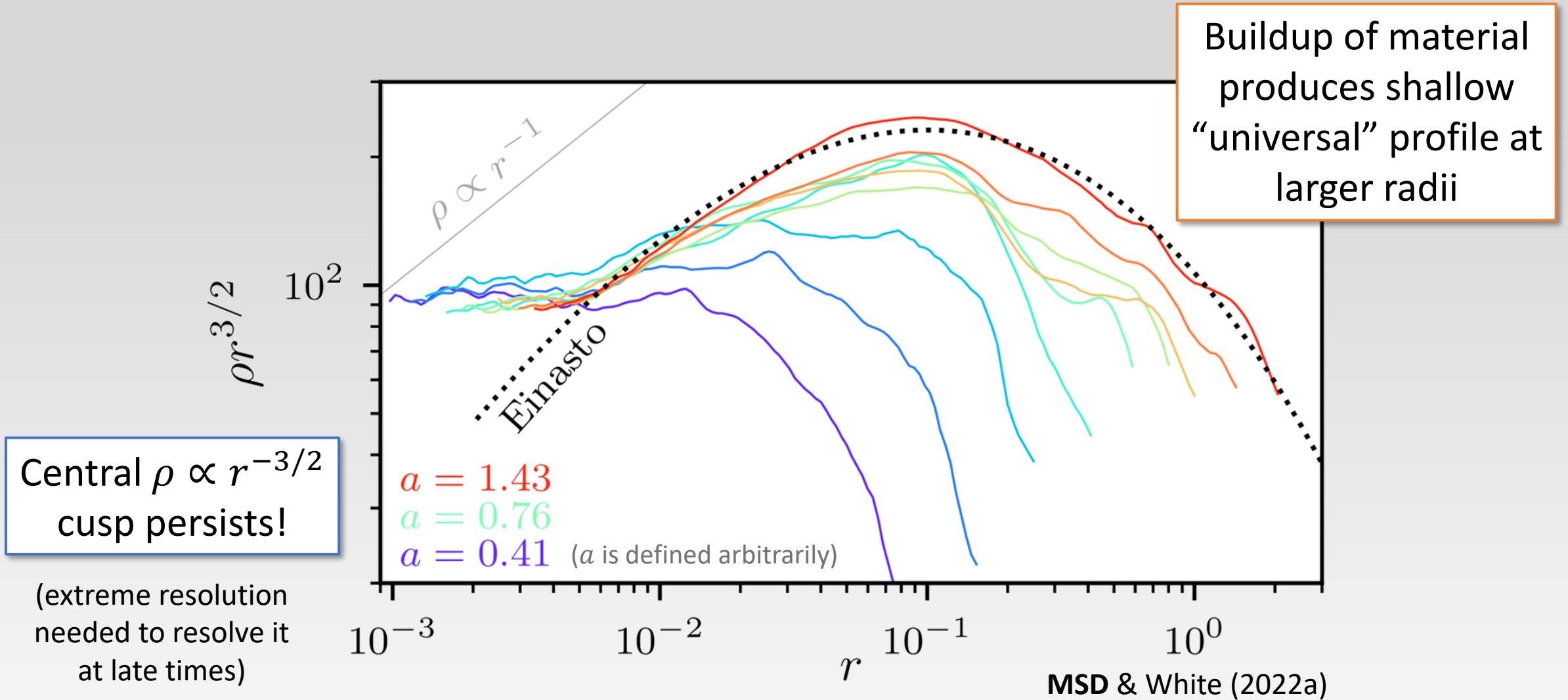
The common view was that  
mergers disrupt steep cusps



Shallowing in idealized merger simulations



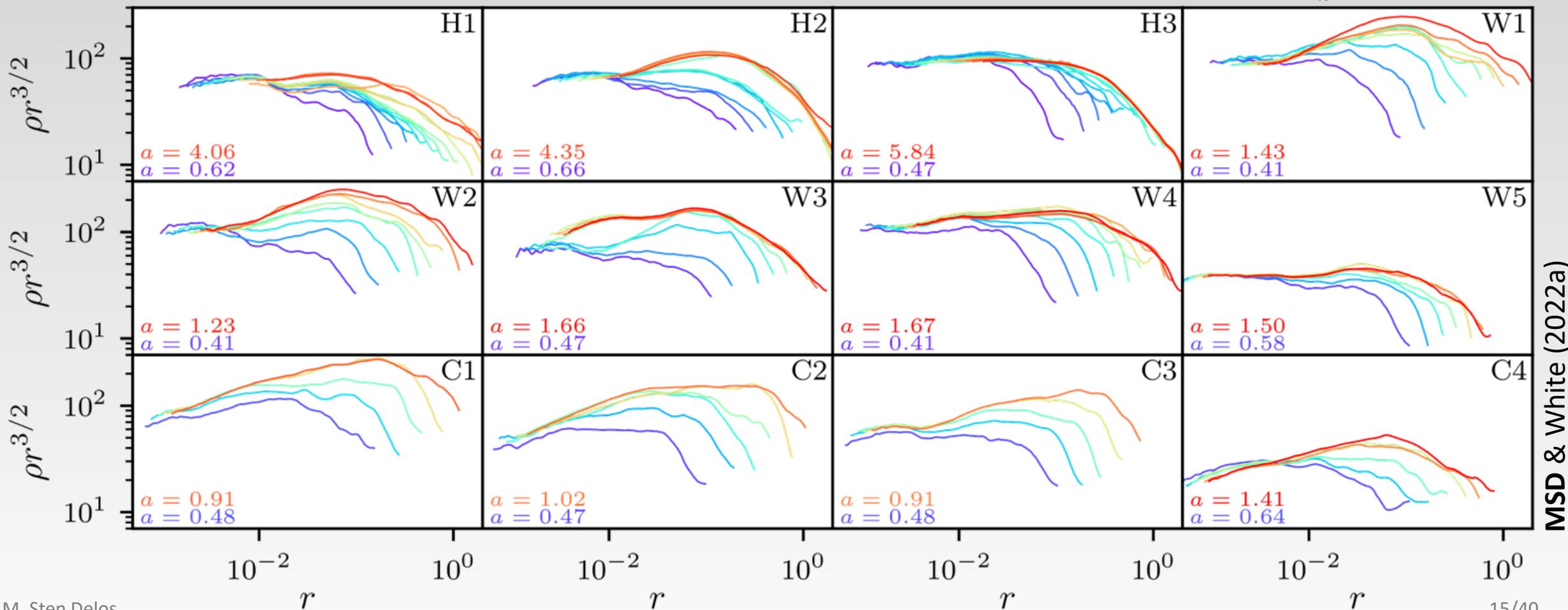
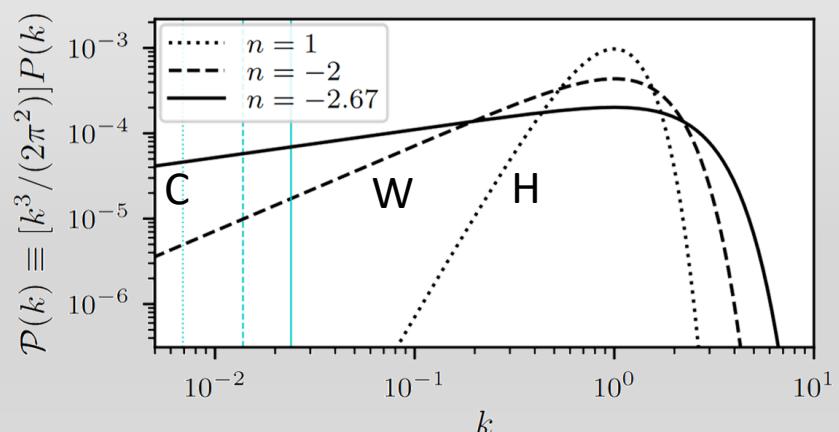
# Prompt cusp persistence



Outcome: standard DM density profile + prompt cusp

# Prompt cusps: broader picture

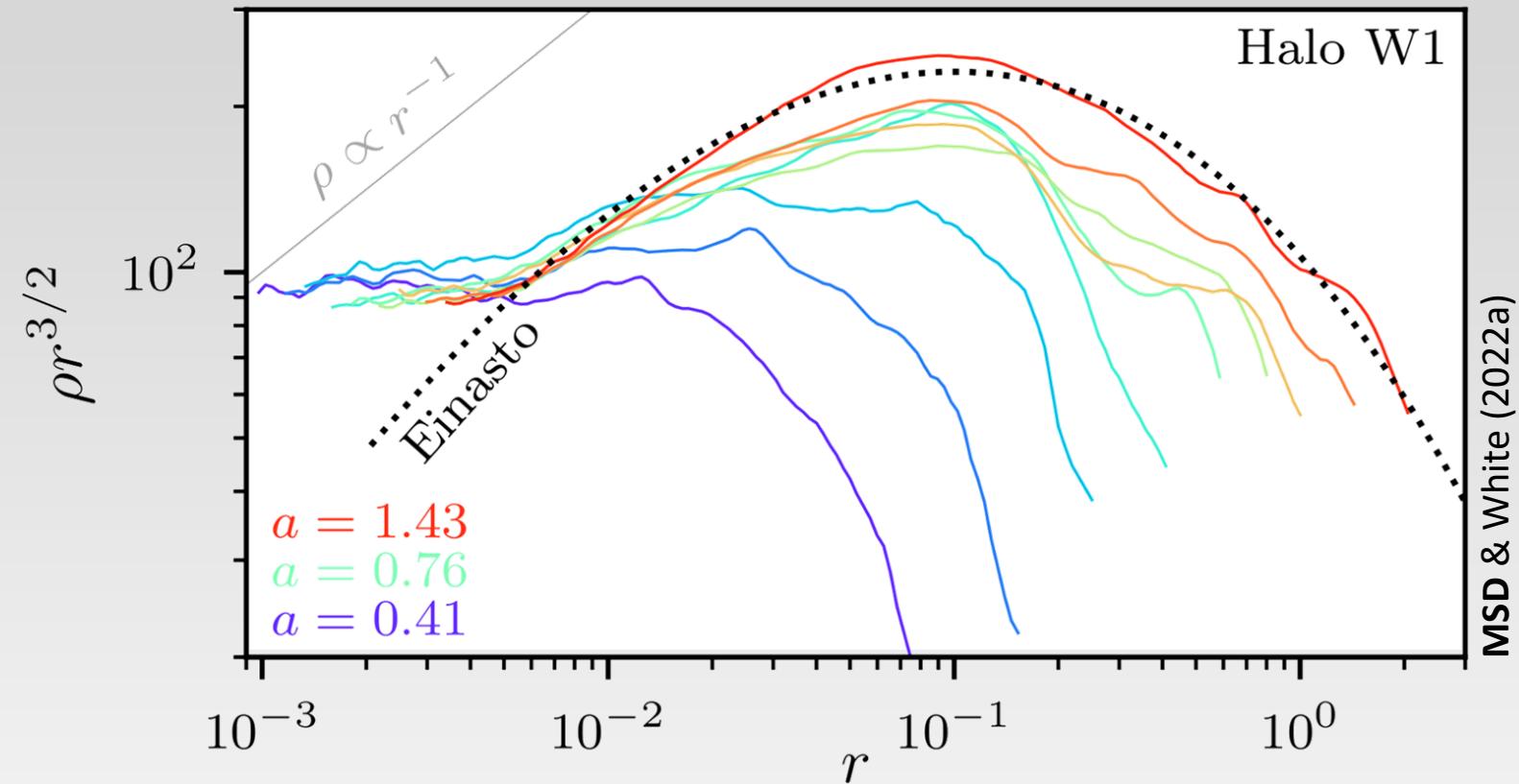
Twelve high-resolution halos from three cosmologies:  
Prompt cusp forms at collapse; no evidence for disruption



# Prompt cusp persistence is natural

Most new material has  
too much energy and  
angular momentum to  
sink to the center

Only major mergers  
can deposit material  
into the center, but  
impact is minor

