

$$b = \frac{\text{Cov}(X, Y)}{\text{VAR}(X)}, \quad a = \bar{y} - b\bar{x}$$

</LARS>

$$\text{Precision} = \frac{TP}{TP + FP}$$

⇒ Out of all predicted positive, how many actually have cancer?

$$\text{Recall} = \frac{TP}{TP + FN}$$

⇒ out of all cancer patients, how many are we predicting?

workable

<you enter here>

Note: This is not an accidental ink

spill at all ⇒ 100% Intentional

ML Lab Project

Structural Similarity

* Problem with MSE is that it only estimate absolute error

SSIM: AKA Structural Similarity is a perception based model

↳ Considers image degradation
↳ As perceived change in structural information

Structural Information

⇒ Idea that pixels have strong interdependencies especially when they are spatially close.

$SSIM$ is calculated on various $N \times N$ windows of the image

Say window x [$N \times N$]

and window y [$N \times N$]

$$SSIM(x, y) = \frac{(2\mu_x\mu_y + c_1)(2\sigma_{xy} + c_2)}{(\mu_x^2 + \mu_y^2 + c_1)(\sigma_x^2 + \sigma_y^2 + c_2)}$$

Where

μ_x = average of x

σ_x^2 = var of x

σ_{xy} = covar (x, y)

And $c_1 = (k_1 L)^2$; $c_2 = (k_2 L)^2$

L is the dynamic range of pixel value

$$L = 2^{\text{#bits per pixel}} - 1$$

$$k_1 = 0.01, k_2 = 0.03$$

Formula Components

$SSIM$ is based on 3 comparison measurements between the samples of x & y
Luminance, Contrast & Structure
(μ) (σ) (σ_{xy})

where

$$\text{Luminance } l(x, y) = \frac{2\mu_x\mu_y + c_1}{\mu_x^2 + \mu_y^2 + c_1}$$

$$\text{Contrast } c(x, y) = \frac{2\sigma_x\sigma_y + c_2}{\sigma_x^2 + \sigma_y^2 + c_2}$$

$$\text{Structure } s(x, y) = \frac{\sigma_{xy} + c_3}{\sigma_x\sigma_y + c_3}$$

$$\text{Note: } c_3 = c_2/2$$

S_{sim} is a weighted combination of these comparative measures

ie $S_{sim}(x, y) = l(x, y)^\alpha c(x, y)^\beta s(x, y)^\gamma$

If $\alpha = \beta = \gamma = 1$, we get

$$S_{sim}(x, y) = \frac{(2\mu_x\mu_y + c_1)(2\sigma_{xy} + c_3)}{(\mu_x^2 + \mu_y^2 + c_1)(\sigma_x^2 + \sigma_y^2 + c_2)}$$

S_{sim} is not a distance measure as it does not obey triangle inequality