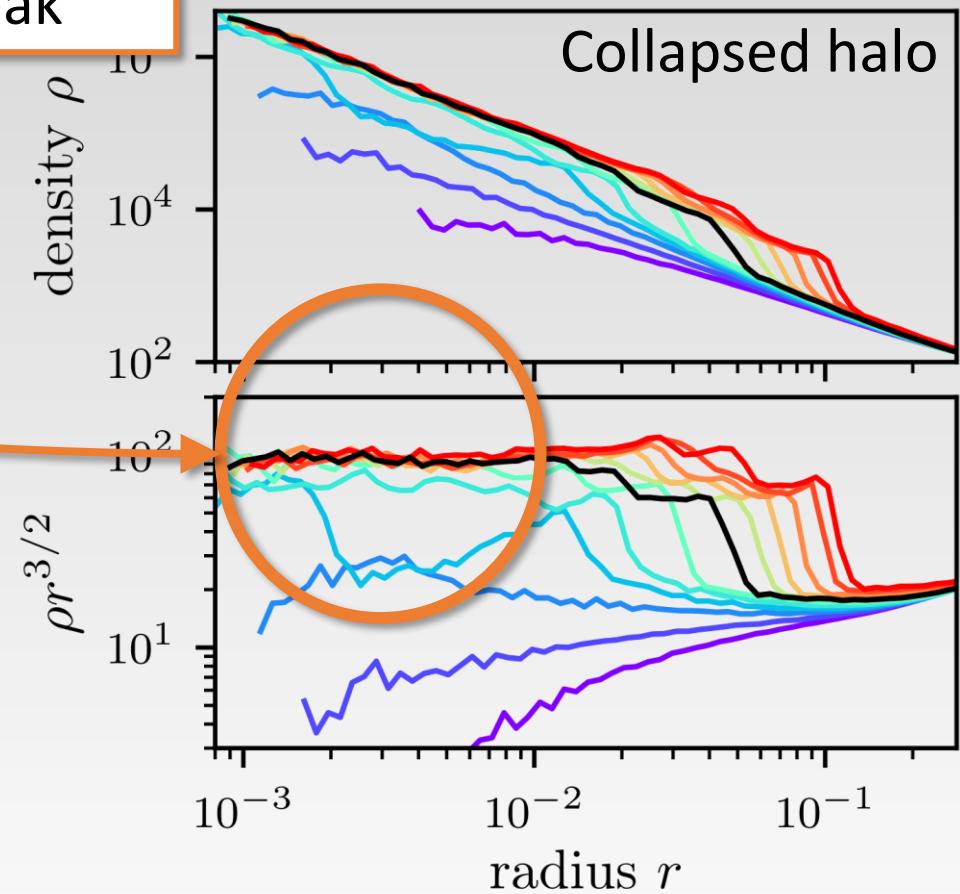
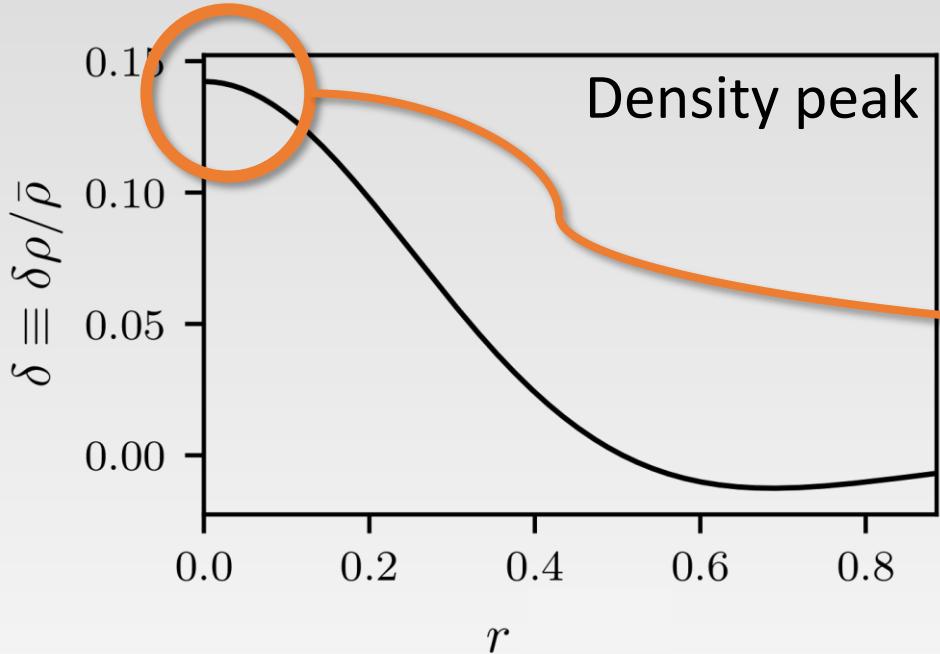


Consequence: every (sub)halo has a central prompt cusp!

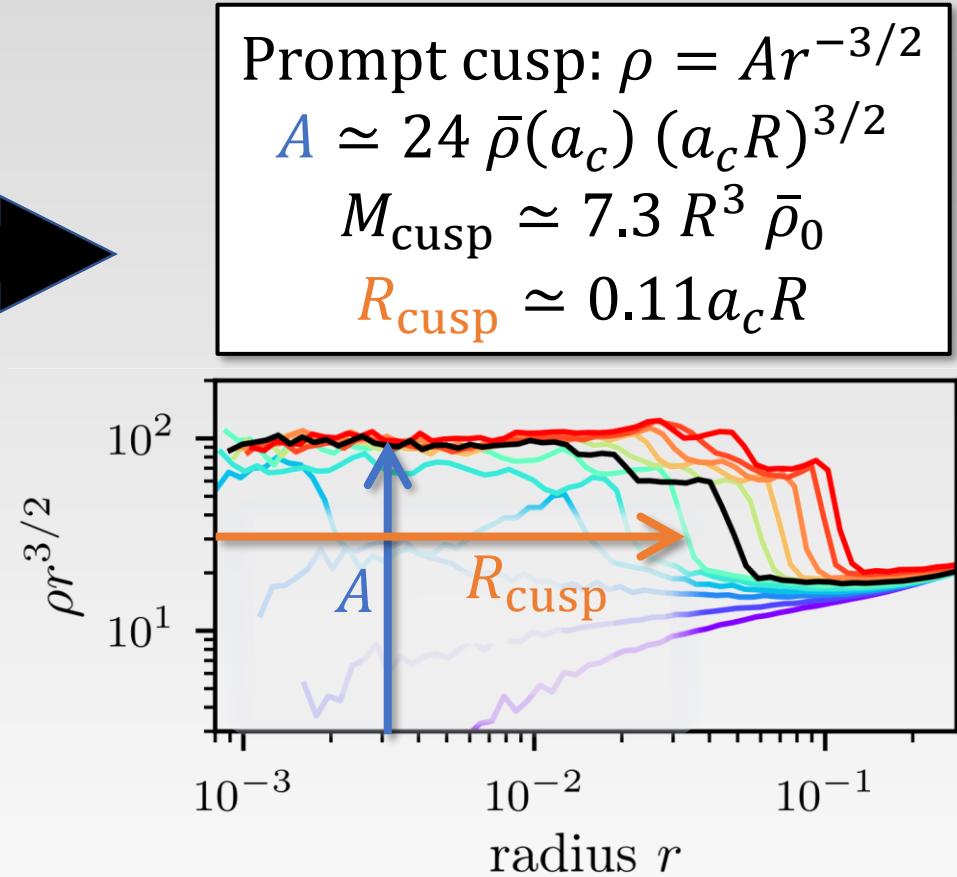
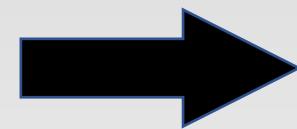
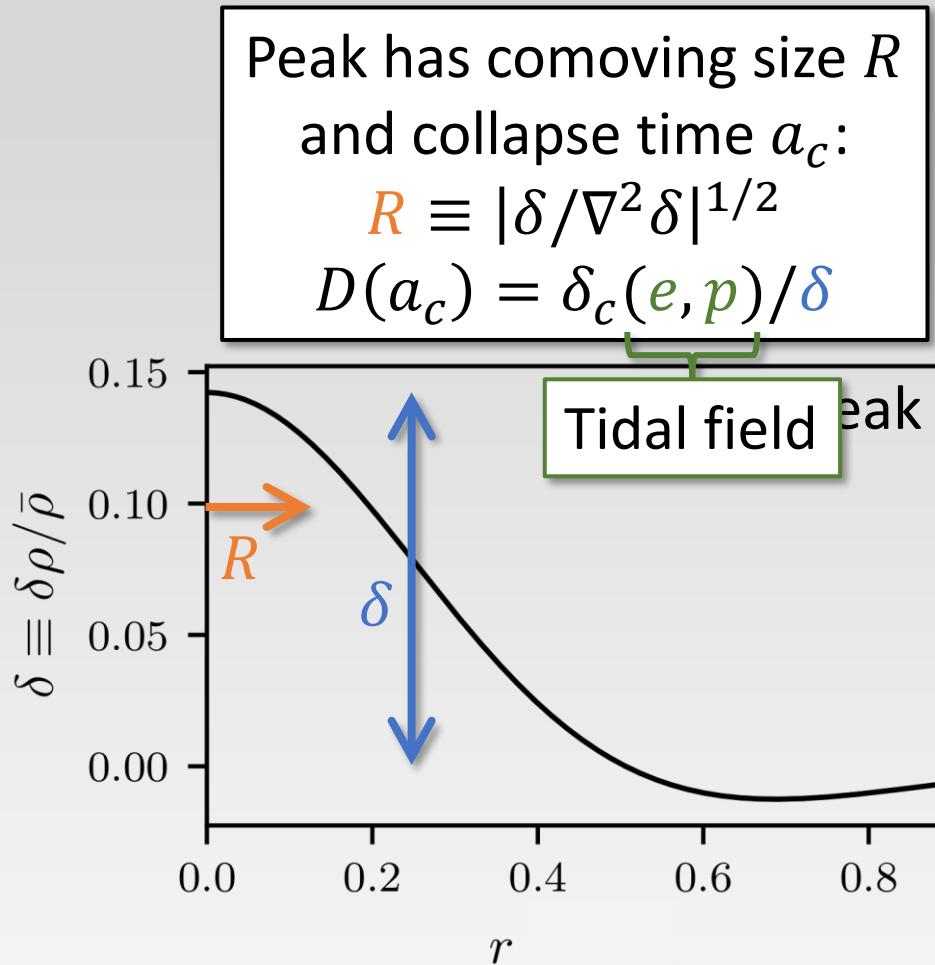
# What sets prompt cusp properties?

## Cusp set at formation time

∴ only sensitive to neighborhood of density peak  
i.e.,  $\delta \equiv \delta\rho/\bar{\rho}$ ,  $\nabla^2\delta$ , and tidal field at peak

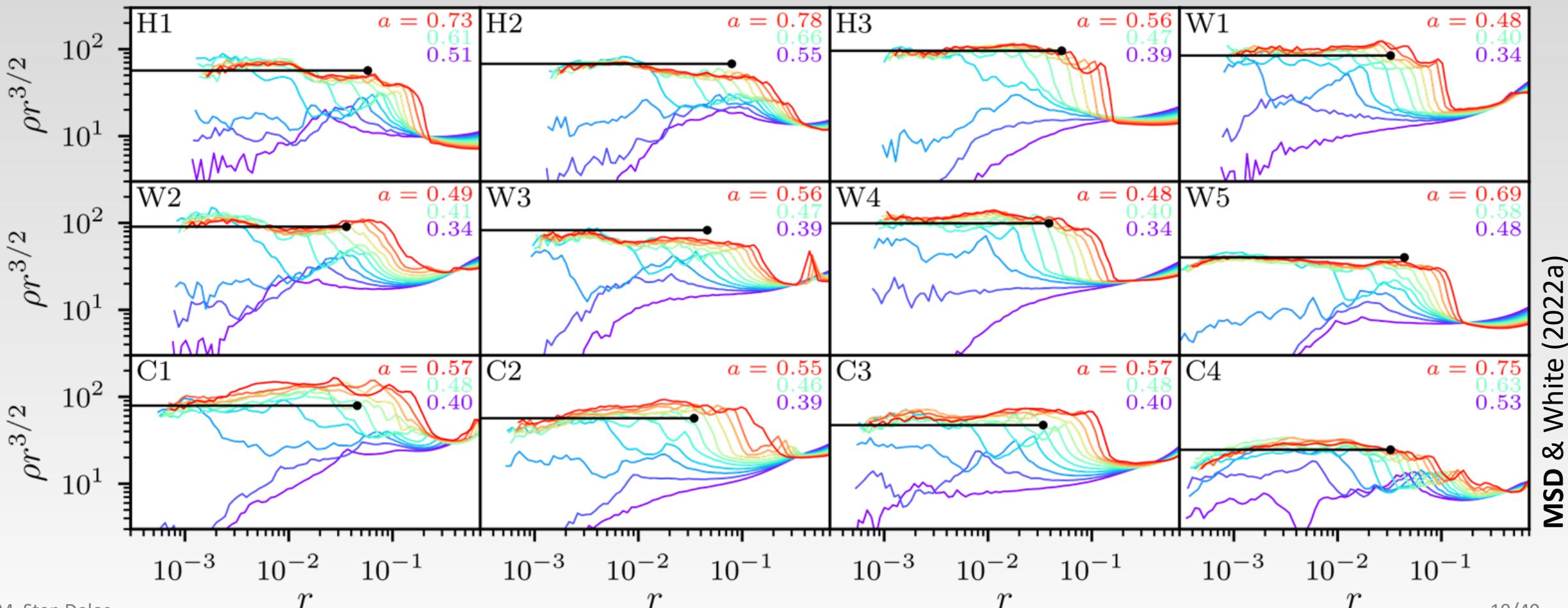


# What sets prompt cusp properties?



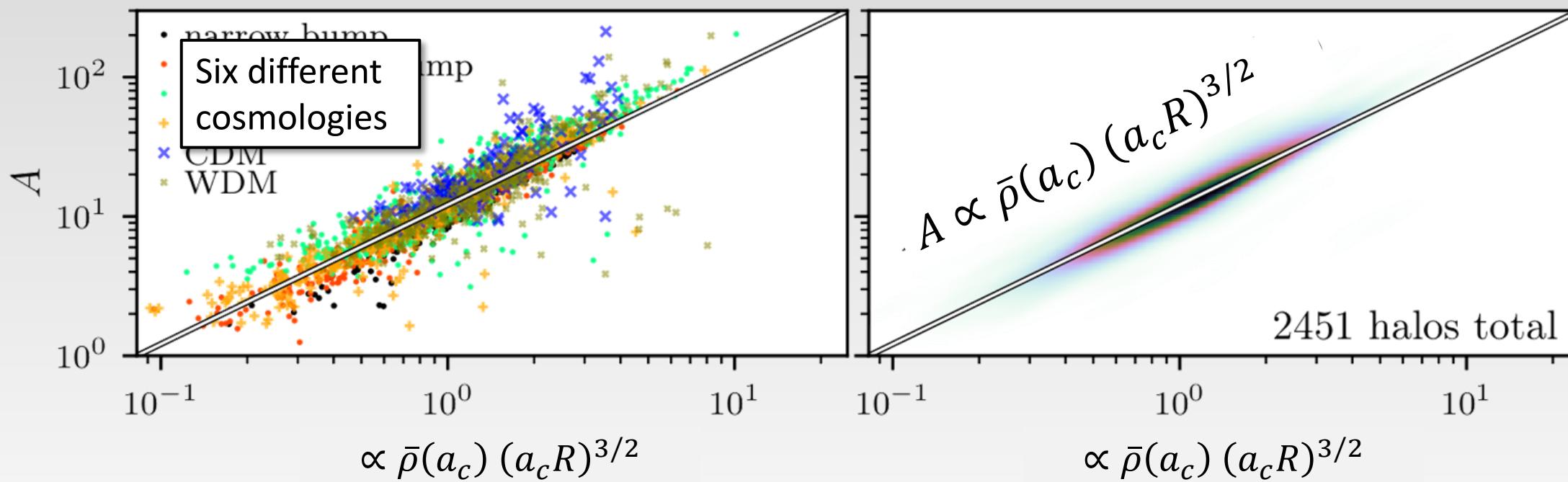
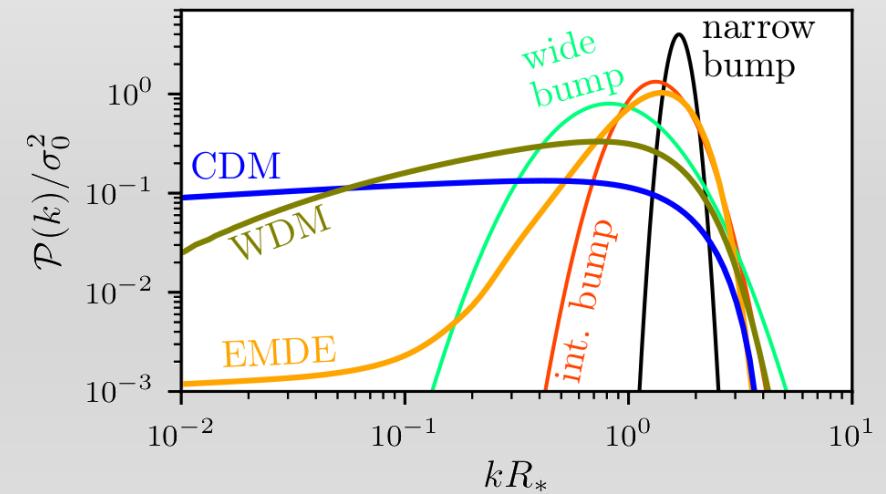
# Cusp properties from peaks

Twelve high-resolution halos from three cosmologies:  
**Predictions [black] work well!**



# Cusp properties from peaks

Prediction for  $A = \rho r^{3/2}$  also validated  
using a much larger halo sample



MSD, Bruff, Erickcek (2019)

# Statistics of peaks

Connection between cusps  
and peaks is clear.

What is the distribution of peaks?

## THE STATISTICS OF PEAKS OF GAUSSIAN RANDOM FIELDS

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Physics Department, University of Washington

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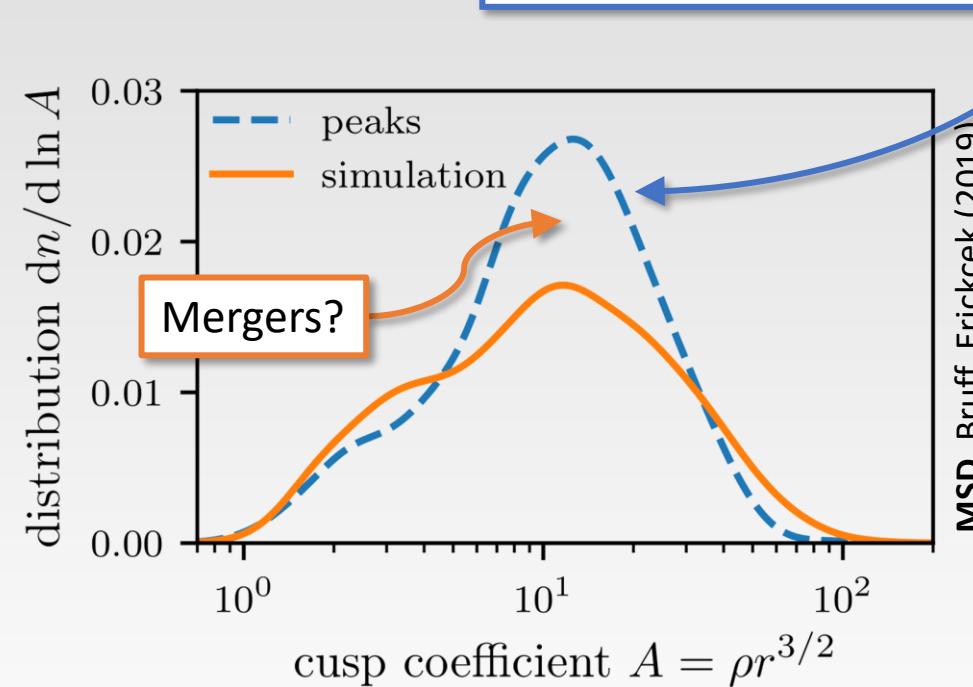
Astronomy Department, University of California at Berkeley, and Institute of Astronomy, Cambridge University

AND

A. S. SZALAY<sup>1</sup>

Astrophysics Group, Fermilab

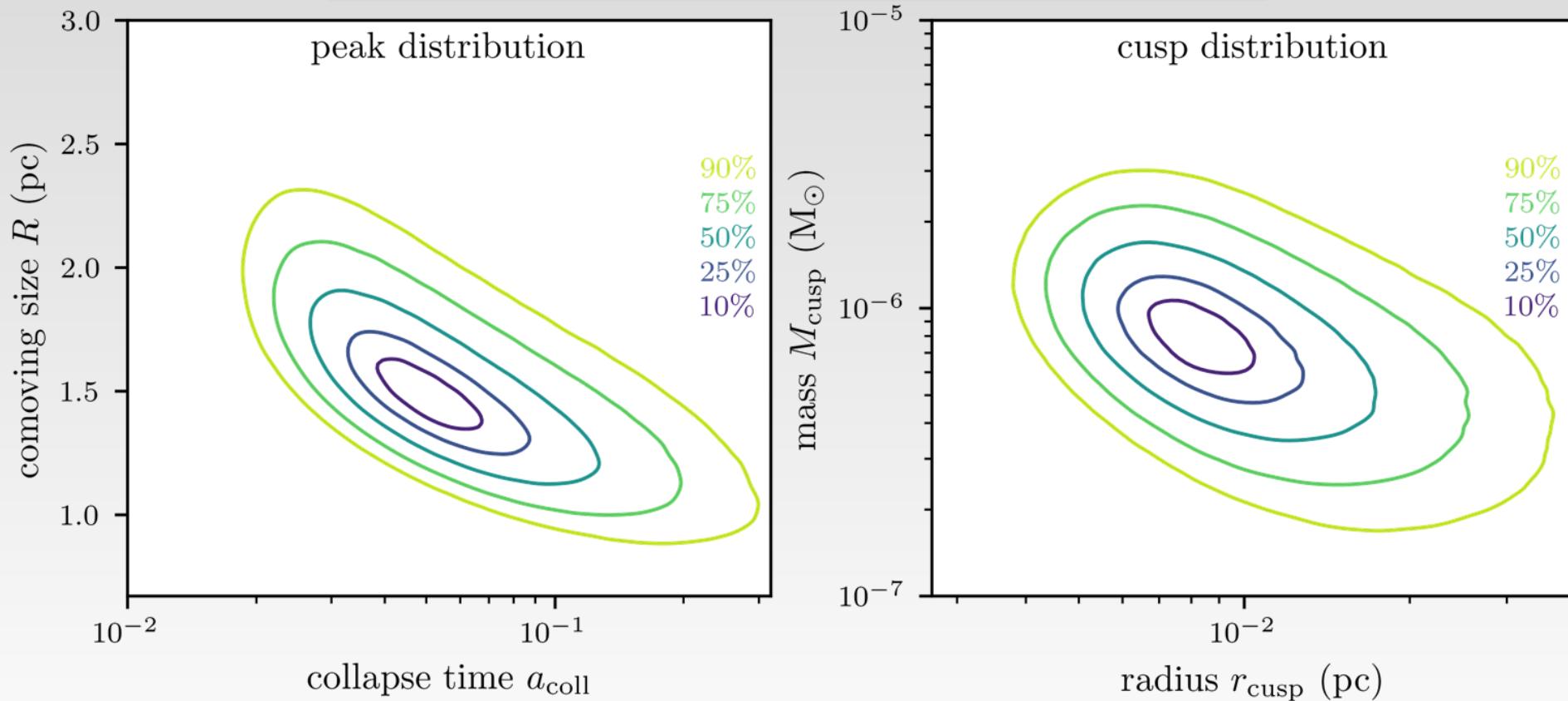
Received 1985 July 25; accepted 1985 October 9



# Statistics of prompt cusps

Example: standard 100 GeV WIMP

average peak/cusp number density  $\simeq 10^{-3} \text{ pc}^{-3}$   
 $\sim 40000 M_{\odot}^{-1}$



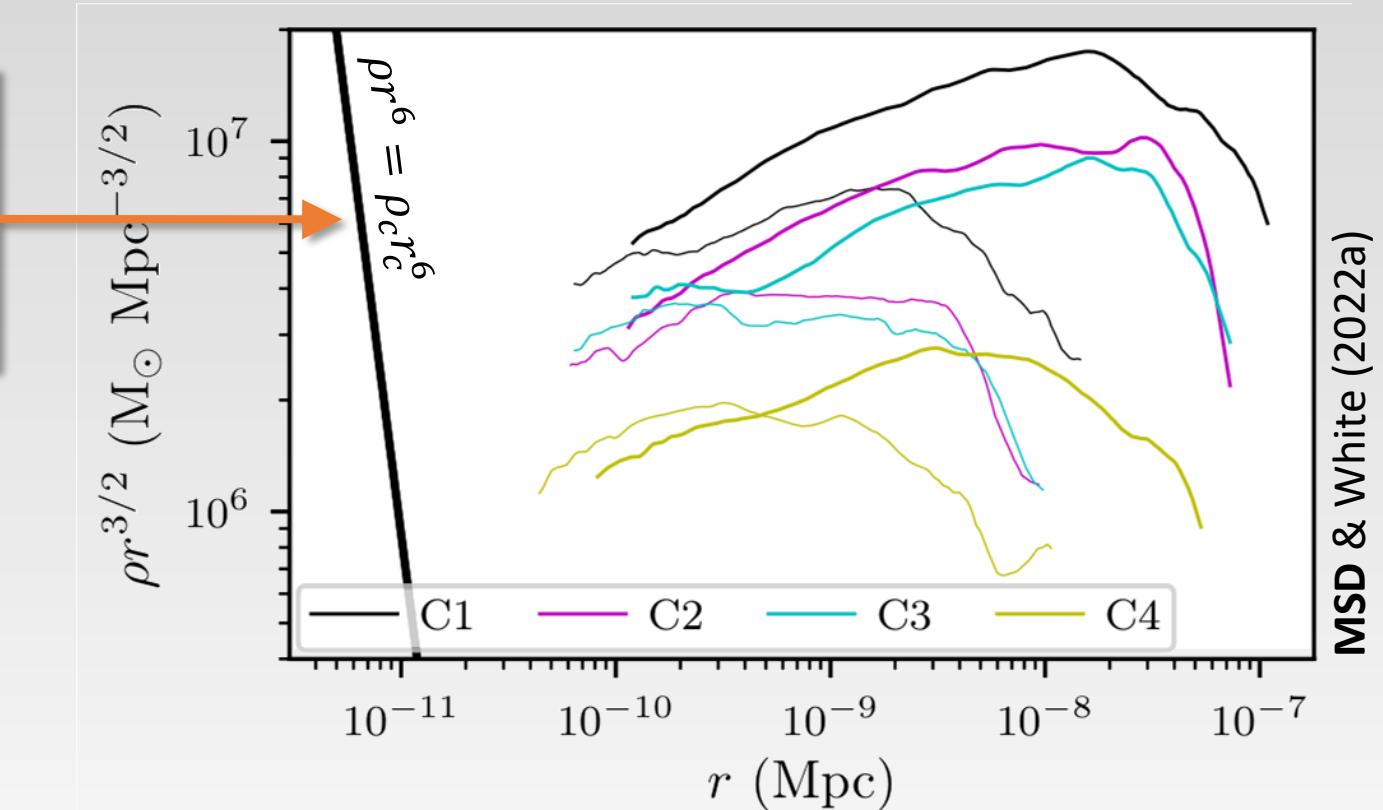
# Central cores

Any density cusp must give way to a **finite-density core** at small radii  
due to phase-space conservation

Core radius  $r_c$  and density  $\rho_c$

$$\rho_c r_c^6 \simeq 3 \times 10^{-5} G^{-3} f_{\max}^{-2}$$

$f_{\max}$  = phase-space density  
of the early universe  
 $\sim \bar{\rho}(a)\sigma(a)^{-3}$



$\rho \propto r^{-3/2}$  cusps cover a factor of  $R_{\text{cusp}}/r_c \sim 500$  in radius

# Outline

Dark matter halos

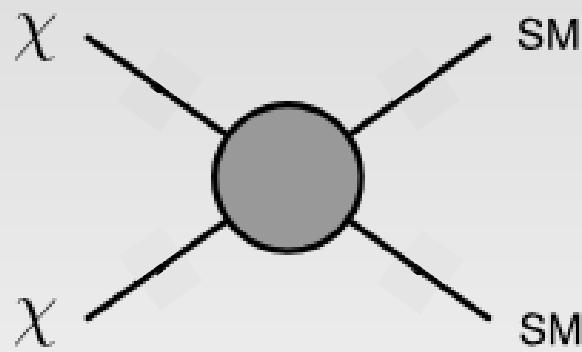
Prompt cusps of the first halos

**Dark matter annihilation and indirect detection**

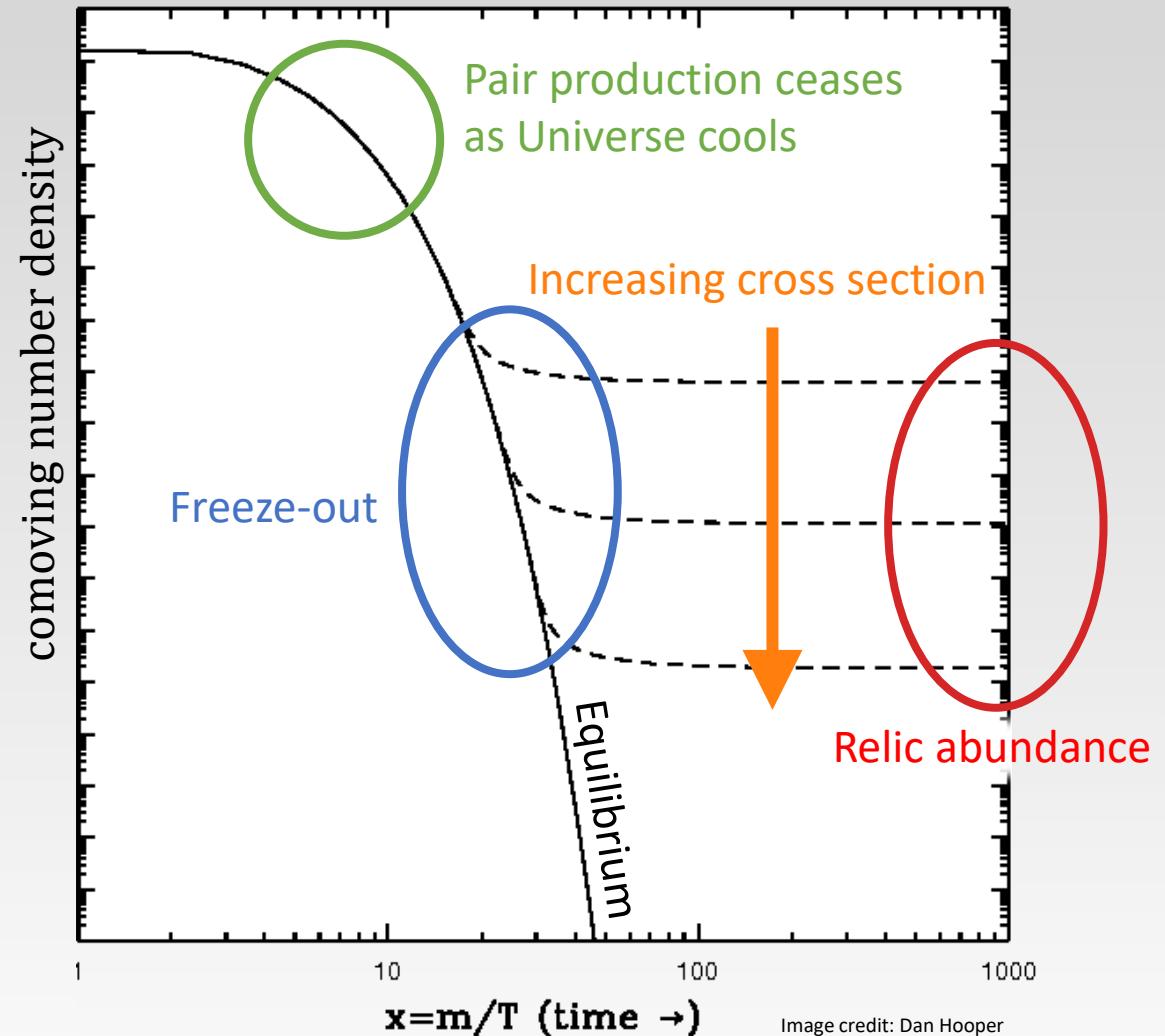
Annihilation in prompt cusps

# What is dark matter?

Well motivated possibility:  
**thermal relic** dark matter particle  $\chi$ ,  
pair-produced in the early universe.

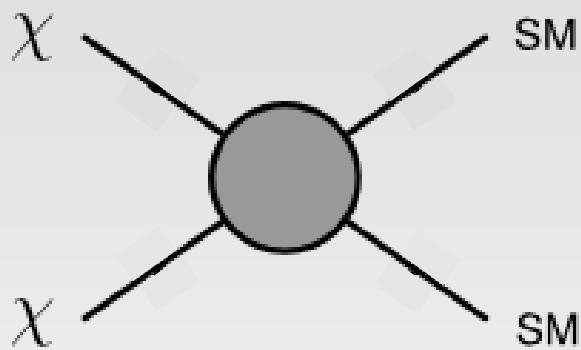


Thermal relic cross section:  
 $\langle \sigma v \rangle \simeq 3 \times 10^{-26} \text{ cm}^3/\text{s}$



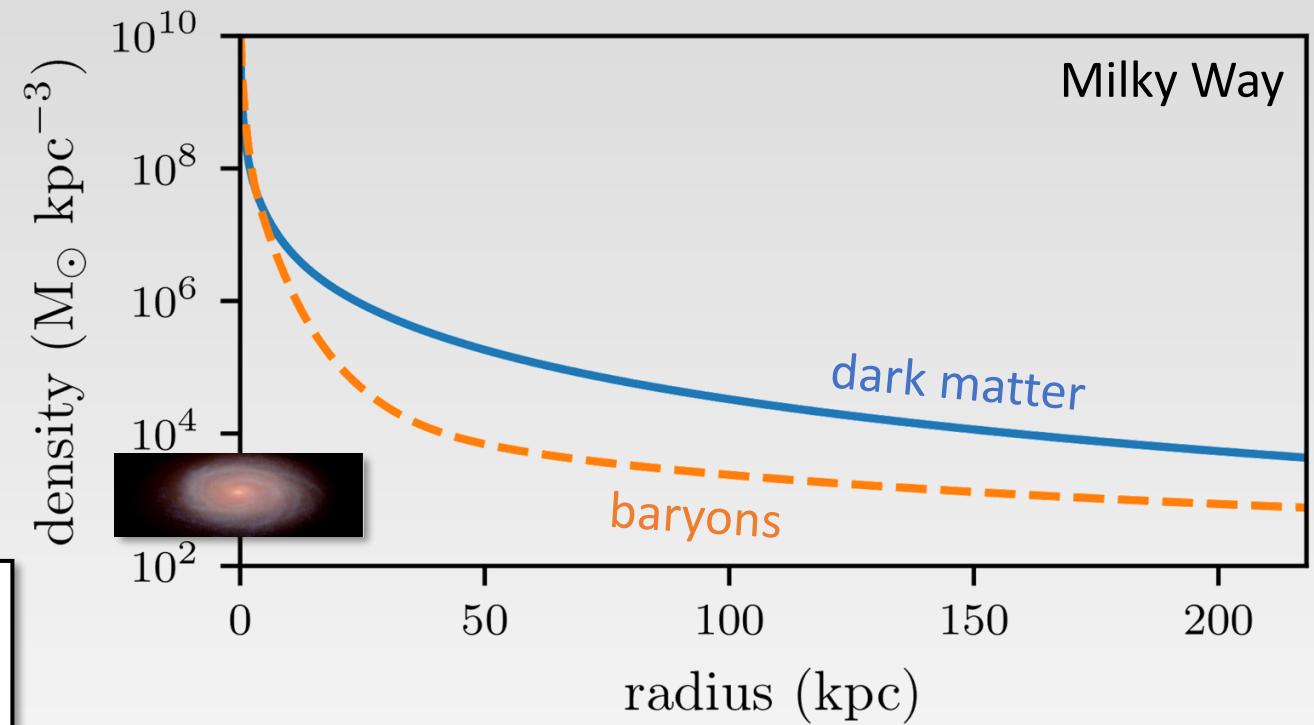
# Indirect detection

Then dark matter can annihilate  
into detectable SM particles today!

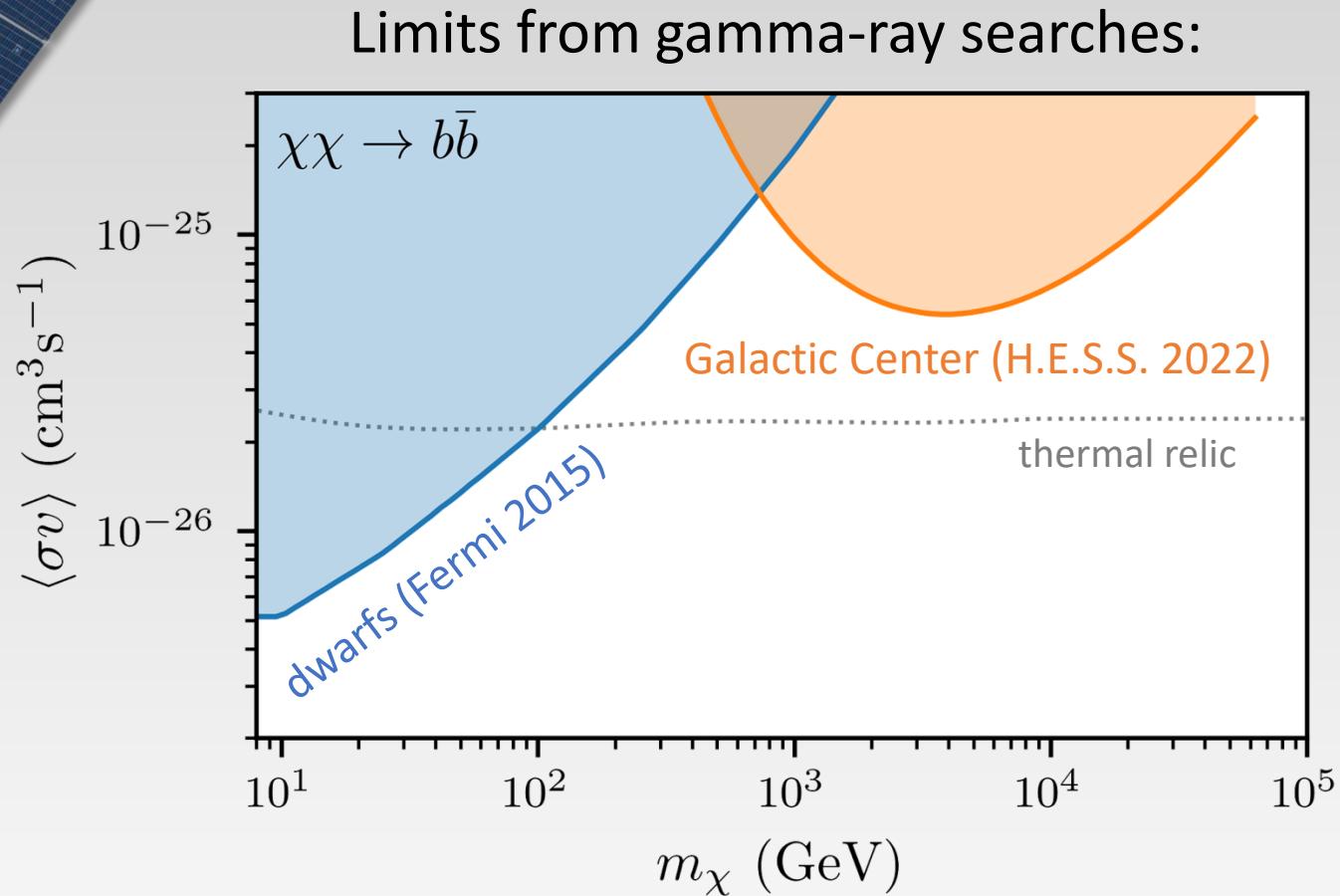
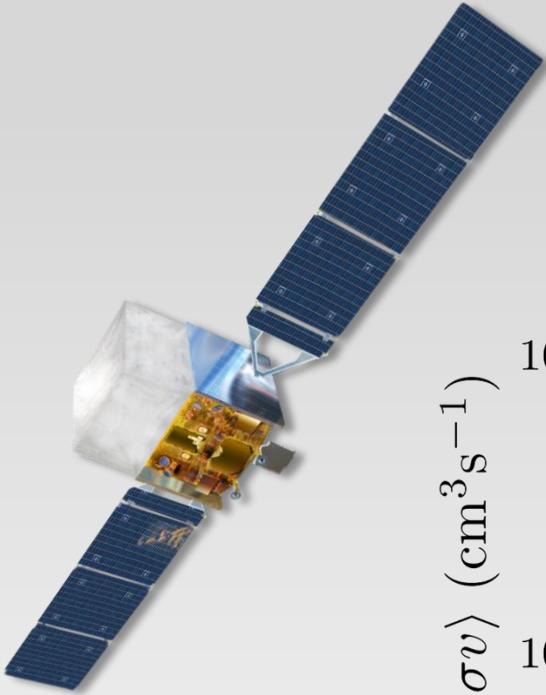


Annihilation rate  $\propto \rho^2$ :

**Search the dense centers of galaxies**



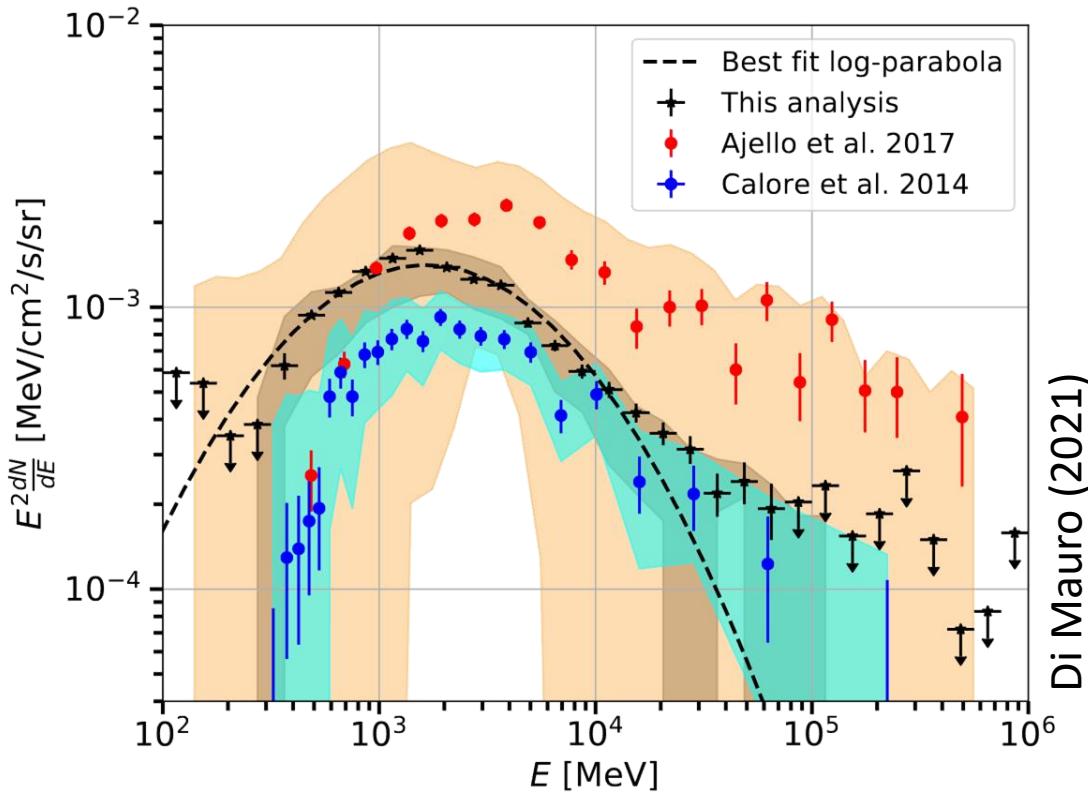
# Indirect-detection limits



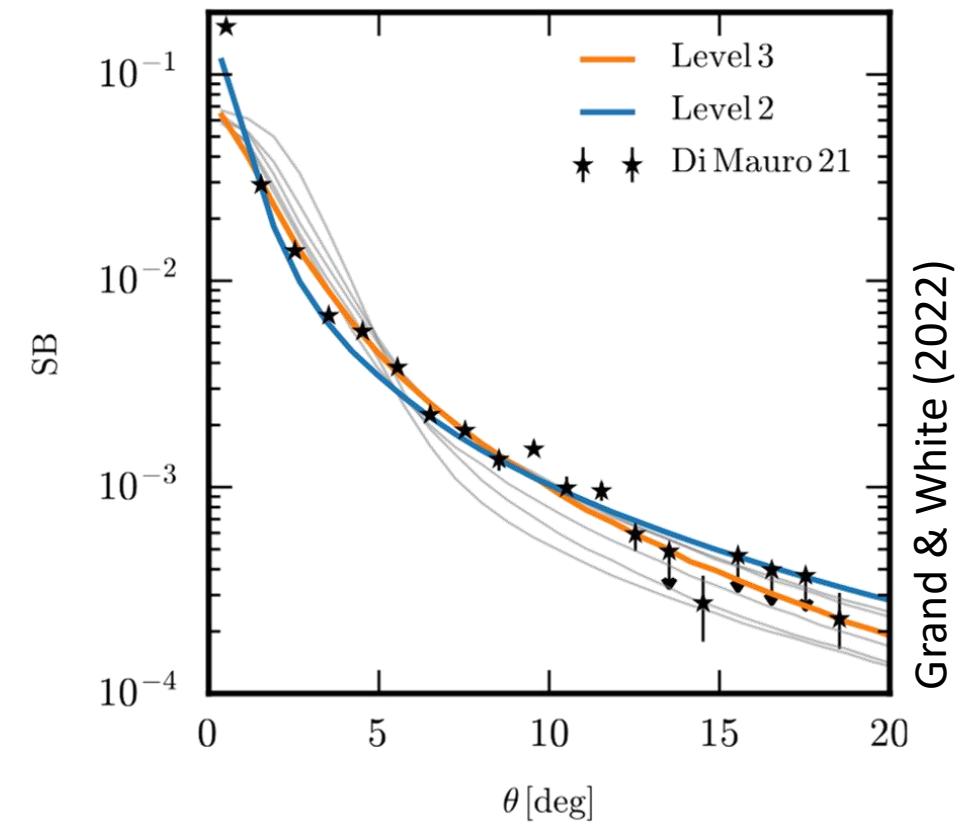
# Indirect detection?

The Galactic Center gamma-ray excess

Excess of  $\gamma$  rays detected by *Fermi* in the 1-10 GeV energy range

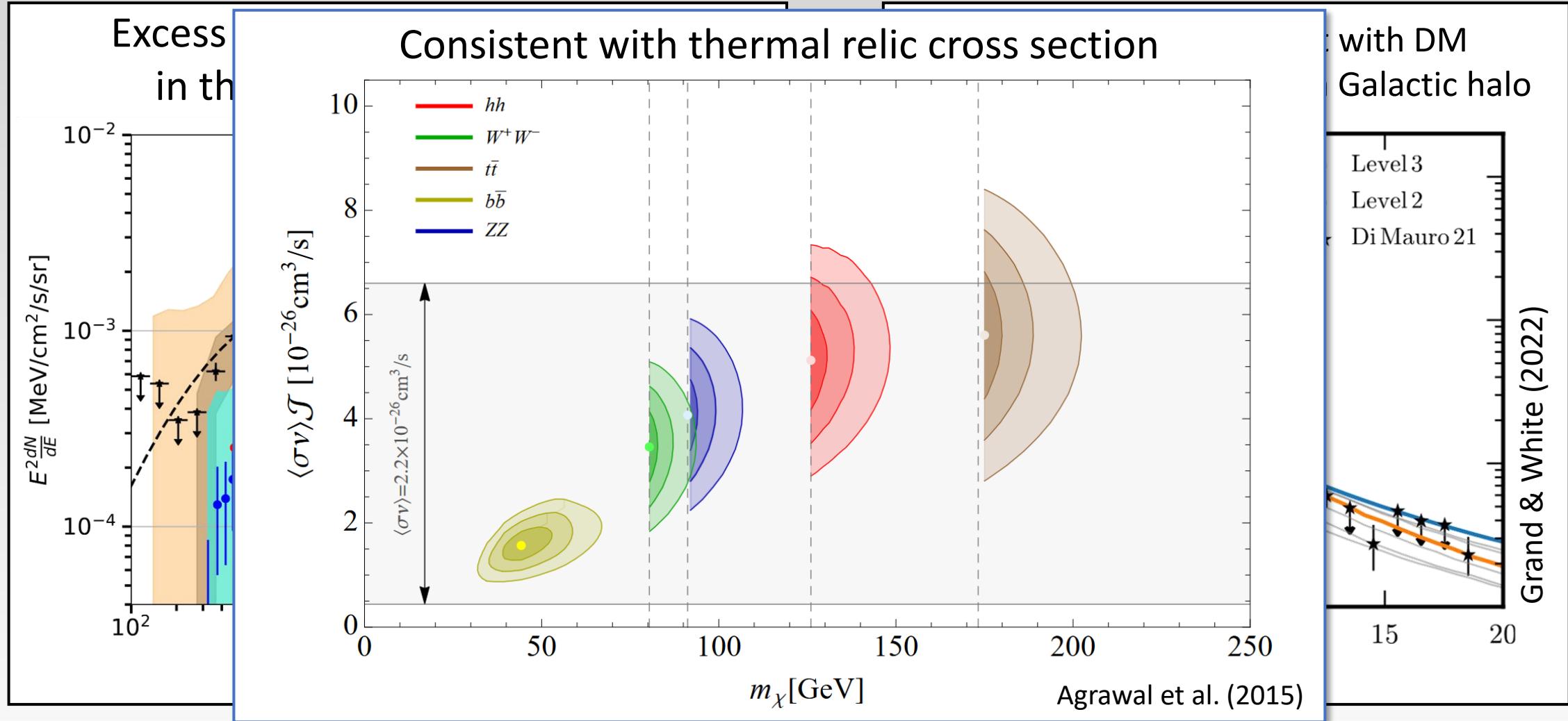


Morphology consistent with DM annihilation from a smooth Galactic halo



# Indirect detection?

The Galactic Center gamma-ray excess

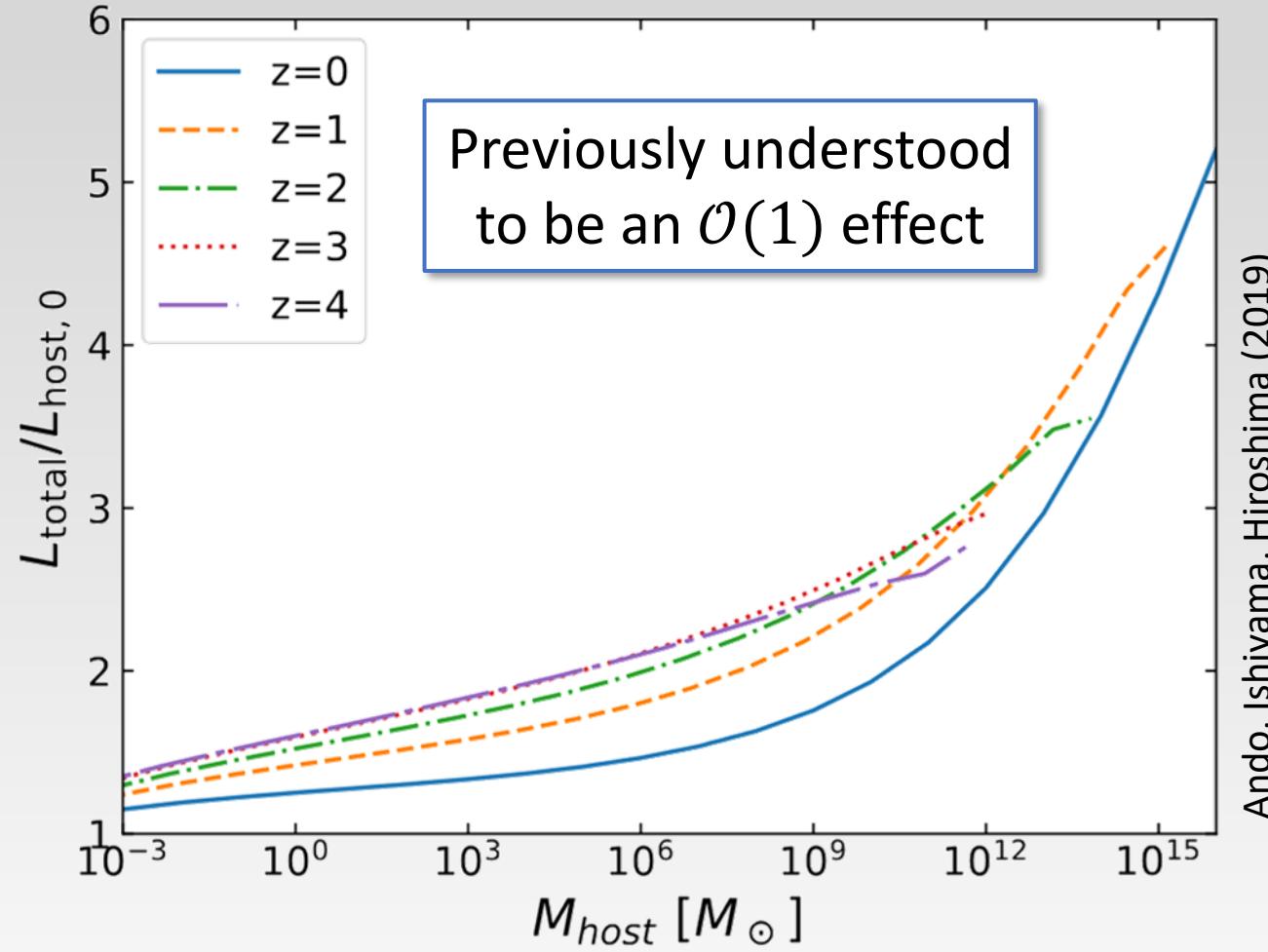


# Substructure boost

The annihilation rate inside a halo is boosted by the presence of subhalos



(due to  $\rho^2$  scaling)



# Outline

Dark matter halos

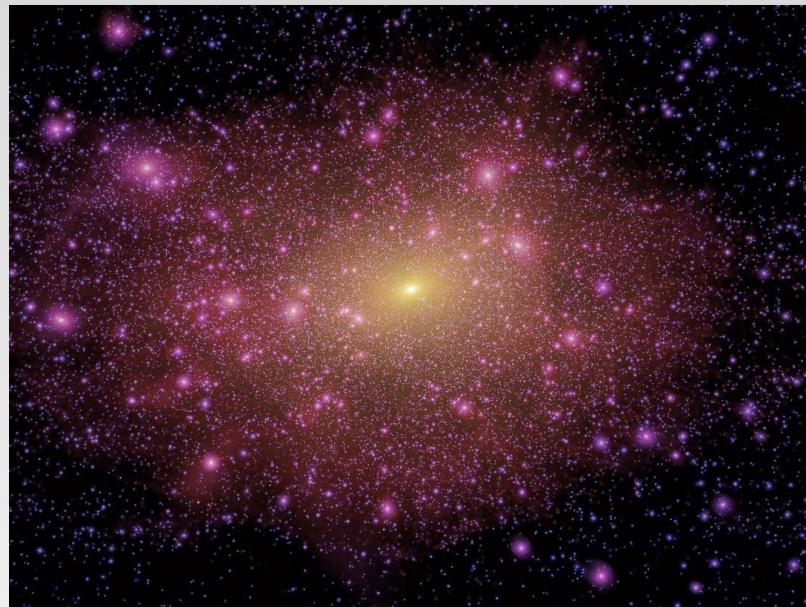
Prompt cusps of the first halos

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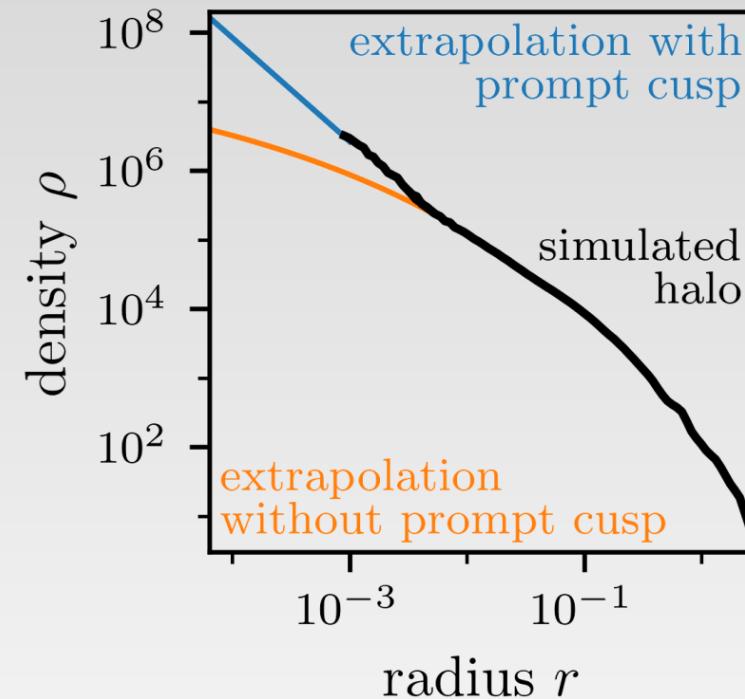
**Annihilation in prompt cusps**

# Prompt cusps and dark matter annihilation

Prompt cusp survival implies  
**every halo and subhalo** has one



Extreme density inside prompt cusps  
boosts the annihilation rate

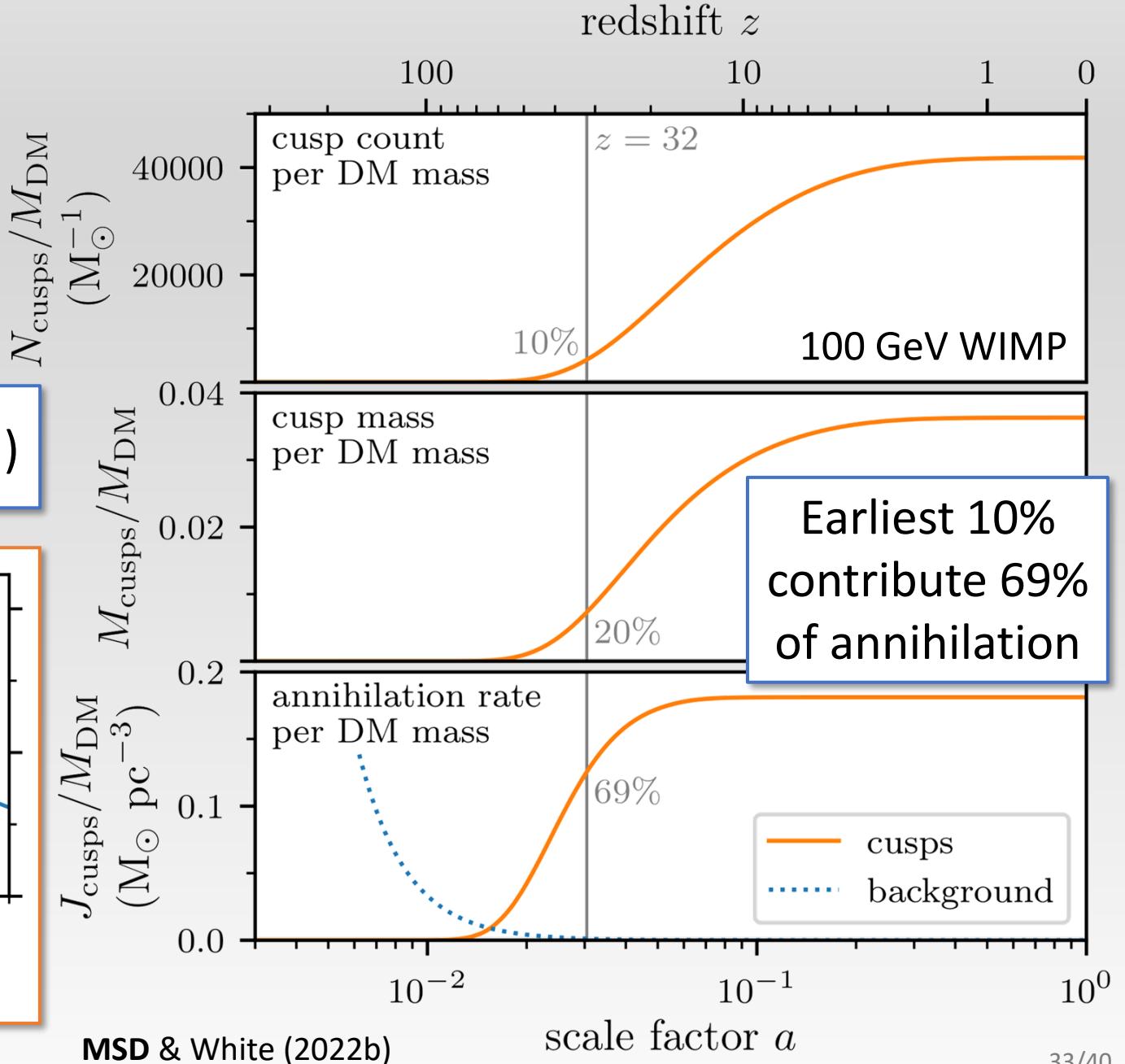
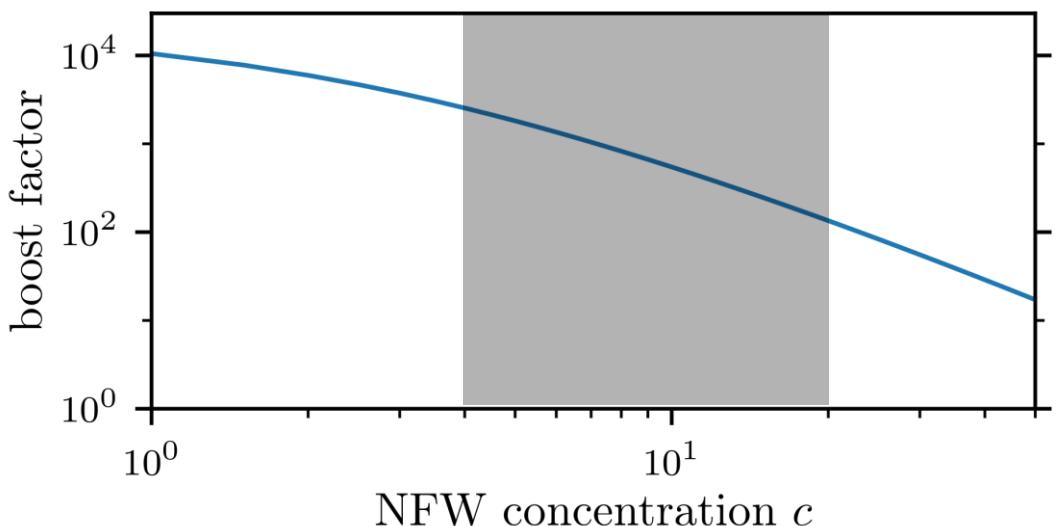


Egalitarian: every halo, no matter its size, has (roughly) **the same prompt cusp**

# Annihilation in prompt cusps

Compute using peak statistics

$$\frac{\text{annihilation rate}}{\text{DM mass}} \propto \frac{\int \rho dM}{M_{\text{DM}}} \simeq 150 \bar{\rho}(z = 32)$$



# Prompt cusp survival

Subhalo evolution studies have focused on  $\rho \propto r^{-1}$  cusps;  
steeper cusps are not well studied. However:

## Theoretical studies

- Stücker et al 2022
- Drakos et al 2022
- Benson & Du 2022
- Amorisco 2021

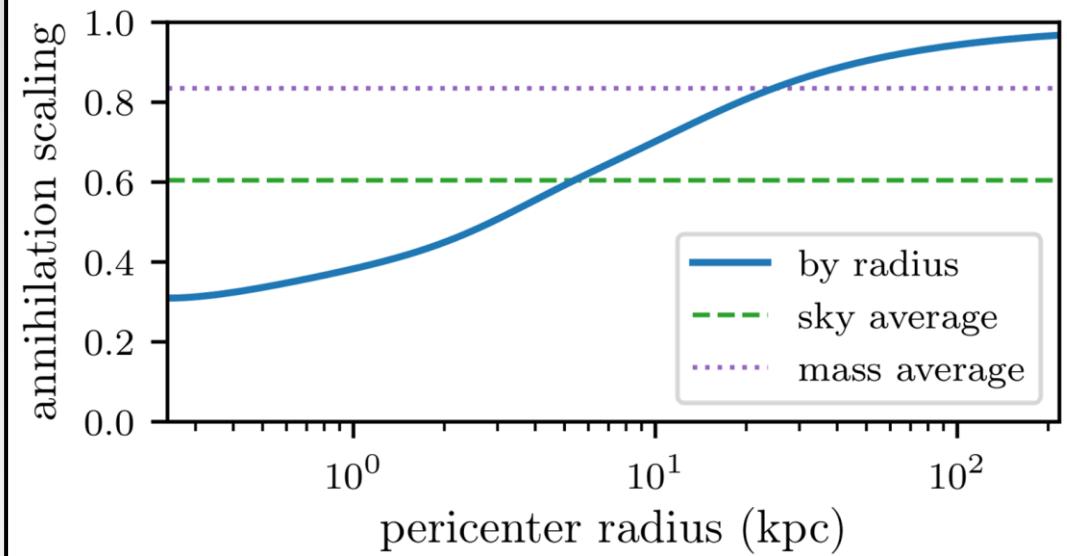
predict **cusps are always preserved at sufficiently small radii**

Steeper cusps are more resistant to tidal effects:

- More tightly bound
- Lower particle apocenters

Annihilation rate in a  $\rho \propto r^{-3/2}$  cusp is **only logarithmically sensitive** to the outer radius

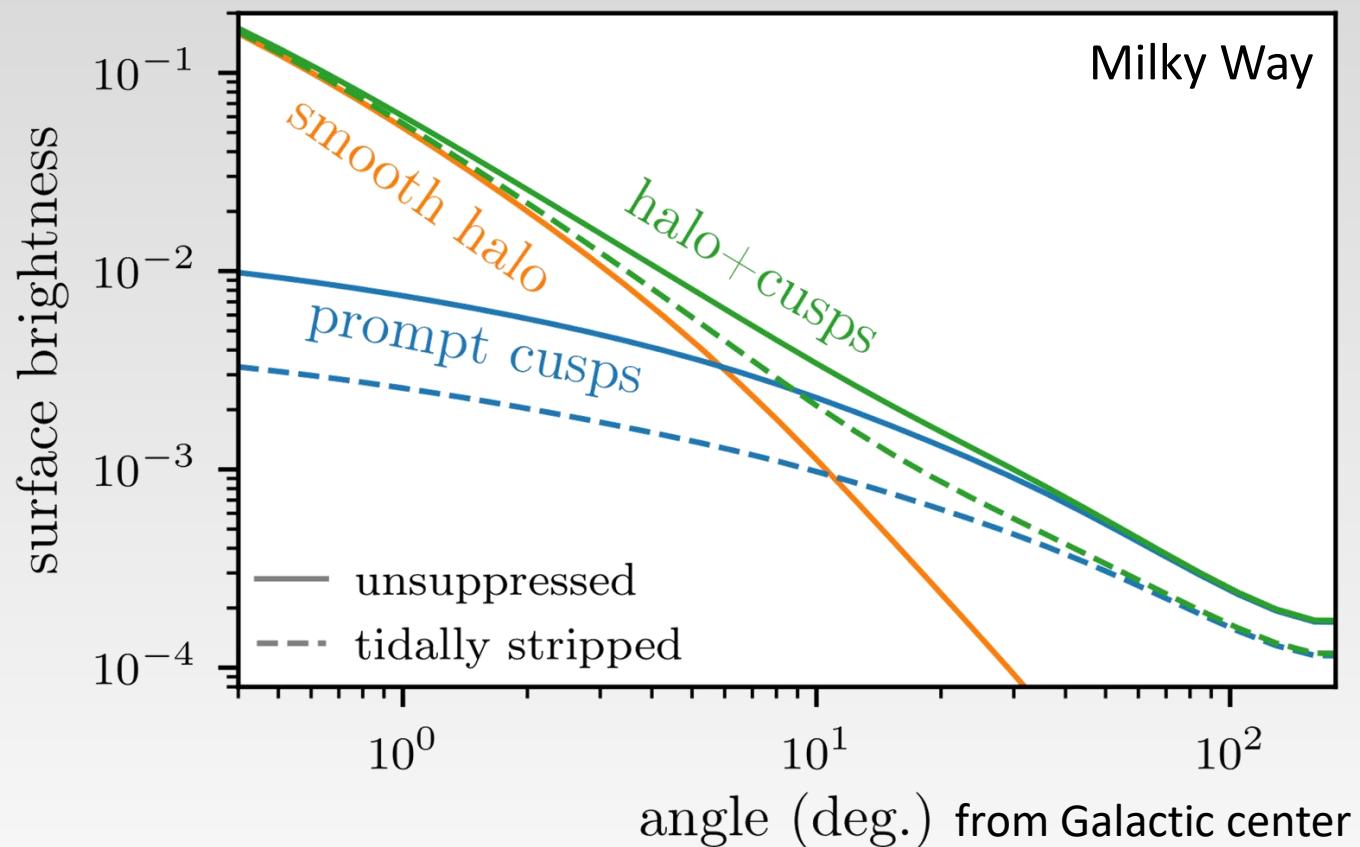
Adiabatic-tides (Stücker et al) prediction for **prompt cusp survival in our Galactic halo**:



MSD & White (2022b)

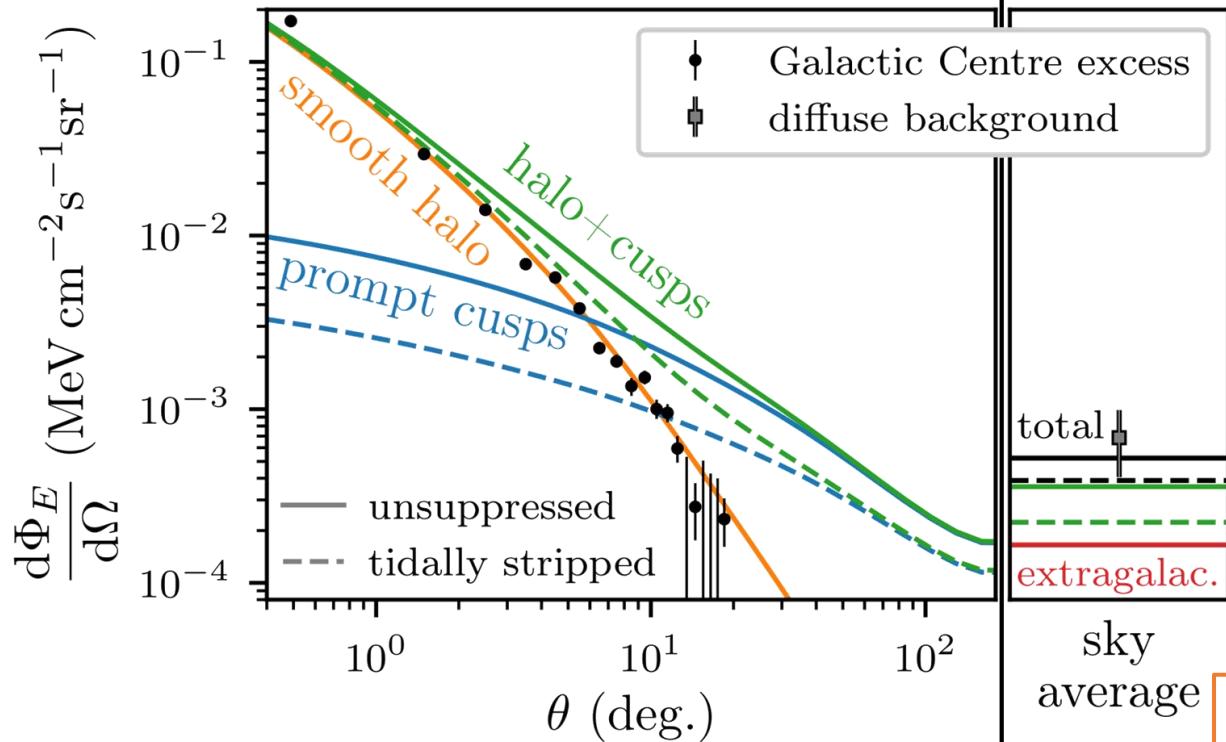
# Annihilation signal

Spatial distribution of annihilation signal changes:  
annihilation rate in prompt cusps  $\propto$  smoothed density  $\rho$ , not  $\rho^2$



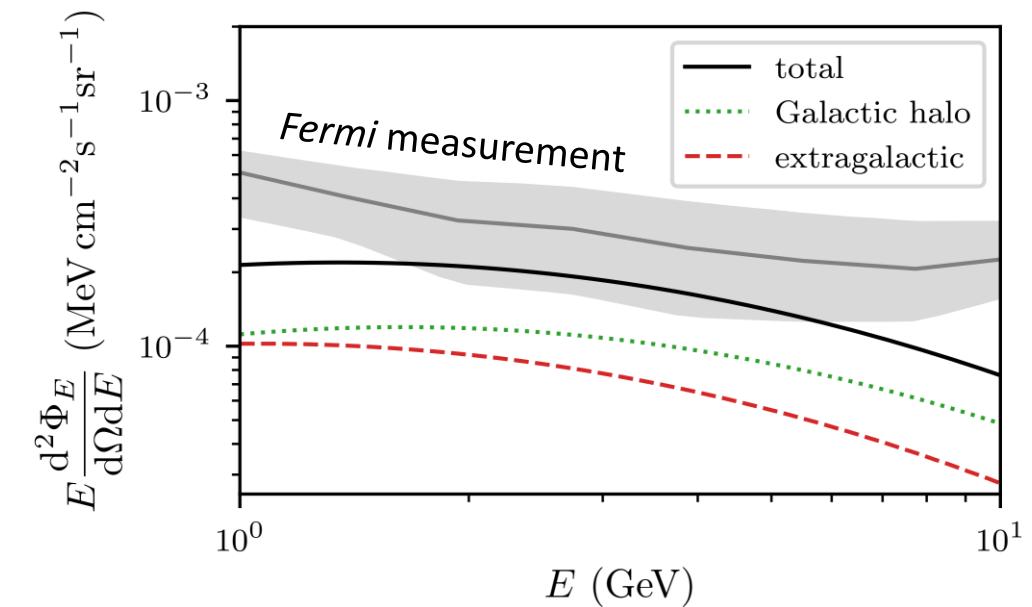
# Prompt cusps and the Galactic Center excess

Prompt cusps alter the DM annihilation morphology ( $\rho$ , not  $\rho^2$ )



GCE is no longer consistent with annihilating DM.  
Uncertainty about disruption by stars, though...

Prompt cusps boost the background annihilation signal

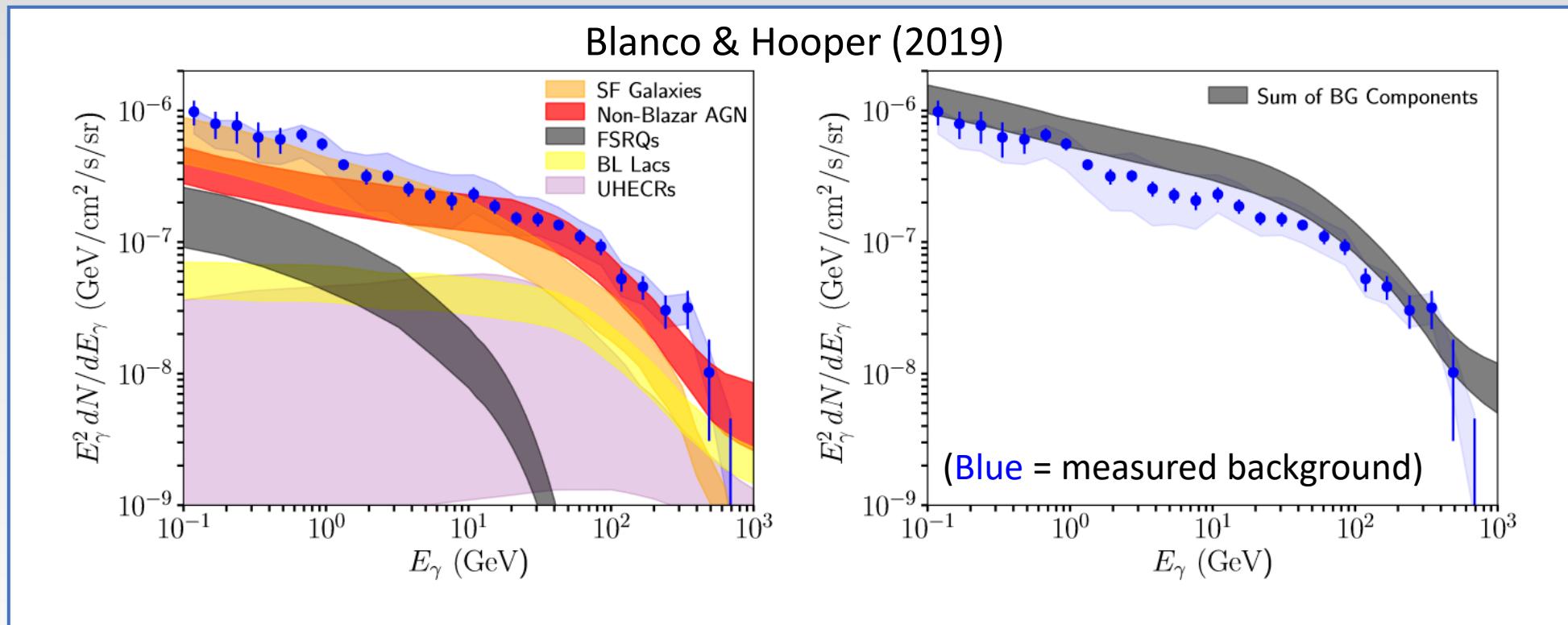


If GCE is annihilating DM, diffuse  $\gamma$ -ray background must also be largely annihilating DM...

# Prompt cusps and the Galactic Center excess

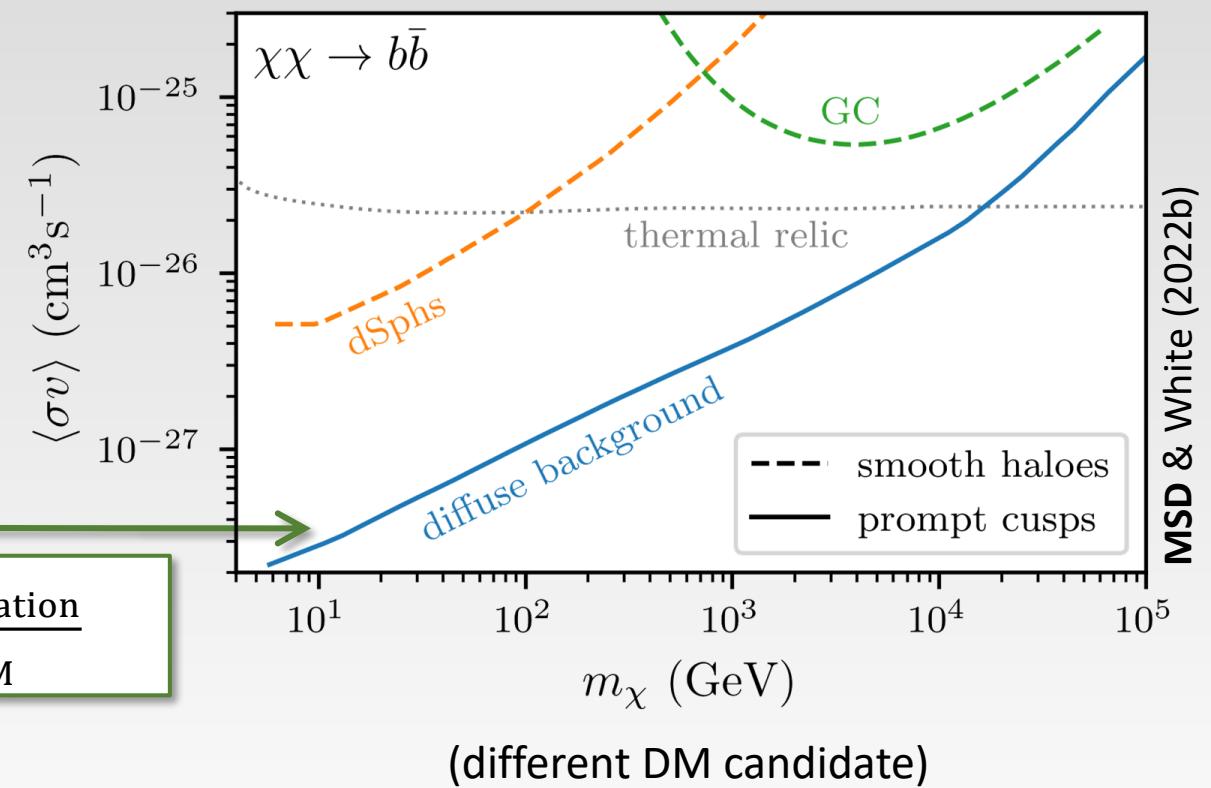
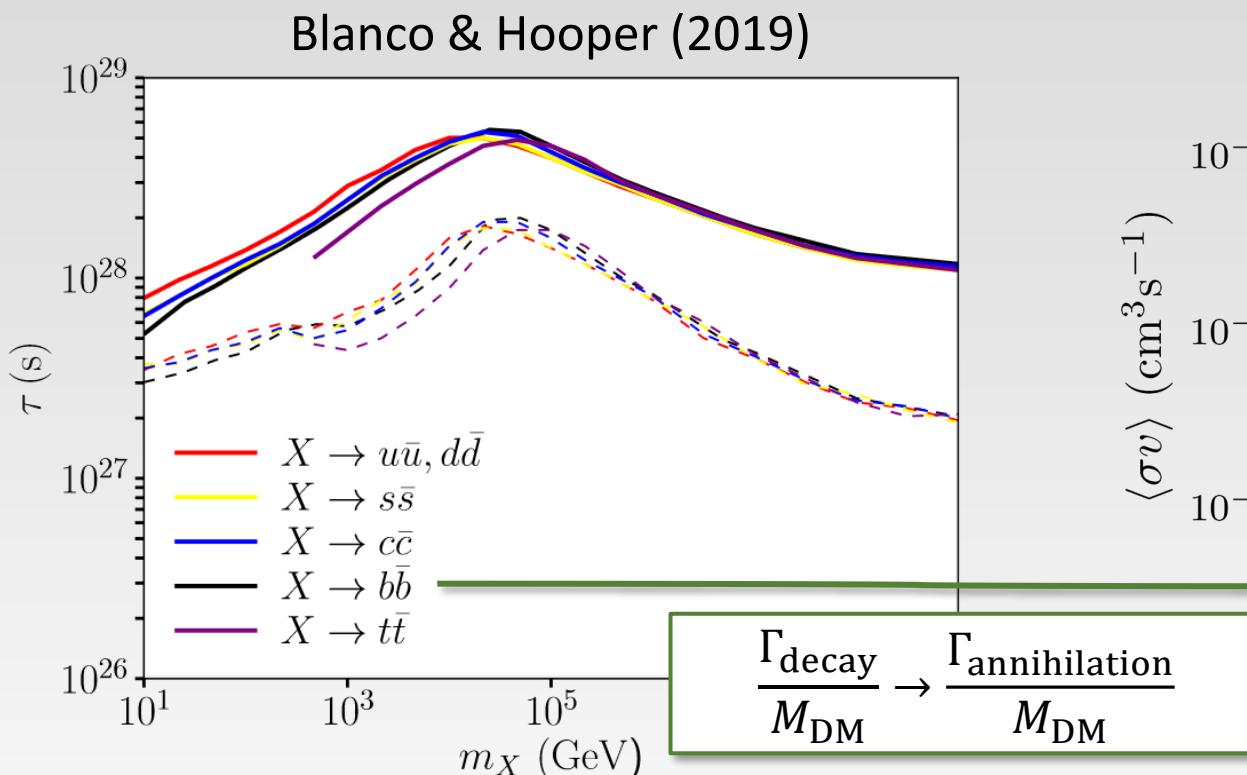
If GCE is annihilating DM, diffuse  $\gamma$ -ray background must also be largely annihilating DM...

In tension with claims that almost all of the diffuse background comes from known astrophysical sources:



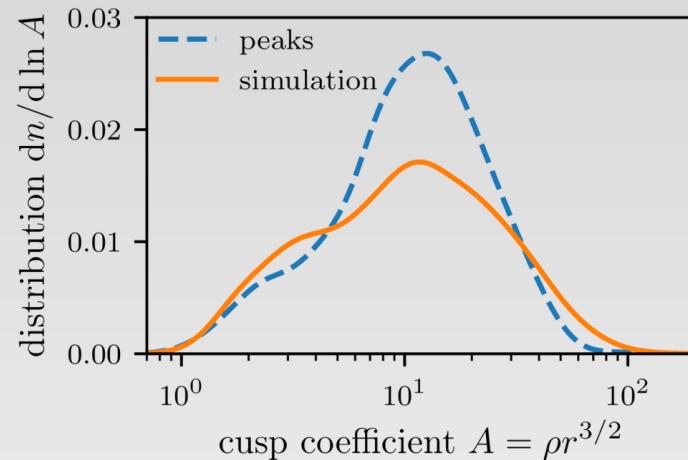
# Limits on DM annihilation

Signal from DM annihilation in unresolved prompt cusps  $\simeq$  signal from DM decay  
so we can convert between them:



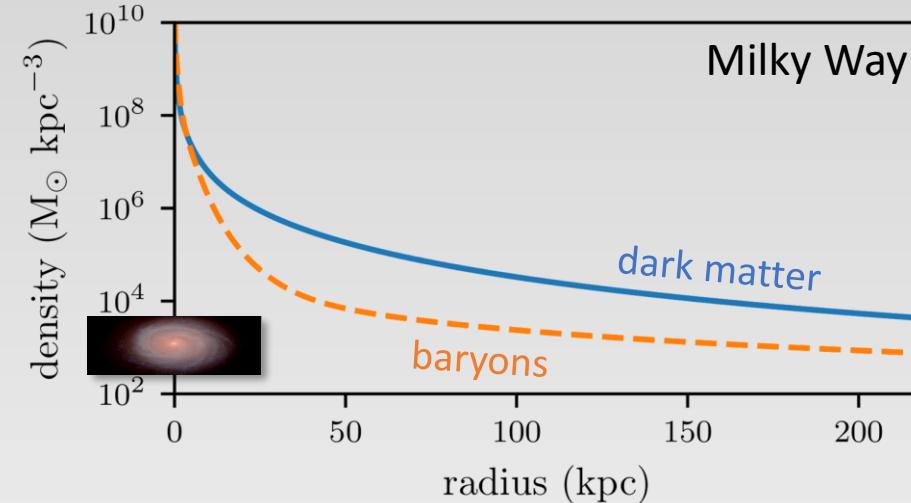
# Outlook

Reduction in prompt cusp number  
due to mergers?



(highly unequal masses lead to  
subhalo, both cusps preserved)

How much disruption by stars?



~30% of Galactic DM crosses disk

If DM is a thermal relic, expect an annihilation signal not only from the densest regions  
**but from diffuse regions as well**

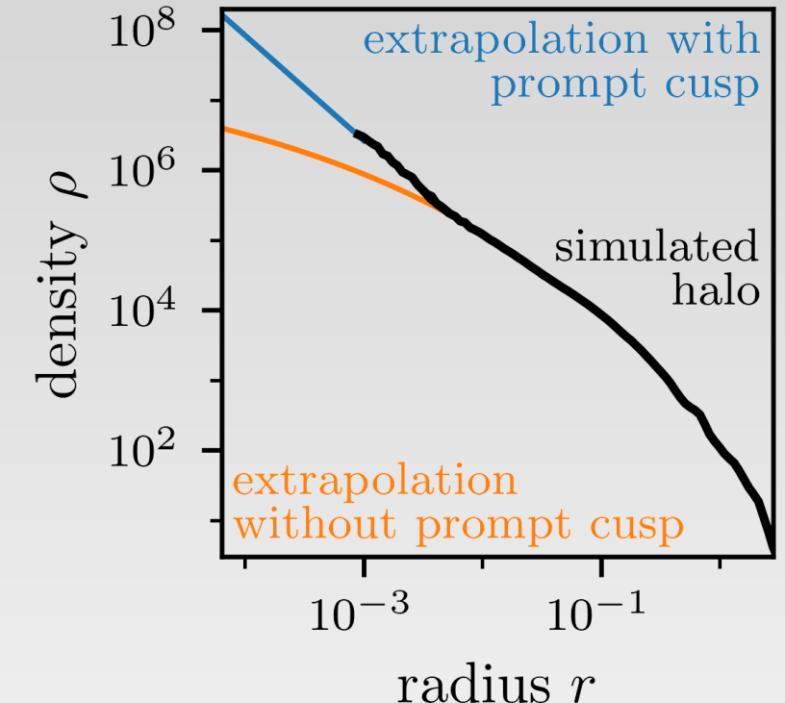
# Summary

The first halos develop  $\text{prompt } \rho \propto r^{-3/2}$  cusps, which

- persist through halo growth
- are particularly resistant to subhalo evolution
- have straightforwardly predictable properties

Prompt cusps have a major impact on DM annihilation

- Boost factors can range from hundreds to thousands
- Different morphology: rate  $\propto \rho$  instead of  $\rho^2$
- Unprecedentedly strong limits on annihilating DM



If DM is a thermal relic, expect an annihilation signal not only from the densest regions  
**but from diffuse regions as well**